External Sort

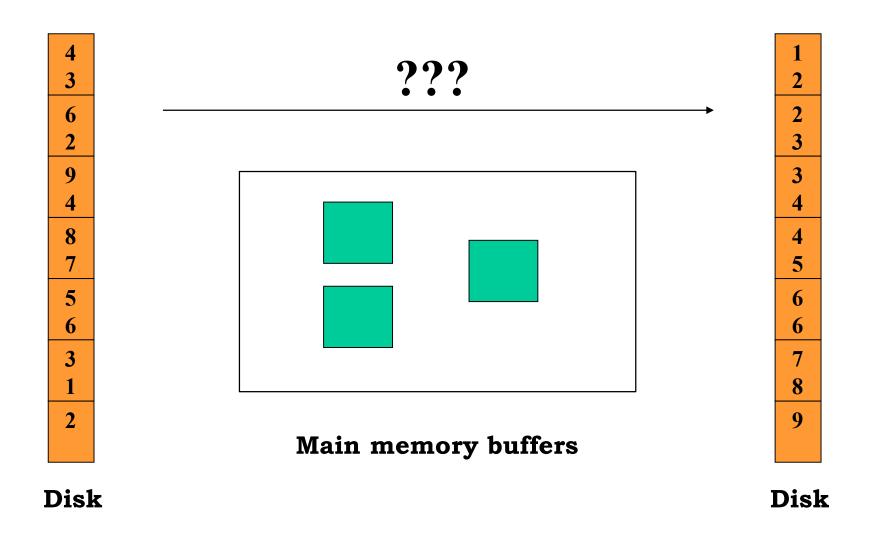
"There it was, hidden in alphabetical order."

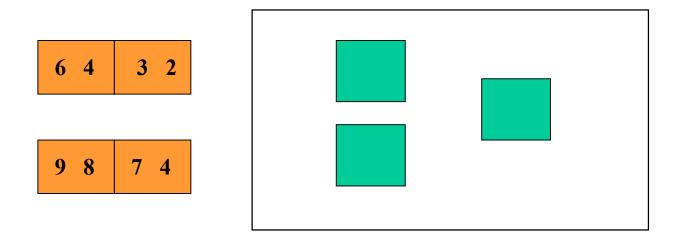
Rita Holt

External Sorting

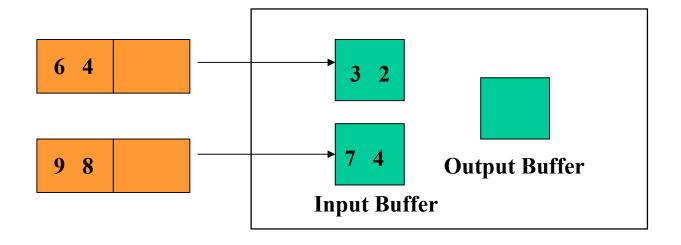
- A classic problem in computer science!
- Data requested in sorted order
 - e.g., find employees in increasing salary order
- Sorting is used in many applications
 - First step in bulk loading operations
 - Eliminating duplicate copies in a collection of records (How?)
 - Evaluating join or set operations (How?)

