Data Structures with Multiple Organization





For Boys, we have a lot

of these







When you got it wrong











Got it Right

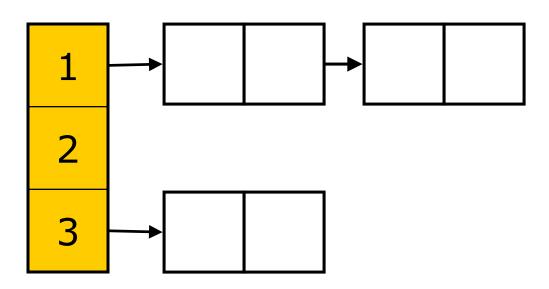


Basic Data Structures

- Array
- Linked List
- Trees

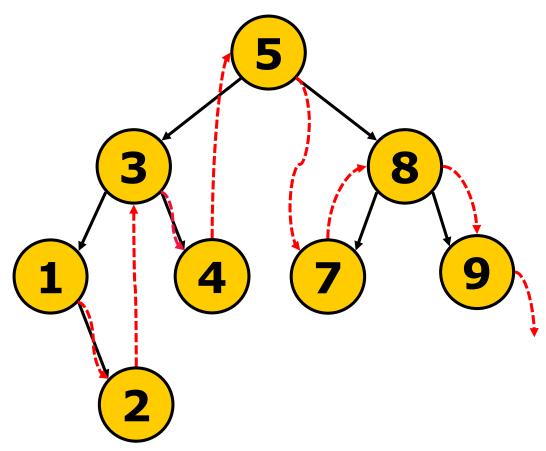
Mix-and-Match 1

Array of Linked-List



Mix-and-Match 2

Binary Search Tree + Linked-List



More Examples

- Need an ADT for
 - enqueue(item)
 - dequeue(item)
 - peek()
 - printInOrder()
 - Not "in-order" traversal
 - Just print them according to ascending or descending order

Use a Queue (Linked List)

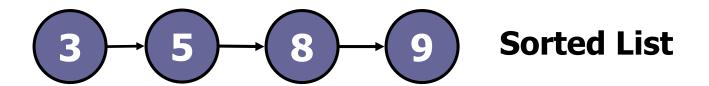
enqueue(item)	O(1)
dequeue()	O(1)
peek()	O(1)
printInOrder()	O(N log N)



Use a Sorted Linked List

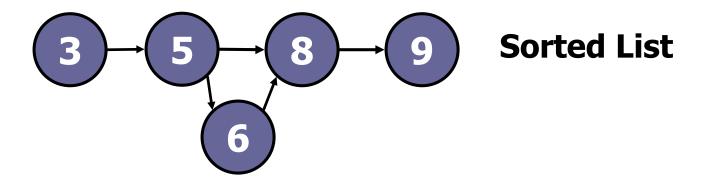
enqueue(item)	?	
dequeue()	?	
peek()	?	
printInOrder()	O(N)	

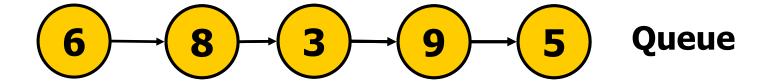
Use both



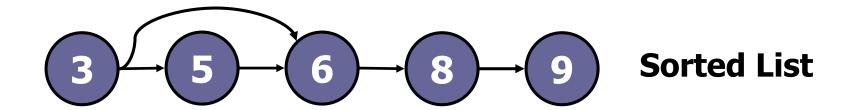


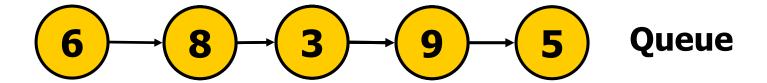
Enqueue(6)



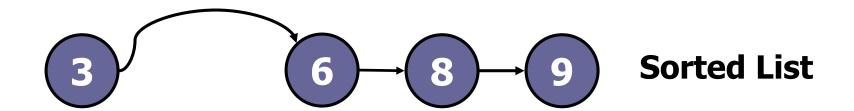


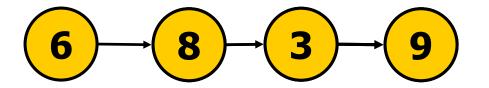
Dequeue()





