



Map of LA

A is an $n \times n$ matrix

$$T_A : \mathbf{R}^n \rightarrow \mathbf{R}^n$$

| | | |
|--|--------------------|---|
| A is invertible | chapter 2 | A is not invertible |
| $\det A \neq 0$ | chapter 2 | $\det A = 0$ |
| rref of A is identity matrix | chapter 1 | rref of A has a zero row |
| $AX = 0$ has only the trivial solution | chapter 1 | $AX = 0$ has non-trivial solutions |
| $AX = b$ has a unique solution | chapter 1 | $AX = b$ has no solution or infinitely many solutions |
| rows (columns) of A are linearly independent | chapter 3 | rows (columns) of A are linearly dependent |
| nullity(A) = 0 | rank(A) = n | chapter 4 |
| 0 is not an eigenvalue of A | chapter 6 | rank(A) < n |
| $R(T_A) = \mathbf{R}^n$ | chapter 7 | nullity(A) > 0 |
| | | 0 is an eigenvalue of A |
| | | $R(T_A) \neq \mathbf{R}^n$ |