

# Lecture 1: Encryption

(first step towards security)

1.1: Definition: Encryption/decryption/Keys

1.2: Classical ciphers + illustration of attacks

1.3: Modern Ciphers + recommended key length

1.4: Examples of attacks on crypto

    1.4.1: Meet-in-the-middle

    1.4.2: Padding Oracle & notion of “Oracle”

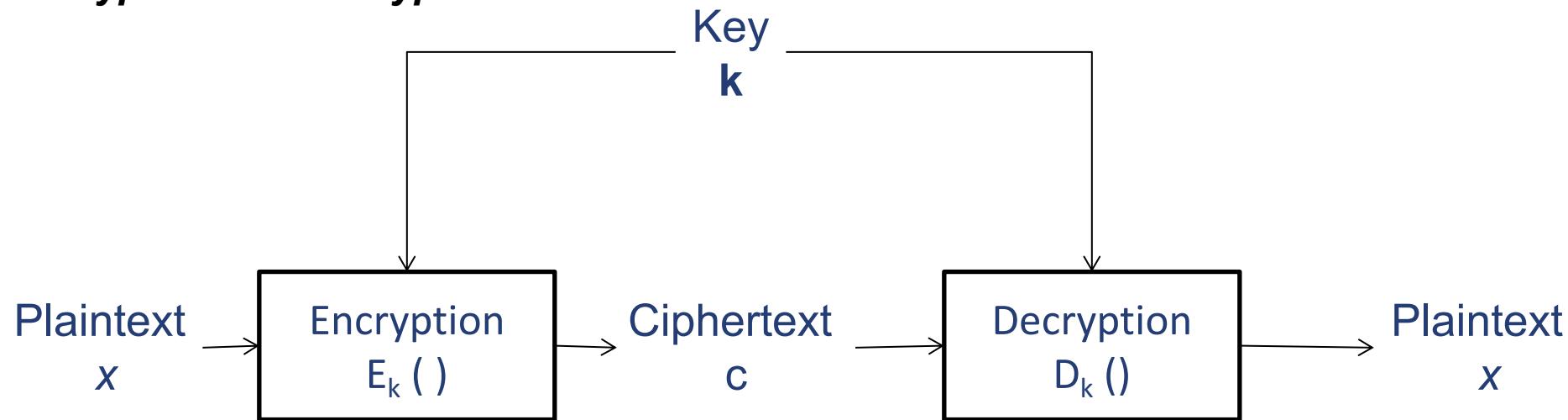
1.5: Pitfalls in usages and implementations

1.6: Interesting Historical facts

# **1.1 Definitions**

# Encryption

An *encryption scheme* (also known as *cipher*) consists of two algorithms: **encryption** and **decryption**.



An encryption must meet the correctness property:

**Correctness:** For any plaintext  $x$  and key  $k$ ,

$$D_k(E_k(x)) = x$$

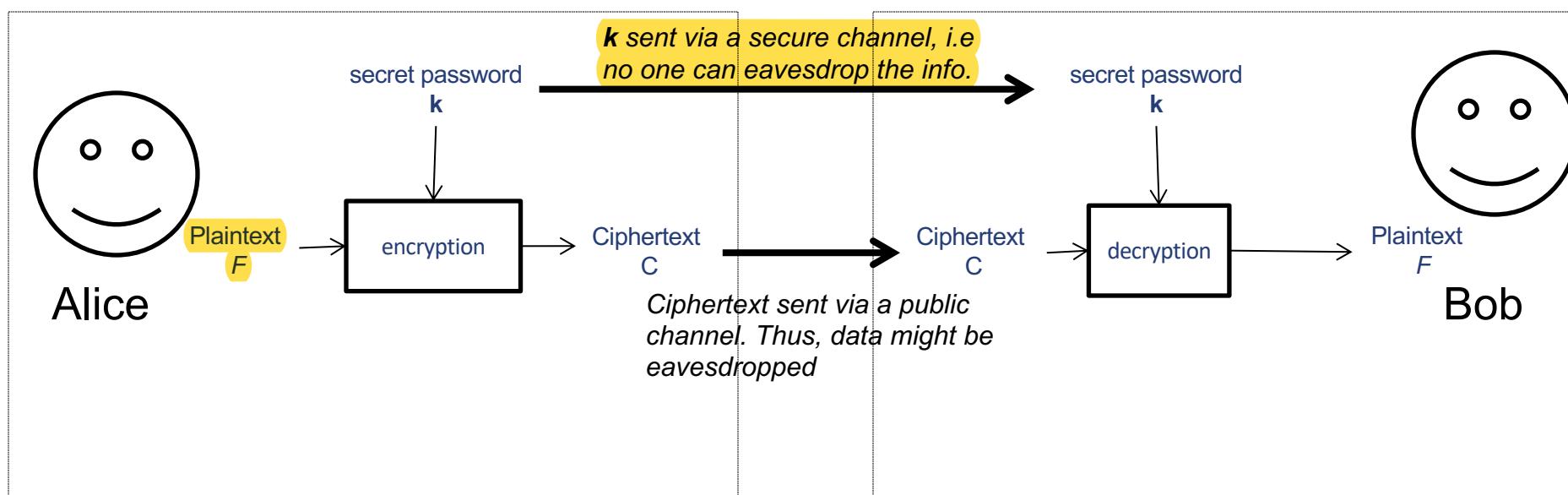
It also must be secure. Formal formulation of security is difficult (take the crypto class to learn more).

**Security:** Informally, from the ciphertext, it is “difficult” to derive useful information of the key  $k$ , and the plaintext  $x$ . To someone who doesn’t know the key, the ciphertext resemble sequences of random bytes. (There are many refined formulations of security requirements, e.g. semantic security. In this module, we will not go into details).

# An application scenario

Alice has a large file **F** (say info on her bank accounts and financial transactions in Excel). She “encrypted” the file **F** using winzip with a password “13j8d7wjnd” and obtained the ciphertext **C**. Next, she called Bob to tell him the 10-character password, and subsequently, she sent the ciphertext to Bob via email attachment. Later, Bob received **C** and decrypted the ciphertext with the password to obtain the plaintext **F**.

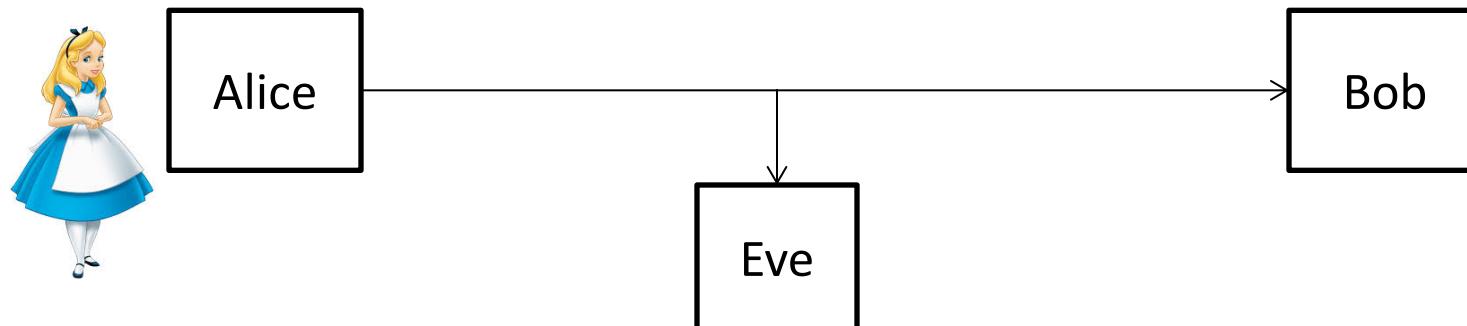
Anyone who has obtained **C**, without knowing the password, is unable to get any information on **F**. Although **C** indeed contains info of **F**, the information is “hidden”. To someone who doesn’t know the secret, **C** resembles a sequence of random bits.



Remark: Winzip is **not** an encryption scheme. It is an application that employs standard encryption schemes such as AES.

# Cryptography (cryptology)

- Is the study of techniques in securing communication in the present of adversaries who have access to the communication.
- Although cryptography is commonly associated with encryption, note that encryption is just one of the primitives in cryptography (other include cryptographic hash, digital signature etc).
- Terminology: Common placeholders used in cryptography are Alice (usually the originator of message), Bob (usually the recipient), Eve (eavesdropper: can only listen), Mallory (malicious: can modify messages), (see the interesting list in [https://en.wikipedia.org/wiki/Alice\\_and\\_Bob](https://en.wikipedia.org/wiki/Alice_and_Bob))
- Depending on context, Alice may not be a human. She could be the machine that encrypts the message.



In this module,

“see”: Info that is good to know.

“read”: Part of the teaching materials. Read it.

“optional”: Optional information.

## 1.2 Classical Ciphers

For illustration, we will look into a few classical ciphers. Classical ciphers are not secure in the computer era. (exception: the “unbreakable” one-time-pad).

(see <http://ciphermachines.com/index>

for a good listing of classical ciphers and cipher machines used during WWII.)

- 1.2.1. Substitution Cipher
- 1.2.2. Permutation Cipher
- 1.2.3. One time Pad

## **1.2.1 Substitution Cipher**

# Substitution Cipher

- **Plaintext** and **ciphertext**: a string over a set of symbols  $U$ .

E.g.

Let  $U = \{“a”, “b”, “c”, …, “z”, “_”\}$ .

e.g. of plaintext: “hello\_world”

- **Key:** a substitution table  $S$  representing an 1-1 onto function from  $U$  to  $U$ .

E.g.

a	b	c	d	e	f	g	h	i	j	k	l	m	n	o	p	q	r	s	t	u	v	w	x	y	z	_
g	v	w	b	n	e	f	h	d	a	t	l	u	c	q	m	z	i	r	s	j	x	o	y	k	_	p

$$S(a) = g, S(b) = v, \dots$$

The inverse of  $S$

$$S^{-1}(g) = a, S^{-1}(v) = b$$

$\log_2(27!)$

- The **key space** is the set of all possible keys. The **key space size** or **size of key space** is the total number of possible keys. The **key size** or **key length** is the number of bits required to represent a key. Here, the **key space size** is  $(27!)$ . **Key size** is approximately 94 bits.

# Substitution cipher: encryption/decryption

**Encryption:** Given a plaintext, which is a string

$$X = x_1 \ x_2 \ x_3 \ \dots \ x_n$$

and the key S, output the ciphertext

$$E_S(X) = S(x_1) \ S(x_2) \ S(x_3) \ \dots \ S(x_n)$$

Cannot repeatedly substitute, all substitution will just become 1 key

E.g.

plaintext: h e l l o \_ w o r l d

ciphertext: h n l l q p o q i l b

**Decryption:** Given a string of ciphertext of length n

$$C = c_1 \ c_2 \ c_3 \ \dots \ c_n$$

and the key S, output the plaintext

$$D_S(C) = S^{-1}(c_1) \ S^{-1}(c_2) \ S^{-1}(c_3) \ \dots \ S^{-1}(c_n)$$

a	b	c	d	e	f	g	h	i	j	k	l	m	n	o	p	q	r	s	t	u	v	w	x	y	z	_
g	v	w	b	n	e	f	h	d	a	t	l	u	c	q	m	z	i	r	s	j	x	o	y	k	_	p

# Attacks on Ciphers

- The attacker's goal is to find the key, or to obtain some information of the **plaintext** (if the key can be found, then the plaintext can be obtained. Nevertheless, the converse not necessary holds.)
- The attackers need access to some information before commencing the attack. E.g, a large number of ciphertexts all encrypted using the same key, or pairs of ciphertext and the corresponding plaintext, etc.
- A simple attack is to exhaustively search the keys, i.e. examine all possible keys one by one. Using exhaustive search, eventually (although this might take very very long) the correct key can be found\*.
- So, for a cipher to be secure, exhaustive search must be computationally *infeasible*, e.g. taking millions of years using state-of-the-art supercomputer (surprisingly, it is feasible to exhaustively search some modern ciphers, e.g. DES)
- Sophisticated attacks exploit weakness of the encryption scheme so that it can break faster than exhaustive search.

\*: Exception: “Information theoretic secure” such as one-time-pad.

# Exhaustive search (aka brute-force-search).

Therefore scheme is secured via exhaustive search

- Consider the substitution cipher (with table size of 27).
- We assume that the attacker knows a ciphertext  $C$  and the corresponding plaintext  $X$ . The attacker want to find the key.

Let  $S$  be the set of all possible substitution tables. Given  $X, C$ .

- 
1. For each  $S$  in  $S$
  2. Compute  $X' = D_S(C)$ ; If  $(X' == X)$  then break;
  3. end-for
  4. Display ( "The key is ",  $S$  );

- The running time depends on the size of the key space  $S$ .
- Since a key can be represented by a sequence of 27 symbols. The size is key space is  $27!$   
(So, in any representation, the key length is at least  $\log_2(27!) \approx 94$  bits. )
- Eventually, exhaustive search will find the key. However, in the worst case, the exhaustive search needs to carry out  $27! \approx 2^{94}$  loops, and on average  $\approx 2^{93}$  loops. This is infeasible using current compute power (see tutorial 1).

# Attack: Known-plaintext-attack on Substitution Cipher

- You probably have realized that the attacker doesn't need to carry out exhaustive search. Given a plaintext and ciphertext, e.g

plaintext: h e l l o \_ w o r l d  
ciphertext: h n l l q p o q i l b

The attacker can figure out the entries in the key

a	b	c	d	e	f	g	h	i	j	k	l	m	n	o	p	q	r	s	t	u	v	w	x	y	z	_
		b	n			h				l			q			i						o				p

For sufficiently long ciphertext, the full table can be found.

- "Known plaintext attack"**: a scenario where the attackers have access to pairs of ciphertexts and the corresponding plaintexts.
- If the adversary can successfully derive the key, we say that the scheme is
  - "not secure under known plaintext attack"** or
  - "broken under known plaintext attack"**

Hence, substitution cipher is not secure under known plaintext attack.