Challenge: Sort 1TB of data with 1GB of RAM



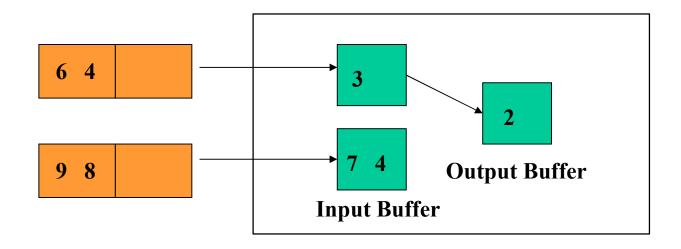


Main memory buffers

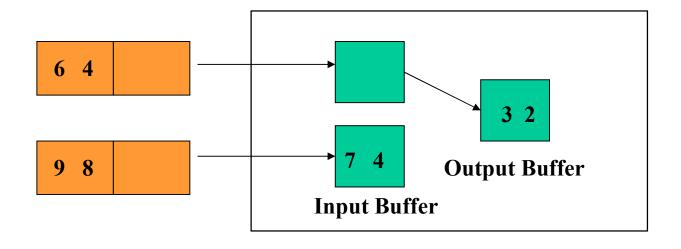


Main memory buffers

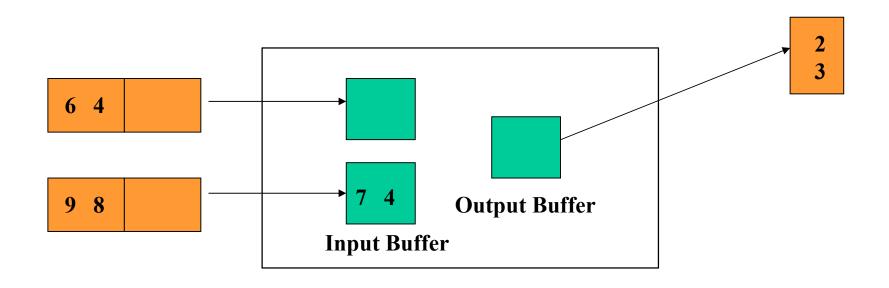
compare within the 2 buffers themselves



Main memory buffers

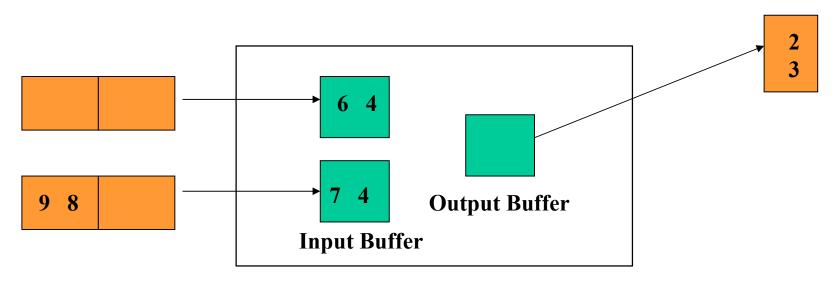


Main memory buffers

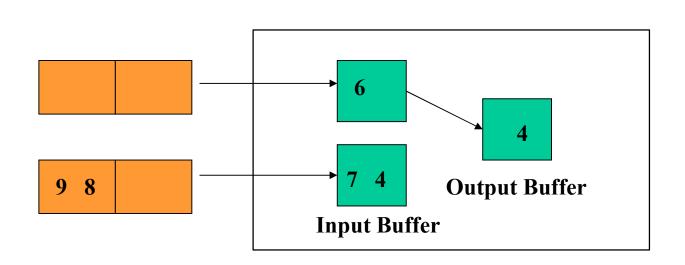


Main memory buffers

here is just loading a new page once the buffer is empty

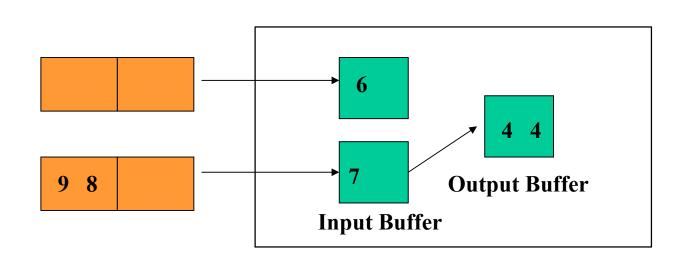


Main memory buffers



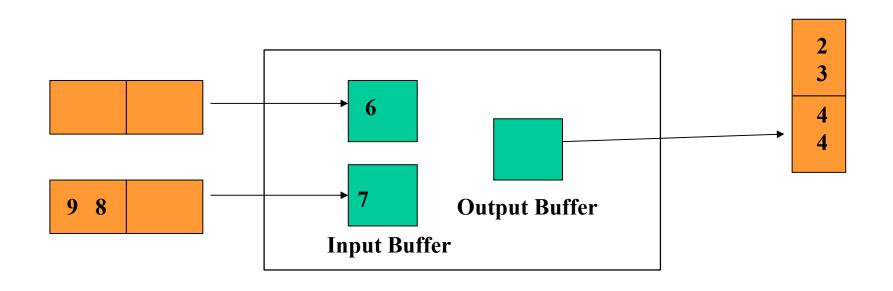
2 3

Main memory buffers



2 3

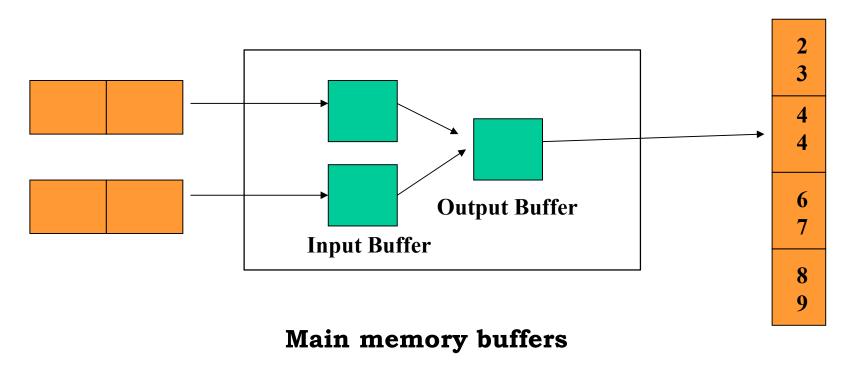
Main memory buffers



Main memory buffers

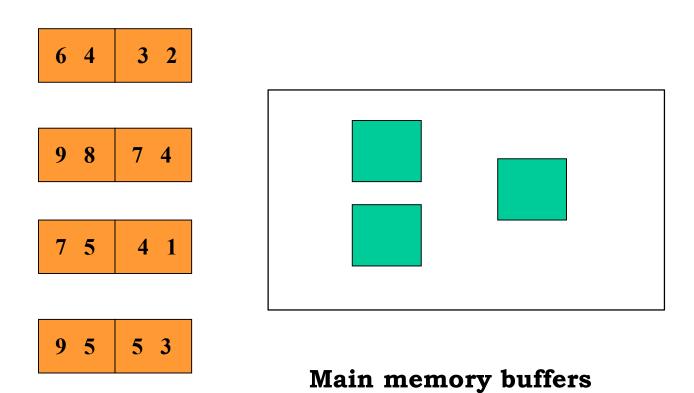
Disk Disk

thus 3 buffer pages is required to sort 2 files into 1 sorted file



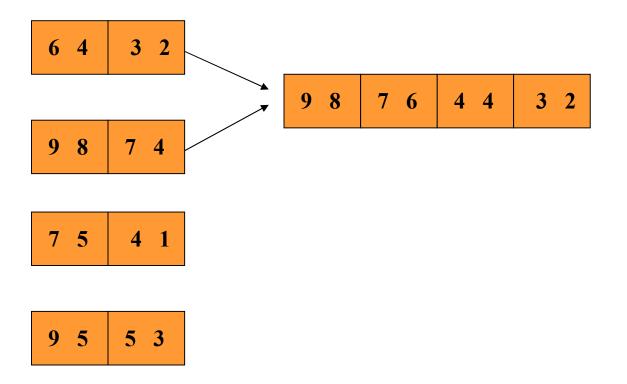
Disk Disk

What if there are many more runs (sorted files)?