Dequeue()





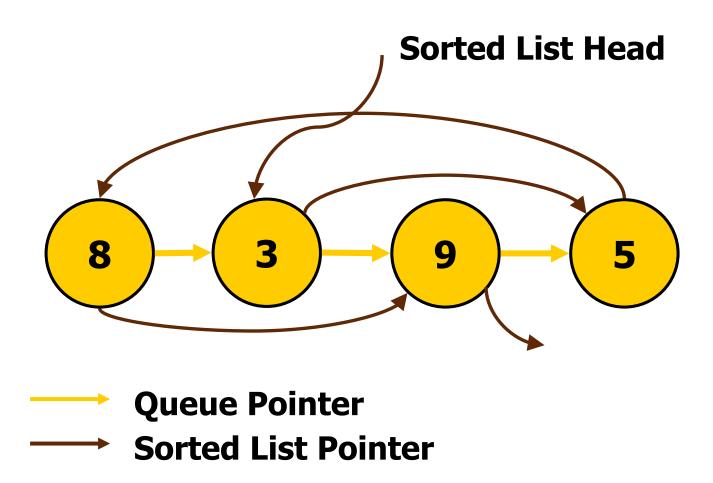
Queue

Use Queue and Linked List

enqueue(item)	O(N)
dequeue()	O(N)
peek()	O(1)
printInOrder()	O(N)



Improvement



Combine Queue and Linked List

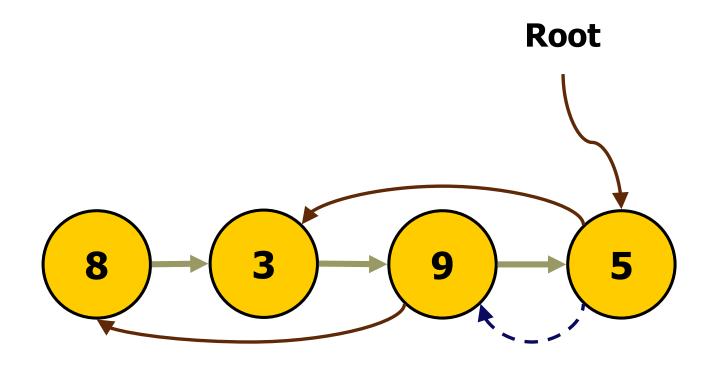
enqueue(item)	O(N)
dequeue()	0(1)
peek()	O(1)
printInOrder()	O(N)

Combine Queue and BST

enqueue(item)	O(log N)
dequeue()	O(1)
peek()	O(1)
printInOrder()	O(N)



More Improvement

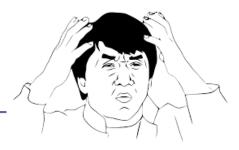


- **Queue Pointer**
- **── Left Child Pointer**
- --→ Right Child Pointer

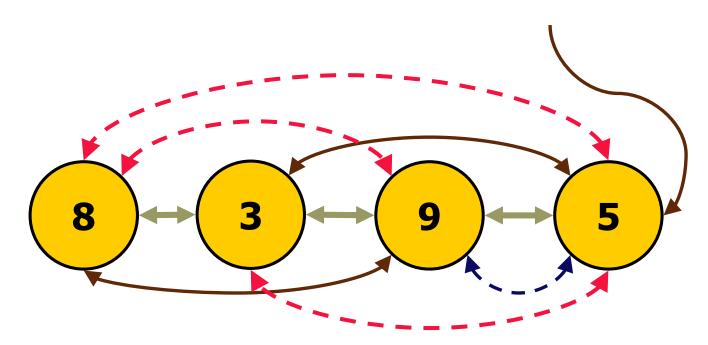
Combine Queue and BST

enqueue(item)	O(log N)
dequeue()	0(1)
peek()	O(1)
printInOrder()	O(N)