# Attack on Substitution cipher (Ciphertext only attack)

- **Ciphertext only attack:** The attackers have access to ciphertext only (i.e. without the corresponding plaintext).
- Suppose an attacker knows that the plaintext is an English sentence, can he find the key using exhaustive search under ciphertext only attack ? Yes.

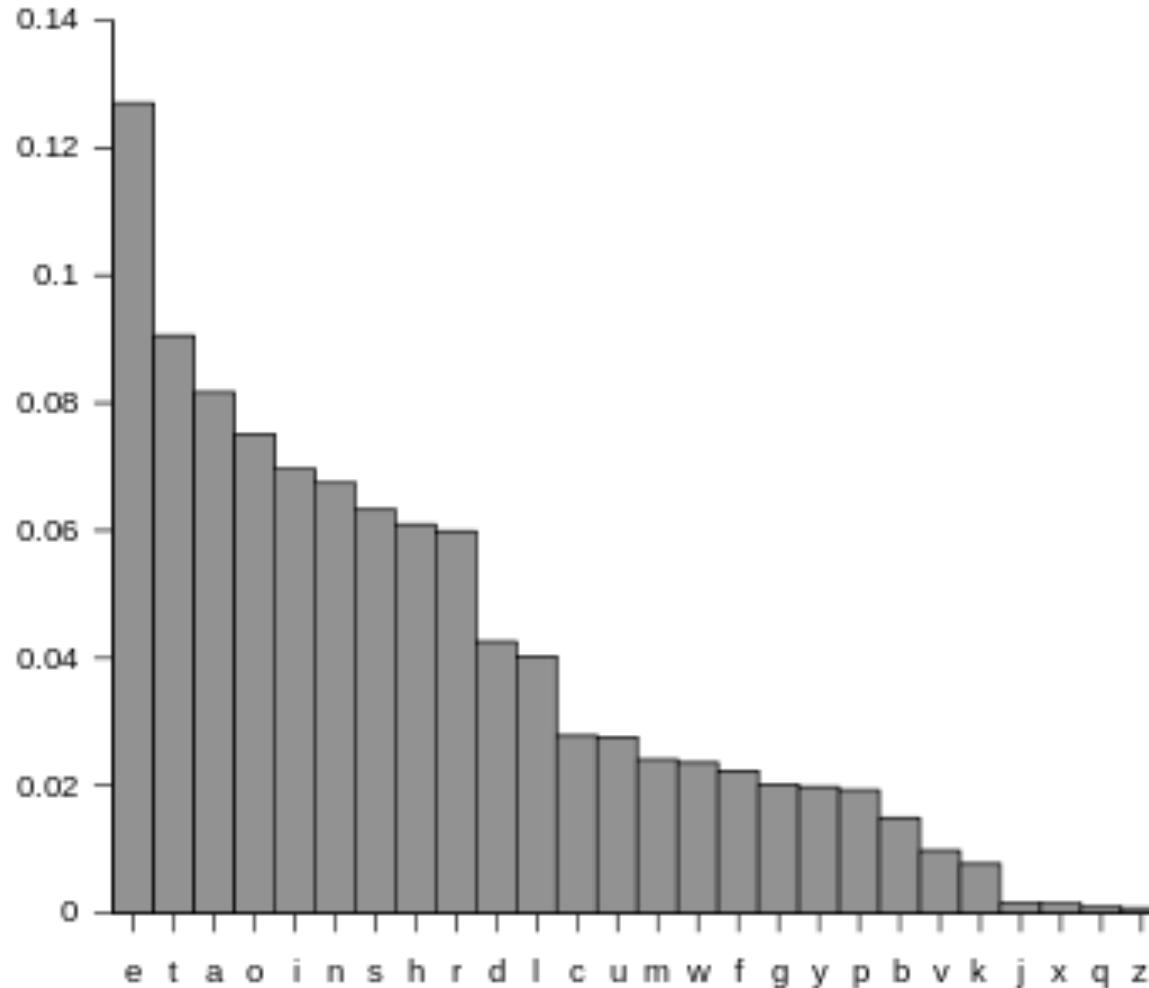
Let  $S$  be the set of all possible substitution table. Given  $C$ .

1. For each  $S$  in  $S$
2. Compute  $X = D_S(C)$ ; if  $X$  contains words in the English dictionary, then break;
3. end-for
4. Display ( "The key is ",  $S$  );

- Likewise, eventually, the exhaustive search will find the key. However, the attack is computationally infeasible. (There is a very small probability that the above found the wrong key. For long ciphertext, say 50 characters long, the probability that a wrong key will give a meaningful English sentence is very low. The probability is so small that we treat it as "*negligible*").
- Are there efficient ciphertext only attacks on substitution cipher? Yes.

- Substitution cipher is vulnerable to **frequency analysis** attack.
- Note that in the hello\_world example, “o” appears 2 times in the plaintext, whereas the corresponding “q” also appears 2 times in the ciphertext.
- Suppose the plaintexts are English sentences. The frequency of letters used in English is not uniform, for e.g. “e” is more commonly used than “z”. Given a sufficiently long ciphertext (say, around 50 characters), adversary may be able to guess the plaintext by mapping the frequently occurred letters in the ciphertext to the frequent letters used in English.
- If adversary is aware that the plaintexts are English sentences, then he could successfully carry out frequency analysis attack. Hence, substitution cipher is **not secure under ciphertext only attack**, when the plaintexts are English sentences.

## Frequency of letters in English text.



from [http://en.wikipedia.org/wiki/Letter\\_frequency](http://en.wikipedia.org/wiki/Letter_frequency)

## Remarks on Known plaintext attack.

To carry out known plaintext attack, the attacker needs to obtain at least a pair of ciphertext and the corresponding plaintext.

This is possible in practice. Eg, for email, certain words in the header are fixed such as “From”, “Subject”, etc. The first few bytes of many protocols are also fixed with only a few choices, or can be easily guessed (e.g. first few bytes of network packets).

During WWII, cryptologists exploited commonly used words like “weather” and “nothing to report” as the known plaintext to guess the secret keys.  
(optional: read more about “Enigma Machine”)

## **1.2.2 Permutation cipher**

# Permutation Cipher

permutation is special case of matrix multiplication  
- similar to the repeat one

- Also known as transposition cipher.

The encryption first groups the plaintext into blocks of  $t$  characters, and then applied a secret “permutation” to each block by shuffling the characters.

The key is the secret “permutation”, which is an 1-1 onto function  $e$  from  $\{1,2,\dots,t\}$  to  $\{1,2,\dots,t\}$ . The size  $t$  could be part of the key, that is,  $t$  is also kept secret. We can write the permutation  $p$  as a sequence

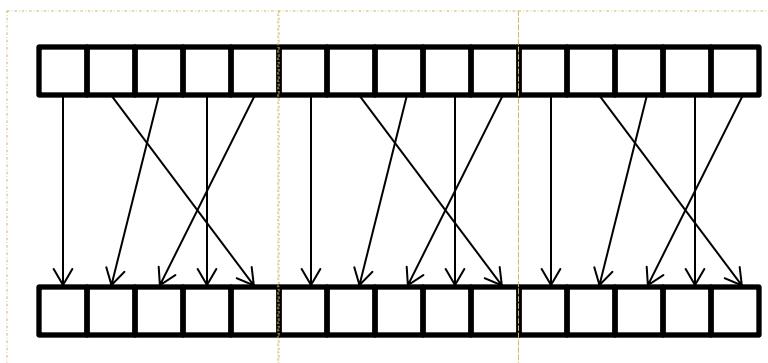
$$p = (p_1, p_2, p_3, \dots, p_t)$$

which shift the character at position  $i$  (position within the block) to the position  $p_i$ .

Example:

Given the plaintext and the key  $t=5$ ,  $p=(1,5,2,4,3)$

plaintext



ciphertext

# Cryptanalysis (known-plaintext attack)

Cannot repeatedly permute since it will just be a new permutation

- Permutation cipher fails miserably under known-plaintext attack.

Given a plaintext and a ciphertext, it is very easy to determine the secret key.

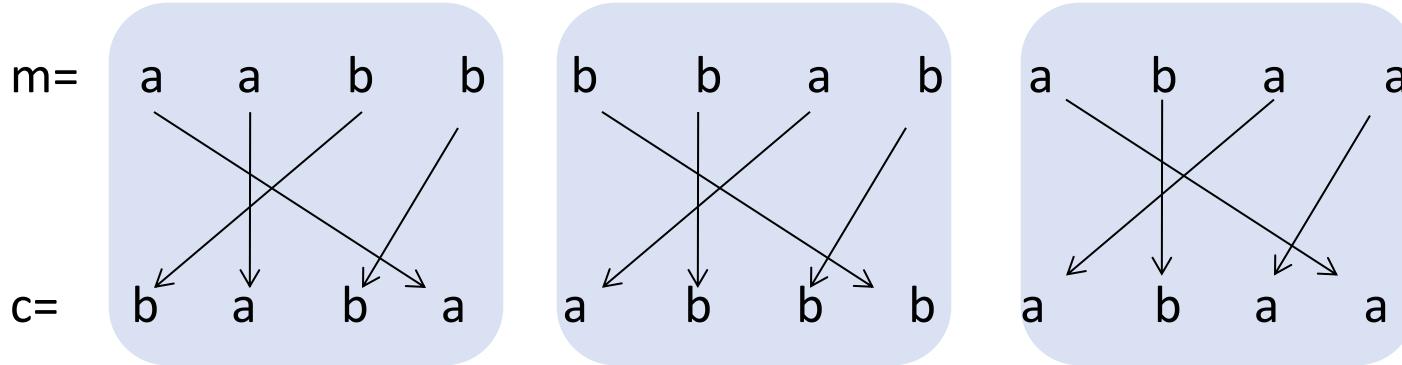
$m = \begin{matrix} a & a & b & b & b & a & b & a & b & a & a \end{matrix}$

$c = \begin{matrix} b & a & b & a & a & b & b & b & a & b & a & a \end{matrix}$

in the above, what is the block size  $t$ ? What is the permutation?

- Permutation cipher is also easily broken under ciphertext only attack if the plaintext is English text.

$$\begin{pmatrix} 0 & 1 & \cdots \\ \vdots & \ddots & \\ 0 & & 0 \end{pmatrix} \begin{pmatrix} 1 \\ 1 \\ 3 \\ 3 \end{pmatrix} = \begin{pmatrix} 3 \\ -1 \\ 3 \\ -1 \end{pmatrix}$$



AES/DES are using S-P-S-P-S... combinations

- Since mixing them up will allow for a new combi

## 1.2.3 One Time Pad

XOR operation

A	B	$A \oplus B$
0	0	0
0	1	1
1	0	1
1	1	0

Some interesting properties:

- Commutative:  $A \oplus B = B \oplus A$
- Associative:  $A \oplus (B \oplus C) = (A \oplus B) \oplus C$
- Identity element:  $A \oplus 0 = A$
- Self-inverse:  $A \oplus A = 0$

$$A \oplus B = (A+B) \bmod 2$$

# One-time-pad

Encryption:

Given n-bit Plaintext:  $x_1, x_2, \dots, x_n$  and n-bit key:  $k_1, k_2, \dots, k_n$   
ciphertext  $C = (x_1 \oplus k_1), (x_2 \oplus k_2), (x_3 \oplus k_3), \dots, (x_n \oplus k_n)$

Decryption:

Given n-bit ciphertext:  $c_1, c_2, \dots, c_n$  and n-bit key:  $k_1, k_2, \dots, k_n$   
plaintext  $X = (c_1 \oplus k_1), (c_2 \oplus k_2), (c_3 \oplus k_3), \dots, (c_n \oplus k_n)$

## E.g. One-time-pad

Encryption:  $\text{plaintext} \oplus \text{key} \rightarrow \text{ciphertext}$   
Decryption:  $\text{ciphertext} \oplus \text{key} \rightarrow \text{plaintext}$

PlainText	0	0	1	0	1	1	0
Key	1	1	0	0	1	1	1
Ciphertext	1	1	1	0	0	0	1

decryption

encryption

**Correctness** (decrypting the ciphertext give back the plaintext):

$$\text{For any } x, k, \quad (\text{ciphertext} \oplus k) \oplus k = x \oplus (k \oplus k) = (x \oplus 0) = x$$

plaintext

# Security of one-time-pad

- From a pair of ciphertext and plaintext, the attacker can derive the key. However, such key is useless, since it will not be used any more.
- Note that even exhaustive search can't work on one-time-pad. (Suppose we are given a 1Kbytes ciphertext, and are told that the plaintext is a jpeg image. By using exhaustive search, can we eventually find the plaintext?)
- In fact, It can be shown that one-time-pad leaks no information of the plaintext, even if the attacker has arbitrary running time. Hence, it is sometime called “unbreakable”.
- CS4236 would look into the formulation of “Perfect Secrecy” of one-time-pad

- However, the length of the key is the same as plaintext.  
Useless in many applications.

<http://ciphermachines.com/otp>

- Nevertheless, it is practical in some scenarios.

see <http://ciphermachines.com/otp>

and the Venona Story  
(where one-time-pads fails)

(optional:

<https://www.nsa.gov/Portals/70/documents/about/cryptologic-heritage/historical-figures-publications/publications/coldwar/venon>



# Intuitively, Perfect Secrecy means:

Attacker's prior knowledge of the unknown plaintext  $x$ . (before knowing  $y$ )

Definition: A cryptosystem has *perfect secrecy* if  
for any distribution  $X$ , for all  $x, y$

$$\Pr(X=x | Y=y) = \Pr(X=x).$$

Attacker's updated knowledge of the unknown plaintext, after the attacker had seen the ciphertext  $y$ .

for any ciphertext  $y$  and plaintext  $x$ , the chances that an attacker correctly predicts  $x$  before knowing  $y$ , and after knowing  $y$ , are the same.