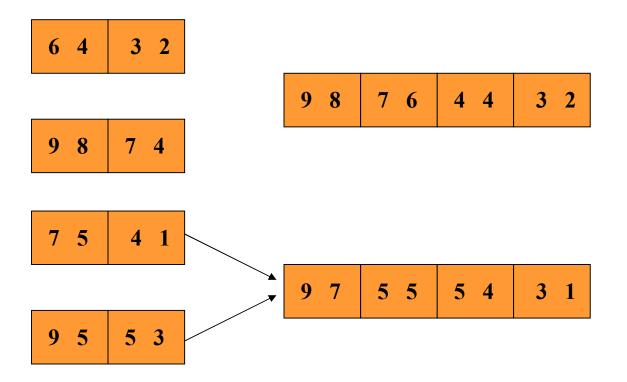


Disk Disk

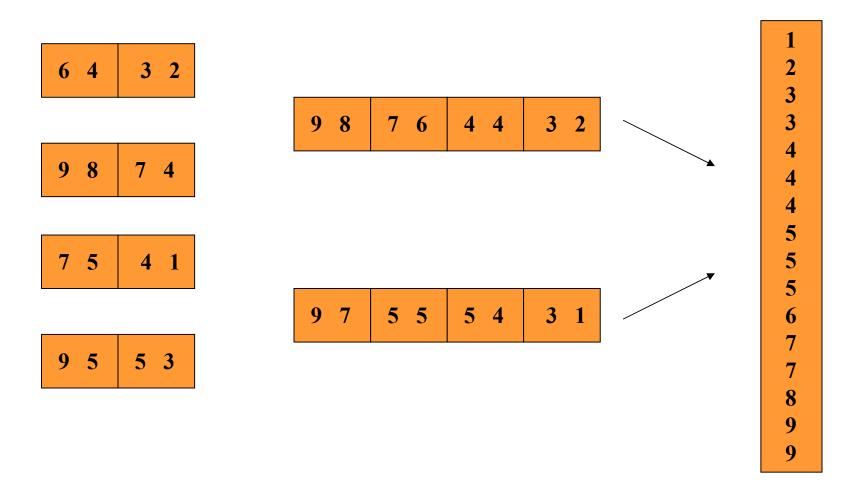
What if there are many more runs?

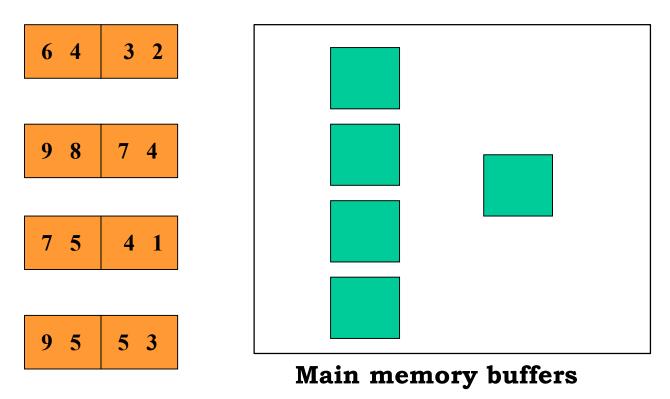


What if there are many more runs?

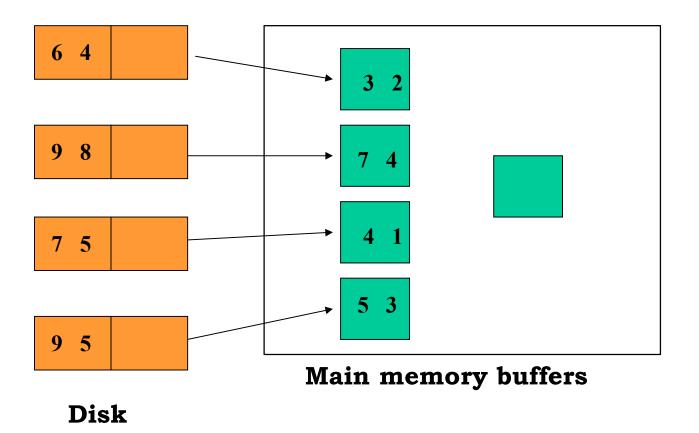


What if there are many more runs?

