Data Analysis

Pipe It Up!: Nagaprasad Rudrapatna, Karen Deng, Jackson Muraika, Anna Zolotor 2020-04-17

```
library(tidyverse)
library(broom)
library(stringr)
library(knitr)
library(tidyverse)
library(gridExtra)
library(leaps)
library(rms)
nba_social_power <- read_csv("../data/nba.csv")</pre>
nba_2016_2017_100 <- nba_social_power
nba_social_power_mod <- nba_social_power %>%
  filter(TWITTER_HANDLE != "0") %>%
  select(PLAYER_NAME,
         TEAM_ABBREVIATION,
         AGE,
         W_PCT,
         OFF_RATING,
         DEF_RATING,
         NET RATING,
         AST_RATIO,
         REB PCT,
         USG_PCT,
         PIE,
         SALARY MILLIONS,
         ACTIVE_TWITTER_LAST_YEAR,
         TWITTER_FOLLOWER_COUNT_MILLIONS,
         PTS)
```

Research Question and Objective

The research question explored in this analysis is: Is there a relationship between measures of athletic success (win percentage, offensive and defensive ratings, etc.) and the internet "popularity" of NBA athletes, measured in the number of Twitter followers?

The objective of this analysis is to predict Twitter follower counts of NBA players using measures of athletic success.

The Data

The dataset we use in this analysis includes on-court performance data for NBA players in the 2016-2017 season, along with their salaries and Twitter engagement. The dataset is from Kaggle and references ESPN, Basketball-Reference, Twitter, Five-ThirtyEight, and Wikipedia as data sources. Because we are examining the relationship between player stats and the number of Twitter followers, we filtered for players who had an

active Twitter account, by filtering for values where TWITTER_HANDLE is not "NA" (0). After filtering, we have 95 observations.

The response variable is TWITTER_FOLLOWER_COUNT_MILLIONS, which measures players' Twitter follower counts at the time the data was collected.

Exploratory Data Analysis

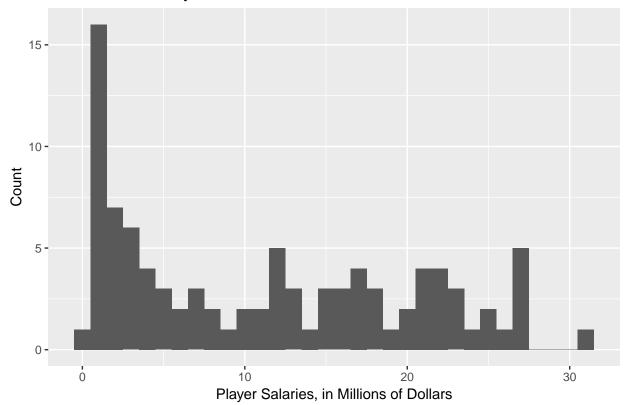
Although thorough and extensive EDA was done, this part of the analysis only contains portions of the EDA deemed to be important. All additional EDA can be found in the additional analysis section.

Univariate

Complete univariate EDA was done and can be found in additional analysis. Only the distributions of player salaries and twitter follower counts were noticeably non-normal and non-symmetrical, thus giving us important information about the data that needs to be kept in mind for our model, are shown here.

Here, we'll look into players' salaries, in millions of dollars:

Distribution of Player Salaries



```
nba_social_power_mod %>%
summarise(mean = mean(SALARY_MILLIONS),
```

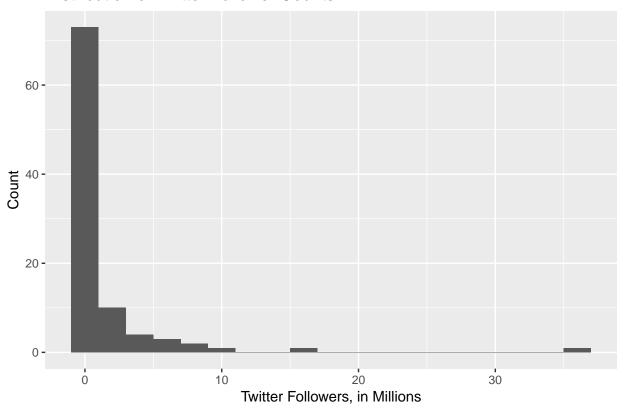
```
min= min(SALARY_MILLIONS),
            Q1 = quantile(SALARY_MILLIONS, .25),
            median = median(SALARY_MILLIONS),
            Q3 = quantile(SALARY_MILLIONS, .75),
            max = max(SALARY_MILLIONS))
## # A tibble: 1 x 6
##
                    Q1 median
      mean
            min
                                 QЗ
                        <dbl> <dbl> <dbl>
     <dbl> <dbl> <dbl>
## 1 11.3 0.31 2.47
                         11.3 18.5 31.0
nba_social_power_mod %>%
  arrange(desc(SALARY_MILLIONS)) %>%
  select(PLAYER_NAME, SALARY_MILLIONS) %>%
  head(10)
```

```
## # A tibble: 10 x 2
##
      PLAYER NAME
                        SALARY MILLIONS
##
      <chr>
                                   <dbl>
   1 LeBron James
                                    31.0
##
    2 Russell Westbrook
                                    26.5
    3 Kevin Durant
                                    26.5
##
##
  4 Mike Conley
                                    26.5
  5 DeMar DeRozan
                                    26.5
## 6 Al Horford
                                    26.5
   7 James Harden
##
                                    26.5
  8 Dirk Nowitzki
                                    25
## 9 Carmelo Anthony
                                    24.6
## 10 Damian Lillard
                                    24.3
```

As we can see from the histogram, the distribution of salaries is somewhat right-skewed, with most of the players making less than 20 million dollars a year. The mean salary is 11.3 million dollars a year. The player who earns the most, at 30.96 million dollars per year, is LeBron James (LeBron could be an influential point, so we will revisit this after the model selection phase). On the other hand, Russell Westbrook, Kevin Durant, Mike Conley, DeMar DeRozan, and Al Horford each earn 26.54 million dollars per year.

Here, we'll look into the response variable, TWITTER_FOLLOWER_COUNT_MILLIONS:

Distribution of Twitter Follower Counts



```
nba_social_power_mod %>%
  summarise(mean = mean(TWITTER_FOLLOWER_COUNT_MILLIONS),
            min= min(TWITTER_FOLLOWER_COUNT_MILLIONS),
            Q1 = quantile(TWITTER FOLLOWER COUNT MILLIONS, .25),
            median =
                       median(TWITTER_FOLLOWER_COUNT_MILLIONS),
            Q3 = quantile(TWITTER_FOLLOWER_COUNT_MILLIONS, .75),
            max = max(TWITTER_FOLLOWER_COUNT_MILLIONS))
## # A tibble: 1 x 6
##
      mean
             min
                     Q1 median
                                   QЗ
     <dbl> <dbl> <dbl> <dbl> <dbl> <dbl> <
## 1 1.60 0.002 0.0595 0.246 0.912
nba_social_power_mod %>%
  arrange(desc(TWITTER_FOLLOWER_COUNT_MILLIONS)) %>%
  head(2)
## # A tibble: 2 x 15
##
     PLAYER_NAME TEAM_ABBREVIATI~
                                     AGE W_PCT OFF_RATING DEF_RATING NET_RATING
                                   <int> <dbl>
##
     <chr>>
                 <chr>>
                                                    <dbl>
                                                                <dbl>
                                                                           <dbl>
## 1 LeBron Jam~ CLE
                                                                             7.7
                                      32 0.689
                                                     115.
                                                                 107.
## 2 Kevin Dura~ GSW
                                      28 0.823
                                                     117.
                                                                 101.
                                                                            16
## # ... with 8 more variables: AST_RATIO <dbl>, REB_PCT <dbl>,
       USG_PCT <dbl>, PIE <dbl>, SALARY_MILLIONS <dbl>,
## #
       ACTIVE_TWITTER_LAST_YEAR <int>, TWITTER_FOLLOWER_COUNT_MILLIONS <dbl>,
       PTS <dbl>
```

From the histogram, we can see that the distribution of Twitter follower counts is extremely right-skewed. The number of Twitter followers ranges from .002 million to 37 million, with a mean of 1.6 million and a

median of .246 million. There are two obvious outliers: Kevin Durant, with 16.2 million followers, and LeBron James, with 37 million followers.

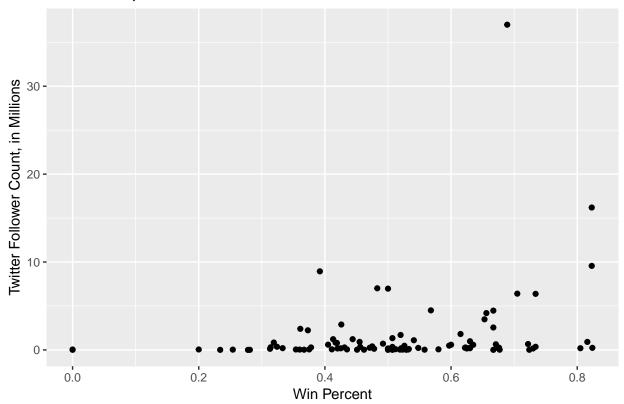
Bivariate

Next, we will do bivariate EDA, looking into the relationships of some of the predictor variables with the response variables. We won't do bivariate EDA on player name, Twitter handle, age, team abbreviation, or whether the players were active on Twitter last year, instead focusing on terms we believe may play a more nuanced / important role in predicting Twitter followers. Complete bivariate EDA is in additional analysis; here, only those variables with evident relationships to the response are included.

First, we'll look for a relationship between win percent and Twitter followers in millions:

```
ggplot(nba_social_power_mod, aes(x = W_PCT, y = TWITTER_FOLLOWER_COUNT_MILLIONS)) +
    geom_point() +
    labs(title = "Relationship Between Win Percent and Twitter Follower Count",
    x = "Win Percent", y = "Twitter Follower Count, in Millions")
```

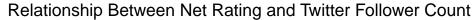
Relationship Between Win Percent and Twitter Follower Count

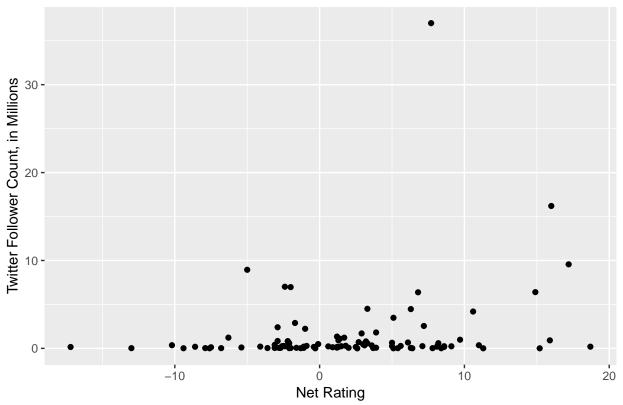


From the above plot, we can see that win percent and Twitter follower count may have a very weak positive orrelations. The players with significantly higher-than-average Twitter follower counts tend to have higher win percentages; however, this relationship is very weak.

Next, we'll look at the relationship between net rating, which combines offensive and defensive rating, and Twitter follower count:

```
ggplot(nba_social_power_mod, aes(x = NET_RATING, y = TWITTER_FOLLOWER_COUNT_MILLIONS)) +
   geom_point() +
   labs(title = "Relationship Between Net Rating and Twitter Follower Count",
        x = "Net Rating", y = "Twitter Follower Count, in Millions")
```

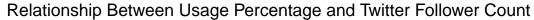


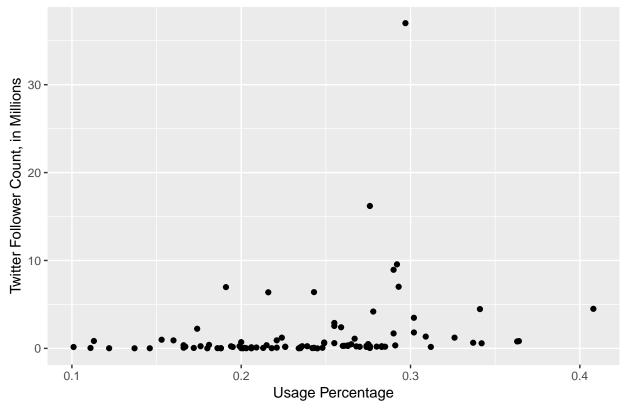


Similarly to win percent, Twitter follower count and net rating seem to have a very weak positive relationship. The players with the highest net ratings more often have higher-than-average Twitter follower counts, and more players with positive net ratings have high Twitter follower counts than those with negative net ratings.

Next, we'll examine whether there is a relationship between usage percentage and Twitter follower count:

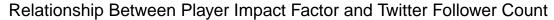
```
ggplot(nba_social_power_mod,
    aes(x = USG_PCT,
        y = TWITTER_FOLLOWER_COUNT_MILLIONS)) +
geom_point() +
labs(title = "Relationship Between Usage Percentage and Twitter Follower Count",
    x = "Usage Percentage",
    y = "Twitter Follower Count, in Millions")
```

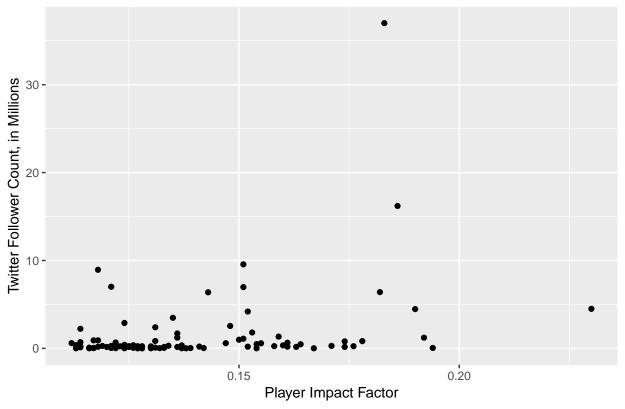




There appears to be a very weak positive correlation between usage percentage and Twitter follower count; players with a high usage percentage tend to have more Twitter followers, on average, than those with a lower usage percentage.