More Improvement

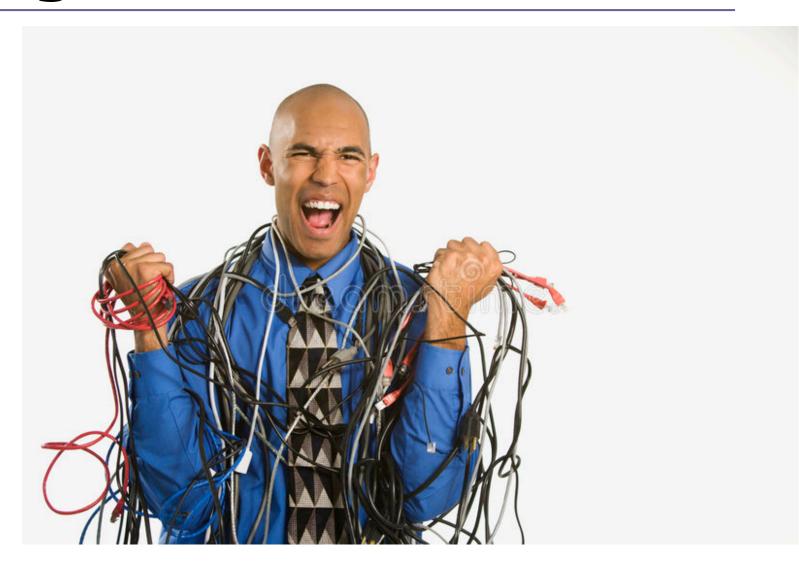


Root



- **Queue Pointer** --→ Succ/Pred Pointer
- **—** Left Pointer **– – –** Right Pointer

Mange the Pointers Well



Every node is...

- a node in a Linked List, as well as,
- a node in a Tree, as well as,
- □ a node in a Queue, as well as....
- Graph...



test in words.

spare (spār), v.f. to use in a frugal manner; part with without inconvenience; omit; treat tenderly; s.f. to live frugally; forbear or forgive: adj. thin or lean; scanty; paramennious; superfluous; reserved, sparing (spārling), adj. frugal] abstemious.

spark (spārling), adj. frugal] abstemious. sparing (sparing), any itages; accessions to sparing (sparing), any itages; accessions a sparing (sparing), and a small particle of fire or ignited substance thrown off in combustion; small shining body or transient light; small portion of anything active or vivid; gay young fellow; beau.

sparkle (spirk'l), v.i. to emit sparks; glisten; cantillate; finsh; corrueate, sparks plug (spärk'plug), n. an apparatus for exploding the gas in a gasociene motor by means of an electric spark. Also sparker, sparling (spärling), n. a smelt, sparking (spärling), n. a smelt, sparking to utter articulate sounds; said of human small bind of the Passerine family.

sparrow (spar'd), n. a smelt-known small bird of the Passerine family. sparse (spårs), adj. thinly scattered; not dense; set or planted here and sparsely (spars'li), adv. in a sparse man-

sparseness (spärs'nes), n. the state or quality of being sparse; thinness.

Spartan (spir'tan), ad), pertaining to Sparta; hardy; undaunted; se-

sparterie (spär'tër-i), n. articles spun

beings; talk; say; utter a discourse or speech; make mention; convey ideas; tell; sound: s.t. to utter ar-ticulately; declare or pronounce; publish.

preaser (spēk'ēr), n. one who speaka; one who delivers a discourse in pub-lie; the presiding officer of the popu-lar branch of a legislative body, an of congress or a state legislature.

speaking (spek'ing), p.adj. uttering speech; life-like; n. the act of utter-

sparterie (spür'tér-i), n. articles spun or woven of esparto grass.

spasm (spaxm), n. a sudden, violent, involuntary contraction of the muscles. (Greek.)

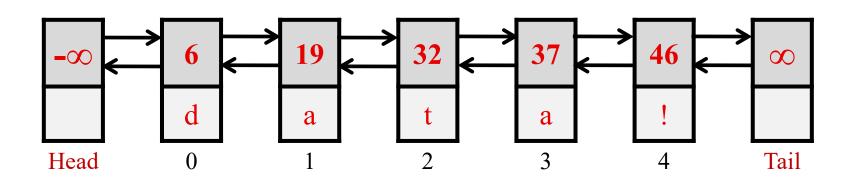
spasmodic (spax-mod'ik), adj. pertaining to, or consisting in, spasms, convulsive; violent but short-lived. Also spasmodically (spax-mod'i-ka-ii), ads. in a spasmodically (spax-mod'i-ka-ii), ads. in a spasmodic manner.





