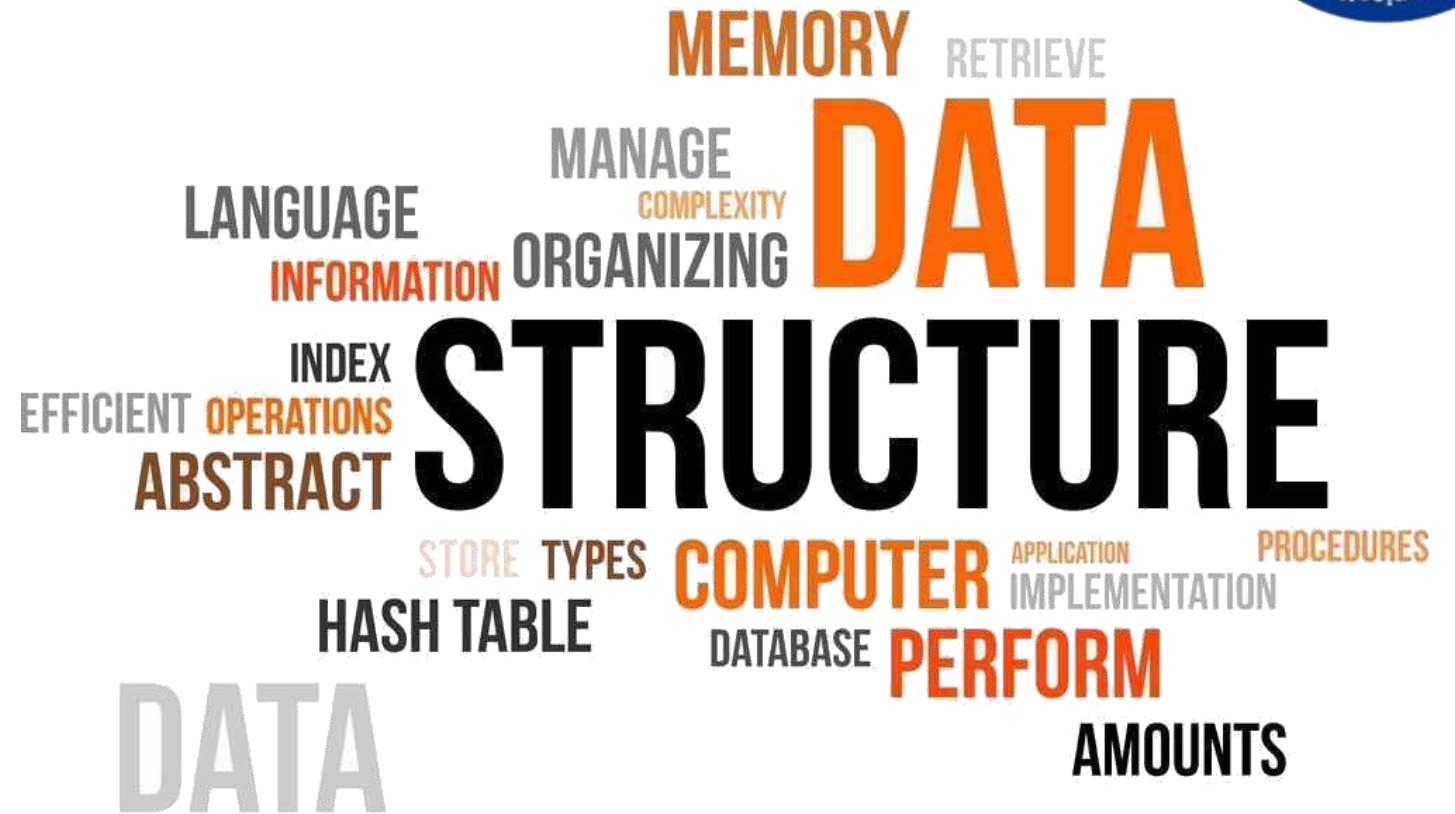




Data Structures

Course code: IT623



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Lectures 12



String Processing...

PATTERN MATCHING ALGORITHM

"Pattern matching is the problem of deciding whether or not a given string pattern P appears in a string text T ."

"Here, we assume that the length of P does not exceed the length of T ."

Notably,

→ Characters are sometimes denoted by lowercase letters (a, b, c, \dots) and exponents may be used to denote repetitions.

$a^2 b^3 a b^2$ for $aabbbaabb$

and

$(cd)^3$ for $cdcdcd$.

Additionally,

• The empty strings are denoted as Λ

* Concatenation $x \cdot y$.

▷ First Pattern Matching Algorithm:-

Here, we compare a given pattern (P) with each of the substrings of (T) , moving from left to right, until we get a match.

$$W_k = \text{SUBSTRING}(T, k, \text{LENGTH}(P))$$

* W_k denote the substring of (T) having the same length as (P) and beginning with the (k^{th}) character of (T) .

* First, we compare (P) , character-by-character, with first substring, W_1

* if all the characters are the same, then $(P = W_1)$ and so P appears in T

* If, we find that some character of (P) is not the same as the corresponding character of W_1 , compare P with (W_2) . If $(P \neq W_2)$ then we compare P with W_3 and so on.

