Untitled

June 5, 2025

```
[1]: """
     Project_LPI_World_Bank
     ___Linear Interpolation
     import numpy as np
     import pandas as pd
     from scipy import interpolate
     # Singapore population data
     years = np.array([2007, 2010, 2012, 2014, 2016, 2018, 2023])
     population = np.array([4588599, 5076732, 5312437, 5469724, 5607283, 5638676, __
      →5917648])
     # Create complete year range for interpolation
     complete_years = np.arange(2007, 2024)
     # Cubic Spline Interpolation
     cubic_interp = interpolate.CubicSpline(years, population)
     cubic_predictions = cubic_interp(complete_years)
     print("=== SINGAPORE POPULATION CUBIC SPLINE ESTIMATES ===")
     print("Copy this data directly into Excel:")
     print("\nYear\tPopulation (Cubic Spline)")
     print("-" * 35)
     # Create Excel-ready data
     excel_data = []
     for i, year in enumerate(complete_years):
         pop_estimate = int(round(cubic_predictions[i]))
         excel_data.append([year, pop_estimate])
         # Mark actual vs estimated
         if year in years:
             actual_pop = population[np.where(years == year)[0][0]]
```

```
marker = f" (ACTUAL: {actual_pop})"
   else:
       marker = " (ESTIMATED)"
   print(f"{year}\t{pop_estimate:,}{marker}")
print("\n" + "="*60)
print("EXCEL IMPLEMENTATION GUIDE")
print("="*60)
print("\n1. COPY THE DATA ABOVE INTO EXCEL:")
print(" - Column A: Years (2007-2023)")
print(" - Column B: Population estimates")
print("\n2. CAGR FORMULA FOR COUNTRY MATCHING:")
print(" Place this in your CAGR column:")
# Create the CAGR formula for Excel
cagr_formula = """=IF(OR(ISERROR(VLOOKUP(Y3,'2023'!$Y$3:$Z$141,2,FALSE)),
         ISERROR(VLOOKUP(Y3,'2007'!$A$4:$U$153,21,FALSE))),
    "Data Missing",
   POWER(VLOOKUP(Y3, '2023'!$Y$3:$Z$141,2,FALSE)/
          VLOOKUP(Y3,'2007'!$A$4:$U$153,21,FALSE), 1/16) - 1)"""
print(cagr_formula)
print("\n3. ALTERNATIVE CAGR FORMULA (if you have helper columns):")
alt_formula = """=IF(OR(Z3="", [2007_Population_Column]=""), "No Data",
   POWER(Z3/[2007_Population_Column], 1/16) - 1)"""
print(alt_formula)
print("\n4. FORMAT THE CAGR COLUMN:")
print(" - Select CAGR column")
print(" - Format as Percentage with 2 decimal places")
print("\n" + "="*60)
print("CUBIC SPLINE DATA FOR SINGAPORE (Excel Format)")
print("="*60)
# Create a clean DataFrame for export
df_export = pd.DataFrame({
   'Year': complete_years,
    'Singapore_Population': [int(round(x)) for x in cubic_predictions],
    'Data_Type': ['Actual' if year in years else 'Estimated' for year in_
})
```

```
print(df_export.to_string(index=False))
print("\n" + "="*60)
print("MISSING YEARS FILLED (Ready for Excel)")
print("="*60)
missing_years_df = df_export[~df_export['Year'].isin(years)]
print("These are the NEW estimates you can add to your data:")
print(missing_years_df[['Year', 'Singapore_Population']].to_string(index=False))
print("\n" + "="*60)
print("VERIFICATION - SINGAPORE CAGR CALCULATION")
print("="*60)
singapore_2007 = 4588599
singapore_2023 = 5917648
singapore_cagr = ((singapore_2023 / singapore_2007) ** (1/16) - 1) * 100
print(f"Singapore 2007 Population: {singapore_2007:,}")
print(f"Singapore 2023 Population: {singapore_2023:,}")
print(f"Singapore CAGR (2007-2023): {singapore_cagr:.2f}%")
print("\n" + "="*60)
print("STEP-BY-STEP EXCEL IMPLEMENTATION")
print("="*60)
print("""