Implementing a dictionary, again...

Store keys in a sorted linked list:



Time:

- Search: O(n)
- Insert: O(n)

Japan Rail System?



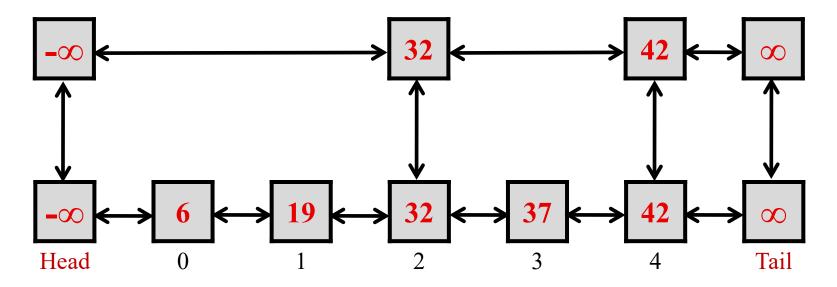
Japan Rail System?



What if...

What if we use two lists?

- Express train
- Local train



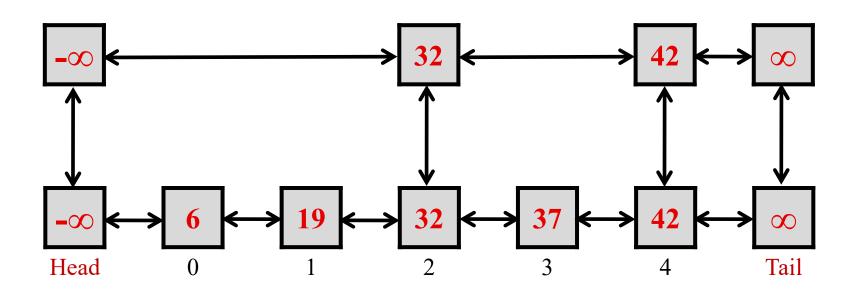
search (37) takes only 3 steps!

What if...

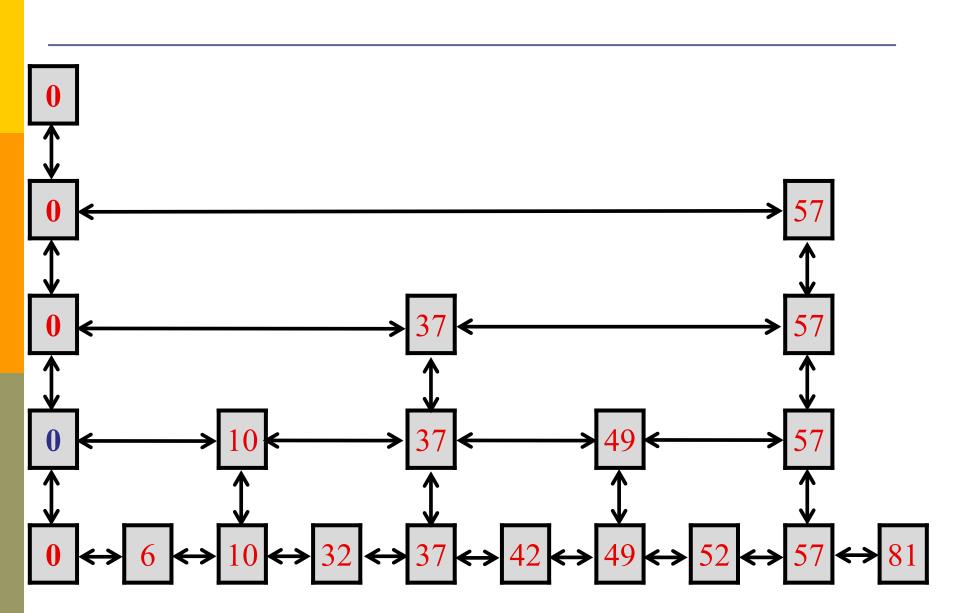
Calculation:

If the "express" list skips 5 elements per "stop", then search takes at most:

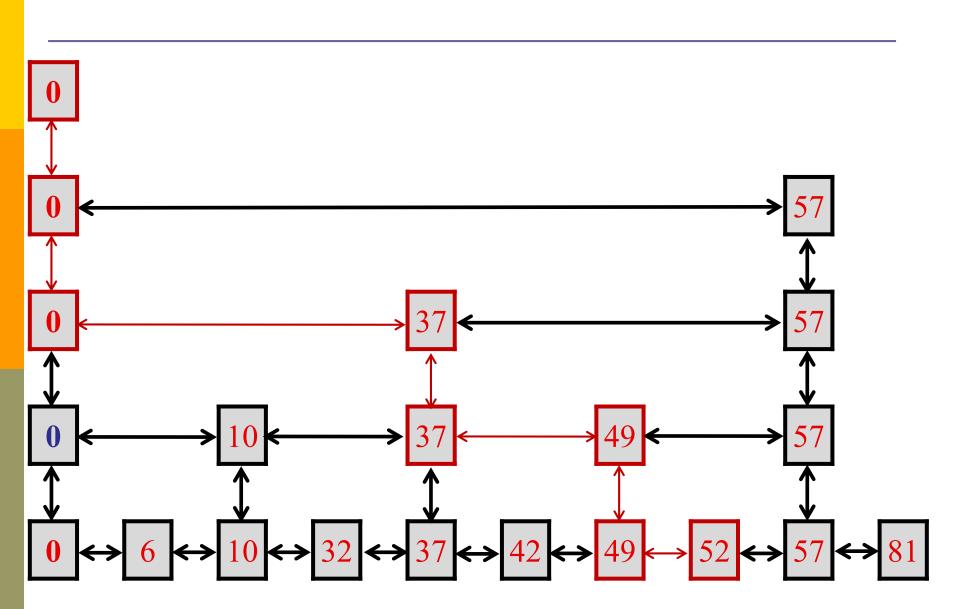
$$n/5 + 5$$
 steps



Another way to think about it...



Example: search (52)

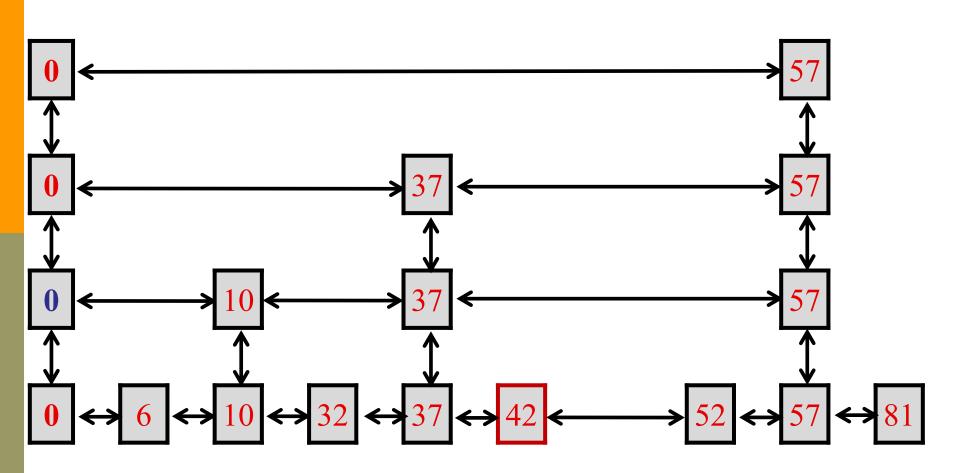


Insertions

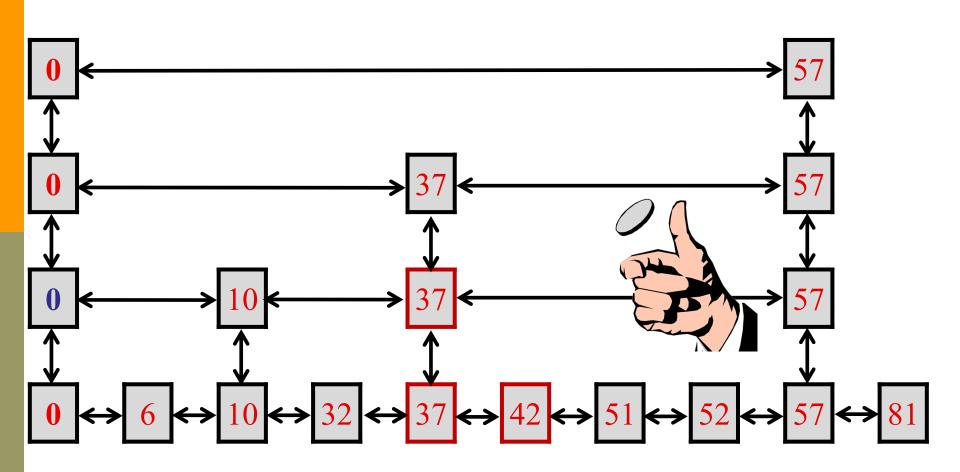
Key idea: flip a coin

```
1. k = 0;
   while (!done) {
        Insert element into level k list.
3.
        Flip a fair coin:
4.
              with probability ½: done = true;
5.
              with probability \frac{1}{2}: k = k+1;
6.
7. }
```

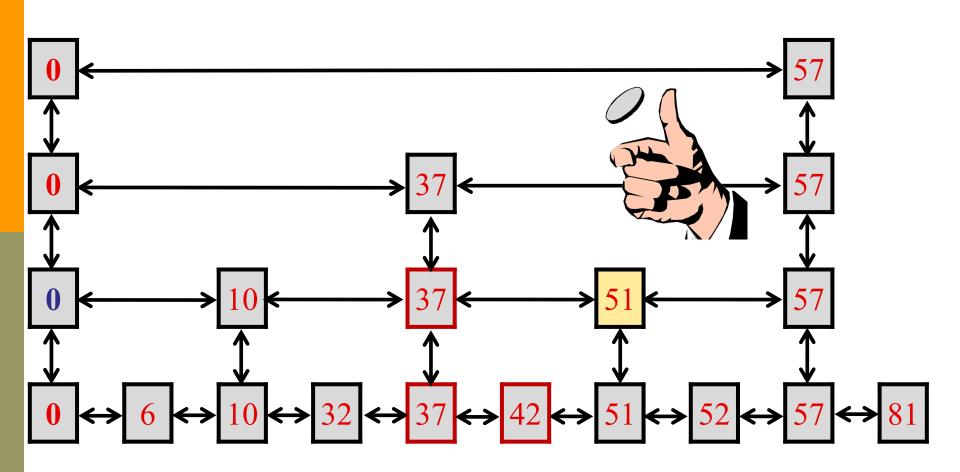
Example: insert (51)



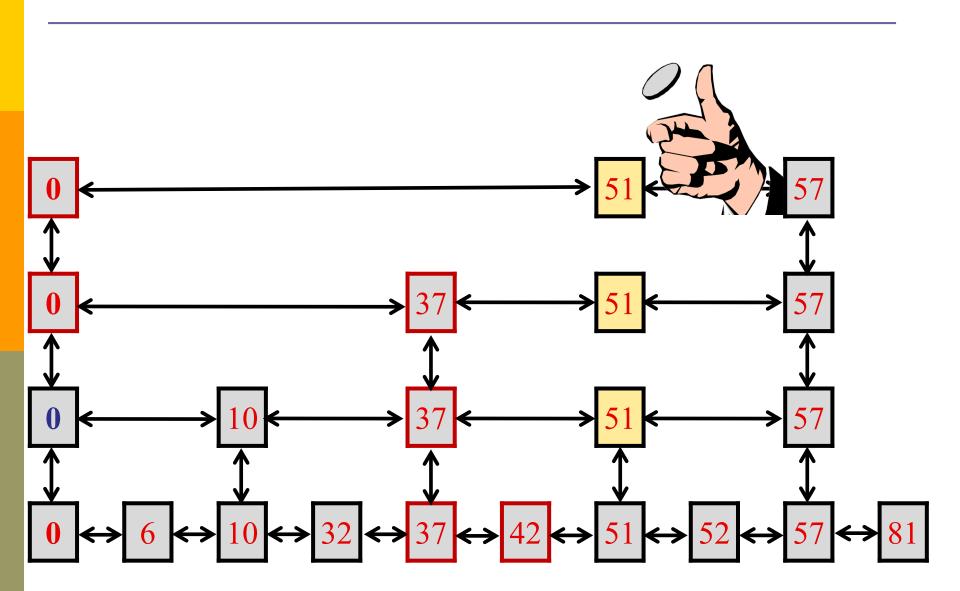
Example: insert (51)



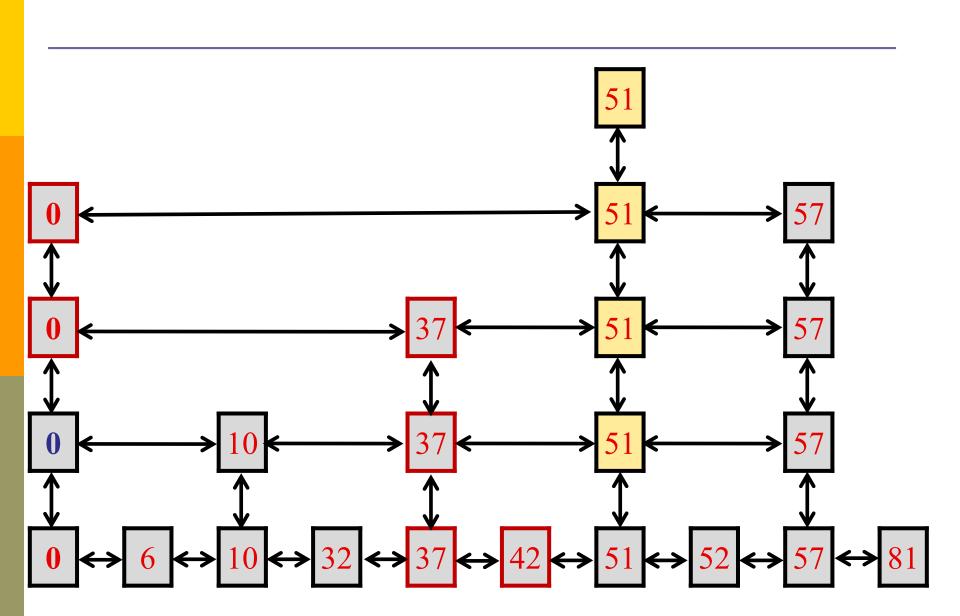
Example: insert (51)



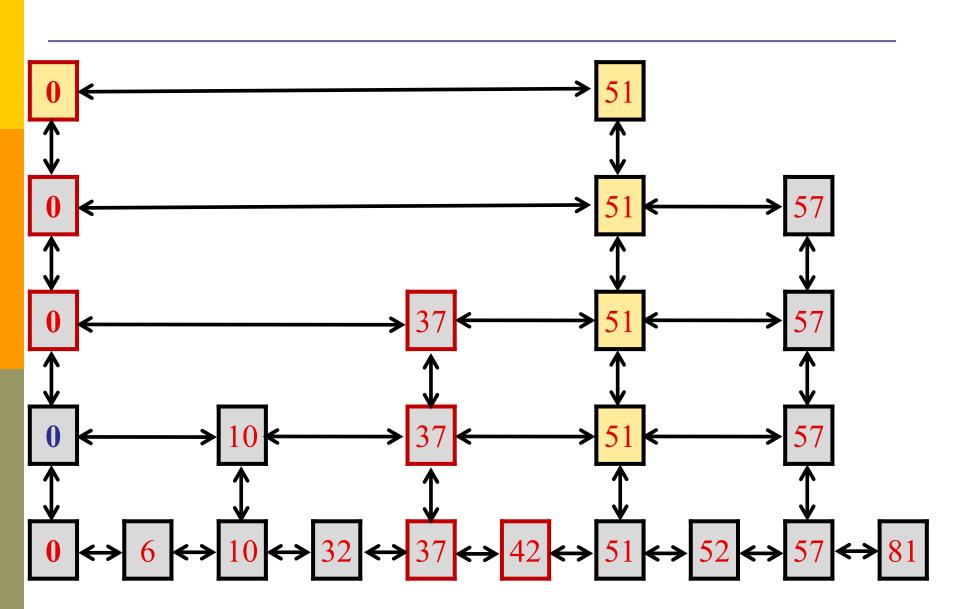
Example: insert (51)



Example: insert (51)



Example: insert (51)



SkipList Analysis

Claim: In expectation, after $O(\log n)$ coin flips, you get $c \log n$ heads.

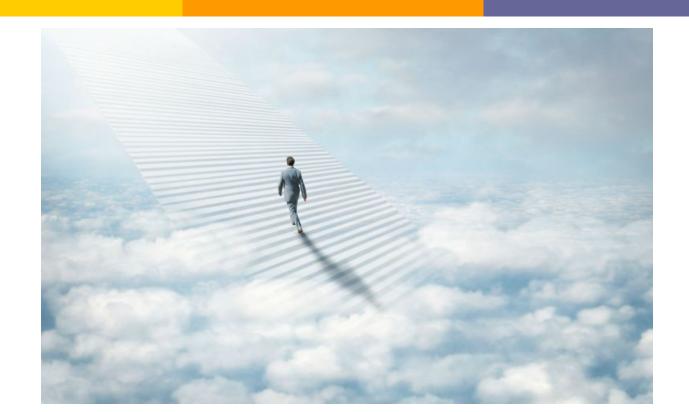
Conclusion: Each search takes $O(\log n)$ steps in expectation.

Mix-and-Match

- Overlay/Merge/Contain multiple data structures
 - Possibly to get the best out of all



Life after CS2040C



Operating System

- how to map filename to location on disk?
 - tables, linked list
- how to manage processes?
 - priority queues

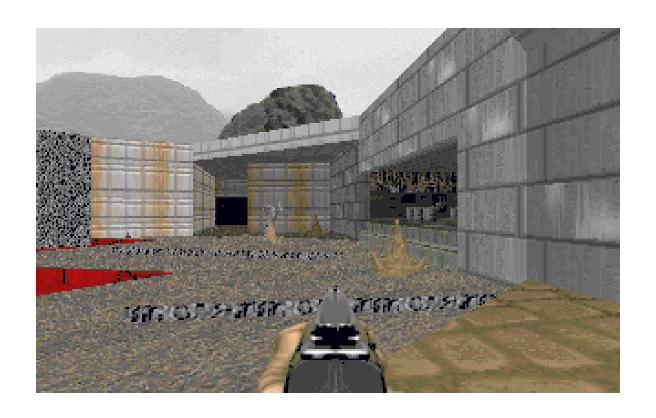
Computer Graphics

- Algorithms
 - Draw with occlusions (sorting)
 - Ray tracing (recursive!)



Computer Graphics

Data structure: Binary Space Partition Tree



Compiler

- How to keep track of variable names, method names, class names?
 - Hash table
- How can computers "understand" programs?
 - Expression tree
 - Syntax tree

Artificial Intelligence

- how does computer play chess?
 - BFS on a tree/graph
- how to understand human language?
 - semantic network (a graph!)
- LISP/ML/Scheme/Prolog
 - plenty of lists and recursions!

CS2040C

- Give an introduction to data structures and algorithms for constructing efficient computer programs.
- Emphasis is on data abstraction issues (through ADTs) in the code development.
- Emphasis on efficient implementations of chosen data structures and algorithms.

Objectives

- Include stacks, queues, trees (including BST, heap and AVL trees), hash tables, and graphs; together with their algorithms (tree and graph traversals, minimum spanning trees).
- Simple algorithmic paradigms, such as search algorithms and divide-and-conquer algorithms will be introduced.
- Elementary analysis of algorithmic complexities will also be taught.