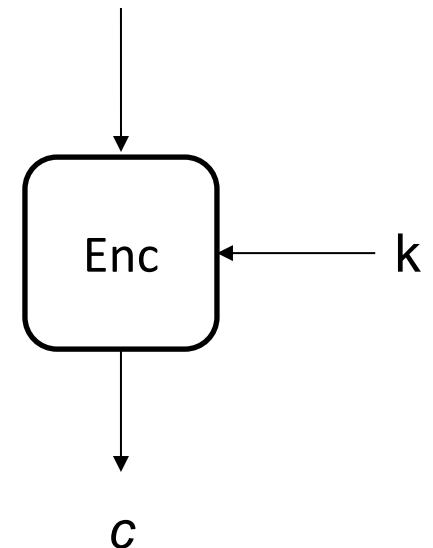
# E.g.

Optional

- Let  $c$  be the ciphertext of the Oscar's winner name, encrypted using some secret key.
- Bob gathered information from many sources and believed that the movie "*Alice in Crypto Land*" has 42% chance of winning.
- Now, suppose somehow, Bob knew  $c$ . With the additional knowledge of  $c$ , could Bob improve his guess? (any slight improvement would be useful).
- Let's assume that Bob has an extremely powerful machine that can exhaustively search all keys. Can he improve the guess?
  - (for DES, the answer is yes! How?)
  - (if the encryption scheme achieves perfect secrecy, the answer is no!)



"And the Oscar  
goes to xxxxxxxxx"



## 1.3 Modern Ciphers

Modern ciphers generally refer to schemes that use computer to encrypt/decrypt.

E.g. RC4, DES, A5, AES, RSA

Many modern symmetric ciphers employed rounds of substitution (the so called “S-box”) and permutation.

## **1.3.1 DES/Exhaustive Search**

# Modern ciphers

Designs of modern ciphers take into considerations of known-plaintext-attack, frequency analysis and other known attacks.

E.g.     DES (Data Encryption Standard, 1977)  
          RC4 (Rivest's Cipher 4, 1987)  
          A5/1 (used in GSM, 1987)  
          AES (Advanced Encryption Standard, 2001)

They are supposed to be “secure”, so that any successful attack does not perform noticeably better than exhaustive search.

(optional: Nevertheless, RC4 is broken in some adoptions, A5/1 is vulnerable, and DES’s key length is too short. Wiki on RC4, A5/1 and DES give quite good description. AES is believed to be secure, and classified as “Type 1” by NSA [https://en.wikipedia.org/wiki/NSA\\_cryptography#Type\\_1\\_Product](https://en.wikipedia.org/wiki/NSA_cryptography#Type_1_Product) )

## Exhaustive search and key length (see Work factor [PF2.3page91])

If the key length is 32 bits, there are  $2^{32}$  possible keys. Hence, the exhaustive search needs to “loop” for  $2^{32}$  times in the worst case. (On average,  $2^{31}$  times)

We can quantify the security of an encryption scheme by the length of the key. Consider a scheme **A** with 64-bit keys and a scheme **B** with 54-bit keys. Scheme **A** is more secure w.r.t. exhaustive search. (note that some schemes, e.g. RSA, have known attacks that are more efficient than exhaustively searching all the keys. In those cases, we still want to quantify the security by the equivalent of exhaustive search. For e.g, in the best known attack on a 2048-bit RSA, roughly  $2^{112}$  searches are required. Hence we treat its security equivalent to 112 bits. So, we say that the 2048-bit RSA has key strength of 112 bits).

How many bits is considered “secure”? (Tutorial 1)

read NIST Recommended key length for AES <http://www.keylength.com/en/4/>

# Exhaustive Search on DES

Key length of DES is 56 bits.

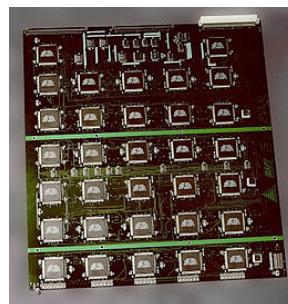
$$2^{56} \approx 2^{54}$$

While exhaustive search on 56 bits seemed infeasible in the 70s, very soon, it is possible using distributed computing or specialized chip.

RSA Security hosted a few challenges on DES. (Note: RSA is an encryption scheme, RSA Security is a company.)

**DES Challenge II-1:** "The secret message is: Many hands make light work." (found in 39 days using distributed computing, early 1998)

**DES Challenge II-2:** "The secret message is: It's time for those 128-, 192-, and 256-bit keys." (found in 56 hours using specialized hardware, 1998)



EFF's DES cracking machine.

A question is, why would an agency design a scheme that can be broken in the near future? Many believed that it was intentional.

# AES

# AES

- In 2000, a new standard for block cipher AES (Advance Encryption Standard) was proposed by NIST. The selection process was transparent and with worldwide involvement.
- NIST called for proposal in 1997 and received 21 submissions by Jun 1998. In 2000, *Rijndael* was selected as AES.
- Rijndael was invented by Belgian researchers Daemen and Rijmen.
- AES block length is 128, and key length can be 128, 192 or 256 bits.
- Currently, no known attacks on AES. (there are some attacks on the mode-of-operation)
- NSA classifies AES as “Suite B Cryptography”.

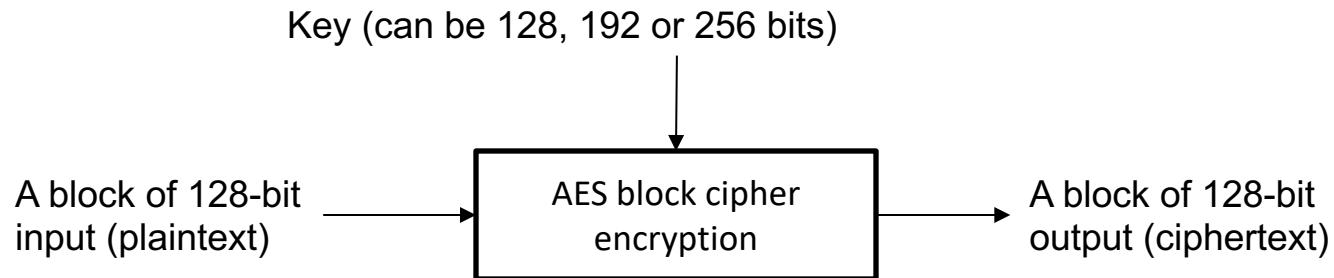
*“NSA Suite B Cryptography is a set of cryptographic algorithms promulgated by the National Security Agency as part of its Cryptographic Modernization Program. It is to serve as an interoperable cryptographic base for both unclassified information and most classified information.”*

see [https://en.wikipedia.org/wiki/NSA\\_Suite\\_B\\_Cryptography](https://en.wikipedia.org/wiki/NSA_Suite_B_Cryptography)

## 1.3.2 Block cipher & Mode-of-Operations

# Block Cipher

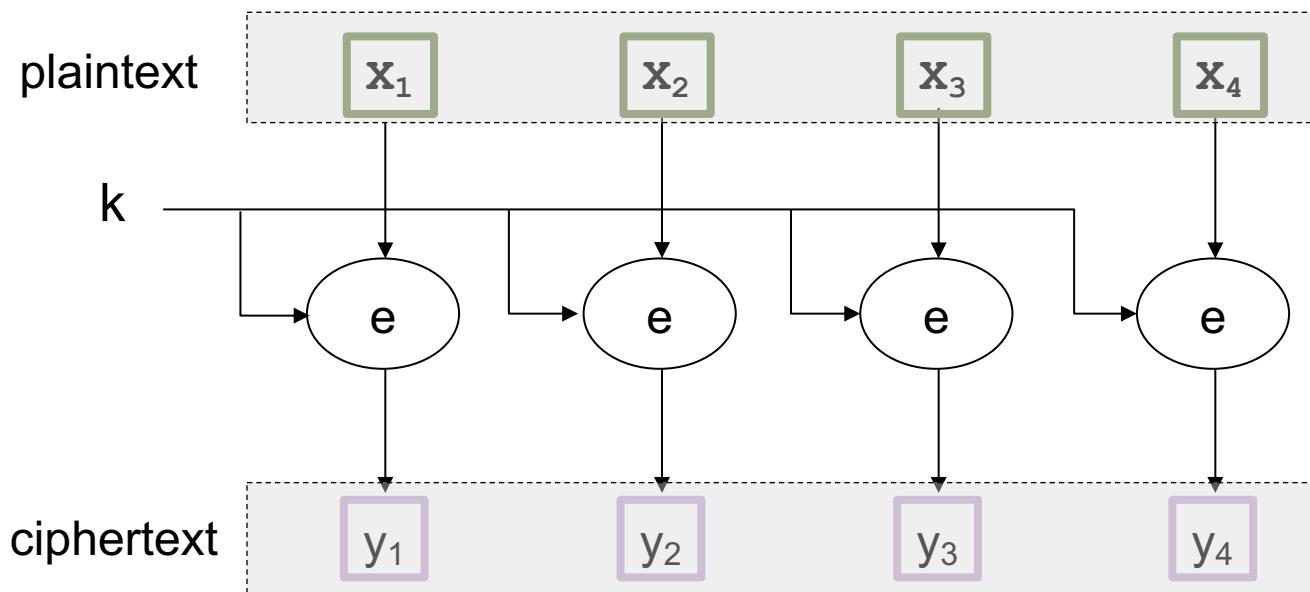
- DES and AES are also known as “Block Cipher”. Block cipher are designed for some fixed size input/output. E.g. AES is designed for 128 bits input/output.  
(I try not to call the input as plaintext, this is because in some mode-of-operations, e.g. Counter Mode, the input is not the plaintext)



- For large plaintext (say 10 MB), it is first divided into blocks, and the block cipher is then applied. The method of extending encryption from a single block to multiple blocks is not straightforward. It is called *mode-of-operation*.

# Mode-of-operation: ECB mode

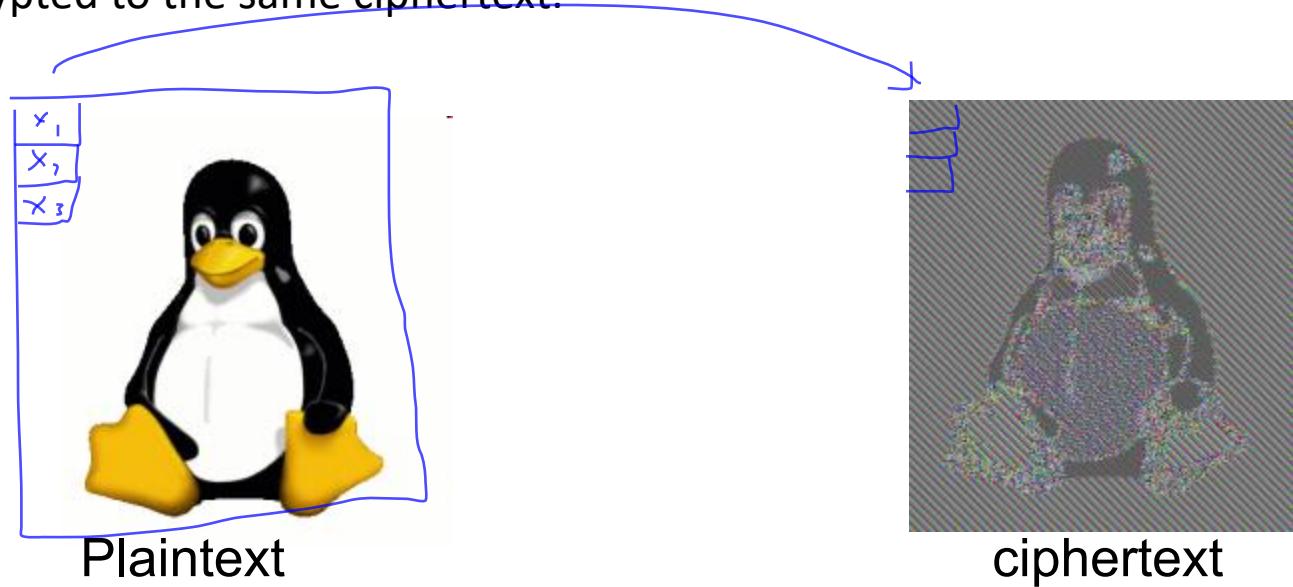
- Electronic Code Book naturally is the first to come into our mind.
- It divides the plaintext into blocks and then applies block cipher to each block, all with the same key.



- ECB is not secure! It leaks information.

# ECB

In the following example, the image is divided into blocks, and encrypted with some deterministic encryption scheme\* using the same key. Since it is deterministic, any two blocks that are exactly the same (for e.g. blocks in the white background) will be encrypted to the same ciphertext.



\*: An encryption scheme is “deterministic” in the sense that, the encryption algorithm will always produce the same output (i.e the ciphertext) when given the same input (i.e. the key and plaintext).