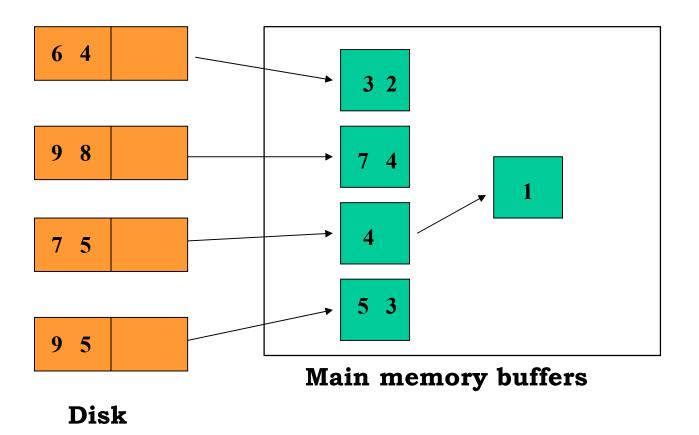




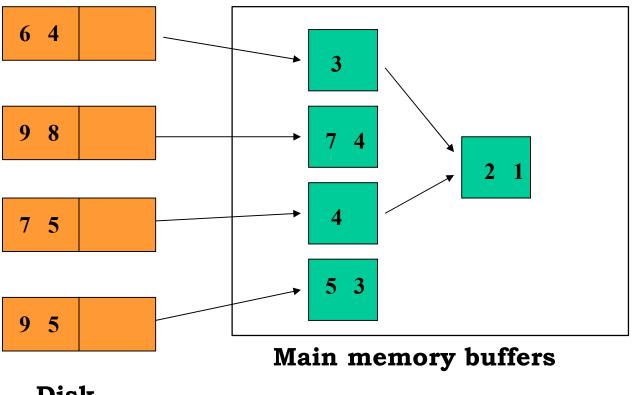
Disk Disk



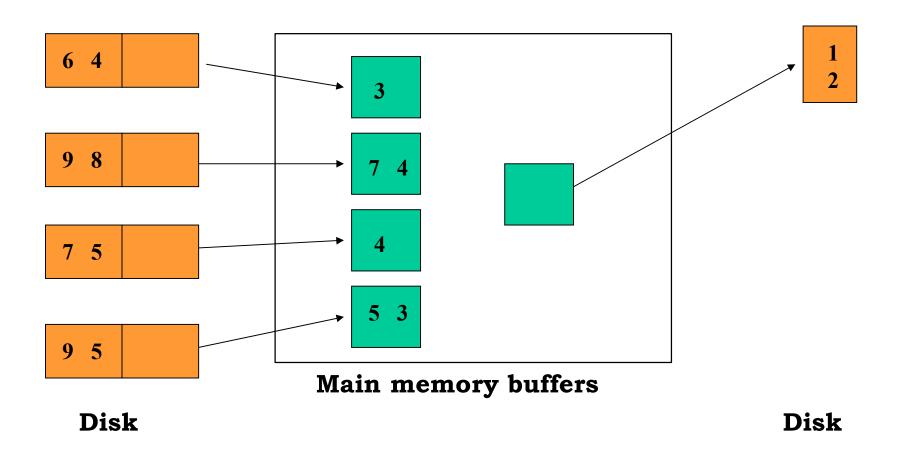
Disk

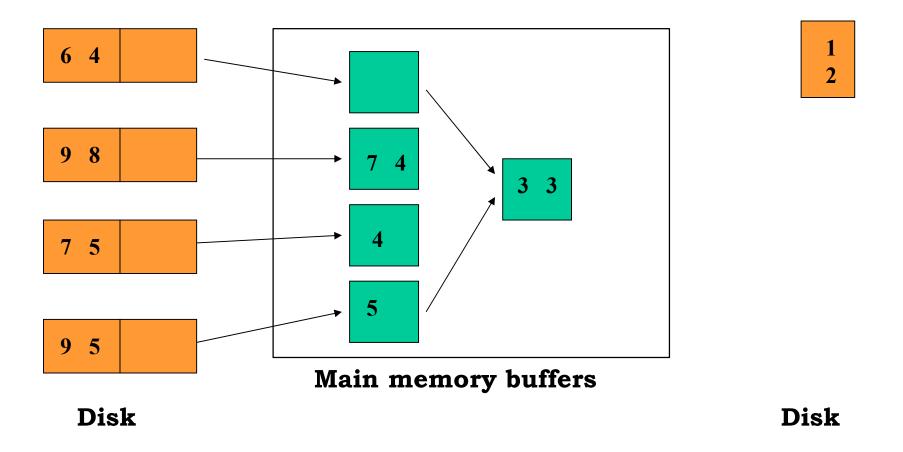


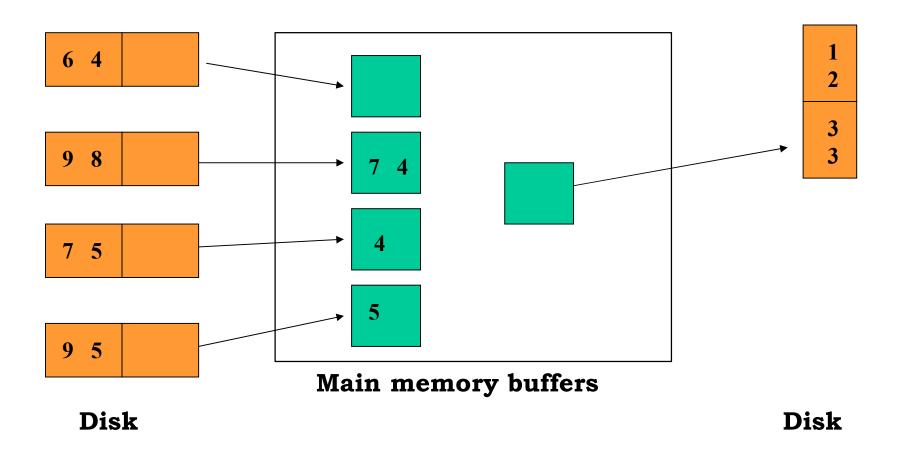
Disk

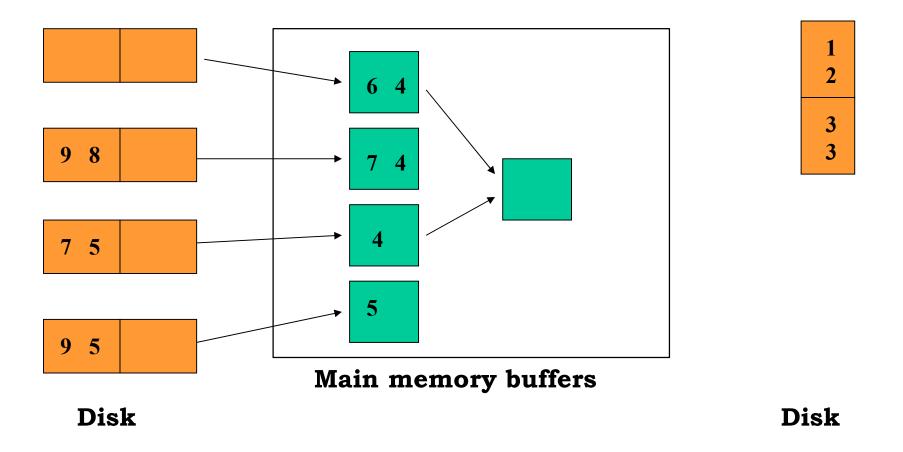


Disk Disk









So far ...