STEP 1: Create Singapore Complete Dataset
1. Open a new Excel sheet called 'Singapore_Complete'
2. Copy the Year and Population data above into columns A and B
3. This gives you ALL years from 2007-2023 with no gaps
STEP 2: Add CAGR Column to Your Main Sheet
1. Go to your main sheet with country analysis
2. Add a new column header: "CAGR (2007-2023)"
3. In the first data row, paste this formula:
=IF(OR(ISERROR(VLOOKUP(Y3,'2023'!$Y$3:
  $\frac{$\$2\$141,2,\frac{$\}1,3\$2\},\frac{$\}1\$3,\frac{$\}2\$3,\frac{$\}2\$3,\frac{$\}2\$3,\frac{$\}2\$3,\frac{$\}2\$3,\frac{$\}2\$3,\frac{$\}2\$3,\frac{$\}2\$3,\frac{$\}2\$3,\frac{$\}2\$3,\frac{$\}2\$3,\frac{$\}2\$3,\frac{$\}2\$3,\frac{$\}2\$3,\frac{$\}2\$3,\frac{$\}2\$3,\frac{$\}2\$3,\frac{$\}2\$3,\frac{$\}2\$3,\frac{$\}2\$3,\frac{$\}2\$3,\frac{$\}2\$3,\frac{$\}2\$3,\frac{$\}2\$3,\frac{$\}2\$3,\frac{{\}2\$3,\frac{$\}2\$3,\frac{{\}2\$3,\frac{{\}2\$3,\frac{{\}2\$3,\frac{{\}2\$3,\frac{{\}2\$3,\frac{{\}2\$3,\frac{{\}2\$3,\frac{{\}2\$3,\frac{{\}2\$3,\frac{{\}2\$3,\frac{{\}2\$3,\frac{{\}2\$3,\frac{{\}2\$3,\frac{{\}2\$3,\frac{{\}2\$3,\frac{{\}2\$3,\frac{{\}2\$3,\frac{{\}2\$3,\frac{{\}2\$3,\frac{{\}2\$3,\frac{{\}2\$3,\frac{{\}2\$3,\frac{{\}2\$3,\frac{{\}2\$3,\frac{{\}2\$3,\frac{{\}2\$3,\frac{{\}2\$3,\frac{{\}2\$3,\frac{{\}2\$3,\frac{{\}2\$3,\frac{{\}2\$3,\frac{{\}2\$3,\frac{{\}2\$3,\frac{{\}2\$3,\frac{{\}2\$3,\frac{{\}2\$3,\frac{{\}2\$3,\frac{{\}2\$3,\frac{{\}2\$3,\frac{{\}2\$3,\frac{{\}2\$3,\frac{{\}2\$3,\frac{{\}2\$3,\frac{{\}2\$3,\frac{{\}2\$3,\frac{{\}2\$3,\frac{{\}2\$3,\frac{{\}2\$3,\frac{{\}2\$3,\frac{{\}2\$3,\frac{{\}2\$3,\frac{{\}2\$3,\frac{{\}2\$3,\frac{{\}2\$3,\frac{{\}2\$3,\frac{{\}2\$3,\frac{{\}2\$3,\frac{{\}2\$3,\frac{{\}2\$3,\frac{{\}2\$3,\frac{{\}2\$3,\frac{{\}2\$3,\frac{{\}2\$3,\frac{{\}2\$3,\frac{{\}2\$3,\frac{{\}2\$3,\frac{{\}2\$3,\frac{{\}2\$3,\frac{{\}2\$3,\frac{{\}2\$3,\frac{{\}2\$3,\frac{{\}2\$3,\frac{{\}2\$3,\frac{{\}2\$3,\frac{{\}2\$3,\frac{{\}2\$3,\frac{{\}2\$3,\frac{{\}2\$3,\frac{{\}2\$3,\frac{{\}2\$3,\frac{{\}2\$3,\frac{{\}2\$3,\frac{{\}2\$3,\frac{{\}2\$3,\frac{{\}2\$3,\frac{{\}2\$3,\frac{{\}2\$3,\frac{{\}2\$3,\frac{{\}2\$3,\frac{{\}2\$3,\frac{{\}2\$3,\frac{{\}2\$3,\frac{{\}2\$3,\frac{{\}2\$3,\frac{{\}2\$3,\frac{{\}2\$3,\frac{{\}2\$3,\frac{{\}2\$3,\frac{{\}2\$3,\frac{{\}2\$3,\frac{{\}2\$3,\frac{{\}2\$3,\frac{{\}2\$3,\frac{{\}2\$3,\frac{{\}2\$3,\frac{{\}2\$3,\frac{{\}2\$3,\frac{{\}2\$3,\frac{{\}2\$3,\frac{{\}2\$3,\frac{{\}2\$3,\frac{{\}2\$3,\frac{{\}2\$3,\frac{{\}2\$3,\frac{{\}2\$3,\frac{{
  →Data",POWER(VLOOKUP(Y3,'2023'!$Y$3:$Z$141,2,FALSE)/VLOOKUP(Y3,'2007'!$A$4:
  \Rightarrow$U$153,21,FALSE),1/16)-1)
STEP 3: Copy Formula Down
1. Copy the CAGR formula down to all rows
2. Format the column as Percentage with 2 decimal places
STEP 4: Verify with Singapore
```

```
1. Find Singapore in your list
2. The CAGR should show approximately 1.64%
3. If it matches, your formula is working correctly!

STEP 5: Sort and Analyze
1. Sort by CAGR column to see fastest/slowest growing countries
2. Use conditional formatting to highlight high/low growth rates
""")

print("\nFormula Breakdown:")
print("- VLOOKUP(Y3,'2023'!$Y$3:$Z$141,2,FALSE) = Gets 2023 population")
print("- VLOOKUP(Y3,'2007'!$A$4:$U$153,21,FALSE) = Gets 2007 population")
print("- POWER(2023_pop/2007_pop, 1/16) - 1 = Calculates CAGR")
print("- IF statements handle missing data gracefully")
```