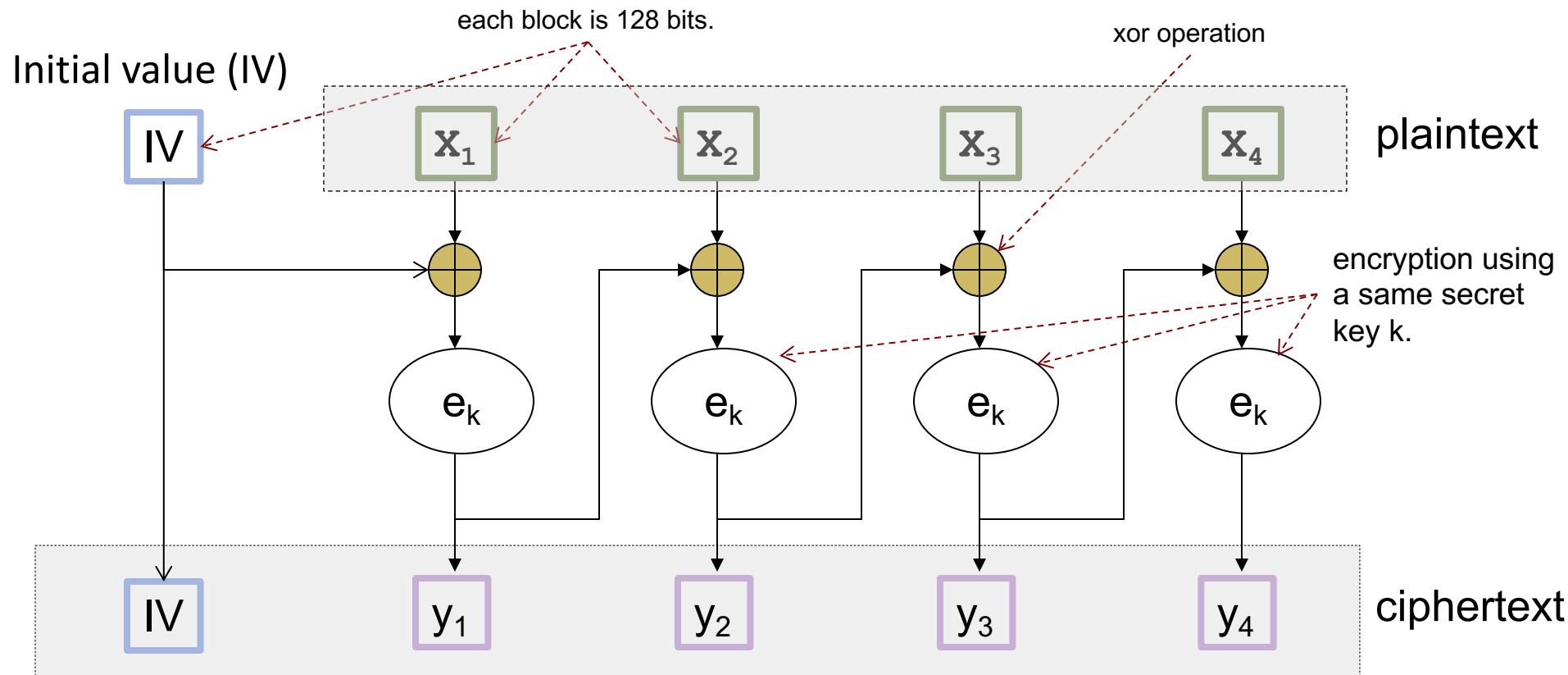
In contrast, a “probabilistic” encryption scheme produces different ciphertext even with the same input (key, plaintext).

AES is deterministic. However, if we employ AES with a randomly chosen initial value (IV), then it is probabilistic.

IV can be used - but not used as much because it will increase ciphertext

- To prevent the leakage of information shown in the previous slide, additional mechanisms are required.
  - One method uses IV for each block. This is rarely adopted as it increased the ciphertext size.
  - More common to adopt mode-of-operations that “link” or “chain” the blocks, so that two blocks with the same content would give different ciphertext. A popular mode-of-operations is CBC.
  - CTR (counter) mode is also popular. In certain sense, it is a stream cipher.

# mode-of-operation: Cipher Block Chaining (CBC) on AES



- The Initial Value (IV) is an arbitrary value chosen during encryption. So, it is different in different encryptions of the same plaintext. Depending on implementation, IV can be randomly chosen, obtain from a counter, or from other info.

$$y_0 = \text{IV.} \quad y_i = E_k(x_i \oplus y_{i-1}) \quad \text{for } i > 0$$

Note: In the above figure, we treat IV as part of the final ciphertext. The terminology is not consistent in the literature.

Some documents may state that “the final message to be sent are the IV and the ciphertext” (i.e. IV is not included in the “ciphertext”). In this module, when it is crucial, we will explicitly state whether IV is included or excluded. (e.g. “Ciphertext together with a IV”).

# Cipher Block Chaining (CBC) decryption

IV

$y_1$

$y_2$

$y_3$

$y_4$

ciphertext

exercise

IV

$x_1$

$x_2$

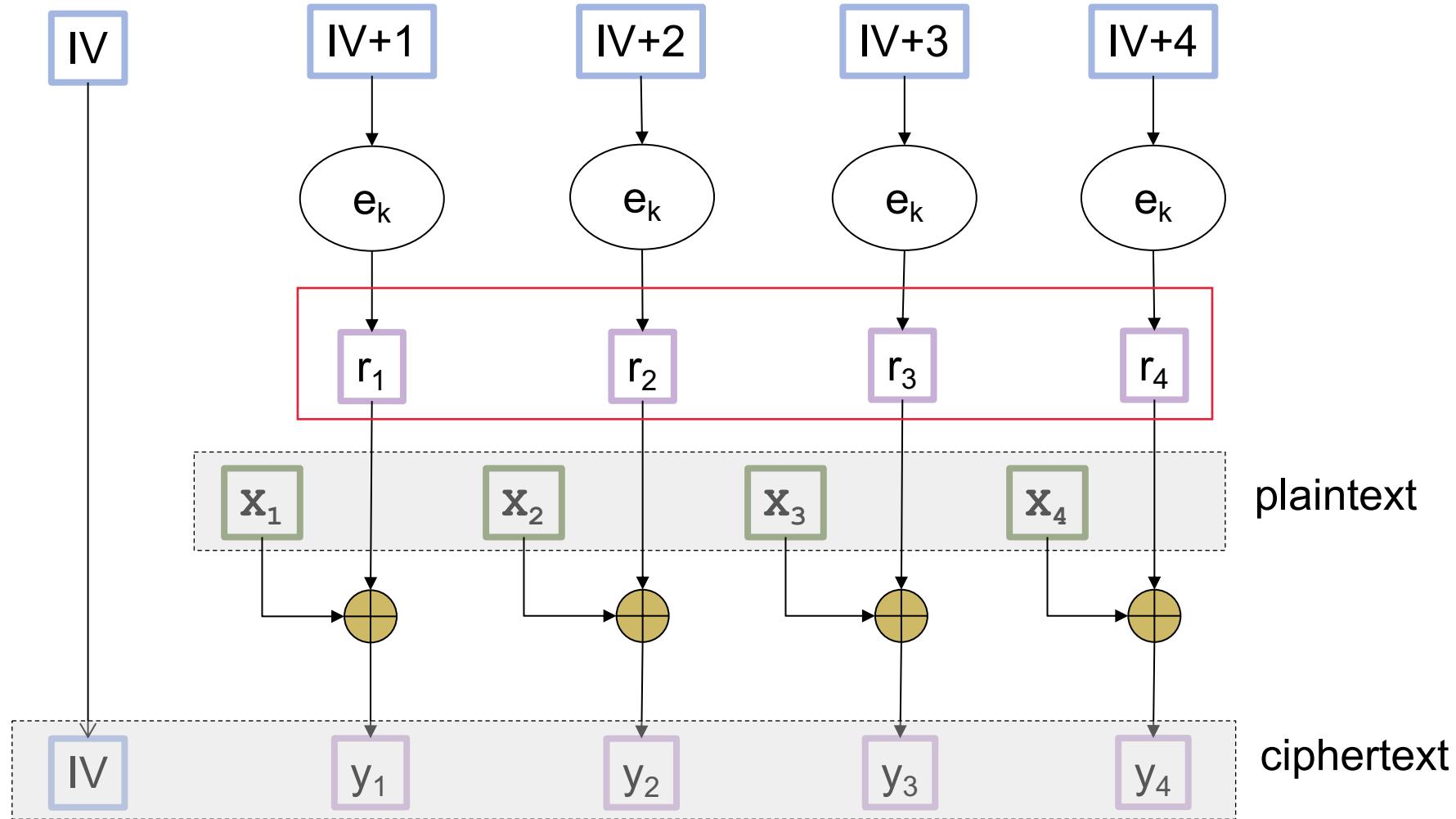
$x_3$

$x_4$

plaintext

# mode-of-operation: Counter mode (CTR) on AES

Initial value (IV)



This is a stream cipher. (next section)

# Programming example

This key can be randomly chosen or set by user (see crypto pitfalls). Of course, if the key is randomly chosen, it has to securely sent to the receiver and/or store in a secure place.

- Python.  
(package PyCryptodome

<https://pycryptodome.readthedocs.io/en/latest/src/cipher/aes.html>)

The IV should be randomly chosen.

```
>>> from Crypto.Cipher import AES
>>>
>>> key = b'Sixteen-byte key'
>>> iv  = b'Sixteen-byte  IV'
>>> cipher = AES.new(key, AES.MODE_CBC, iv)
>>> c=iv+cipher.encrypt(b'Plaintext of length with multiple of 16      bytes')
```

In Python, to display a byte sequence, we can use...

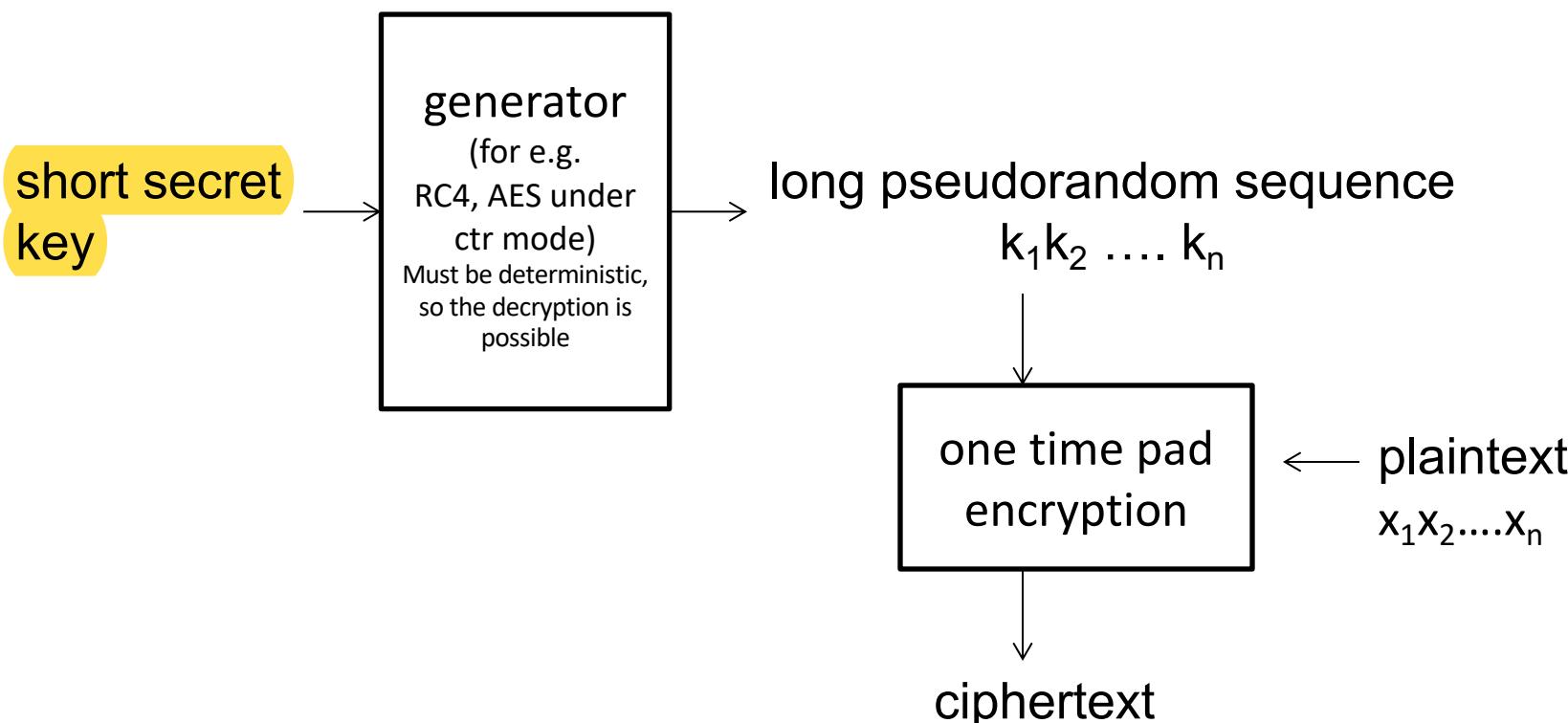
```
>>> from base64 import *
>>> b16encode(c)
b'536978746565E206279746520204956B186083256CACCBD1638AF4877FBF2AAFBEBCB66FE13C403D7CE8EA04D028E66CA6AE1294
FF51C2F363CCC8953137A6A3'
```

### 1.3.3 Stream Cipher and IVs

# Stream Cipher

Stream Cipher is “inspired” by one-time-pad.