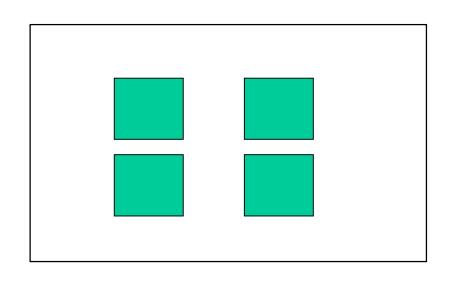
- Given *k* sorted files (runs), we can *merge* them into larger sorted runs, and eventually produce *one* single sorted file
 - Regardless of the size of the sorted files
 - What about the memory size? What is the number of pages needed (regardless of the number of runs)?

Multi-way Merge Sort

- To sort a very large (unsorted) file, we can do it in 2 phases:
 - Phase 1: Generate sorted runs
 - Phase 2: Merge sorted runs (we already know this)

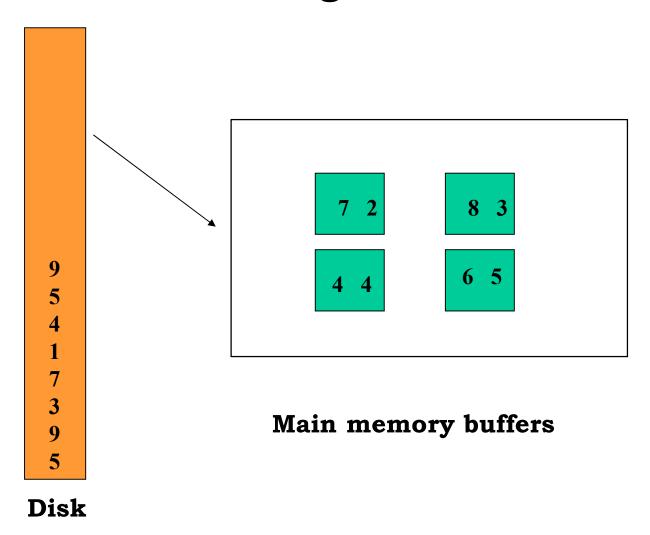
- Read as many records as possible into memory
- Perform in-memory sort (you already know this)
- Write out sorted records as a sorted run
- Repeat the process until all records in the unsorted files are read