Next, we'll examine whether there is a relationship between player impact factor and Twitter follower count:

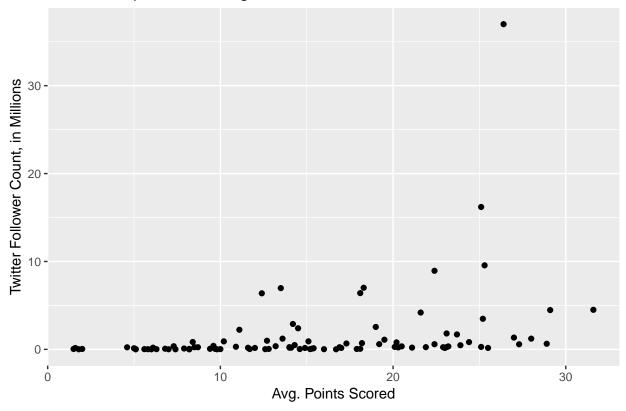




There appears to be a somewhat positive correlation between player impact factor and Twitter follower count; players with a high player impact factor tend to have more Twitter followers, on average, than those with a lower player impact factor.

Now, we'll look for a relationship between average points scored per game and Twitter follower count:

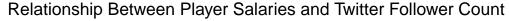
Relationship Between Avg. Points Scored and Twitter Follower Count

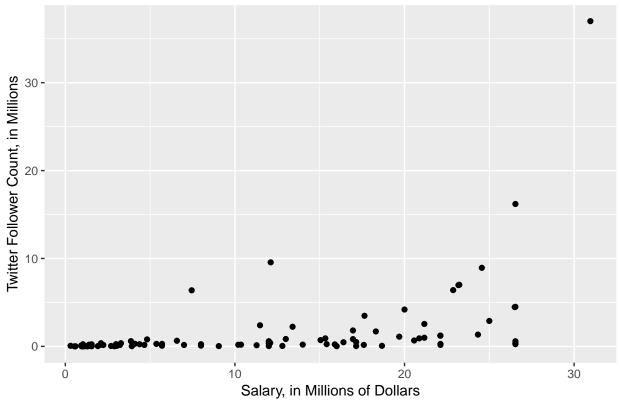


There appears to be a weak positive correlation between average points scored and Twitter follower count; players with higher avg. points scored tend to have more Twitter followers than those with lower avg. points scored.

Finally, we'll look for a relationship between player salaries and points scored:

```
ggplot(nba_social_power_mod, aes(x = SALARY_MILLIONS, y = TWITTER_FOLLOWER_COUNT_MILLIONS)) +
   geom_point() +
   labs(title = "Relationship Between Player Salaries and Twitter Follower Count",
        x = "Salary, in Millions of Dollars",
        y = "Twitter Follower Count, in Millions")
```





There appears to be a positive correlation between salary and Twitter follower count; the players with higher salaries tend to have higher Twitter follower counts.

In sum, there appear to be weak to moderate positive correlations between Twitter follower count and win percentage, net rating, usage percentage, player impact factor, avg. points per game, and player salaries; there is no obvious relationship between Twitter follower count and assist-to-turnover ratio or rebound percentage.

Multivariate Data Analysis

Now, we'll do some multivariate analysis. In this section, we are looking for predictor variables that may affect the way other predictor variables relate to the response variable.

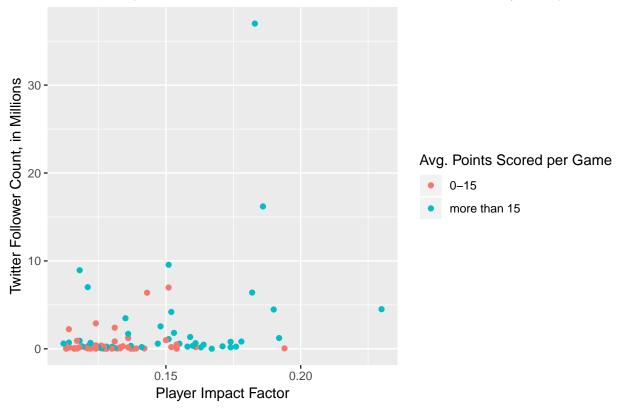
First, we'll look to see if points scored affects the way player impact factor (PIE) relates to Twitter follower count:

```
nba_social_power_mod1 <- nba_social_power_mod %>%
  mutate(PTS_CAT = case_when(
    PTS <= 15 ~ "0-15" ,
    PTS > 15 ~ "more than 15"
))

ggplot(data = nba_social_power_mod1,
    aes(x = PIE,
        y = TWITTER_FOLLOWER_COUNT_MILLIONS,
        color = PTS_CAT)) +
    geom_point() +
  labs(x = "Player Impact Factor",
    y = "Twitter Follower Count, in Millions",
```

```
color = "Avg. Points Scored per Game",
title = "Relationship Between Pts Scored, Twitter Followers, and Player Impact Factor")
```

Relationship Between Pts Scored, Twitter Followers, and Player Impact Fact



As we can see from the above color-coded boxplot, many of the players with the most points scored have higher player impact factors, and player impact factor values have a weak positive correlation with the Twitter follower count. This could be an opportunity for an interaction term.

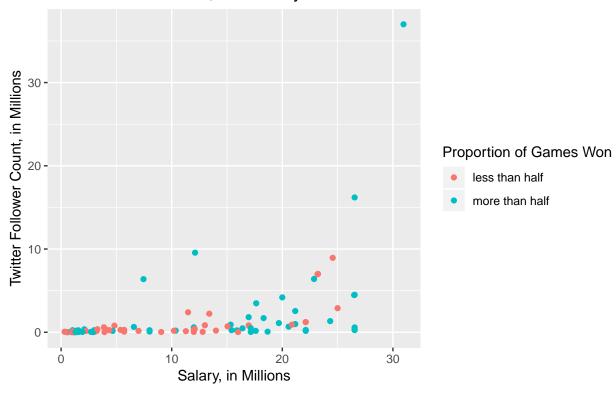
Next, we'll try to determine whether win percentage affects the way salary relates to the Twitter follower count:

```
nba_social_power_mod1 <- nba_social_power_mod %>%
  mutate(W_PCT_CAT = case_when(
    W_PCT <= .5 ~ "less than half" ,
    W_PCT > .5 ~ "more than half" ))

ggplot(data = nba_social_power_mod1,
    aes(x = SALARY_MILLIONS,
        y = TWITTER_FOLLOWER_COUNT_MILLIONS,
        color = W_PCT_CAT)) +
    geom_point() +

labs(x = "Salary, in Millions",
    y = "Twitter Follower Count, in Millions",
    color = "Proportion of Games Won",
    title = "Relationship Between Win Percentage,
    Twitter Followers, and Salary")
```

Relationship Between Win Percentage, Twitter Followers, and Salary



As we can see from the scatterplot, players with higher win percentages tend to be paid more, and high salary has a weak positive correlation with the Twitter follower count. This could also be an opportunity for an interaction term.

Adjustments (Mean-Centering)

Before we proceed with the analysis, we will mean-center the quantitative variables:

Modeling Approach

As our response, TWITTER_FOLLOWER_COUNT_MILLIONS, is a continuous numerical variable, we will use a multiple linear regression model (obviously, we plan to include two or more predictors, so simple linear regression would not apply!).

In regard to model selection, we will begin by fitting a mutiple linear regression model with main effects, as well as interaction effects. We are considering salary_millionsCent * w_pctCent and PIECent * ptsCent as potential interaction terms for our model since multivariate EDA highlighted strong positive relationships between win percentage and player salaries and points scored and PIE (player impact factor).

Next, we will perform two iterations of backward selection on the first model: (i) using AIC as the selection criterion and (ii) using adjusted R-squared as the selection criterion. We decided against trying BIC as the selection criterion because we would prefer more terms in the final model as our objective is to predict the Twitter follower counts of NBA players using measures of athletic success (and predictions are generally more accurate with more relevant predictor variables).

After completing the two iterations of backward selection, we will compare the resulting models and see whether certain terms are removed in both (which would suggest those terms are not statistically significant).

After obtaining a final model, we will determine whether prominent athletes (e.g. LeBron James) are influential points by looking at standardized residuals, leverage, and Cook's Distance (this is important since our objective is to design a model with the best predictive accuracy). We will then learn the impact of including versus excluding prominent athletes in our model. We choose to analyze this at the end of the model selection phase because prominent athletes are also included in the population we want to understand when fitting the multiple linear regression model.

Model 1

We will simply fit a model with eleven main effect terms—ageCent, ast_ratioCent off_ratingCent, def_ratingCent, PIECent, reb_pctCent, usg_pctCent, salary_millionsCent, w_pctCent, ptsCent, and ACTIVE_TWITTER_LAST_YEAR—and two interaction terms (salary_millionsCent * w_pctCent and PIECent * ptsCent). We decided to use off_ratingCent and def_ratingCent as opposed to net_ratingCent because the two individual components potentially provide more important information in predicting the number of Twitter followers.

```
m1 <- lm(TWITTER FOLLOWER COUNT MILLIONS ~ ageCent +
           ast ratioCent +
           off ratingCent +
           def_ratingCent +
           PIECent +
           reb pctCent +
           usg_pctCent +
           salary_millionsCent +
           w_pctCent +
           ptsCent +
           ACTIVE_TWITTER_LAST_YEAR +
           salary millionsCent * w pctCent +
           PIECent * ptsCent,
         data = nba_social_power_mod)
tidy(m1, conf.int = TRUE) %>%
  kable(format = "markdown", digits = 3)
```

| term | estimate | std.error | statistic | p.value | conf.low | conf.high |
|----------------|----------|-----------|-----------|---------|----------|-----------|
| (Intercept) | -2.386 | 2.744 | -0.869 | 0.387 | -7.845 | 3.074 |
| ageCent | 0.262 | 0.123 | 2.131 | 0.036 | 0.017 | 0.507 |
| ast_ratioCent | 0.017 | 0.064 | 0.269 | 0.788 | -0.109 | 0.144 |
| off_ratingCent | 0.026 | 0.106 | 0.247 | 0.805 | -0.185 | 0.237 |
| def_ratingCent | 0.086 | 0.118 | 0.732 | 0.467 | -0.149 | 0.321 |
| PIECent | 13.104 | 27.617 | 0.474 | 0.636 | -41.846 | 68.053 |
| reb_pctCent | 7.689 | 12.120 | 0.634 | 0.528 | -16.426 | 31.803 |

| term | estimate | std.error | statistic | p.value | conf.low | conf.high |
|-----------------------------------|----------|-----------|-----------|---------|----------|-----------|
| usg_pctCent | 0.052 | 14.017 | 0.004 | 0.997 | -27.838 | 27.942 |
| salary_millionsCent | 0.086 | 0.070 | 1.240 | 0.219 | -0.052 | 0.225 |
| $w_pctCent$ | 7.095 | 3.834 | 1.850 | 0.068 | -0.534 | 14.725 |
| ptsCent | 0.063 | 0.132 | 0.481 | 0.632 | -0.199 | 0.325 |
| ACTIVE_TWITTER_LAST_YEAR | 3.523 | 2.758 | 1.278 | 0.205 | -1.964 | 9.011 |
| $salary_millionsCent:w_pctCent$ | 0.999 | 0.344 | 2.901 | 0.005 | 0.314 | 1.684 |
| PIECent:ptsCent | 1.293 | 2.293 | 0.564 | 0.574 | -3.269 | 5.855 |

Based on the output, the equation of the linear model is: TWITTER_FOLLOWER_COUNT_MILLIONS-hat = -2.386 + 0.262 * ageCent + 0.017 * ast_ratioCent + 0.026 * off_ratingCent + 0.086 * def_ratingCent + 13.104 * PIECent + 7.689 * reb_pctCent + 0.052 * usg_pctCent + 0.086 * salary_millionsCent + 7.095 * w_pctCent + 0.063 * ptsCent + 3.523 * ACTIVE_TWITTER_LAST_YEAR1 + 0.999 * salary_millionsCent * w_pct_Cent + 1.293 * PIECent * ptsCent.