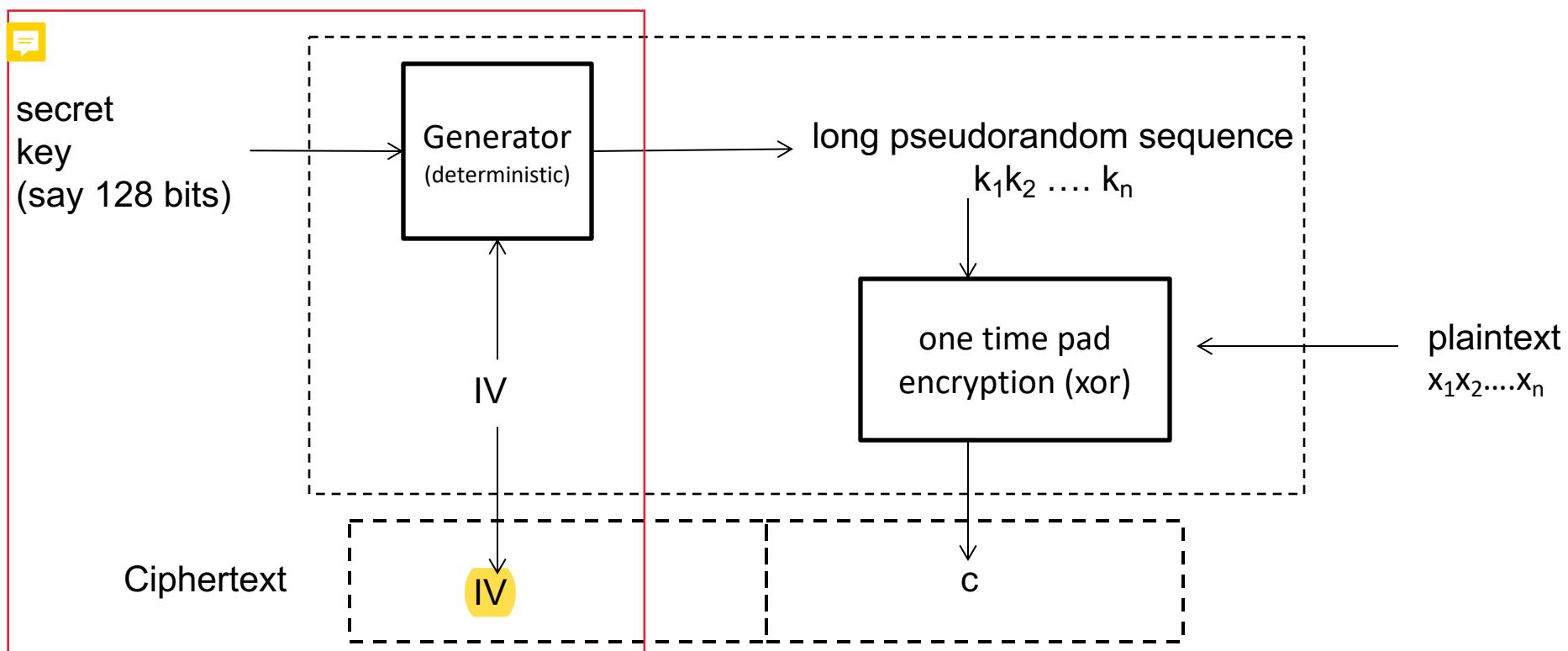
Suppose the plaintext is  $2^{20}$  bits, but the secret key is only 256 bits. Stream cipher generates a  $2^{20}$ -bit sequence from the key, and takes the generated sequence as the secret key in one-time-pad. The generator must be carefully designed, so that it gives ***cryptographically secure pseudorandom sequence***. (security requirement: difficult to distinguish the sequence from a truly random sequence – this is quite a strong requirement. It implies that it is difficult to get the short secret key from the sequence. It also implies that it is difficult to get part of the sequence after seen another part of the sequence.)



# Stream Cipher with IV

Most ciphers, including stream ciphers, have an Initial Value (IV). The IV can be randomly chosen, or from a counter.

- In stream cipher, a long pseudorandom sequence is generated from the secret key together with the IV. The final ciphertext contains the IV, followed by the output of the one-time-pad encryption.
- For decryption, the IV is extracted from the ciphertext. From the IV and the key, the same pseudorandom sequence can be generated and thus obtain the plaintext.



e.g.

**Encryption:** Given

15-bit Plaintext X = 0 0 0 0 0 1 1 1 1 1 0 0 0 0 0

short key = 0 1 0 1

Step 1: Randomly generates an IV, say

IV = 0 0 0 1

Step 2: From the short key and IV, generates a 20-bit sequence

K= 0 1 1 0 1 0 1 0 0 1 0 0 1 1 0

Step 3: outputs IV, follow by K xor X



**Decryption:** Given the short key and the ciphertext with the IV.

Step 1: Extracts the IV from the ciphertext

Step 2: From the short key and IV, generates the long sequence.

Step 3: Performs xor to get the plaintext.

# Why IV? What if the IV is always the same?

Suppose there isn't an IV (or the IV is always set to be a string of 0's)

Consider the situation where the same key is used to encrypt two different plaintexts

$$X = x_1, x_2, x_3, x_4, x_5 \text{ and}$$

$$Y = y_1, y_2, y_3, y_4, y_5$$

Further suppose that an attacker eavesdropped and obtained the two corresponding ciphertexts  $U, V$ .

The attacker can now compute

$$U \oplus V = (X \oplus K) \oplus (Y \oplus K)$$

By associative and commutative property of xor

$$U \oplus V = (X \oplus Y) \oplus (K \oplus K) = X \oplus Y.$$

So, from  $U$  and  $V$ , the attackers can obtain information about  $X \oplus Y$ , i.e. the following sequence

$$(x_1 \oplus y_1), (x_2 \oplus y_2), (x_3 \oplus y_3), (x_4 \oplus y_4), (x_5 \oplus y_5)$$

# What so big deal about revealing $X \oplus Y$ ?

Suppose  $X$  is an  $80 \times 120$  image of an animal. Each pixel is either black or white (0 or 1). The image can be represented as a  $(80 \times 120)$ -bit sequence where each bit corresponds to a pixel.

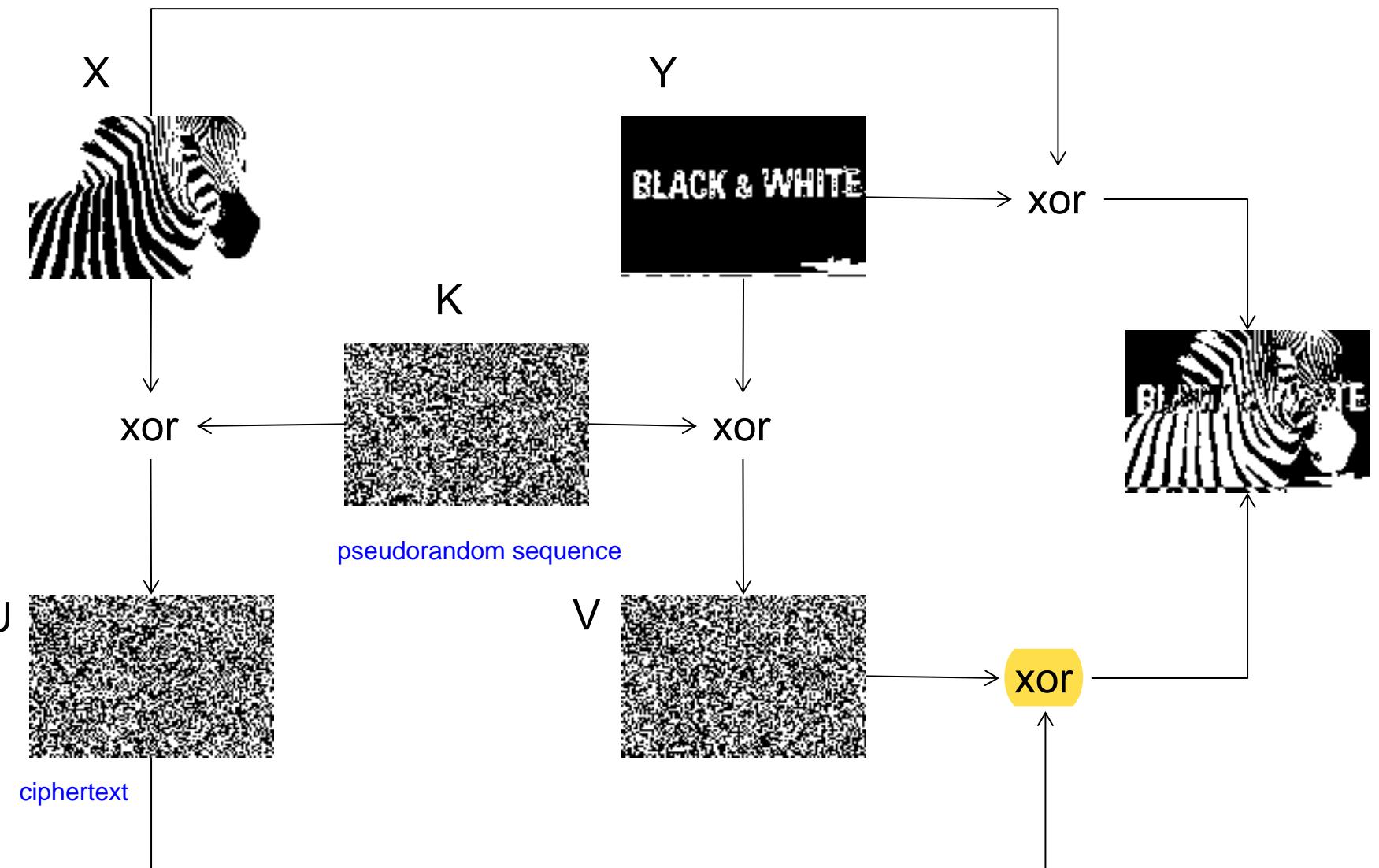
$Y$  is another  $80 \times 120$  pixels image rendering two words, which is similarly represented as a sequence.

Here is  $X \oplus Y$ .

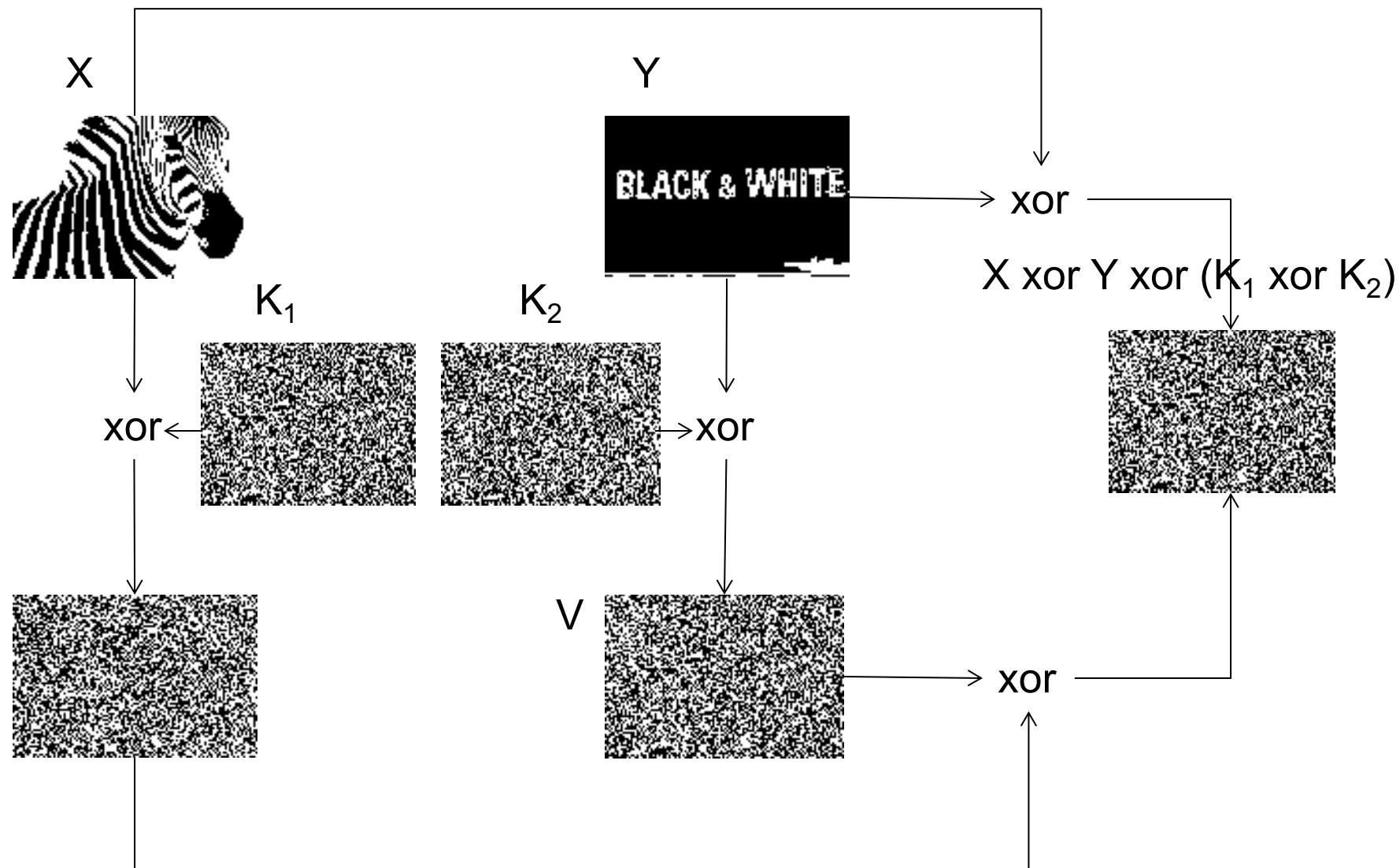


What is  $X, Y$ ?

# stream cipher without IV



# stream cipher with IV



## Role of IV

- If the IVs are different in two different processes of encryption, the two pseudorandom sequences will be different. Hence,
  - The ciphertexts of a same plaintext will be different under these two different encryptions.
  - If the two plaintexts are different, by xor'ing the two ciphertexts would not cancel out the pseudorandom sequences.
- IV makes an encryption “probabilistic”.

## Role of IV

- IV are also applied to CBC. The reason is the same. We want the encryption to be non-deterministic. That is, two different encryptions of the same plaintext would give two different ciphertexts.
- Without IV, the encryption is deterministic. If the encryption is deterministic, this leaks information on whether the plaintext of two ciphertexts are the same.

Consider the scenario where an attacker is given  $C_1$  and  $C_2$ . If the encryption is deterministic, then the attacker can derive that the plaintext are the same iff  $C_1 == C_2$

# 1.4. Examples of attacks

1.4.1 Triple DES & Meet-in-the-middle

1.4.2 Padding Oracle Attack

- Notions of Oracle in security analysis
- The attack
- Implications

## **1.4.1 Triple DES & Meet-in-the-middle attack**

[http://en.wikipedia.org/wiki/Meet-in-the-middle\\_attack](http://en.wikipedia.org/wiki/Meet-in-the-middle_attack)

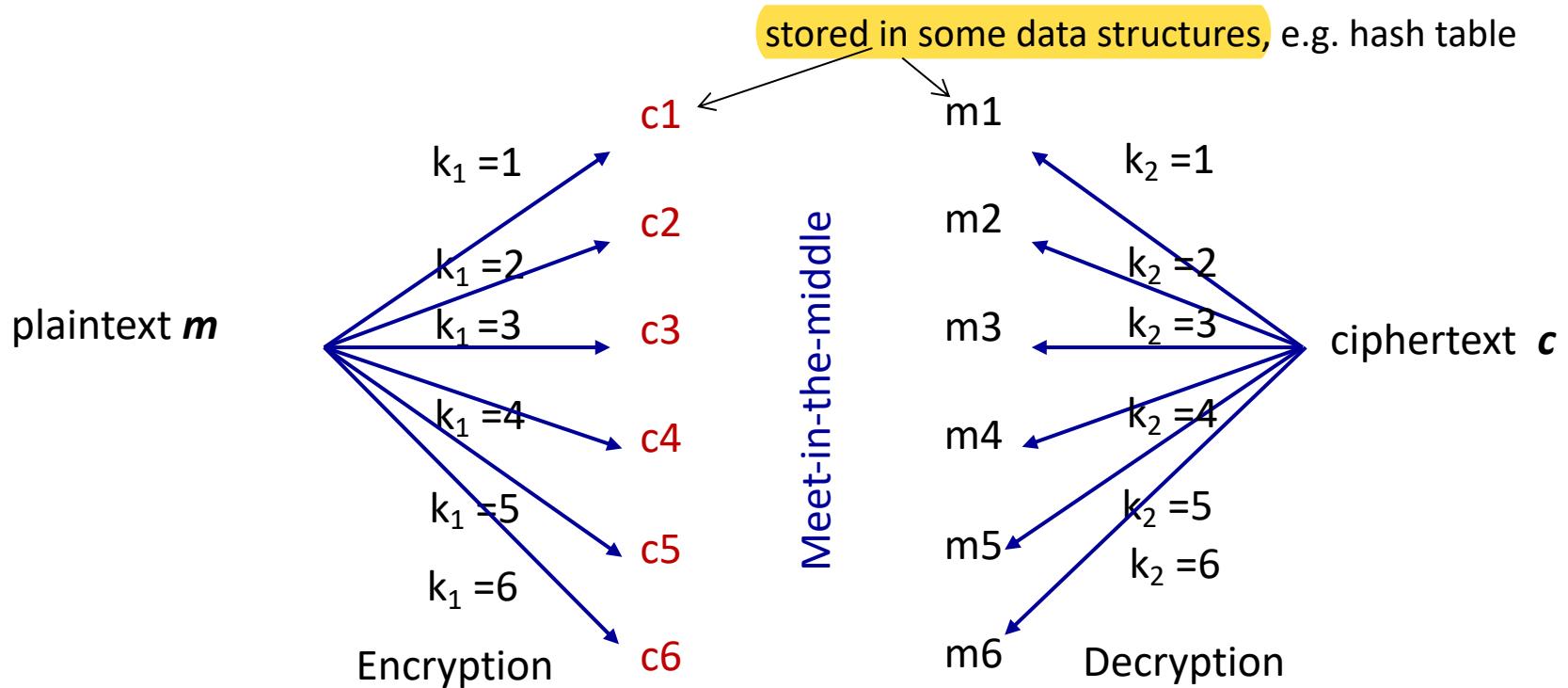
## (d) Triple DES

- DES is not secure w.r.t. today computing power. One way to improve it is by multiple encryptions: encrypt the plaintext twice or more, using different keys.
- DES doesn't form a group in the sense that,  $E_{k_1}(E_{k_2}(x))$  is not the same as  $E_{k_3}(x)$  for some  $k_3$ .
- Let us consider *double* encryption and known plaintext attack. That is, the adversary has a plaintext  $m$  and the corresponding ciphertext  $c$ , and wants to find the two secret keys  $k_1, k_2$ .
- Using exhaustive search, what is the amount of DES encryption/decryption required?  $2^{56+56}$ . That is key-strength seems to double to 112. But this is not true. Attacker can do better.... using more storage space.

## Meet-in-the-middle Attack

- Not to confuse “meet-in-the-middle” with “man-in-the-middle” attack.
- Introduced by Diffie & Hellman in 1977.
- This is a *known plaintext attack*. That is, attacker has at least a pair  $(m, c)$  of plaintext and the corresponding ciphertext.

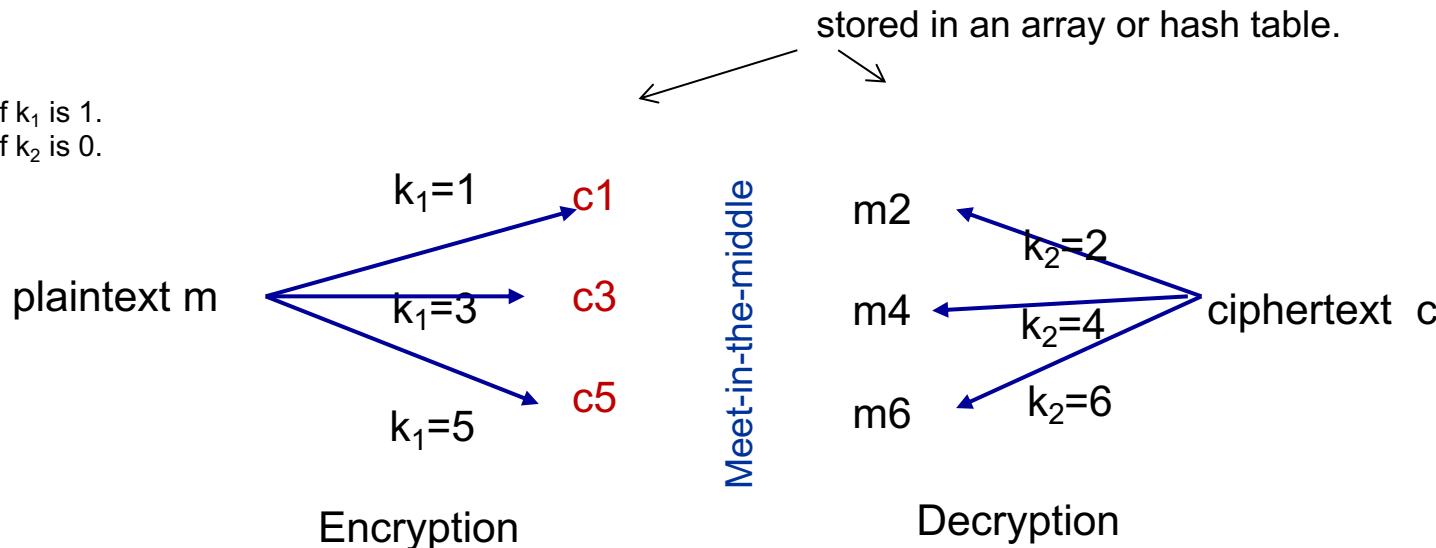
# Meet-in-the-middle attack



- Given  $c$  and  $m$ , find the two keys.
  - Compute two sets  $C$  and  $M$ .  $C$  contains ciphertexts of  $m$  encrypted with all possible keys.  $M$  contains plaintexts of  $c$  decrypted with all possible keys.
  - Find common element in  $C$  and  $M$ . From the common element, we can obtain the two keys.
- In the above meet-in-the-middle attack, the attacker only have to perform 6 encryptions and 6 decryptions. In general, for  $k$ -bit keys, it reduces the number of crypto operations to  $2^{k+1}$  using  $2^{k+1}$  space.

# Tradeoff with time and space

Last bit of  $k_1$  is 1.  
Last bit of  $k_2$  is 0.



- If  $2^{k+1}$  storage is too much, we can have a tradeoff.
- Given  $\mathbf{m}, \mathbf{c}$ .
  1. Exhaustively selects last  $s$  bits of  $k_1$ , and last  $s$  bits of  $k_2$
  2. For each selection above, carries out meet-in-the-middle attack. If successful, stops the exhaustive search.
- The storage requirement dropped to  $2^{k-s+1}$ , but number of cryptographic operations increased to  $2^{2s} 2^{k-s+1} = 2^{s+k+1}$ .

# 3DES

- Remedy--- Use Triple encryptions, but 2 keys.

a)  $E_{k1} ( E_{k2} ( E_{k1} ( x ) ) )$ .

or

b)  $E_{k1} ( D_{k2} ( E_{k1} ( x ) ) )$ .

Both (a) and (b) are believed to have the same level of security. However, version (b) can be more convenient. By choosing  $K1=K2$ , then it is same as single encryption.

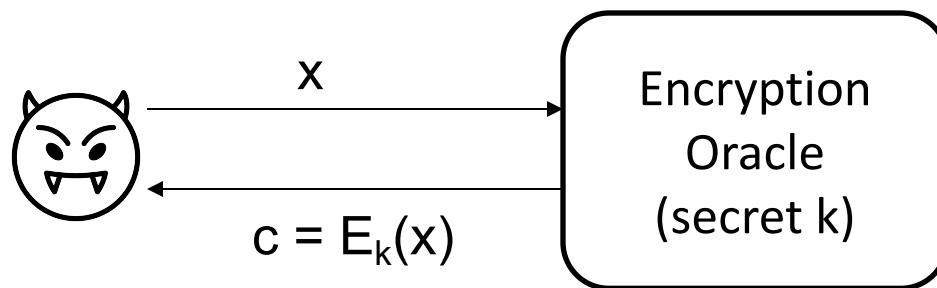
- Also known as 3DES, TDES, TDEA, 2TDES, 3TDES (using 3 keys)

- Currently, there is no known efficient attacks on triple DES.  
However, compare to AES, the triple DES is less efficient w.r.t.  
encryption/decryption time)
- Triple DES is still in used recently. (I do not know an example but won't be surprised that some systems still use it)  
(3DES was the default encryption in Outlook 2007. See its help page: <http://office.microsoft.com/en-sg/outlook-help/encrypt-messages-HP006369952.aspx> )

## 1.4.2 Padding Oracle Attack (assignment 1)

# Oracle in security analysis

- Recap that in security analysis, it is important to formulate (1) what information the attackers have; (2) attackers' goals.
- One type of information is obtained via a query-answer system, known as ***Oracle***. The attackers can send in queries, and the ***Oracle*** will output the answer. E.g.
  - **Encryption Oracle.** On query a plaintext  $x$ , the oracle outputs the ciphertext  $E_k(x)$  where the key  $k$  is a secret key.
  - **Decryption Oracle.** On query a ciphertext  $c$ , the oracle outputs the plaintext  $D_k(x)$  where the key  $k$  is a secret key.
- An attacker can send multiple queries.



# Padding Oracle attack

- The attacker have:
  - A ciphertext which include the iv:  $(iv, c)$
  - Access to the “Padding” Oracle
- Attacker’s goal
  - The plaintext of  $(iv, c)$
- Note: the ciphertext is encrypted with a secret key  $k$ . The Padding Oracle knows  $k$ .
- Padding Oracle:
  - Query: A ciphertext. (the ciphertext is encrypted using  $k$ )
  - Output: YES, if the plaintext is in the correct “padding” format.  
NO, otherwise

# Padding Format

- The block size of AES is 128 bits (or 16 bytes). Suppose the length of the plaintext is 200 bits, it will be fitted into two blocks, with the remaining 56 bits “padded” with some values.



- There are many ways to fill in the values. In any case, an important piece of information must be encoded: the number of padded bit. If this info is missing, the receiver will not know the length of the plaintext.
- Next slide describes a padding format “standard”.

# Padding - PKCS#7

- PKCS#7 is a padding standard.

Read [https://en.wikipedia.org/wiki/Padding\\_\(cryptography\)#PKCS7](https://en.wikipedia.org/wiki/Padding_(cryptography)#PKCS7)

- The following example is self-explanatory.

Suppose the block size is 8 bytes, and the last block has 5 bytes (thus 3 extra bytes required), padding is done as follow:

DD DD DD DD DD DD DD DD

DD DD DD DD DD **03 03 03**

- In general, the paddings are:

01

02 02

03 03 03

04 04 04 04 etc.

- If the last block is full, i.e. it has 8 bytes, an extra block of all zeros is added.

# Padding oracle attack on AES CBC mode.

- AES CBC mode is not secure against padding oracle attack, (when padding is done with PKCS#7) in ciphertext only attack.
- Let us look at this example:
  - Attacker has  $(\text{IV} \parallel \mathbf{c})$ , which is one block of IV, and 1 block of  $\mathbf{c}$ . For convenience, let us assume that the attacker knows that the block is padded with 3 bytes, that is, the length of plaintext is 5 bytes.
  - The attacker wants to find the value of  $x_5$ . (ciphertext only attack)
  - The attacker can send any  $(\text{iv}, \text{ciphertext})$  to the oracle, and the oracle will tell the attacker whether the decrypted plaintext is padded correctly.