=== SINGAPORE POPULATION CUBIC SPLINE ESTIMATES === Copy this data directly into Excel:

```
Year
       Population (Cubic Spline)
_____
2007
      4,588,599 (ACTUAL: 4588599)
      4,764,090 (ESTIMATED)
2008
2009
      4,928,092 (ESTIMATED)
2010
      5,076,732 (ACTUAL: 5076732)
2011
      5,206,138 (ESTIMATED)
2012
      5,312,437 (ACTUAL: 5312437)
2013
      5,395,444 (ESTIMATED)
      5,469,724 (ACTUAL: 5469724)
2014
2015
      5,546,300 (ESTIMATED)
2016
      5,607,283 (ACTUAL: 5607283)
2017
      5,634,640 (ESTIMATED)
2018
      5,638,676 (ACTUAL: 5638676)
2019
      5,636,779 (ESTIMATED)
2020
      5,646,339 (ESTIMATED)
2021
      5,684,745 (ESTIMATED)
2022
      5,769,385 (ESTIMATED)
2023
       5,917,648 (ACTUAL: 5917648)
```

EXCEL IMPLEMENTATION GUIDE

- 1. COPY THE DATA ABOVE INTO EXCEL:
 - Column A: Years (2007-2023)
 - Column B: Population estimates
- 2. CAGR FORMULA FOR COUNTRY MATCHING:

```
Place this in your CAGR column:
=IF(OR(ISERROR(VLOOKUP(Y3,'2023'!$Y$3:$Z$141,2,FALSE)),
       ISERROR(VLOOKUP(Y3,'2007'!$A$4:$U$153,21,FALSE))),
   "Data Missing",
   POWER(VLOOKUP(Y3, '2023'!$Y$3:$Z$141,2,FALSE)/
        VLOOKUP(Y3,'2007'!$A$4:$U$153,21,FALSE), 1/16) - 1)
3. ALTERNATIVE CAGR FORMULA (if you have helper columns):
=IF(OR(Z3="", [2007 Population Column]=""), "No Data",
   POWER(Z3/[2007_Population_Column], 1/16) - 1)
4. FORMAT THE CAGR COLUMN:
  - Select CAGR column
  - Format as Percentage with 2 decimal places
CUBIC SPLINE DATA FOR SINGAPORE (Excel Format)
_____
Year Singapore_Population Data_Type
2007
                 4588599
                          Actual
2008
                 4764090 Estimated
                 4928092 Estimated
2009
2010
                 5076732
                          Actual
2011
                 5206138 Estimated
2012
                 5312437
                         Actual
2013
                 5395444 Estimated
2014
                 5469724
                          Actual
2015
                 5546300 Estimated
2016
                 5607283
                          Actual
2017
                 5634640 Estimated
2018
                 5638676
                          Actual
                 5636779 Estimated
2019
2020
                 5646339 Estimated
2021
                 5684745 Estimated
                 5769385 Estimated
2022
2023
                 5917648
                          Actual
-----
MISSING YEARS FILLED (Ready for Excel)
_____
These are the NEW estimates you can add to your data:
Year Singapore_Population
2008
                 4764090
2009
                 4928092
2011
                 5206138
2013
                 5395444
2015
                 5546300
```