Backward Selection (Iteration 1)

We will now perform the first iteration of backward selection using AIC as the selection criterion:

```
m1_aic <- step(m1, direction = "backward")</pre>
## Start: AIC=265.14
## TWITTER_FOLLOWER_COUNT_MILLIONS ~ ageCent + ast_ratioCent + off_ratingCent +
       def_ratingCent + PIECent + reb_pctCent + usg_pctCent + salary_millionsCent +
       w_pctCent + ptsCent + ACTIVE_TWITTER_LAST_YEAR + salary_millionsCent *
##
##
       w_pctCent + PIECent * ptsCent
##
##
                                                   RSS
                                   Df Sum of Sq
                                                          AIC
## - usg_pctCent
                                          0.000 1153.0 263.14
## - off_ratingCent
                                          0.869 1153.8 263.21
                                    1
## - ast_ratioCent
                                          1.033 1154.0 263.23
                                    1
## - PIECent:ptsCent
                                   1
                                          4.525 1157.5 263.51
## - reb pctCent
                                          5.729 1158.7 263.61
## - def_ratingCent
                                         7.619 1160.6 263.77
                                    1
## - ACTIVE TWITTER LAST YEAR
                                         23.232 1176.2 265.04
## <none>
                                                1153.0 265.14
                                         64.667 1217.6 268.32
## - ageCent
                                    1
## - salary_millionsCent:w_pctCent 1
                                        119.780 1272.7 272.53
##
## Step: AIC=263.14
## TWITTER_FOLLOWER_COUNT_MILLIONS ~ ageCent + ast_ratioCent + off_ratingCent +
       def_ratingCent + PIECent + reb_pctCent + salary_millionsCent +
##
       w_pctCent + ptsCent + ACTIVE_TWITTER_LAST_YEAR + salary_millionsCent:w_pctCent +
##
##
       PIECent:ptsCent
##
                                   Df Sum of Sq
                                                   RSS
                                          0.879 1153.8 261.21
## - off_ratingCent
                                    1
## - ast ratioCent
                                          1.119 1154.1 261.23
                                   1
## - PIECent:ptsCent
                                   1
                                          4.673 1157.6 261.52
## - reb_pctCent
                                   1
                                          6.349 1159.3 261.66
## - def_ratingCent
                                    1
                                          7.812 1160.8 261.78
## - ACTIVE_TWITTER_LAST_YEAR
                                  1
                                         23.398 1176.4 263.05
                                                1153.0 263.14
## <none>
```

```
## - ageCent
                                         65.008 1218.0 266.35
                                    1
## - salary_millionsCent:w_pctCent 1
                                        120.208 1273.2 270.56
## Step: AIC=261.21
## TWITTER_FOLLOWER_COUNT_MILLIONS ~ ageCent + ast_ratioCent + def_ratingCent +
       PIECent + reb pctCent + salary millionsCent + w pctCent +
       ptsCent + ACTIVE TWITTER LAST YEAR + salary millionsCent:w pctCent +
##
##
       PIECent:ptsCent
##
##
                                   Df Sum of Sq
                                                   RSS
                                                           AIC
## - ast_ratioCent
                                          1.551 1155.4 259.34
## - PIECent:ptsCent
                                          3.809 1157.7 259.53
                                    1
## - reb_pctCent
                                    1
                                          6.572 1160.4 259.75
                                         10.226 1164.1 260.05
## - def_ratingCent
                                    1
## - ACTIVE_TWITTER_LAST_YEAR
                                         23.162 1177.0 261.10
                                    1
## <none>
                                                1153.8 261.21
## - ageCent
                                         64.179 1218.0 264.36
                                    1
## - salary_millionsCent:w_pctCent 1
                                        144.592 1298.4 270.43
## Step: AIC=259.34
## TWITTER_FOLLOWER_COUNT_MILLIONS ~ ageCent + def_ratingCent +
       PIECent + reb_pctCent + salary_millionsCent + w_pctCent +
       ptsCent + ACTIVE_TWITTER_LAST_YEAR + salary_millionsCent:w_pctCent +
##
##
       PIECent:ptsCent
##
                                   Df Sum of Sq
                                                   RSS
## - PIECent:ptsCent
                                          5.074 1160.5 257.76
                                    1
                                          5.330 1160.7 257.78
## - reb_pctCent
                                    1
## - def_ratingCent
                                         10.283 1165.7 258.18
                                    1
## - ACTIVE_TWITTER_LAST_YEAR
                                    1
                                         24.144 1179.5 259.31
## <none>
                                                1155.4 259.34
## - ageCent
                                    1
                                         64.470 1219.9 262.50
## - salary_millionsCent:w_pctCent 1
                                       156.501 1311.9 269.41
## Step: AIC=257.76
## TWITTER_FOLLOWER_COUNT_MILLIONS ~ ageCent + def_ratingCent +
       PIECent + reb pctCent + salary millionsCent + w pctCent +
##
       ptsCent + ACTIVE_TWITTER_LAST_YEAR + salary_millionsCent:w_pctCent
##
##
                                   Df Sum of Sq
                                                   RSS
                                                           AIC
## - ptsCent
                                        6.132 1166.6 256.26
## - reb_pctCent
                                          8.021 1168.5 256.41
                                    1
## - def ratingCent
                                         10.161 1170.6 256.58
                                    1
## - PIECent
                                         12.392 1172.9 256.77
                                    1
## - ACTIVE_TWITTER_LAST_YEAR
                                         23.951 1184.4 257.70
                                    1
                                                1160.5 257.76
## <none>
                                         70.150 1230.6 261.33
## - ageCent
                                    1
## - salary_millionsCent:w_pctCent 1
                                        164.153 1324.6 268.32
## Step: AIC=256.26
## TWITTER_FOLLOWER_COUNT_MILLIONS ~ ageCent + def_ratingCent +
       PIECent + reb_pctCent + salary_millionsCent + w_pctCent +
##
##
       ACTIVE_TWITTER_LAST_YEAR + salary_millionsCent:w_pctCent
##
```

```
##
                                   Df Sum of Sq
                                                   RSS
## - reb_pctCent
                                    1
                                          3.143 1169.7 254.51
## - def_ratingCent
                                         11.861 1178.5 255.22
## <none>
                                                1166.6 256.26
## - ACTIVE_TWITTER_LAST_YEAR
                                    1
                                         25.646 1192.2 256.32
## - PIECent
                                        31.477 1198.1 256.79
                                    1
## - ageCent
                                         64.560 1231.2 259.37
                                    1
## - salary_millionsCent:w_pctCent 1
                                       158.085 1324.7 266.33
##
## Step: AIC=254.51
## TWITTER_FOLLOWER_COUNT_MILLIONS ~ ageCent + def_ratingCent +
       PIECent + salary_millionsCent + w_pctCent + ACTIVE_TWITTER_LAST_YEAR +
##
##
       salary_millionsCent:w_pctCent
##
##
                                   Df Sum of Sq
                                                   RSS
                                                           AIC
## - def_ratingCent
                                         11.079 1180.8 253.41
                                                1169.7 254.51
## <none>
## - ACTIVE_TWITTER_LAST_YEAR
                                         25.350 1195.1 254.55
                                    1
## - PIECent
                                        36.705 1206.5 255.45
                                    1
## - ageCent
                                    1
                                         62.548 1232.3 257.46
## - salary_millionsCent:w_pctCent 1
                                       155.368 1325.1 264.36
## Step: AIC=253.41
## TWITTER_FOLLOWER_COUNT_MILLIONS ~ ageCent + PIECent + salary_millionsCent +
       w_pctCent + ACTIVE_TWITTER_LAST_YEAR + salary_millionsCent:w_pctCent
##
##
##
                                   Df Sum of Sq
                                                   RSS
## - ACTIVE_TWITTER_LAST_YEAR
                                         25.051 1205.9 253.40
                                    1
## <none>
                                                1180.8 253.41
## - PIECent
                                    1
                                         32.005 1212.8 253.95
## - ageCent
                                    1
                                         54.622 1235.4 255.70
## - salary_millionsCent:w_pctCent 1
                                        162.024 1342.8 263.62
##
## Step: AIC=253.4
## TWITTER_FOLLOWER_COUNT_MILLIONS ~ ageCent + PIECent + salary_millionsCent +
       w_pctCent + salary_millionsCent:w_pctCent
##
##
                                   Df Sum of Sq
                                                   RSS
                                                           AIC
## <none>
                                                1205.9 253.40
## - PIECent
                                         29.646 1235.5 253.71
## - ageCent
                                         60.024 1265.9 256.02
                                    1
## - salary_millionsCent:w_pctCent 1
                                        158.457 1364.3 263.13
tidy(m1 aic, conf.int = TRUE) %>%
 kable(format = "markdown", digits = 3)
```

| term | estimate | $\operatorname{std.error}$ | statistic | p.value | conf.low | conf.high |
|-----------------------------------|----------|----------------------------|-----------|---------|----------|-----------|
| (Intercept) | 1.175 | 0.397 | 2.957 | 0.004 | 0.386 | 1.964 |
| ageCent | 0.225 | 0.107 | 2.105 | 0.038 | 0.013 | 0.437 |
| PIECent | 27.461 | 18.565 | 1.479 | 0.143 | -9.427 | 64.349 |
| salary_millionsCent | 0.111 | 0.051 | 2.158 | 0.034 | 0.009 | 0.213 |
| $w_pctCent$ | 6.294 | 2.761 | 2.280 | 0.025 | 0.808 | 11.780 |
| $salary_millionsCent:w_pctCent$ | 1.019 | 0.298 | 3.420 | 0.001 | 0.427 | 1.611 |

Based on the output displayed above from the first iteration of backward selection (using AIC as the selection criterion), seven main effect terms (ast_ratioCent off_ratingCent, def_ratingCent, reb_pctCent, usg_pctCent, ptsCent, and ACTIVE_TWITTER_LAST_YEAR1) and one interaction term (PIECent * ptsCent) were removed.

Hence, the equation of the selected linear model is: TWITTER_FOLLOWER_COUNT_MILLIONS-hat = 1.175 + 0.225 * ageCent + 27.461 * PIECent + 0.111 * salary_millionsCent + 6.294 * w_pctCent + 1.019 * salary_millionsCent * w_pctCent.

However, PIECent, which has the highest slope coefficient in the linear model, has a high standard error and a high p-value (0.143). Furthermore, the confidence interval for the slope coefficient is extremely wide (-9.427 to 64.349), not to mention the fact that it includes zero. So, we can reasonably infer PIECent may be a particularly troublesome predictor in the model (especially since it appears to not significantly affect the response, TWITTER_FOLLOWER_COUNT_MILLIONS).

We will proceed with the second iteration of backward selection and will revisit the issue of PIECent after viewing the selected linear regression model based on adjusted R-squared.

Backward Selection (Iteration 2)

Next, we will perform the second iteration of backward selection using adjusted R-squared as the selection criterion:

```
m1_adjR <- regsubsets(TWITTER_FOLLOWER_COUNT_MILLIONS ~ ageCent +</pre>
           ast ratioCent +
           off_ratingCent +
           def_ratingCent +
           PIECent +
           reb pctCent +
           usg_pctCent +
           salary millionsCent +
           w pctCent +
           ptsCent +
           ACTIVE_TWITTER_LAST_YEAR +
           salary_millionsCent * w_pctCent +
           PIECent * ptsCent,
         data = nba_social_power_mod,
         method = "backward")
select_summary <- summary(m1_adjR)</pre>
coef(m1_adjR, which.max(select_summary$adjr2))
```

```
##
                      (Intercept)
                                                          ageCent
##
                       -2.3794214
                                                        0.2146898
##
                          PIECent
                                             salary_millionsCent
##
                       28.5598883
                                                        0.1148099
##
                        w_pctCent
                                        ACTIVE_TWITTER_LAST_YEAR
                        6.6375685
##
                                                        3.6257226
## salary millionsCent:w pctCent
                        1.0306857
```

Based on the output displayed above from the second iteration of backward selection (using adjusted R-squared as the selection criterion), six main effect terms (ast_ratioCent off_ratingCent, def_ratingCent, reb_pctCent, usg_pctCent, and ptsCent) and one interaction term (PIECent * ptsCent) were removed.

Hence, the equation of the selected linear model is: TWITTER_FOLLOWER_COUNT_MILLIONS-hat = -2.379 +

```
0.215 * ageCent + 28.560 * PIECent + 0.115 * salary_millionsCent + 6.638 * w_pctCent + 3.626 * ACTIVE_TWITTER_LAST_YEAR1 + 1.031 * salary_millionsCent * w_pct_Cent.
```

Model Comparison: AIC vs. Adjusted R-squared

We notice that the model selected using adjusted R-squared as the selection criterion includes an additional categorical term (ACTIVE_TWITTER_LAST_YEAR1) which was omitted in the model selected based on the first iteration of backward selection (using AIC as the selection criterion).

If we closely investigate the results of the step() function, we can see that ACTIVE_TWITTER_LAST_YEAR was the last predictor removed during the first iteration of backward selection. In fact, the difference in AIC between the final two steps is only 253.41 - 253.4 = 0.01.

This warrants further consideration:

| term | estimate | std.error | statistic | p.value | conf.low | conf.high |
|-----------------------------------|----------|-----------|-----------|---------|----------|-----------|
| (Intercept) | -2.379 | 2.631 | -0.904 | 0.368 | -7.608 | 2.850 |
| ageCent | 0.215 | 0.106 | 2.018 | 0.047 | 0.003 | 0.426 |
| salary_millionsCent | 0.115 | 0.051 | 2.244 | 0.027 | 0.013 | 0.216 |
| PIECent | 28.560 | 18.493 | 1.544 | 0.126 | -8.190 | 65.310 |
| $w_pctCent$ | 6.638 | 2.759 | 2.406 | 0.018 | 1.155 | 12.120 |
| ACTIVE_TWITTER_LAST_YEAR | 3.626 | 2.654 | 1.366 | 0.175 | -1.648 | 8.899 |
| $salary_millionsCent:w_pctCent$ | 1.031 | 0.297 | 3.475 | 0.001 | 0.441 | 1.620 |

Based on the p-value associated with the slope coefficient for ACTIVE_TWITTER_LAST_YEAR1 (0.175) and the confidence interval associated with this coefficient (-1.648 to 8.899; includes zero), it is clear that ACTIVE_TWITTER_LAST_YEAR is not a significant predictor of TWITTER_FOLLOWER_COUNT_MILLIONS.