**IV** = 

$v_1$	$v_2$	$v_3$	$v_4$	$v_5$	$v_6$	$v_7$	$v_8$
-------	-------	-------	-------	-------	-------	-------	-------

**c** = 

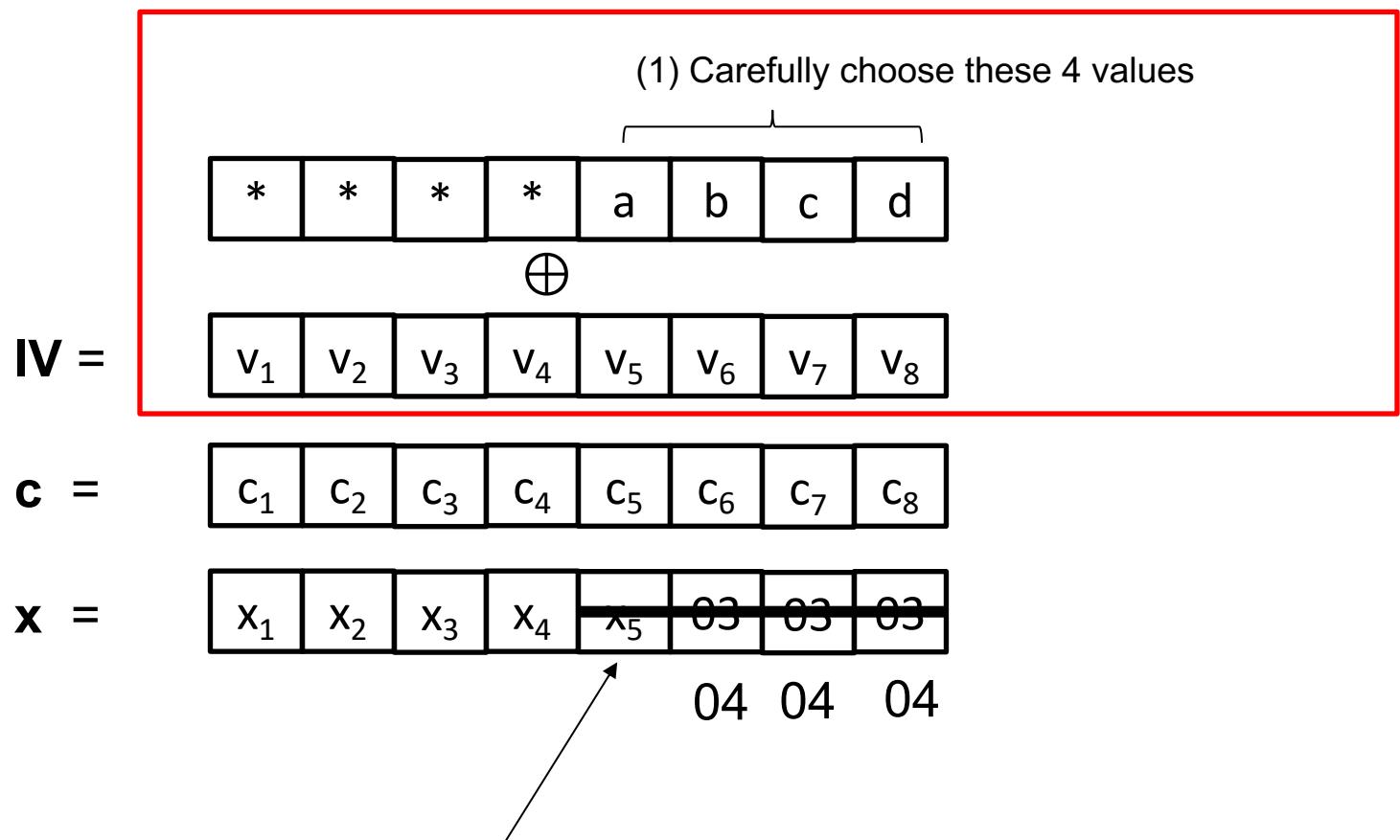
$c_1$	$c_2$	$c_3$	$c_4$	$c_5$	$c_6$	$c_7$	$c_8$
-------	-------	-------	-------	-------	-------	-------	-------

**x** = 

$x_1$	$x_2$	$x_3$	$x_4$	$x_5$	03	03	03
?	?	?	?	?			

# Main idea

- Carefully choose the 4 values, so that  $\mathbf{x}$  is of that form.

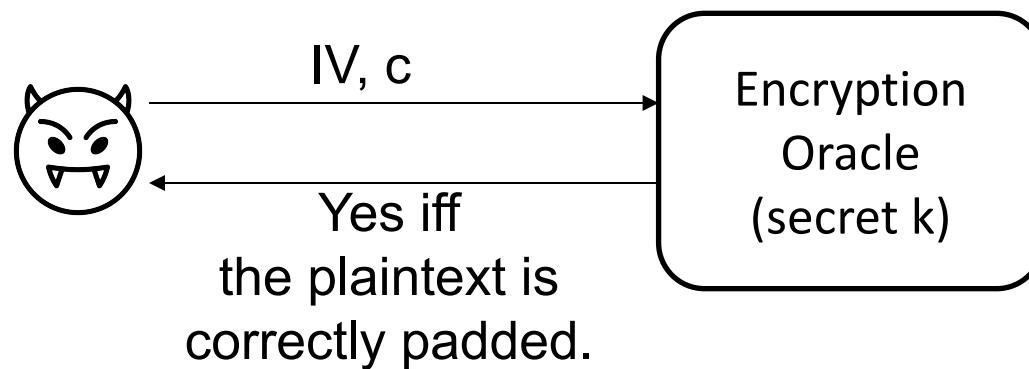


Some value that can be derived  
from  $x_5$  ,  $a$ , and  $v_5$ .

# Padding oracle attack on AES CBC mode.

- This algorithm outputs the value of  $x_5$ .

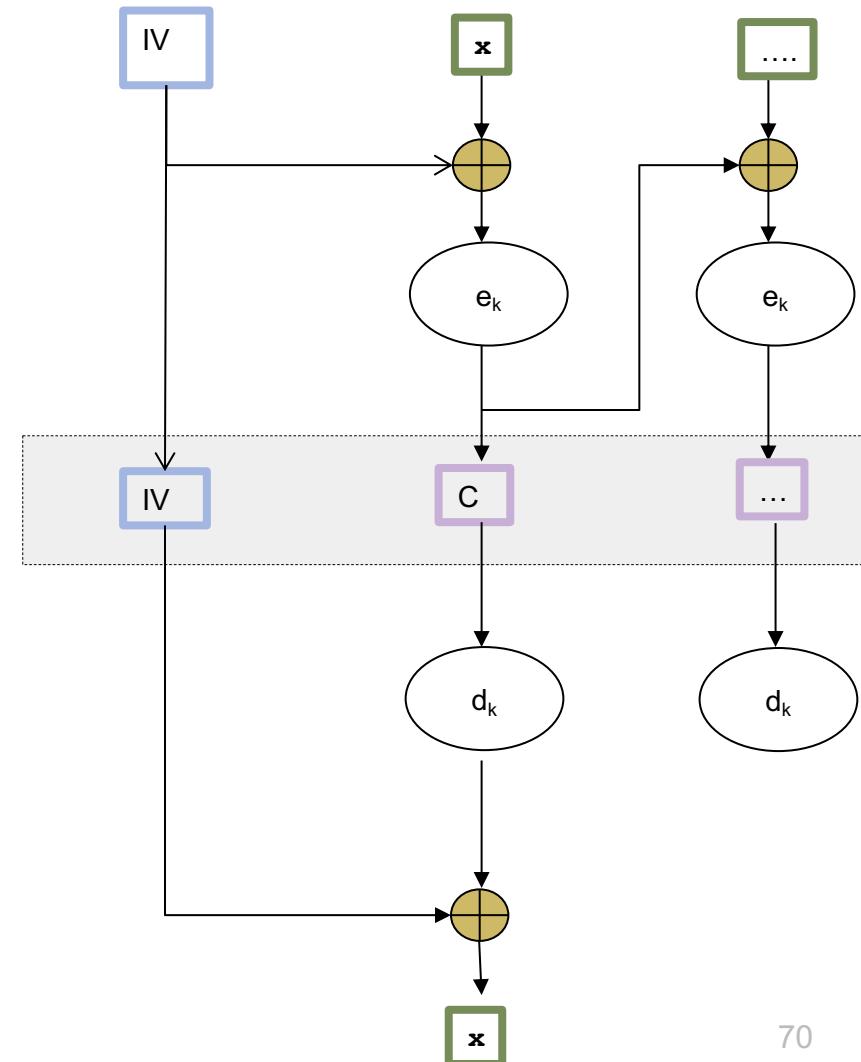
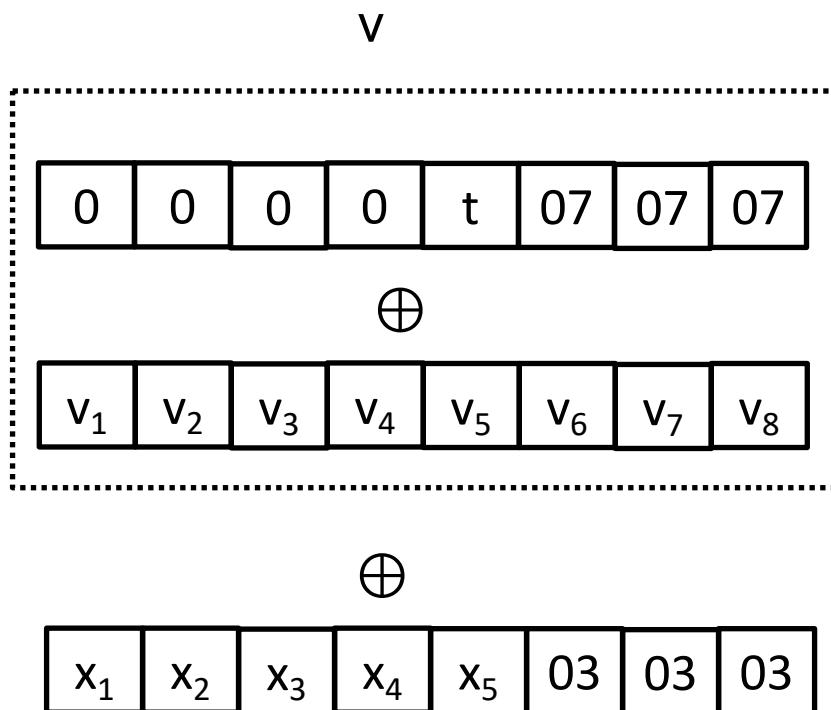
1. For  $t = 0$  to  $255$  *// binary representation*
2. Let  $v = \text{IV} \oplus \boxed{0 \ 0 \ 0 \ 0 \ t \ 07 \ 07 \ 07}$
3. Sends the two-block query ( $v \parallel c$ ) to **Oracle**.
4. If **Oracle** gives YES, then outputs  $(04 \oplus t)$
5. End-for-loop



# Why it works?

- CBC mode

- Note:  $07 \oplus 03 = 04$



## Remarks

- We can easily extend the algorithm to find all the plaintext.
- The algorithm needs to know the plaintext's length. It is possible to determine the length (exercise).
- This attack is practical. There are protocols (*which are interactions between two or more entities*) between a client and server which performs this:

*If the client submits a ciphertext whose plaintext is not padded correctly, the server will reply with an error message.*
- Now if an attacker obtained a ciphertext, the attacker can carry out the protocol with the server so as to get the plaintext.

## The attack illustrates:

- The notion of *Oracle*.
- There are situations where seemingly useless information can be useful. So, leakage of any “bit” of information should be avoided.

# 1.5 Cryptography Pitfalls

A secure encryption scheme can be vulnerable if not implemented properly. This section gives some examples.

1.5.1 – Wrong choice of IV, reusing one-time-pad

1.5.2 – Random number is predictable

1.5.3 – Modify existing or make your own encryption scheme

1.5.4 – Reliance on Obscurity: Kerckhoff's principle.

(to be studied later)

- Using encryption for the wrong purpose (e.g. using encryption scheme to ensure message integrity)
- Side Channel Attack

## 1.5.1 Wrong choices of IV. Reusing one-time-pad

# Wrong choices of IV

Some applications overlooked IV generation. As a result, under some situations, the same IV is reused.

- E.g. To encrypt a file F, the IV is derived from the filename. It is quite common to have files with the same filename.

(**Read Schneier on Security, Microsoft RC4 Flaw.**

[https://www.schneier.com/blog/archives/2005/01/microsoft\\_rc4\\_f.html](https://www.schneier.com/blog/archives/2005/01/microsoft_rc4_f.html)

<http://eprint.iacr.org/2005/007.pdf> )

- E.g. When using AES under the “CBC mode”, the IV has to be unpredictable to prevent a certain type of attack. (So, it is vulnerable to choose IV as 1,2,3,...)

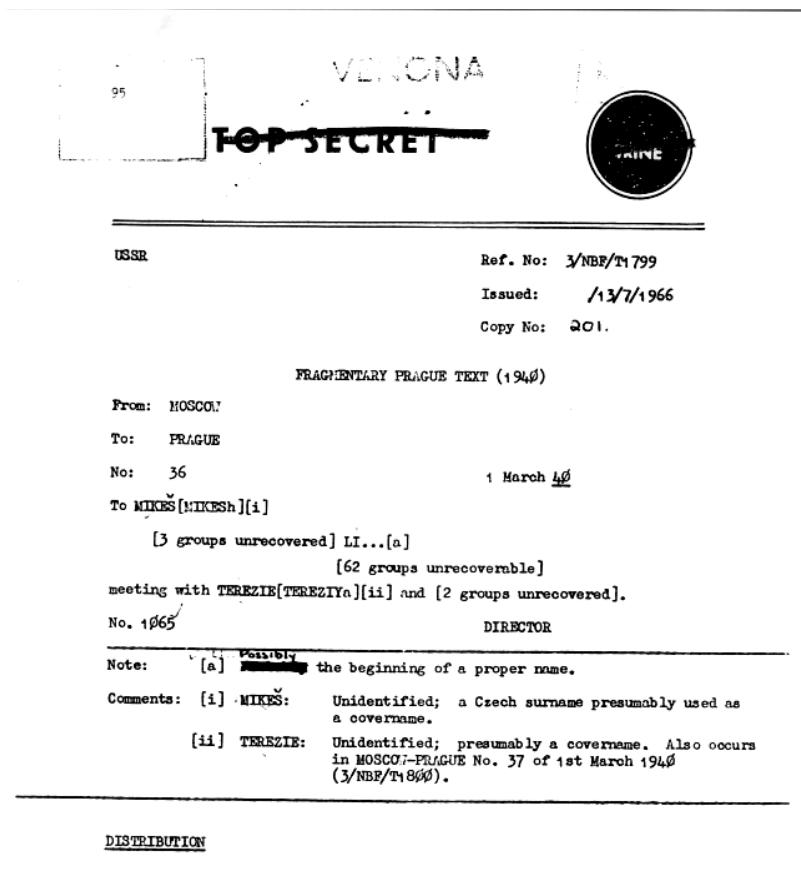
The well-known BEAST attack exploits this.

(optional: <http://resources.infosecinstitute.com/ssl-attacks/> )

# Reusing one-time-pad

- The Verona project is a classic example on such failure.

(optional: [https://www.nsa.gov/about/\\_files/cryptologic\\_heritage/publications/coldwar/venona\\_story.pdf](https://www.nsa.gov/about/_files/cryptologic_heritage/publications/coldwar/venona_story.pdf) )



## 1.5.2 Predictable secret generation

(tutorial)

- **Scenario 1:**
  - You are coding a program for a simulation system, for e.g. to simulate road traffic.
  - In the program, you need a sequence of random numbers, for e.g. to decide the speed of the cars.
  - How to get these random numbers?
- **Scenario 2:**
  - You are coding a program for a security system.
  - In the program, you need a random number. For e.g. you need to generate a random number as a temporary secret key.
  - How to get these random numbers?

# to be discussed in tutorial

- In Java, what is the different between the following?
  - `java.util.Random`
  - `java.security.SecureRandom`
- In C, what is the different between using the following

```
#include <time.h>
#include <stdlib.h>

srand(time(NULL)) ;
int r = rand() ;
```

and a complicated version below?

```
int byte_count = 64;
char data[64];
FILE *fp;
fp = fopen("/dev/urandom", "r");
fread(&data, 1, byte_count, fp);
fclose(fp);
```

## 1.5.3 Designing your own cipher

- Don't design your own crypto, or even make slight modification to existing scheme... unless you has in-depth knowledge on the topic.
- “Don’t roll your own crypto”

read <http://security.stackexchange.com/questions/2202/lessons-learned-and-misconceptions-regarding-encryption-and-cryptology/2210#2210>

## 1.5.4 Reliance on Obscurity: Kerckhoffs's Principle

## Kerckhoffs's principle

A system should be secure even if everything about the system, except the secret key, is public knowledge.

## Security through Obscurity

To hide the design of the system in order to achieve security.

# Examples (against obscurity)

- RC4 was introduced in 1987 and its algorithm was a trade secret. In 1994, a description of its algorithm was anonymously posted in a mailing group. <http://en.wikipedia.org/wiki/RC4>
- MIFARE Classic, a contactless smartcard widely used in Europe. It uses a set of proprietary protocols/algorithms. However, they are reverse-engineered in 2007. It turns out that the encryption algorithms are already known to be weak (using only 48bits) and breakable.

<http://en.wikipedia.org/wiki/MIFARE>

Presentation (video) by the researcher who reversed-engineered it:

(optional) <http://www.youtube.com/watch?gl=SG&hl=en-GB&v=QJyxUvMGLr0>

(the algo was revealed at 14:00)

# Examples (for obscurity)

- It is not advisable to reveal the computer network structure and settings (for example, location of firewall and the firewall rules), although these are not “secrets”, and many users within the organization may already know the settings.
- Although the algorithm has to be made public, it is not advisable to publish the actual program used in a smart-card. By publishing the program/code, advisory may able to identify implementation flaw that was previously unaware of, or carry out side-channel attacks. Nevertheless, a sophisticated advisory may able to reverse-engineer and obtain the program/code.
- Usernames are not secrets. However, it is not advisable to publish all the usernames.
- In general, obscurity can be used as one layer of a ***defense in depth*** strategy. It could deter or discourage novice attackers, but ineffective against attackers with high skill and motivation.

see

<http://technet.microsoft.com/en-us/magazine/2008.06.obscurity.aspx>

[http://en.wikipedia.org/wiki/Security\\_through\\_obscurity](http://en.wikipedia.org/wiki/Security_through_obscurity)

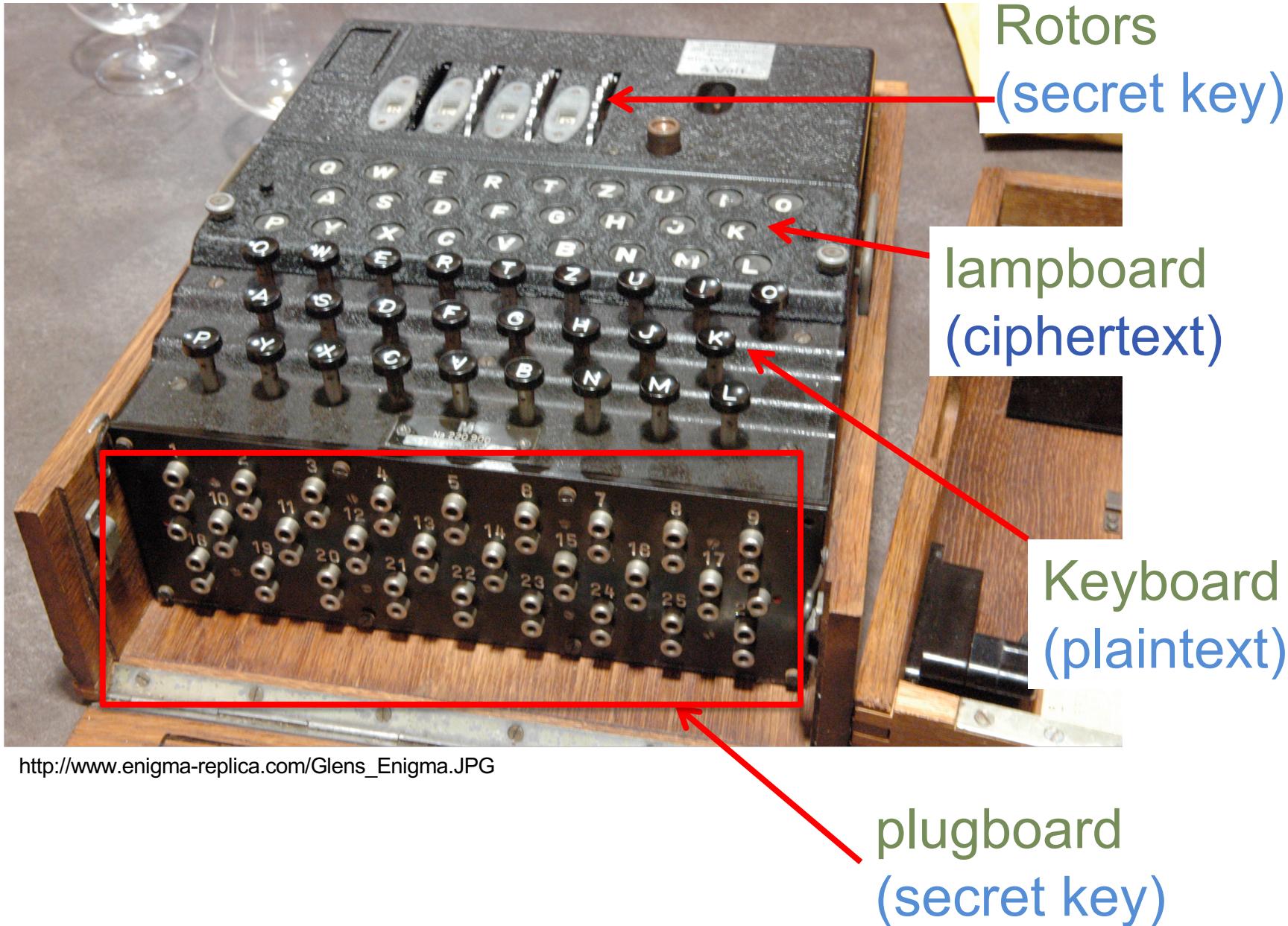
In this module, we always assume that the attackers know the algorithms.

## **1.6 Some historical Facts**

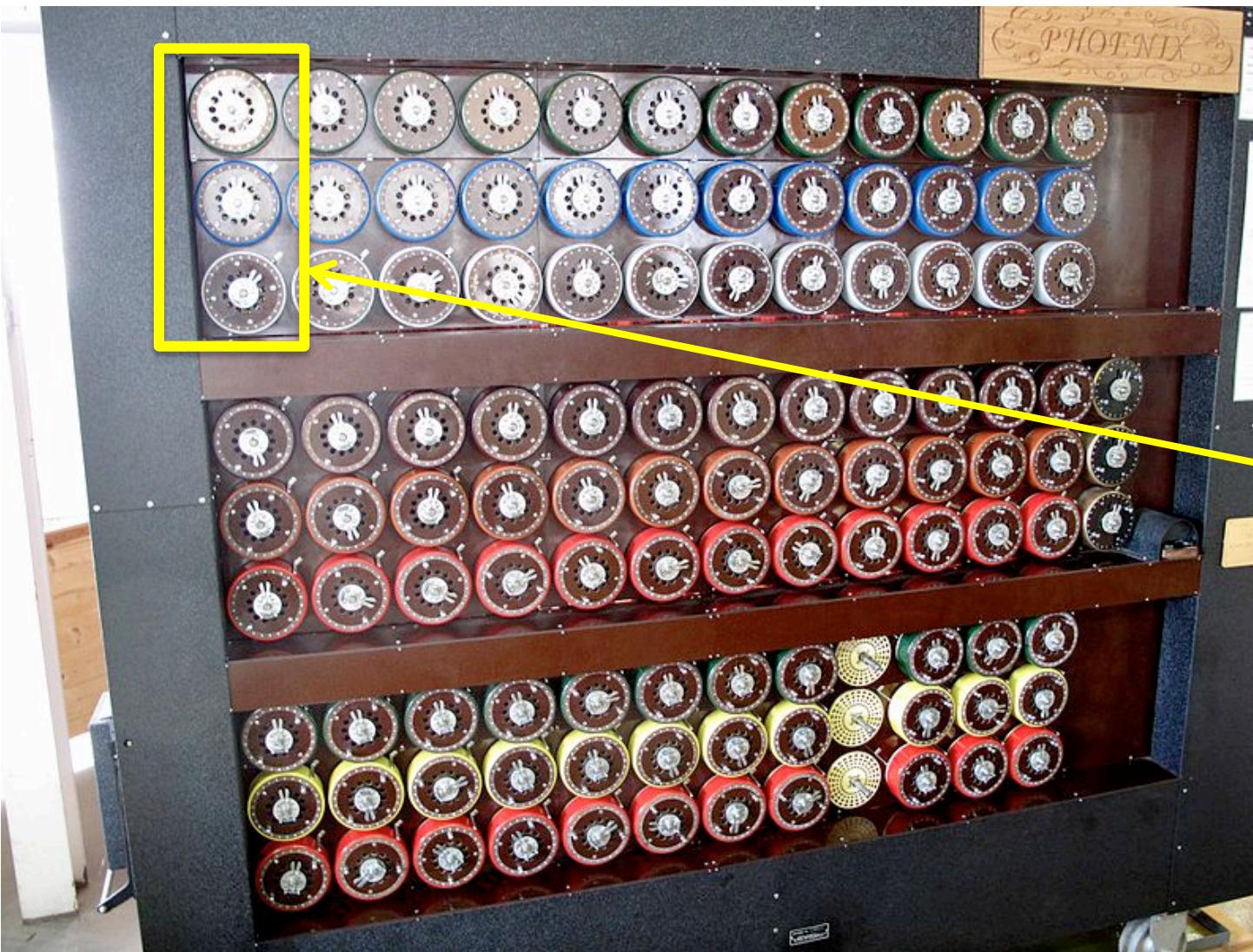
# Cryptography: History

- Cryptography is closely related to warfare and can be traced back to ancient Greece. Its role became significant when information is sent over-the-air. Cryptanalysis is one of the driving forces to the invention of computer (e.g. Colossus computer [https://en.wikipedia.org/wiki/Colossus\\_computer](https://en.wikipedia.org/wiki/Colossus_computer)).
- WWII: Famous encryption machines include the Enigma, and the Bombe (that helped to break Engima).

# Enigma



# Working rebuilt bombe at Bletchley Park museum.



simulates  
the 3  
rotors  
in one  
Enigma  
machine

# Modern Ciphers

## DES

- 1977: DES (Data Encryption Standard), 56 bits.

During cold war, cryptography, in particular DES was considered as “Munition”, and subjected to export control. (Currently, export of certain cryptography products is still controlled by US.)

Read the section on Singapore in <http://www.cryptolaw.org/cls2.htm>

- 1998: A DES key broken in 56 hours.  
Triple DES (112 bits) is still in used.
- 2001: AES (Advanced Encryption Standard). NIST. 128, 192, 256 bits.

## RC4

- Designed by Ron Rivest (RSA Security) in 1987.
- Initially a trade secret. Algorithm leaked in 1994.
- Used in WEP (for wifi) in 1999. WEP implementation has 40 or 104-bit key. WEP was widely popular.
- 2001: a weakness in how WEP adopts RC4 is published by Fluhrer, Mantin, Shamir.
- 2005: a group from FBI demonstrated the attack.
- Industry switched to WPA2. (with WPA as an intermediate solution).

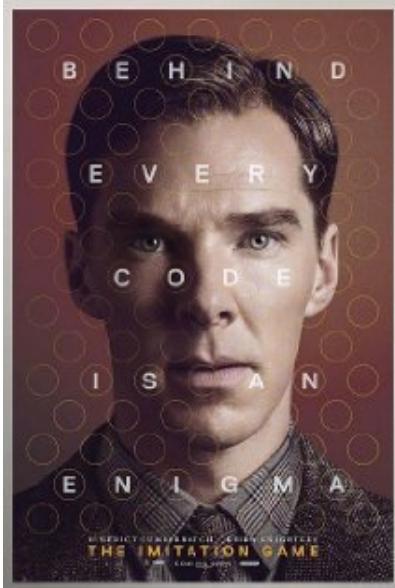
*Question:*

*Bob encrypted a .mp3 music file using winzip, which uses the 256-bit key AES. He choose a 6-digit number as password. Winzip will generate the 256-bit key from the 6-digit password using a “hash” function, say SHA1.*

*Alice obtained the ciphertext. Alice also knew that Bob used a 6-digit password.*

*Given a “guess” of the 256-bit key, Alice can determine whether the key can successfully decrypted the file. How many guesses Alice needed to make in order to get the video?*

# Movie about encryption



## The Imitation Game.

During World War II, mathematician Alan Turing tries to crack Enigma with help from fellow mathematicians.

<http://www.imdb.com/title/tt2084970/>



## U-571

Fictional plot on how a U-boat was captured. Actual U-boat captured: U-110, U-505, U-570, U-744, U-1024.

Prize of capturing a u-boat instead of sinking it.... Engima!