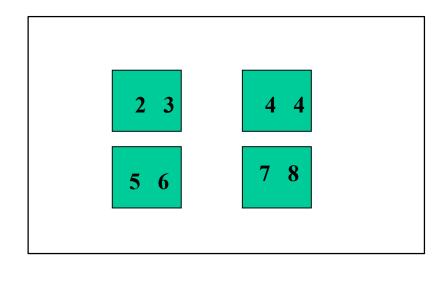
9 9



Main memory buffers

Disk



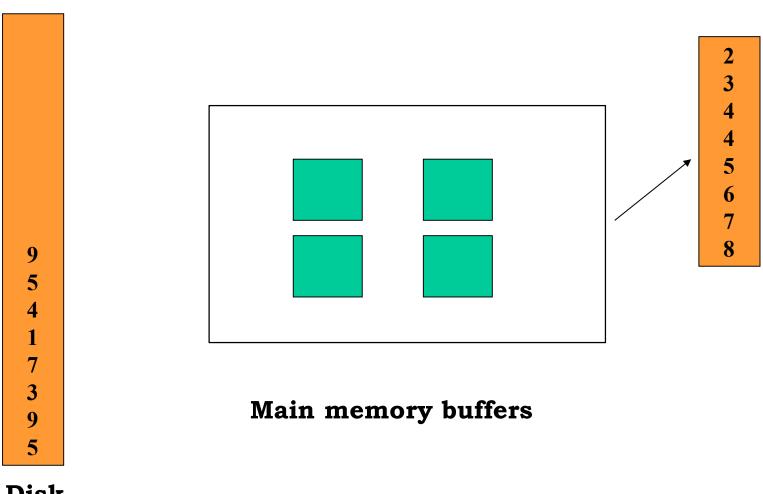


Main memory buffers

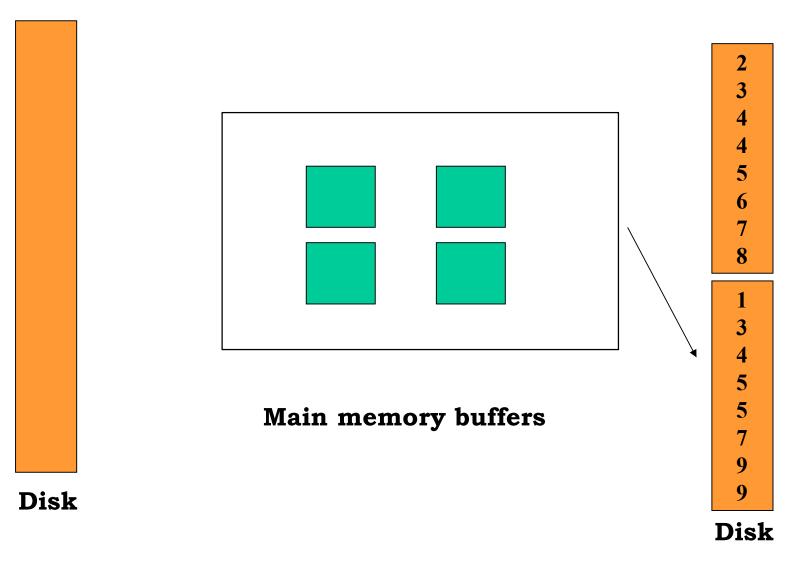
Disk

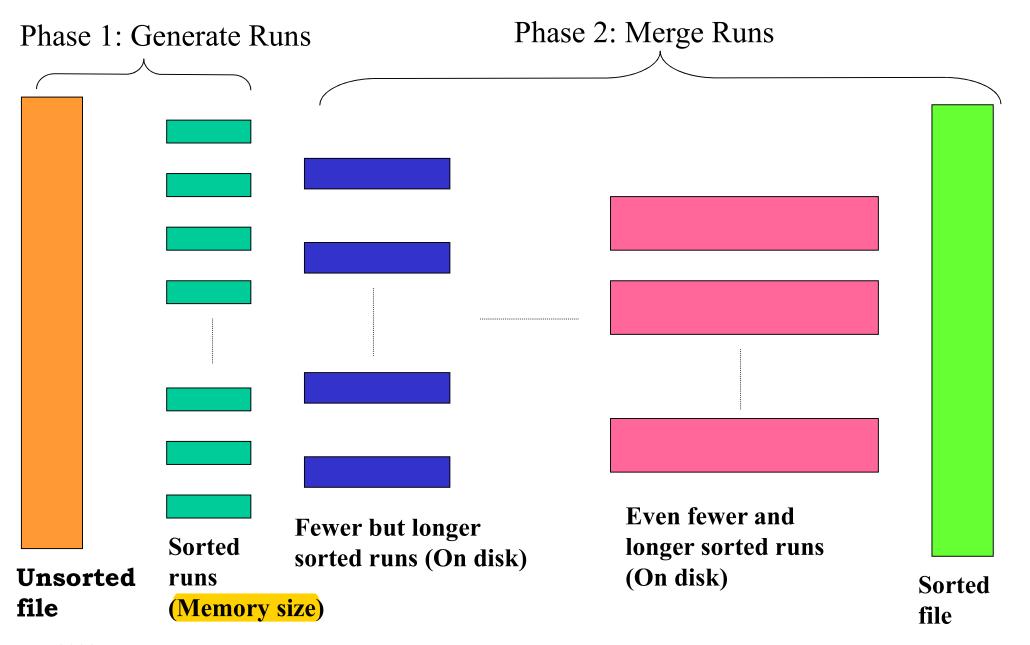
3

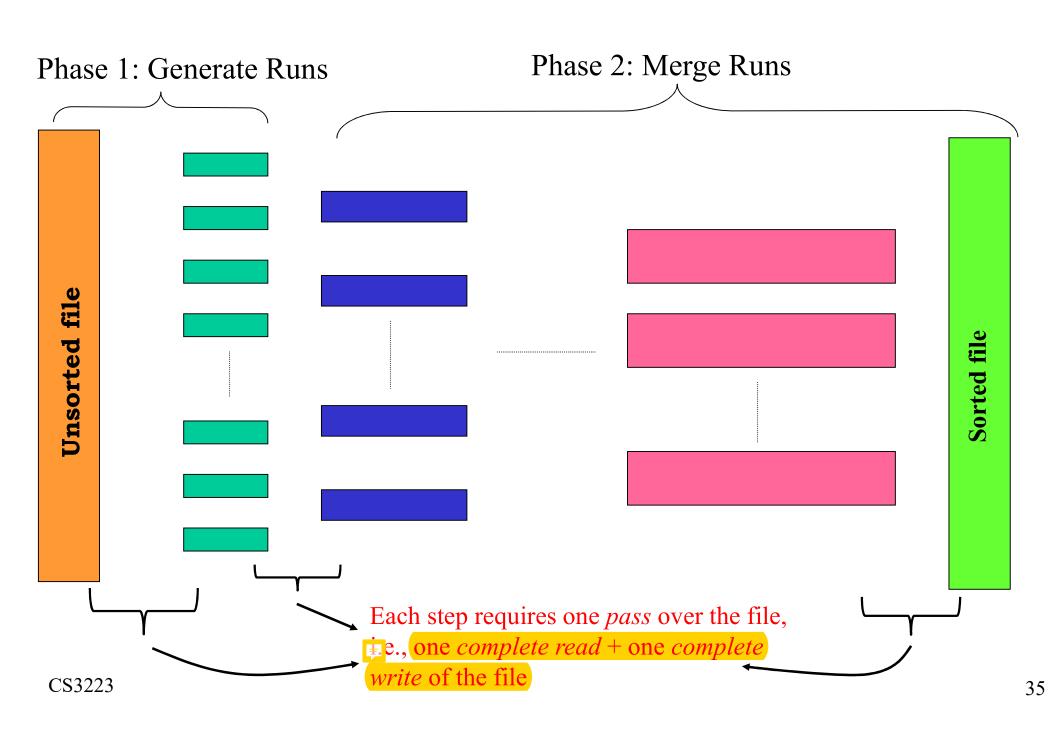
9



Disk







Multi-way Merge Sort

- To sort a file with N pages using B buffer pages (B ≥ 3):
 - Phase 1: create sorted runs
 - Use B buffer pages
 - Read in B pages each time, sort the records, and produce a B page sorted run (except possibly for the last run)
 - Number of sorted runs = \[\text{N / B} \]
 - 1 pass (read + write) over the file (i.e., equal to 2*N I/Os)
 - Phase 2: Merge sorted runs
 - Use *B*-1 buffer pages for input and one buffer page for output
 - Perform (B-1)-way merge iteratively until one sorted run is produced
 - Each iteration requires 1 pass (read + write) over the file
 - \[\log_{B-1} \[\text{N / B } \] \] passes

Cost of Multi-way Merge Sort

- Number of passes: 1 + \[\log \]_1 \[\log \]_1
- Cost = 2N * (# of passes)
- E.g., with 5 buffer pages, to sort 108 page file:
 - Phase 1: \[108 / 5 \] = 22 sorted runs of 5 pages each (last run is only 3 pages)
 - Phase 2:
 - Pass 1: \[22 / 4 \] = 6 sorted runs of 20 pages each (last run is only 8 pages)
 - Pass 2: 2 sorted runs, 80 pages and 28 pages
 - Pass 3: Sorted file of 108 pages
 - Cost = (2*108)*4 = 864

Number of Passes of External Sort

N	B=3	B=5	B=9	B=17	B=129	B=257	
100	7	4	3	2	1	1	
1,000	10	5	4	3	2	2	
10,000	13	7	5	4	2	2	
100,000 A relatively small buffer size can sort a							
1,000,000 very large file with just a few passes							
10,000,000	23	12	8	6	4	3	
100,000,000	26	14	9	7	4	4	
1,000,000,000	30	15	10	8	5	4	

More buffers may not always be beneficial!

Internal Sort Algorithm

- Quicksort is a fast way to sort in memory
- Given N data pages, and B buffers, multi-way sort will generate N/B runs
- Can we further reduce the number of runs (i.e., generate longer runs that the memory size)?
 - What's the advantage??
- An alternative is *replacement selection*

- 109, 49, 34, 68, 45, 60, 2, 38, 28, 47, 16, 19, 35, 59, 98, 78, 76, 40, 35, 86, 10, 27, 61, 92
- suppose each block contains one record and B=5

• 109, 49, 34, 68, 45, 60, 2, 38, 28, 47, 16, 19, 35, 59, 98, 78, 76, 40, 35, 86, 10, 27, 61, 92

109 49 34 68 45

• 109, 49, 34, 68, 45, 60, 2, 38, 28, 47, 16, 19, 35, 59, 98, 78, 76, 40, 35, 86, 10, 27, 61, 92

 $109 \quad 49 \quad 34 \quad 68 \quad 45 \quad \longrightarrow \quad 34$

• 109, 49, 34, 68, 45, 60, 2, 38, 28, 47, 16, 19, 35, 59, 98, 78, 76, 40, 35, 86, 10, 27, 61, 92

• 109, 49, 34, 68, 45, 60, 2, 38, 28, 47, 16, 19, 35, 59, 98, 78, 76, 40, 35, 86, 10, 27, 61, 92

• 109, 49, 34, 68, 45, 60, 2, 38, 28, 47, 16, 19, 35, 59, 98, 78, 76, 40, 35, 86, 10, 27, 61, 92

• 109, 49, 34, 68, 45, 60, 2, 38, 28, 47, 16, 19, 35, 59, 98, 78, 76, 40, 35, 86, 10, 27, 61, 92

109, 49, 34, 68, 45, 60, 2, 38, 28, 47, 16, 19, 35,
59, 98, 78, 76, 40, 35, 86, 10, 27, 61, 92

```
      109
      49
      34
      68
      45
      \longrightarrow
      34
      45

      60
      \longrightarrow
      34
      45
      49

      2
      \longrightarrow
      34
      45
      49
      60

      38
      \longrightarrow
      34
      45
      49
      60
```

• 109, 49, 34, 68, 45, 60, 2, 38, 28, 47, 16, 19, 35, 59, 98, 78, 76, 40, 35, 86, 10, 27, 61, 92

109, 49, 34, 68, 45, 60, 2, 38, 28, 47, 16, 19, 35,
59, 98, 78, 76, 40, 35, 86, 10, 27, 61, 92

109, 49, 34, 68, 45, 60, 2, 38, 28, 47, 16, 19, 35,
59, 98, 78, 76, 40, 35, 86, 10, 27, 61, 92

Replacement Selection (Cont.)

thus replacement selection has the potential to create an output longer than memory

- Final results:
 - 34
 45
 49
 60
 68
 109
 - 2 16 19 28 35 38 47 55 76 78 86 98
 - 10 27 35 40 61 92
- Would have been 5 runs using Quicksort

in this case, with only 3 runs, 5 buffer pages would be enough to allow this to complete in only 1 pass

Internal Sort Algorithm: Replacement Selection

Read **B** blocks into memory

Output: move record with smallest sort key value, say s, to output buffer

Read in a new record r

if r.key > s.key, then GOTO Output else *freeze* r

if all records in memory are frozen, then all records that have been output constitute a run; unfreeze all records and start a new run

GOTO Output

More on Replacement Selection

- Fact: average length of a run is 2B
- Worst-Case
 - What is the (max) number of runs?
 - How does this arise?
- Best-Case
 - What is the (min) number of runs?
 - How does this arise?
- Quicksort is faster, but longer runs often means fewer passes!

Sequential vs Random I/Os

- Is minimizing passes *optimal*? Is merging as many runs as possible the best solution?
- Suppose we have 80 sorted runs, each 100 pages long and we have 81 pages of buffer space
- We can merge all 80 runs in a single (i.e., one) pass
 - Minimal number of passes!
- We can also merge the 80 runs in two passes
 - Pass 1: merge 16 runs first, resulting in 5 longer runs
 - Pass 2: merge the 5 runs
- Which is better??

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Sequential vs Random I/Os

Sequential I/O

 If k pages are accessed sequentially, we need only 1 seek for the k pages (assuming the k pages are stored consecutively on the same track) plus retrieving the k pages sequentially

Random I/O

 If k pages are stored at k/2 random locations such that 2 pages are stored consecutively, then we need k/2 seeks plus k page accesses

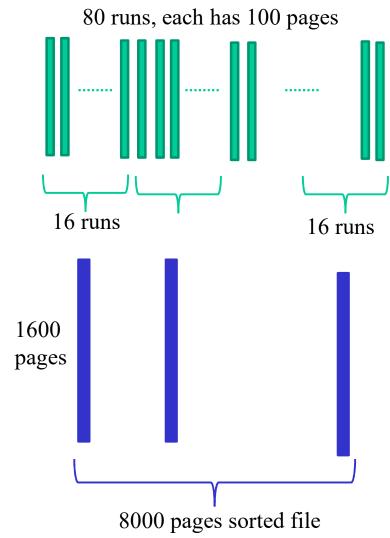
Sequential vs Random I/Os

- Suppose we have 80 sorted runs, each 100 pages long and we have 81 pages of buffer space
- We can merge all 80 runs in a single (i.e., one) pass
 - each page requires a seek to access (Why?)
 - there are 100 pages per run, so 100 seeks per run
 - total cost = 80 runs X 100 seeks = 8000 seeks

so now we are using seek as the metric instead of I/O - since seek can take longer than I/O

Sequential vs Random I/Os (Cont)

- We can merge all 80 runs in two steps
 - 5 sets of 16 runs each
 - read 80/16 pages of one run
 - 16 runs result in sorted run of 1600 pages
 - each merge requires 100/5X16 = 320 seeks
 - for 5 sets, we have 5X320 = 1600 seeks
 - merge 5 runs of 1600 pages
 - read 80/5=16 pages of one run
 1600/16=100 seeks in total
 - 5 runs => 5X100 = 500 seeks
 - total: 1600+500=2100 seeks!!!
- Number of passes increases, but number of seeks decreases!



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the main focus is to differentiate between sequential and random I/O

Using B+ Trees for Sorting

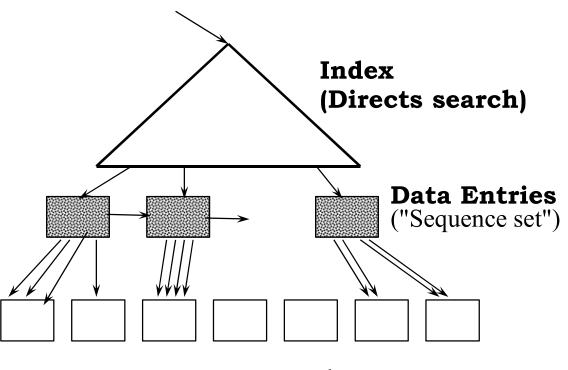
- Scenario: Table to be sorted has B⁺ tree index on sorting column(s)
- Idea: Can retrieve records in order by traversing leaf pages
- Is this a good idea?

Clustered B⁺ Tree Used for Sorting

 Cost: root to the left-most leaf, then retrieve all leaf pages (<key,record> pair organization)

 If <key, rid> pair organization is used? Additional cost of retrieving data records: each

data page fetched just once



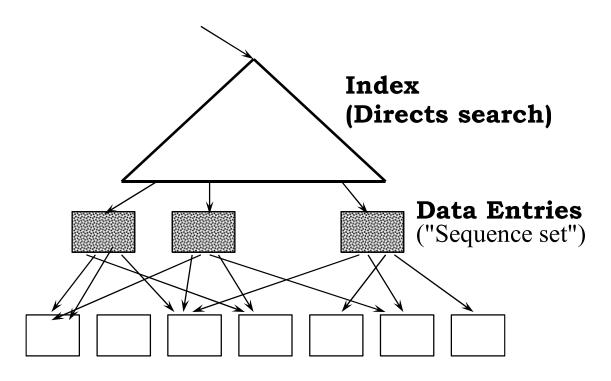
Data Records

thus usually only required to read once

Always better than external sorting!??

Unclustered B+ Tree Used for Sorting

 each data entry contains <key, rid > of a data record. In general, one I/O per data record!



Does it mean that this will never be used to retrieve records in sorted order???

Data Records

External Sorting vs. Unclustered Index

N	Sorting	p=1	p=10	p=100
100	200	100	1,000	10,000
1,000	2,000	1,000	10,000	100,000
10,000	40,000	10,000	100,000	1,000,000
100,000	400,000	100,000	1,000,000	10,000,000
1,000,000	6,000,000	1,000,000	10,000,000	100,000,000
10,000,000	60,000,000	10,000,000	100,000,000	1,000,000,000

^{*} *p*: # of records per page

^{*} *B*=1,000

^{*} p=100 is the more realistic value

Summary

- External sorting is important; DBMS may dedicate part of buffer pool for sorting!
- External merge sort minimizes disk I/O cost:
 - (Phase 1) First pass of file: Produces sorted runs of size B (# buffer pages)
 - Replacement selection can reduce the number of runs
 - (Phase 2) Subsequent passes: merge runs
- Clustered B+ tree is good for sorting; unclustered tree is usually very bad