Again, recalling our objective in this analysis—to predict Twitter follower counts of NBA players—we choose to leave ACTIVE_TWITTER_LAST_YEAR out of the final model because, although the information provided by this categorical variable may, at first glance, appear relevant to the response, TWITTER_FOLLOWER_COUNT_MILLIONS (which measures players' total Twitter follower counts), the p-value and confidence interval associated with this predictor's slope coefficient suggests otherwise. When designing a model for predictive purposes, we are mostly interested in variables which are strong predictors of the response. Hence, we concur with the model selected by backward selection using AIC as the selection criterion in regard to ACTIVE_TWITTER_LAST_YEAR.

Now, as promised, we return to the issue of PIECent. Unfortunately, both selected models included PIECent; thus, we must decide whether to keep the variable in the model, or to ignore the results from the two iterations of backward selection and remove it.

To answer this question, we will compare the AIC and adjusted R-squared values for the model selected based on AIC as the selection criterion (first iteration) and the same model except without PIECent, remembering that we have already excluded ACTIVE_TWITTER_LAST_YEAR:

```
m1_modV2 <- lm(TWITTER_FOLLOWER_COUNT_MILLIONS ~ ageCent +</pre>
               salary millionsCent +
               PIECent +
               w_pctCent +
               salary_millionsCent * w_pctCent,
             data = nba_social_power_mod)
m1_modV3 <- lm(TWITTER_FOLLOWER_COUNT_MILLIONS ~ ageCent +
                 salary_millionsCent +
                 w_pctCent +
                 salary_millionsCent * w_pctCent,
               data = nba social power mod)
glance(m1 modV2)$AIC
## [1] 525.001
glance(m1 modV2)$adj.r.squared
## [1] 0.3141706
glance(m1_modV3)$AIC
## [1] 525.3083
glance(m1_modV3)$adj.r.squared
```

[1] 0.3051171

Based on the output of the glance() function, the AIC of the model with PIECent is 525.001. Conversely, the AIC of the model without PIECent is 525.3083.

Moreover, the adjusted R-squared value for the model with PIECent is roughly 0.314, whereas the adjusted R-squared value for the model without PIECent is about 0.305.

Therefore, the model with PIECent maximizes adjusted R-squared and minimizes AIC. But our qualms with the large standard error, high p-value, and wide confidence interval (including zero) cannot be ignored, especially considering the purpose of our analysis-prediction. Hence, as with ACTIVE_TWITTER_LAST_YEAR, we will leave PIECent out of the model because including a variable which is not a strong predictor of the response will result in wider prediction intervals.

Of course, this means the only measures of athletic success remaining in the model are: mean-centered win percentage and (to a lesser degree due to salary cap restrictions) player salaries. Nevertheless, we have tailored our model selection phase towards our objective–predicting the number of Twitter followers–and cannot be too upset since such a model will yield relatively narrow prediction intervals.

Now, examining the current model:

```
tidy(m1_modV3, conf.int = TRUE) %>%
kable(format = "markdown", digits = 3)
```

| term | estimate | std.error | statistic | p.value | conf.low | conf.high |
|-----------------------------------|----------|-----------|-----------|---------|----------|-----------|
| (Intercept) | 1.142 | 0.399 | 2.859 | 0.005 | 0.348 | 1.935 |
| ageCent | 0.192 | 0.105 | 1.829 | 0.071 | -0.017 | 0.401 |
| salary_millionsCent | 0.137 | 0.048 | 2.844 | 0.006 | 0.041 | 0.234 |
| $w_pctCent$ | 7.131 | 2.720 | 2.622 | 0.010 | 1.727 | 12.535 |
| $salary_millionsCent:w_pctCent$ | 1.099 | 0.295 | 3.729 | 0.000 | 0.514 | 1.685 |

But now we notice another problem: ageCent has a high p-value (0.071) and a confidence interval including zero. Hence, we will also remove ageCent using the same rationale as with ACTIVE_TWITTER_LAST_YEAR and PIECent.

Final Model

Thus, our final model is:

| term | estimate | std.error | statistic | p.value | conf.low | conf.high |
|-----------------------------------|----------|-----------|-----------|---------|----------|-----------|
| (Intercept) | 1.184 | 0.404 | 2.933 | 0.004 | 0.382 | 1.986 |
| salary_millionsCent | 0.163 | 0.047 | 3.479 | 0.001 | 0.070 | 0.256 |
| $w_pctCent$ | 7.761 | 2.733 | 2.840 | 0.006 | 2.334 | 13.189 |
| $salary_millionsCent:w_pctCent$ | 0.997 | 0.293 | 3.401 | 0.001 | 0.415 | 1.579 |

The equation of the final model is: TWITTER_FOLLOWER_COUNT_MILLIONS-hat = 1.184 + 0.163 * salary_millionsCent + 7.761 * w_pctCent + 0.997 * salary_millionsCent * w_pct_Cent.

Impact of Prominent Players

Lastly, before proceeding to discuss assumptions, we would like to examine the impact of including versus excluding prominent athletes in our model. Since he is widely regarded as one of the best NBA players of all-time, we will use LeBron James as a case study for preliminary analysis:

```
## 2 Russell Westbrook
                                   26.5
## 3 Kevin Durant
                                   26.5
## 4 Mike Conley
                                   26.5
## 5 DeMar DeRozan
                                   26.5
## 6 Al Horford
                                   26.5
## 7 James Harden
                                   26.5
## 8 Dirk Nowitzki
                                   25
                                   24.6
## 9 Carmelo Anthony
## 10 Damian Lillard
                                   24.3
```

```
nba_social_power_mod %>%
arrange(desc(TWITTER_FOLLOWER_COUNT_MILLIONS)) %>%
```

```
select(PLAYER_NAME, TWITTER_FOLLOWER_COUNT_MILLIONS) %>%
head(10)
## # A tibble: 10 x 2
```

```
PLAYER_NAME
                        TWITTER_FOLLOWER_COUNT_MILLIONS
##
##
      <chr>
##
   1 LeBron James
                                                   37
##
   2 Kevin Durant
                                                   16.2
## 3 Stephen Curry
                                                    9.56
## 4 Carmelo Anthony
                                                    8.94
## 5 Dwyane Wade
                                                    7.01
## 6 Dwight Howard
                                                    6.97
## 7 Chris Paul
                                                    6.4
## 8 Pau Gasol
                                                    6.38
## 9 Russell Westbrook
                                                    4.5
## 10 James Harden
                                                    4.47
```

Based on the tables above, it is seems like LeBron James is an outlier, both in regard to his annual salary and Twitter follower count. So, we will remove LeBron from the dataset and see how the model changes:

```
nba_social_power_mod2 <- nba_social_power_mod %>%
  filter(PLAYER_NAME != "LeBron James")
glimpse(nba_social_power_mod2)
```

```
## Observations: 94
## Variables: 26
## $ PLAYER NAME
                                     <chr> "Russell Westbrook", "Demetriu...
                                     <chr> "OKC", "BOS", "NOP", "HOU", "G...
## $ TEAM_ABBREVIATION
## $ AGE
                                     <int> 28, 22, 24, 27, 28, 32, 26, 22...
## $ W_PCT
                                     <dbl> 0.568, 0.200, 0.413, 0.667, 0....
## $ OFF_RATING
                                     <dbl> 107.9, 124.2, 104.2, 113.6, 11...
                                     <dbl> 104.6, 117.8, 102.5, 107.3, 10...
## $ DEF RATING
## $ NET_RATING
                                     <dbl> 3.3, 6.3, 1.7, 6.3, 16.0, 14.9...
## $ AST RATIO
                                     <dbl> 23.4, 31.1, 7.3, 27.6, 18.4, 3...
                                     <dbl> 0.167, 0.103, 0.170, 0.123, 0....
## $ REB_PCT
## $ USG_PCT
                                     <dbl> 0.408, 0.172, 0.326, 0.341, 0....
## $ PIE
                                     <dbl> 0.230, 0.194, 0.192, 0.190, 0....
## $ SALARY_MILLIONS
                                     <dbl> 26.54, 1.45, 22.12, 26.50, 26....
## $ ACTIVE_TWITTER_LAST_YEAR
                                     <int> 1, 1, 1, 1, 1, 1, 1, 1, 0, 1, ...
## $ TWITTER_FOLLOWER_COUNT_MILLIONS <dbl> 4.500, 0.049, 1.220, 4.470, 16...
## $ PTS
                                     <dbl> 31.6, 2.0, 28.0, 29.1, 25.1, 1...
## $ ageCent
                                     <dbl> 0.6105263, -5.3894737, -3.3894...
## $ ast ratioCent
                                     <dbl> 6.274737, 13.974737, -9.825263...
## $ off ratingCent
                                     <dbl> -0.009473684, 16.290526316, -3...
## $ def_ratingCent
                                     <dbl> -1.39368421, 11.80631579, -3.4...
## $ net_ratingCent
                                     <dbl> 1.3810526, 4.3810526, -0.21894...
                                     <dbl> 0.09073684, 0.05473684, 0.0527...
## $ PIECent
## $ reb_pctCent
                                     <dbl> 0.033778947, -0.030221053, 0.0...
## $ usg pctCent
                                     <dbl> 0.170, -0.066, 0.088, 0.103, 0...
                                     <dbl> 15.2351368, -9.8548632, 10.815...
## $ salary_millionsCent
                                     <dbl> 0.056589474, -0.311410526, -0....
## $ w pctCent
                                     <dbl> 16.3176842, -13.2823158, 12.71...
## $ ptsCent
```

Based on the glimpse() output, we can see LeBron has been removed from the dataset (94 observations

remaining).

Now, to assess the impact of his absence on the final model:

| term | estimate | std.error | statistic | p.value | conf.low | conf.high |
|-----------------------------------|----------|-----------|-----------|---------|----------|-----------|
| (Intercept) | 1.087 | 0.229 | 4.742 | 0.000 | 0.632 | 1.543 |
| salary_millionsCent | 0.109 | 0.027 | 4.035 | 0.000 | 0.055 | 0.162 |
| $w_pctCent$ | 4.609 | 1.568 | 2.940 | 0.004 | 1.495 | 7.724 |
| $salary_millionsCent:w_pctCent$ | 0.431 | 0.171 | 2.513 | 0.014 | 0.090 | 0.771 |

The equation of the final model without LeBron James is: TWITTER_FOLLOWER_COUNT_MILLIONS-hat = $1.087 + 0.109 * \text{salary_millionsCent} + 4.609 * \text{w_pctCent} + 0.431 * \text{salary_millionsCent} * \text{w_pct_Cent}$.

```
nba_social_power_mod %>%
arrange(desc(W_PCT)) %>%
select(PLAYER_NAME, W_PCT) %>%
head(15)
```

```
## # A tibble: 15 x 2
##
      PLAYER_NAME
                        W_PCT
##
      <chr>>
                        <dbl>
##
  1 David West
                        0.824
##
   2 Kevin Durant
                        0.823
## 3 Stephen Curry
                        0.823
## 4 Draymond Green
                        0.816
## 5 JaVale McGee
                        0.805
## 6 Pau Gasol
                        0.734
## 7 David Lee
                        0.734
## 8 Kawhi Leonard
                        0.73
## 9 Dewayne Dedmon
                        0.724
## 10 LaMarcus Aldridge 0.722
## 11 Chris Paul
                        0.705
## 12 LeBron James
                        0.689
## 13 Clint Capela
                        0.677
## 14 Al Horford
                        0.676
## 15 George Hill
                        0.673
```

Comparing the two equations, we notice a relatively sizable discrepancy in the slope coefficient of $w_pctCent$. This makes sense since LeBron has the twelfth-highest win percentage in the league (0.689), so eliminating him from the dataset dramatically affects the average win percentage (as well as the spread, or standard deviation).

More generally, to determine whether prominent athletes are influential points, we will look at standardized residuals, leverage, and Cook's Distance:

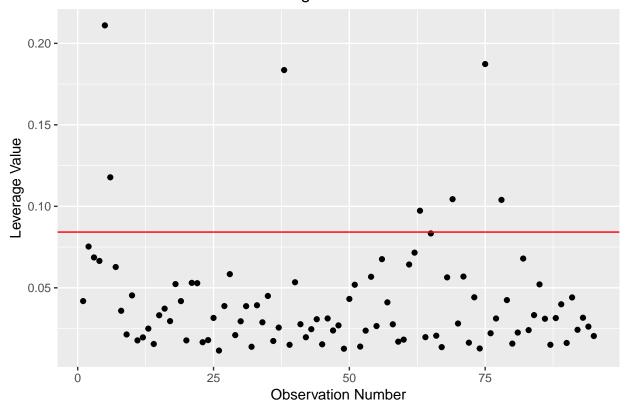
```
augmented_data <- augment(m_final)
augmented_data <- augmented_data %>%
```

```
mutate(obs_num = row_number())

threshold <- ((2 * (3 + 1)) / 95)

ggplot(data = augmented_data, aes(x = obs_num, y = .hat)) +
    geom_point() +
    geom_hline(yintercept = threshold, color = "red") +
    labs(x = "Observation Number",
        y = "Leverage Value",
        title = "Observation Number vs. Leverage Value")</pre>
```

Observation Number vs. Leverage Value



```
augmented_data %>%
filter(.hat > threshold) %>%
select(obs_num, .hat)
```

```
## # A tibble: 7 x 2
##
     obs_num
             .hat
       <int> <dbl>
##
## 1
          5 0.211
## 2
          6 0.118
## 3
          38 0.184
## 4
          63 0.0973
## 5
          69 0.104
          75 0.187
## 6
## 7
         78 0.104
```

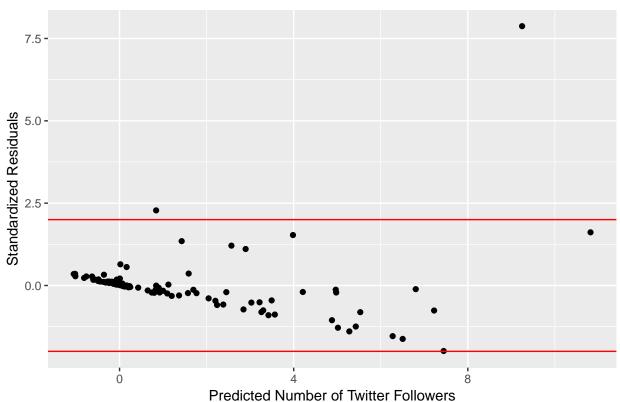
```
## # A tibble: 7 x 2
    obs num PLAYER NAME
##
       <int> <chr>
## 1
          5 Kevin Durant
## 2
          6 LeBron James
## 3
          38 Josh Huestis
## 4
          63 JaVale McGee
          69 David West
## 5
## 6
          75 Jarnell Stokes
## 7
          78 Carmelo Anthony
```

Based on the threshold (2(p + 1) / n), Kevin Durant, LeBron James, Josh Huestis, JaVale McGee, David West, Jarnell Stokes, and Carmelo Anthony are considered high leverage players (and hence potential influential points).

Now, to identify outliers within these candidates, we will look at the standardized residuals:

```
ggplot(data = augmented_data, aes(x = .fitted, y = .std.resid)) +
  geom_point() +
  geom_hline(yintercept = 2, color = "red") +
  geom_hline(yintercept = -2, color = "red") +
  labs(x = "Predicted Number of Twitter Followers",
        y = "Standardized Residuals",
        title = "Standardized Residuals vs. Predicted Twitter Follower Counts")
```

Standardized Residuals vs. Predicted Twitter Follower Counts



```
filter(.std.resid > 2 | .std.resid < -2) %>%
  select(obs_num, .std.resid)
## # A tibble: 2 x 2
##
     obs_num .std.resid
##
       <int>
                   <dbl>
## 1
                   7.87
           6
          78
                   2.28
nba_std_resid <- nba_social_power_mod %>%
  mutate(obs_num = row_number()) %>%
  filter(obs_num == 6 | obs_num == 78)
nba_std_resid %>%
```

```
## # A tibble: 2 x 2
## obs_num PLAYER_NAME
## <int> <chr>
## 1 6 LeBron James
## 2 78 Carmelo Anthony
```

select(obs_num, PLAYER_NAME)

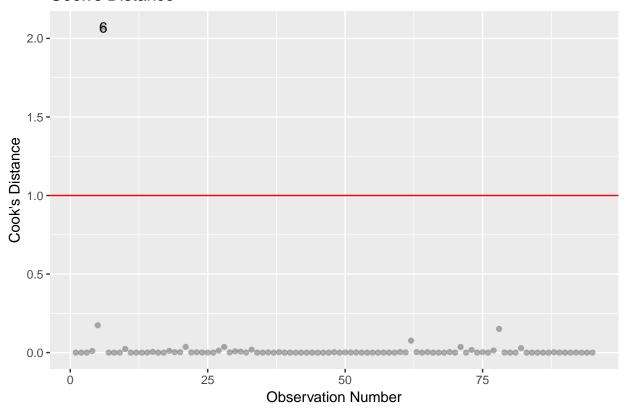
augmented_data %>%

The players with standardized residuals of magnitude greater than 2 are LeBron James and Carmelo Anthony—two players who are also classified as high leverage points. By definition, LeBron and Carmelo are outliers; however, it remains to be seen whether Carmelo impacts the regression line (we already examined LeBron's effect).

To assess the impact of prominent athletes (identified by high leverage and/or high standardized residuals)

on the regression line, we examine Cook's Distance:

Cook's Distance



```
nba_std_resid %>%
filter(obs_num == 6) %>%
select(obs_num, PLAYER_NAME)
```

```
## # A tibble: 1 x 2
## obs_num PLAYER_NAME
## <int> <chr>
## 1 6 LeBron James
```

It is clear from the plot of Cook's Distance vs. observation number that LeBron James is the only influential point.

Since our objective is to accurately predict the Twitter follower counts of NBA players, it is probably best to exclude LeBron to avoid overestimating for less prominent athletes. Hence, we will continue our analysis by using the multiple linear regression model without LeBron James (m_final_noLJ).

To conclude, we will display the final model once more:

```
tidy(m_final_noLJ, conf.int = TRUE) %>%
kable(format = "markdown", digits = 3)
```

| term | estimate | std.error | statistic | p.value | conf.low | conf.high |
|-----------------------------------|----------|-----------|-----------|---------|----------|-----------|
| (Intercept) | 1.087 | 0.229 | 4.742 | 0.000 | 0.632 | 1.543 |
| salary_millionsCent | 0.109 | 0.027 | 4.035 | 0.000 | 0.055 | 0.162 |
| $w_pctCent$ | 4.609 | 1.568 | 2.940 | 0.004 | 1.495 | 7.724 |
| $salary_millionsCent:w_pctCent$ | 0.431 | 0.171 | 2.513 | 0.014 | 0.090 | 0.771 |

Discussion of Assumptions

According to our dataset, 5 observations have players who are missing Twitter handles. These values are missing at random because missingness depends on other observed variables (like the person's social media usage, etc.). The probability that a variable is missing depends on information not included in our dataset. We decided to remove the 5 players from our dataset because there were very few observations with missing values, and after removing these variables, we still had 95 observations. The observations with missingness are also random, so the resulting analysis will not be biased because the missingness does not differ systematically from the complete observations. In addition, since our objective is predicting the number of Twitter followers for NBA athletes, players without Twitter accounts are outside of the model's predictive capabilities and hence do not belong in the dataset.

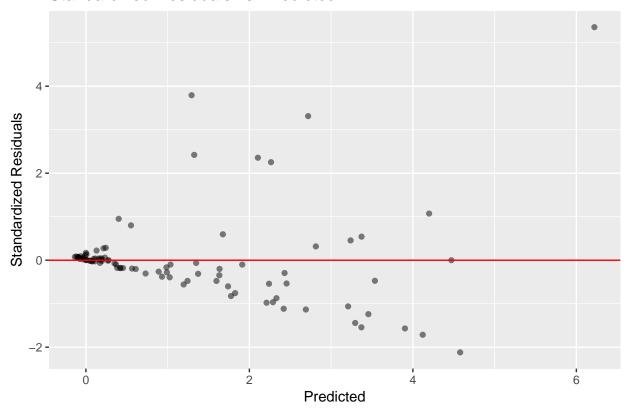
One other modification we have made to our original dataset is removing LeBron James. We decided, based on Cook's distance, standardized residuals, and leverage, LeBron was an influential point with a significant effect on the regression line. Consequently, we removed LeBron to avoid overestimation in our model. Because we removed LeBron, we will use standardized residuals from here on out

Therefore, we are left with 94 observations, which is still a large enough sample population to build a model which can be generalized to a larger population of NBA athletes.

Next, we will check the linearity, constant variance, normality, and independence assumptions to see if inference and predictions will be reliable.

First, we will check for linearity and whether the response variable has a linear relationship with the predictor variables in the model. We will check the plot of standardized residuals vs. predicted values:

Standardized Residuals vs. Predicted



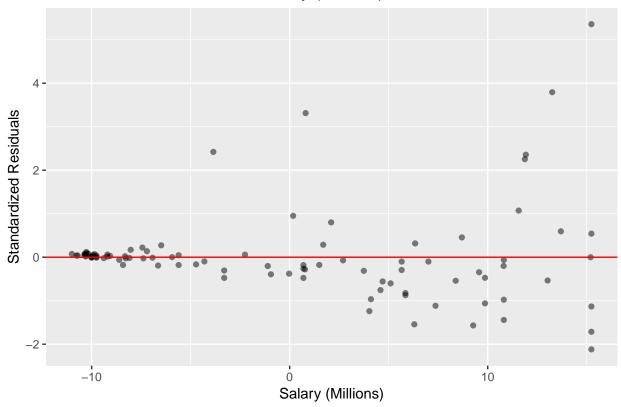
When observing for constant variance, the height of the cloud of points seems to increase as you move from left to right. Points are clustered at the very left then grow to be more spare as you move along the graph. Therefore, constant variance is not satisfied.

There is no obvious pattern and the shape of the graph seems to be linear. Hence, this plot presents no issues with the linearity assumption.

Next, we will observe the plot of residuals vs. predictors:

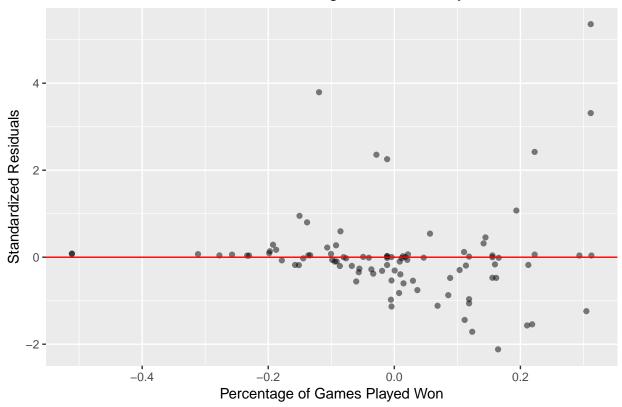
```
ggplot(data = m_final_aug, aes(x = salary_millionsCent, y = .std.resid)) +
geom_point(alpha = 0.5) +
geom_hline(yintercept = 0, color = "red") +
labs(x = "Salary (Millions)", y = "Standardized Residuals",
    title = "Standardized Residuals vs. Salary (Millions)")
```

Standardized Residuals vs. Salary (Millions)



There looks to be a pattern in the plot because towards the end it curves upward drastically. Therefore, this pattern suggests that interactions or higher-order terms (like quadratic terms) are required. Thus, linearity is not satisfied.

Standardized Residuals vs. Percentage of Games Played Won



There looks to be a pattern in the plot because towards the end it also curves upward drastically. Therefore, this pattern suggests that interactions or higher-order terms (like quadratic terms) are required. Linearity is not satisfied.

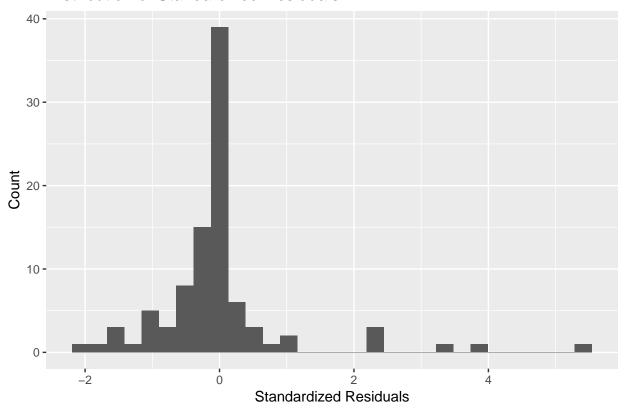
Next, we will check for the normality assumption by creating a histogram of the residuals and a normal QQ-plot of the residuals.

```
nba_social_power_mod2 <- nba_social_power_mod2 %>%
    mutate(predicted = predict.lm(m_final_noLJ), std_resid = rstandard(m_final_noLJ))

ggplot(data = nba_social_power_mod2, mapping = aes(x = std_resid)) + geom_histogram() + labs(title = "D")

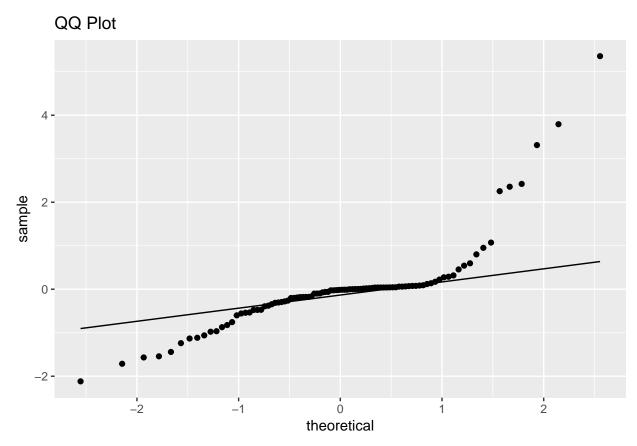
## `stat_bin()` using `bins = 30`. Pick better value with `binwidth`.
```

Distribution of Standardized Residuals



Normality is violated because the histogram of residuals is heavily right skewed because the height of the graphs decreases dramatically from right to left.

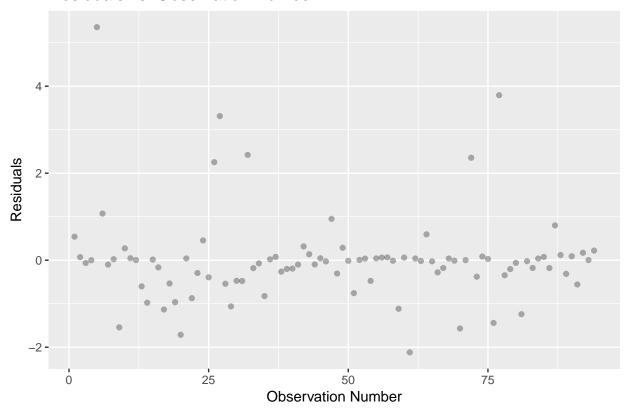
ggplot(data = nba_social_power_mod2, mapping = aes(sample = std_resid)) + stat_qq() + stat_qq_line() +



However, normality is not satisfied because some of the points don't follow the diagonal line.

Lastly, we will check for independence. Data was not taken over time, so we know there is no temporal correlation. There is also no spatial correlation because data was not taken in space. We can check to see if there is some structure/order to the dataset according to observation number. There is no purposeful order to how the dataset was collected according to Kaggle, but we will check just in case:

Residuals vs. Observation Number



Looking at the graph, there is no distinguishable pattern in the graph. The number of Twitter followers of one player will not affect the number of Twitter followers of another player. Therefore, independence is satisfied.

Therefore, because constant variance and normality and linearity are not satisfied, but independence is, we will make some adjustments to our model. We can adjust for linearity by adding squared terms for salary and percentage of games played won because those standardized residuals vs. predictor variable plots violated linearity. For constant variance, we can log-transform the response variable because our standardized residuals vs. predicted values violated constant variance. Lastly, for normality regression there were outliers observed in the histograms, so we can try to remove all 7 outlier players from our model as mentioned previously above because Kevin Durant, LeBron James, Josh Huestis, JaVale McGee, David West, Jarnell Stokes, and Carmelo Anthony are considered high leverage players (and hence potential influential points).

After making these adjustments our model looks like this:

| term | estimate | std.error | statistic | p.value | conf.low | conf.high |
|-----------------------------------|----------|-----------|-----------|---------|----------|-----------|
| (Intercept) | -1.169 | 0.279 | -4.188 | 0.000 | -1.725 | -0.614 |
| salary_millionsCent | 0.148 | 0.020 | 7.532 | 0.000 | 0.109 | 0.187 |
| I(salary_millionsCent * | -0.004 | 0.003 | -1.592 | 0.115 | -0.010 | 0.001 |
| salary_millionsCent) | | | | | | |
| $w_pctCent$ | 2.081 | 1.218 | 1.708 | 0.091 | -0.342 | 4.505 |
| I(w_pctCent * w_pctCent) | 6.565 | 7.571 | 0.867 | 0.388 | -8.496 | 21.625 |
| $salary_millionsCent:w_pctCent$ | -0.109 | 0.173 | -0.629 | 0.531 | -0.454 | 0.236 |

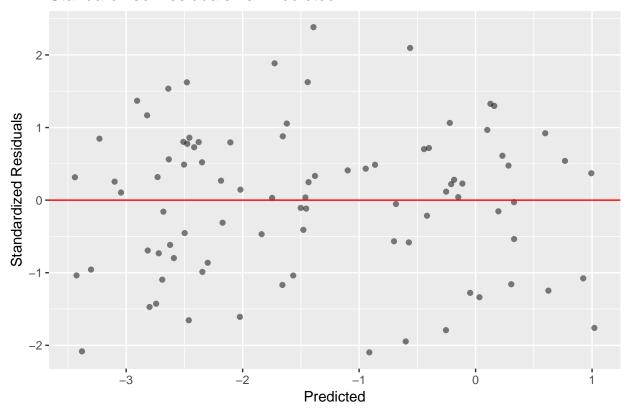
However, because the interaction effect and w_pctCent squared terms and the salary_millionsCent have p-values that are very large and > 0.05, we will remove them from our model to produce this model. We will attempt to see if the log transformation of our response variable is enough to support our assumptions.

| term | estimate | std.error | statistic | p.value | conf.low | conf.high |
|---------------------|----------|-----------|-----------|---------|----------|-----------|
| (Intercept) | -1.398 | 0.149 | -9.370 | 0.000 | -1.694 | -1.101 |
| salary_millionsCent | 0.133 | 0.018 | 7.250 | 0.000 | 0.097 | 0.170 |
| $w_pctCent$ | 2.336 | 1.152 | 2.029 | 0.046 | 0.047 | 4.626 |

We will check for all assumptions again:

First, we will check for linearity and whether the response variable has a linear relationship with the predictor variables in the model. We will check the plot of standardized residuals vs. predicted values:

Standardized Residuals vs. Predicted



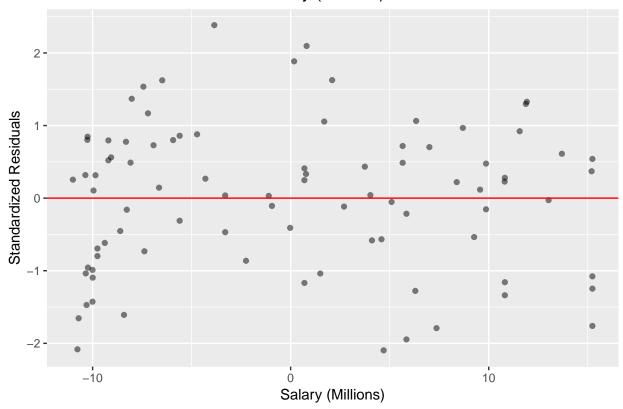
When observing for constant variance, the height of the cloud of points seems to be constant as you move from left to right. Therefore, constant variance is satisfied.

There is no obvious pattern and the shape of the graph seems to be linear. Hence, this plot presents no issues with the linearity assumption.

Next, we will observe the plot of residuals vs. predictors:

```
ggplot(data = m_final_adj_aug, aes(x = salary_millionsCent, y = .std.resid)) +
  geom_point(alpha = 0.5) +
  geom_hline(yintercept = 0, color = "red") +
  labs(x = "Salary (Millions)", y = "Standardized Residuals",
      title = "Standardized Residuals vs. Salary (Millions)")
```

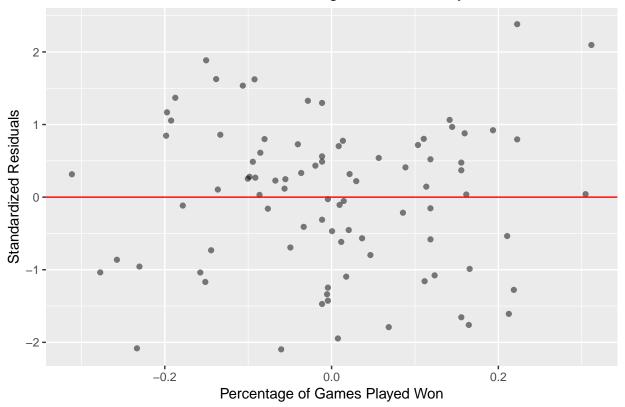
Standardized Residuals vs. Salary (Millions)



There is no distinguishable pattern in our plot because there are no discernible curves. Therefore, we satisfy linearity.

```
ggplot(data = m_final_adj_aug, aes(x = w_pctCent, y = .std.resid)) +
  geom_point(alpha = 0.5) +
  geom_hline(yintercept = 0, color = "red") +
  labs(x = "Percentage of Games Played Won", y = "Standardized Residuals",
      title = "Standardized Residuals vs. Percentage of Games Played Won")
```

Standardized Residuals vs. Percentage of Games Played Won

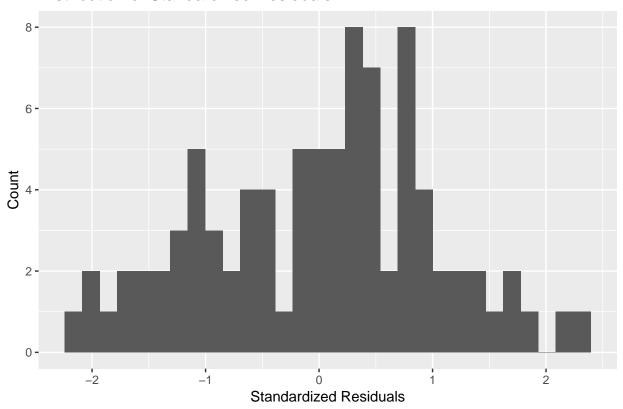


There looks to be no distinguishable pattern in the plot as well, so therefore linearity is supported because there have been previous violations of linearity.

Next, we will check for the normality assumption by creating a histogram of the residuals and a normal QQ-plot of the residuals.

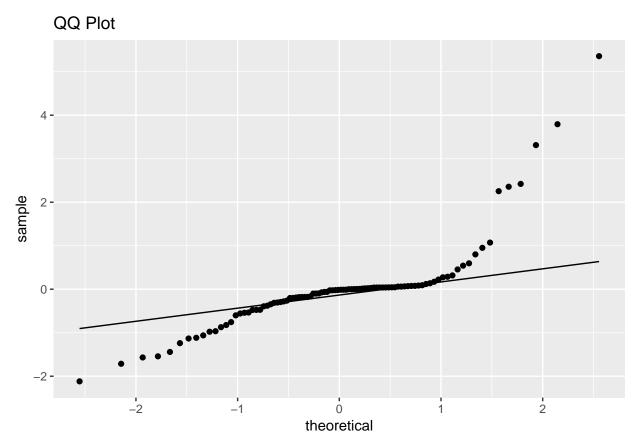
`stat_bin()` using `bins = 30`. Pick better value with `binwidth`.

Distribution of Standardized Residuals



Normality is not supported because the histogram of residuals is not normal and is now slightly left skewed because the height increases as you move across the graph, then drastically decreases, but the distribution is unimodal.

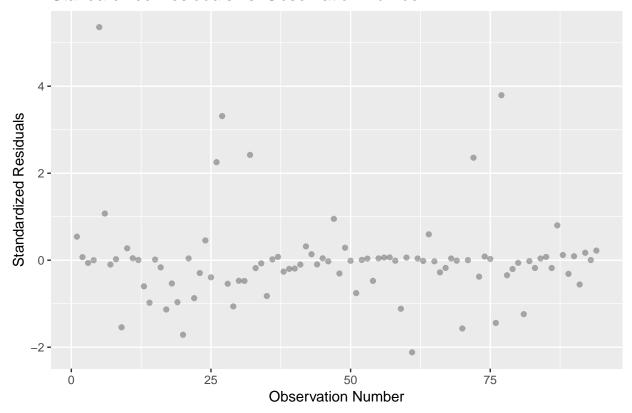
```
ggplot(data = nba_social_power_mod2, mapping = aes(sample = std_resid)) + stat_qq() + stat_qq_line() +
```



However, normality is not satisfied because some of the points don't follow the diagonal line.

Lastly, we will check for independence. Data was not taken over time, so we know there is no temporal correlation. There is also no spatial correlation because data was not taken in space. We can check to see if there is some structure/order to the dataset according to observation number. There is no purposeful order the data was collected in according to Kaggle, but we will check just in case:

Standardized Residuals vs. Observation Number



Looking at the graph, there is no distinguishable pattern in the graph. The number of Twitter followers of one player will not affect the number of Twitter followers of another player. Therefore, independence is satisfied.

Linearity, constant variance, and normality are all satisfied in this model. We have done everything we can to the best of our knowledge to fix normality, so we will continue on with this model for interpretations. Our final model output is:

```
tidy(m_final_adjust, conf.int = TRUE) %>%
kable(format = "markdown", digits = 3)
```

| term | estimate | std.error | statistic | p.value | conf.low | conf.high |
|------------------------|----------|-----------|-----------|---------|----------|-----------|
| (Intercept) | -1.398 | 0.149 | -9.370 | 0.000 | -1.694 | -1.101 |
| $salary_millionsCent$ | 0.133 | 0.018 | 7.250 | 0.000 | 0.097 | 0.170 |
| $w_pctCent$ | 2.336 | 1.152 | 2.029 | 0.046 | 0.047 | 4.626 |

TWITTER FOLLOWER COUNT MILLIONS LOG-hat = -1.401 + 0.133* salary millionsCent + 2.442* pct Cent

The p-values for each of these predictor variables are all < 0.05, so we know each of the predictor variables is a significant predictor for our response variable.

Lastly, we will also check for multicollinearity in our model. If two or more predictor variables are highly correlated in our model, our regression may change eratically in response to small changes in our data.

We will check the variance inflation factor (VIF) for every predictor variable to check for concerns with multicollinearity:

None of the variables have VIFs greater than or equal to 10, so there are no issues with multicollinearity.

Interpretations

Additional Analysis

Complete EDA:

The plots that were included in the EDA in the main body of our analysis are NOT included again here, only the ones that were created but we did not decide to include above.

Univariate

First, we will do univariate EDA on the dataset. Player name will be used to refer to observations in our dataset, but since each player name is distinct we do not need to do EDA on the PLAYER_NAME variable.

Here, we'll take a look at how many players there are from each team in the dataset:

```
nba_social_power_mod %>%
  count(TEAM_ABBREVIATION) %>%
  arrange(n)
```

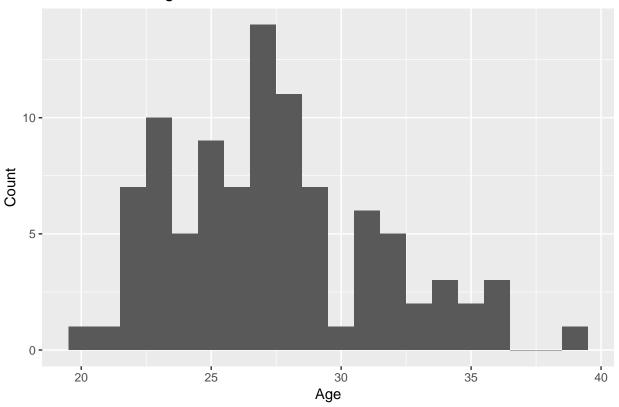
```
## # A tibble: 30 x 2
##
      TEAM_ABBREVIATION
                              n
##
      <chr>
                          <int>
##
    1 SAC
                              1
    2 CHI
##
                              2
##
    3 IND
                              2
                              2
##
    4 LAL
##
   5 MIA
                              2
                              2
##
    6 MIN
##
    7 ORL
                              2
##
    8 WAS
                              2
##
   9 ATL
                              3
## 10 BKN
                              3
## # ... with 20 more rows
```

As we can see from the output, there is only one team that is represented just once in the dataset: SAC, the Sacramento Kings. The greatest number of times teams are represented in the dataset is 5. GSW (Golden State Warriors), LAC (Los Angeles Clippers), and SAS (San Antonio Spurs) are all represented 5 times.

Now, we'll explore the distribution of the AGE variable in the dataset:

```
ggplot(data = nba_social_power_mod, aes(x= AGE)) +
  geom_histogram(binwidth = 1) +
  labs(x = "Age", y = "Count", title = "Distribution of Age")
```

Distribution of Age



```
nba_social_power_mod %>%
  summarise(mean = mean(AGE), min= min(AGE), Q1 = quantile(AGE, .25), median = median(AGE),
            Q3 = quantile(AGE, .75),
            \max = \max(AGE))
## # A tibble: 1 x 6
##
                    Q1 median
                                  QЗ
      mean
             min
                                       max
##
     <dbl> <dbl> <dbl> <dbl> <dbl> <dbl> <
## 1 27.4
              20 24.5
                            27
                                  29
nba_social_power_mod %>%
  arrange(desc(AGE)) %>%
 head(1)
## # A tibble: 1 x 26
                                     AGE W_PCT OFF_RATING DEF_RATING NET_RATING
##
     PLAYER_NAME TEAM_ABBREVIATI~
```

```
##
     <chr>>
                 <chr>>
                                   <int> <dbl>
                                                    <dbl>
                                                               <dbl>
                                                                           <dbl>
## 1 Dirk Nowit~ DAL
                                      39 0.426
                                                     105.
                                                                 106.
                                                                            -1.7
## # ... with 19 more variables: AST_RATIO <dbl>, REB_PCT <dbl>,
       USG_PCT <dbl>, PIE <dbl>, SALARY_MILLIONS <dbl>,
       ACTIVE_TWITTER_LAST_YEAR <int>, TWITTER_FOLLOWER_COUNT_MILLIONS <dbl>,
## #
## #
       PTS <dbl>, ageCent <dbl>, ast_ratioCent <dbl>, off_ratingCent <dbl>,
## #
       def_ratingCent <dbl>, net_ratingCent <dbl>, PIECent <dbl>,
## #
       reb_pctCent <dbl>, usg_pctCent <dbl>, salary_millionsCent <dbl>,
```

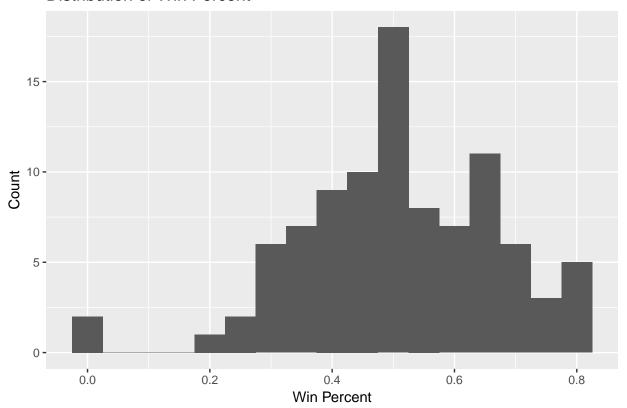
```
## # w_pctCent <dbl>, ptsCent <dbl>
```

As we can see from the histogram, age is somewhat normally distributed in the dataset, with a mode around 27 and a surprisingly low number of 30-year olds. The mean age, 27.39, and median age, 27, are very close together, indicating little skew. The lowest age is 20 and the highest is 39. The oldest player by far, at 39, is Dirk Nowitzki.

Now, we'll examine the distribution of win percent, W_PCT:

```
ggplot(data = nba_social_power_mod, aes(x= W_PCT)) +
geom_histogram(binwidth = .05) +
labs(x = "Win Percent", y = "Count", title = "Distribution of Win Percent")
```

Distribution of Win Percent



```
## # A tibble: 1 x 6
## mean min Q1 median Q3 max
## <dbl> <dbl> <dbl> <dbl> <dbl> <dbl> <dbl> 3 0.507 0.63 0.824
```

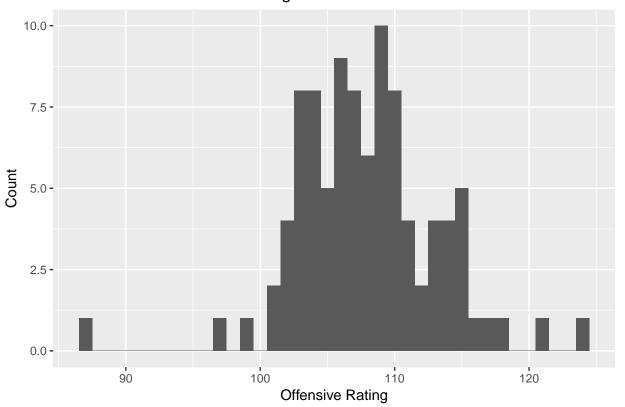
As we can see from the histogram, win percent is also somewhat normally distributed, with a mode around 50 percent. The minimum win percent in the dataset is 0, while the maximum is 82.4. The median of 50.7 is very similar to the mean of 51%. The fact that the mean and median win percents in the dataset fall so close to 50% indicate good randomness in the dataset, b/c the mean and median win percents for all nba players are 50%.

Next, we'll look at the distributions for offensive rating, OFF_RATING and defensive rating DEF_RATING, as

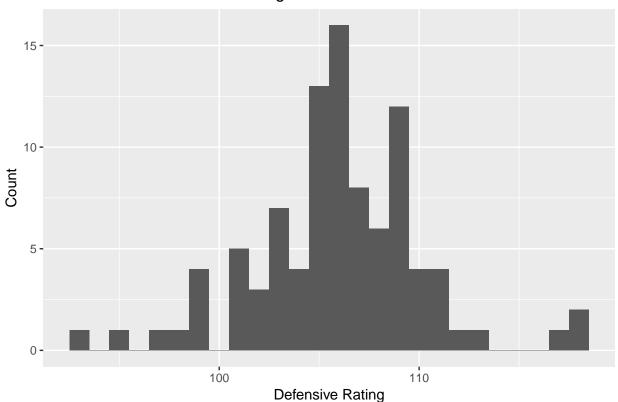
well as the distribution for NET_RATING, which is the average of the offensive and defensive rating:

```
ggplot(data = nba_social_power_mod, aes(x= OFF_RATING)) +
geom_histogram(binwidth = 1) +
labs(x = "Offensive Rating", y = "Count",
    title = "Distribution of Offensive Rating")
```

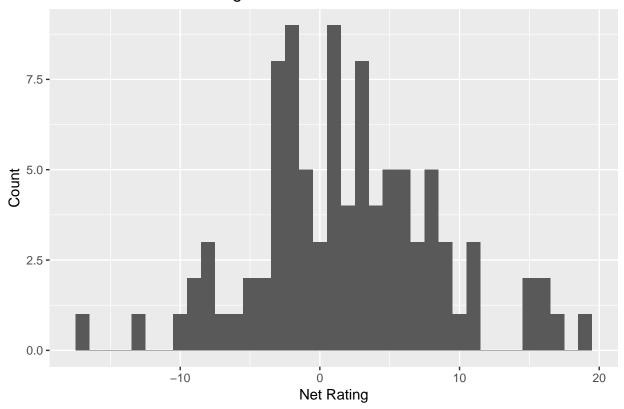
Distribution of Offensive Rating



Distribution of Defensive Rating



Distribution of Net Rating



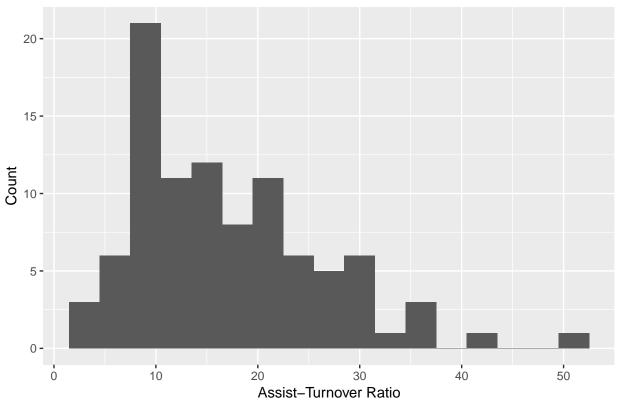
```
## # A tibble: 1 x 3
## min median max
## <dbl> <dbl> <dbl> <dbl> ## 1 -17.2 1.5 18.7
```

Defensive rating, offensive rating, and net rating do not stray far from normally distributed. Offensive rating varies from 86.8 to 124.2, with a median of 107.6. Defensive rating varies from 93 to 118.3, with a median of 106. Thus, the dataset contains a larger range in terms of offensive rating, and the median is also slightly higher for defensive rated players. The distribution of net rating has multiple nearly equal modes around -2 to -3 and around 1 and 3. The median net rating is 1.5, and the net ratings in the dataset vary from -17.2 to 18.7.

Next, we'll look at the distribution of the assist-to-turnovers ratio, AST_RATIO:

```
ggplot(data = nba_social_power_mod, aes(x= AST_RATIO)) +
geom_histogram(binwidth = 3) +
labs(x = "Assist-Turnover Ratio", y = "Count",
    title = "Distribution of Assist-Turnover Ratio")
```

Distribution of Assist-Turnover Ratio



```
nba_social_power_mod %>%
  summarise(mean = mean(AST_RATIO),
            min= min(AST_RATIO),
            Q1 = quantile(AST RATIO, .25),
            median = median(AST_RATIO),
            Q3 = quantile(AST RATIO, .75),
            max = max(AST_RATIO))
## # A tibble: 1 x 6
      mean min
                    Q1 median
##
                                 QЗ
     <dbl> <dbl> <dbl> <dbl> <dbl> <dbl> <
               4 9.75
                           15 22.2 51.5
## 1 17.1
nba_social_power_mod %>%
  arrange(desc(AST_RATIO)) %>%
  head(2)
## # A tibble: 2 x 26
##
     PLAYER_NAME TEAM_ABBREVIATI~
                                    AGE W_PCT OFF_RATING DEF_RATING NET_RATING
##
     <chr>
                 <chr>
                                  <int> <dbl>
                                                    <dbl>
                                                               <dbl>
                                                                          <dbl>
## 1 Jarnell St~ DEN
                                      23 0
                                                                           -3.1
                                                     115.
                                                                118.
                                      26 0.373
## 2 Ricky Rubio MIN
                                                     109.
                                                                110.
                                                                           -1
## # ... with 19 more variables: AST_RATIO <dbl>, REB_PCT <dbl>,
       USG_PCT <dbl>, PIE <dbl>, SALARY_MILLIONS <dbl>,
## #
       ACTIVE_TWITTER_LAST_YEAR <int>, TWITTER_FOLLOWER_COUNT_MILLIONS <dbl>,
       PTS <dbl>, ageCent <dbl>, ast_ratioCent <dbl>, off_ratingCent <dbl>,
## #
## #
       def_ratingCent <dbl>, net_ratingCent <dbl>, PIECent <dbl>,
## #
       reb_pctCent <dbl>, usg_pctCent <dbl>, salary_millionsCent <dbl>,
```

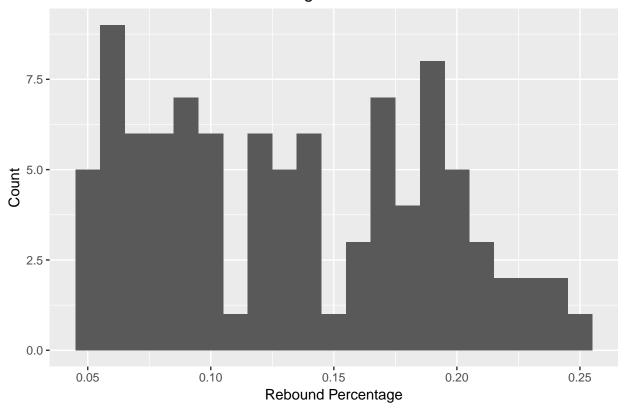
w_pctCent <dbl>, ptsCent <dbl>

As we can see from the histogram, the assist-turnover ratio is very right skewed. The mode is at around 10, even though the median is at 15, and the mean is 17.12526, all of which are summary statistics that emphasize the right skew. This means that while most players in the dataset had a very high assist-turnover ratio (meaning they had many more assists than turnovers), there is a wider variation among players with a high ratio and the players with lower ratios are concentrated around a few numbers. The dataset minimum ratio of 4 means that there were no players with more turnovers than assists. Notably, this is the first variable we've examined so far with a significantly non-normal distribution. The two players with very high assist-turnover ratios, 51.5 and 41.3, are Jarnell Stokes and Ricky Rubio, respectively.

Next, we'll examine the variation of REB_PCT, the percent of rebounds a player makes:

```
ggplot(data = nba_social_power_mod, aes(x= REB_PCT)) +
geom_histogram(binwidth = .01) +
labs(x = "Rebound Percentage", y = "Count",
    title = "Distribution of Rebound Percentage")
```

Distribution of Rebound Percentage



```
nba_social_power_mod %>%
summarise(mean = mean(REB_PCT),
    min= min(REB_PCT),
    Q1 = quantile(REB_PCT, .25),
    median = median(REB_PCT),
    Q3 = quantile(REB_PCT, .75),
    max = max(REB_PCT))
```

```
## # A tibble: 1 x 6
## mean min Q1 median Q3 max
## <dbl> <dbl> <dbl> <dbl> <dbl> <dbl>
```

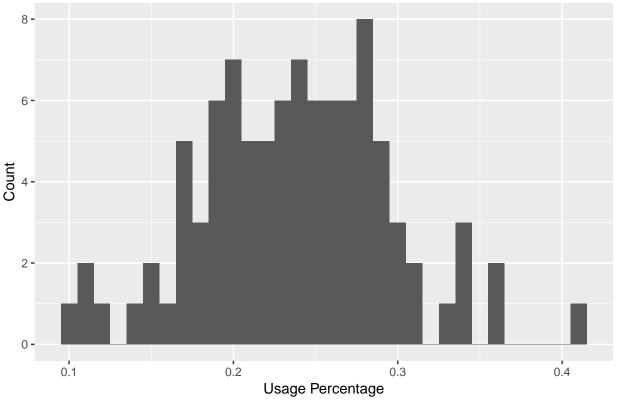
```
## 1 0.133 0.045 0.0825 0.127 0.180 0.252
```

The distribution of rebound percentage has a minimum of 0.045 and a maximum of 0.252. The distribution is not very skewed one way or another, as supported by the similar mean of .133 and median of .127. However, the distribution is not normal in that it does not resemble a bell curve; with exceptions, the data is somewhat evenly distributed from the minimum to near the maximum (although there is some trail-off towards the right side of the distribution). This non-normal spread is likely partially an indication of the fact that the dataset contains both offensive and defensive players, because whether a player is on offense or defense has a significant effect on their rebound percentage.

Next, we'll look at USG_PCT, usage percentage, which is an estimate of how often a player makes team plays:

```
ggplot(data = nba_social_power_mod, aes(x= USG_PCT)) +
geom_histogram(binwidth = .01) +
labs(x = "Usage Percentage", y = "Count",
    title = "Distribution of Usage Percentage")
```

Distribution of Usage Percentage



```
nba_social_power_mod %>%
summarise(mean = mean(USG_PCT),
    min= min(USG_PCT),
    Q1 = quantile(USG_PCT, .25),
    median = median(USG_PCT),
    Q3 = quantile(USG_PCT, .75),
    max = max(USG_PCT))
```

```
## # A tibble: 1 x 6
## mean min Q1 median Q3 max
## <dbl> <dbl> <dbl> <dbl> <dbl> <dbl> <dbl> <dbl> <0.242 0.276 0.408</pre>
```

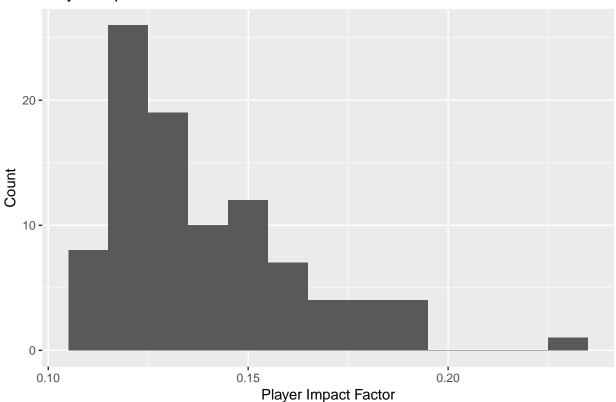
```
nba_social_power_mod %>%
  arrange(desc(USG_PCT)) %>%
  head(1)
```

```
## # A tibble: 1 x 26
     PLAYER NAME TEAM ABBREVIATI~
                                  AGE W PCT OFF RATING DEF RATING NET RATING
##
     <chr>>
                 <chr>>
                                  <int> <dbl>
                                                    <dbl>
                                                               <dbl>
                                                                           <dbl>
## 1 Russell We~ OKC
                                     28 0.568
                                                     108.
                                                                105.
                                                                            3.3
## # ... with 19 more variables: AST_RATIO <dbl>, REB_PCT <dbl>,
      USG PCT <dbl>, PIE <dbl>, SALARY MILLIONS <dbl>,
       ACTIVE TWITTER LAST YEAR <int>, TWITTER FOLLOWER COUNT MILLIONS <dbl>,
## #
## #
      PTS <dbl>, ageCent <dbl>, ast_ratioCent <dbl>, off_ratingCent <dbl>,
## #
       def ratingCent <dbl>, net ratingCent <dbl>, PIECent <dbl>,
## #
       reb_pctCent <dbl>, usg_pctCent <dbl>, salary_millionsCent <dbl>,
       w_pctCent <dbl>, ptsCent <dbl>
## #
```

The distribution of usage percentage, with a minimum of .101 and a maximum of .408, is fairly normally distributed. The mean, .238, and median, .242, are similar. The fairly wide spread may indicate that the dataset contains a decent sampling of players- some 'star player' types and others that are not the centerpieces of their teams. The maximum of .408, while perhaps not quite an outlier, is separated from most of the other points; this usage percentage belongs to Russell Westbrook.

Next, we'll examine PIE, player impact factor, a statistic roughly measuring a player's impact on the games that they play that's used by nba.com:

Player Impact Factor Distribution



```
## <dbl> <dbl> <dbl> <dbl> <dbl> <dbl> <dbl> <dbl> <dbl> 
## 1 0.139 0.112 0.122 0.131 0.152 0.23

nba_social_power_mod %>%
    arrange(desc(PIE)) %>%
    select(PLAYER_NAME, PIE) %>%
```

```
## # A tibble: 10 x 2
##
     PLAYER_NAME
                             PIE
##
      <chr>
                            <dbl>
## 1 Russell Westbrook
                           0.23
## 2 Demetrius Jackson
                           0.194
## 3 Anthony Davis
                           0.192
## 4 James Harden
                           0.19
## 5 Kevin Durant
                           0.186
## 6 LeBron James
                           0.183
## 7 Chris Paul
                           0.182
```

mean

head(10)

min

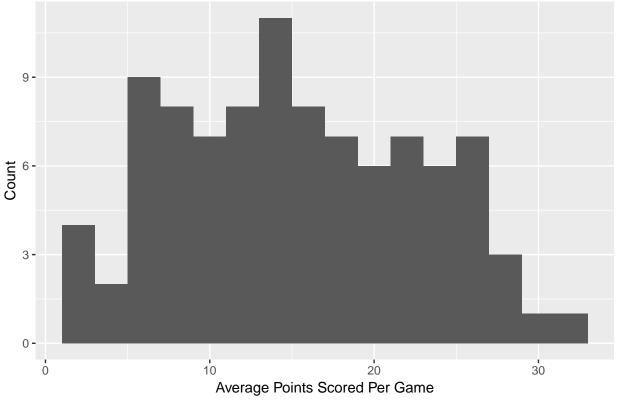
Q1 median

QЗ

As we can see from the histogram, the player impact factor, with a minimum of .112 and a maximum of .23, is quite right-skewed. The median player impact factor is .131, and the mean is .139, evidence of the right skew. The mode is around the median. The maximum, .23, is a significant outlier, and is that of Russell Westbrook, the same player who had by far the highest usage percentage; clearly, his data will need to be examined more closely later to see if it ultimately affects our model.

Next, we'll look at average points scored per game:

Distribution of Average Points Scored Per Game



```
## # A tibble: 1 x 6
## mean min Q1 median Q3 max
## <dbl> <dbl> <dbl> <dbl> <dbl> <dbl>
```

```
## 1 15.3 1.5 9.5 14.6 21.4 31.6
```

As we can see from the histogram, the distribution of average points scored is slightly normal, with some obvious departures from normality. The median number of points scored per game is 14.6, and the mean is 15.28232. The maximum is 31.6, but this does not seem to be an obvious outlier.

Next, we'll examine the variable ACTIVE_TWITTER_LAST_YEAR, which tells us whether or not each player posted on Twitter the year before the data was collected:

```
nba_social_power_mod <- nba_social_power_mod %>%
  mutate(ACTIVE_TWITTER_LAST_YEAR = as.factor(ACTIVE_TWITTER_LAST_YEAR))

nba_social_power_mod %>%
  count(ACTIVE_TWITTER_LAST_YEAR)
```

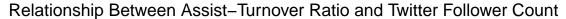
```
## # A tibble: 2 x 2
## ACTIVE_TWITTER_LAST_YEAR n
## <fct> <int>
## 1 0 2
## 2 1 93
```

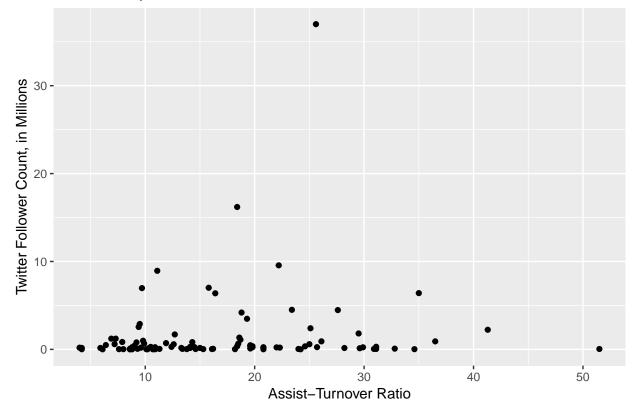
Out of the 95 players in our modified dataset, 2 were not active on Twitter the year before the data was collected and and 93 were.

Bivariate

Next, we will do bivariate EDA, looking into the relationships of some of the predictor variables with the response variables. We won't do bivariate EDA on player name, Twitter handle, age, team abbreviation, or whether the players were active on Twitter last year, instead focusing on terms we believe may play a more nuanced / important role in predicting Twitter followers.

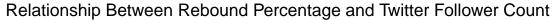
Here, we'll look at the relationship between assist-to-turnovers ratio and Twitter follower count:

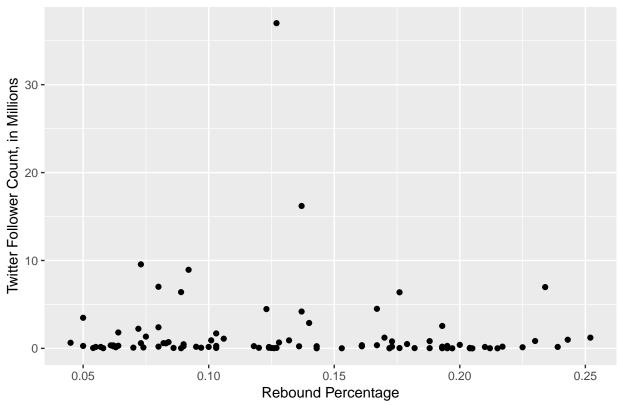




There is no evident relationship between assist-turnover ratio and Twitter follower count.

Next, we'll examine whether there is a relationship between rebound percentage and Twitter follower count:





There is no evident relationship between rebound percentage and Twitter follower count.

There may have been some slight linearity issues with our current model. Though there is not a discernible pattern in our residuals plot for salary, there was slight curvature, so we were interested to see if we could fix this with a log-transformation:

Warning in log(salary_millionsCent): NaNs produced

```
tidy(m_final_add, conf.int = TRUE) %>%
kable(format = "markdown", digits = 3)
```

| term | estimate | std.error | statistic | p.value | conf.low | conf.high |
|---|----------|-----------|-----------|---------|----------|-----------|
| (Intercept) | -0.621 | 0.431 | -1.441 | 0.157 | -1.492 | 0.250 |
| $\log(\text{salary_millionsCent})$ | 0.165 | 0.224 | 0.736 | 0.466 | -0.288 | 0.618 |
| $w_pctCent$ | 4.088 | 2.759 | 1.482 | 0.146 | -1.489 | 9.665 |
| $\log({\rm salary_millionsCent}) : w_pctCent$ | -1.157 | 1.653 | -0.700 | 0.488 | -4.497 | 2.183 |

Our p-values are extremely high for all coefficients, which means that predicted variables are not significant predictors for the response variable. Therefore, we will not continue with this model, because our final model from before is significant and satisfies assumptions fairly well.