Termination Criteria

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- 1. The process stops when we find a match of P with some substring w_k and so P appears in T and $\text{INDEX}(T, P) = k$.
- 2. When we exhaust all the w_k 's with no match and hence P does not appear in T .

The maximum value MAX of the subscript k is equal to $\text{LENGTH}(T) - \text{LENGTH}(P) + 1$.

* For example,

Let us consider P is a 4-character string and that T is a 20-character string, and that P and T appear in memory as linear arrays with one character per element.

$P = P[1] P[2] P[3] P[4]$

and

$T = T[1] T[2] \dots T[19] T[20]$

* P is compared with each of the following 4-character substrings of T: 16

$$\left\{ W_1 = T[1]T[2]T[3]T[4], W_2 = T[2]T[3]T[4]T[5], \dots, W_{17} = T[17]T[18]T[19]T[20] \right\}$$

$MAX = 20 - 4 + 1 = 17$ such substrings of T.

(Pattern Matching) P and T are strings with lengths R and S, respectively, and are stored as arrays with one character per element. This algorithm finds the INDEX of P in T.

1. [Initialize.] Set $K := 1$ and $MAX := S - R + 1$.
2. Repeat Steps 3 to 5 while $K \leq MAX$:
3. Repeat for $L = 1$ to R : [Tests each character of P.]
 If $P[L] \neq T[K + L - 1]$, then: Go to Step 5.
 [End of inner loop.]
4. [Success.] Set $INDEX = K$, and Exit.
5. Set $K := K + 1$.
 [End of Step 2 outer loop.]
6. [Failure.] Set $INDEX = 0$.
7. Exit.

**Pattern
Matching First
Algorithm**

* The complexity of the pattern matching algorithm is measured by the number (17) of (C) comparison between characters of the text (T)

* To determine (C) we let (N_k) denote the number of comparisons that take place in the inner loop when P is compared with (W_k) .

$$C = N_1 + N_2 + \dots + N_L$$

where (L) is the position L in T where P first appears or $(L = \text{MAX})$ if P does not appear in (T) .

This example computes C for some specific P and T where $LENGTH(P) = 4$ and $LENGTH(T) = 20$ and so $MAX = 20 - 4 + 1$.

(a) Suppose $P = aaba$ and $T = cdcd \dots cd = (cd)^{10}$. Clearly P does not occur in T . Also, for each of the 17 cycles, $N_k = 1$ since the first character of P does not match w_k , hence

$$C = 1 + 1 + 1 + \dots + 1 = 17$$

(b) Let $P = aaba$ and $T = ababaaba \dots$. Observe that P is a substring of T . In fact, $P = w_5$ and so $N_5 = 4$. Also, comparing P with $w_1 = abab$, we obtain that $N_1 = 2$, since the first letters do match; but comparing P with $w_2 = baba$ we obtain $N_2 = 1$. Similarly $N_3 = 2$ and $N_4 = 1$.

$$C = 2 + 1 + 2 + 1 + 4 = 10$$

(C) Let $P = aaab$ and $T = aa \dots a = a^{20}$. Here (P) does not appear in T . Also, (19)
 every $W_k = aaaa$; hence every $N_k = 4$

$$C = 4 + 4 + \dots + 4 = 17 \cdot 4 = 68$$

Let (P) is on (π) character string and T is on (S) character string, the data size for the algorithm is

$$n = \pi + S$$

The worst case occurs when every character of (P) except the last matches every substring W_k , as in above example.

$$C(n) = \pi(S - \pi + 1).$$

For fixed (n) , we have $S = n - \pi$, so that :- " $C(n) = \pi(n - 2\pi + 1)$ "

* The maximum value of $C(n)$ occurs when $n = (n+1)/4$. Accordingly, substituting this value for n in the formula for $C(n)$ yields:

$$C(n) = \frac{(n+1)^2}{8} = O(n^2)$$

Now, we get $n = n+1/4$

$$\frac{dc}{dn} = ?$$

Please note down

* The complexity of the average case in any actual situation depends on certain probabilities which are usually unknown.

* When the character of (P) and (T) are randomly selected from some finite alphabet, the complexity of the average case is still not easy to analyze, but the complexity of the average case is still a factor of the worst-case.

* The complexity of this pattern matching algorithm is equal to $O(n^2)$.

Second Pattern Matching Algorithm:-

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* The second pattern matching algorithm uses a table which is derived from a particular pattern P but is independent of the text T . For definiteness, suppose

\Rightarrow " $P = aabab$ " pattern

* First we give the reason for the table entries and how they are used.

* Let $T = T_1 T_2 T_3 \dots$, where T_i denotes the i^{th} character of T ; and suppose the first two characters of T match those of P ; i.e. suppose $T = aa \dots$. Then T has one of the following three forms

(i) $T = aab \dots$,

(ii) $T = aaa \dots$,

(iii) $T = aax$

Where x is any character different from a or b .