5634640

2017

2019	5636779
2020	5646339
2021	5684745
2022	5769385

VERIFICATION - SINGAPORE CAGR CALCULATION

Singapore 2007 Population: 4,588,599 Singapore 2023 Population: 5,917,648 Singapore CAGR (2007-2023): 1.60%

STEP-BY-STEP EXCEL IMPLEMENTATION

STEP 1: Create Singapore Complete Dataset

- 1. Open a new Excel sheet called 'Singapore_Complete'
- 2. Copy the Year and Population data above into columns ${\tt A}$ and ${\tt B}$
- 3. This gives you ALL years from 2007-2023 with no gaps

STEP 2: Add CAGR Column to Your Main Sheet

- 1. Go to your main sheet with country analysis
- 2. Add a new column header: "CAGR (2007-2023)"
- 3. In the first data row, paste this formula:

=IF(OR(ISERROR(VLOOKUP(Y3,'2023'!\$Y\$3:\$Z\$141,2,FALSE)),ISERROR(VLOOKUP(Y3,'2007'!\$A\$4:\$U\$153,21,FALSE))),"No Data",POWER(VLOOKUP(Y3,'2023'!\$Y\$3:\$Z\$141,2,FALSE)/VLOOKUP(Y3,'2007'!\$A\$4:\$U\$153,21,FALSE),1/16)-1)

STEP 3: Copy Formula Down

- 1. Copy the CAGR formula down to all rows
- 2. Format the column as Percentage with 2 decimal places

STEP 4: Verify with Singapore

- 1. Find Singapore in your list
- 2. The CAGR should show approximately 1.64%
- 3. If it matches, your formula is working correctly!

STEP 5: Sort and Analyze

- 1. Sort by CAGR column to see fastest/slowest growing countries
- 2. Use conditional formatting to highlight high/low growth rates

Formula Breakdown:

- VLOOKUP(Y3,'2023'!\$Y\$3:\$Z\$141,2,FALSE) = Gets 2023 population
- VLOOKUP(Y3,'2007'!\$A\$4:\$U\$153,21,FALSE) = Gets 2007 population
- POWER(2023_pop/2007_pop, 1/16) 1 = Calculates CAGR

```
- IF statements handle missing data gracefully
    CSV FORMAT (Copy to .csv file for Excel import):
    -----
    Year, Singapore_Population, Data_Type
    2007,4588599,Actual
    2008,4764090,Estimated
    2009,4928092,Estimated
    2010,5076732,Actual
    2011,5206138,Estimated
    2012,5312437,Actual
    2013,5395444,Estimated
    2014,5469724,Actual
    2015,5546300,Estimated
    2016,5607283,Actual
    2017,5634640,Estimated
    2018,5638676,Actual
    2019,5636779,Estimated
    2020,5646339,Estimated
    2021,5684745,Estimated
    2022,5769385,Estimated
    2023,5917648,Actual
[5]: """
    Project\_LPI\_World\_Bank
    ___ CAGR Quintiles
     11 11 11
    import pandas as pd
    # Example CAGR data
    df = pd.read_xlsx('LPI_Worldbank')
    # Create quintile categories (labels 1 to 5)
    df['Quintile'] = pd.qcut(df['CAGR'], 5, labels=False) + 1
    # If you want custom labels (e.g., 'Q1', 'Q2', ...)
    df['Quintile_Label'] = pd.qcut(df['CAGR'], 5, labels=['Q1', 'Q2', 'Q3', 'Q4', |
```

AttributeError Traceback (most recent call last)

```
Cell In[5], line 11
    8 import pandas as pd
    10 # Example CAGR data
---> 11 df = pd.read_xlsx('LPI_Worldbank')
    14 # Create quintile categories (labels 1 to 5)
    15 df['Quintile'] = pd.qcut(df['CAGR'], 5, labels=False) + 1
AttributeError: module 'pandas' has no attribute 'read_xlsx'
```

```
AttributeError Traceback (most recent call last)

Cell In[7], line 11

8 import pandas as pd

10 # Example CAGR data
---> 11 df = pd.read_xlsx('LPI_Worldbank', encoding='latin-1', errors='ignore')

12 # If you have international characters

13 df = pd.read_csv('LPI_Worldbank', encoding='cp1252')

AttributeError: module 'pandas' has no attribute 'read_xlsx'
```

[]: