Содержание

1 Настройка CLion

1. В файле `CMakeLists.txt` дописать строчку `add_compile_definitions(LOCAL)`. Нажать появившуюся опцию в правом верхнем углу `enable auto-reload`.

2. Вбить шаблон в `main.cpp`:

```
#ifdef LOCAL
#define _GLIBCXX_DEBUG
#endif
#include<bits/stdc++.h>

using namespace std;

#define int long long
#define app push_back
#define all(x) x.begin(), x.end()
#ifdef LOCAL
#define debug(...) [](auto...a){ ((cout << a << ' '
    ), ...) << endl; }(#__VA_ARGS__, ":",
    __VA_ARGS__)
#define debugv(v) do { cout << #v << ": "; for (
    auto x : v) cout << x << ' '; cout << endl; }
    while(0)
#else
#define debug(...)
#define debugv(v)
#endif

int32_t main() {
    cin.tie(0);ios_base::sync_with_stdio(0);
    int n = 2; vector<int> a(n, n);
    debug(n); debugv(a);
}
//6d2c29
```

Скомпилировать, чтобы проверить отсутствие опечаток.

3. Запустить терминал (crtl + alt + T)

```
$ cd workspace/CLionProjects
$ for c in {A..Z}; do cp main.cpp $c.cpp && echo "
    add_executable($c $c.cpp)" >> CMakeLists.txt;
    done
```

Далее отключаем подсветку и форматирование в настройках (ctrl+alt+S)

- Editor → Code Style → Formatter → `Do not format` прописать *
- Editor → Inspections → C/C++ → static analysis tools → CLang-Tidy отключить
- Editor → Inlay Hints → отключаем всё (достаточно первых трёх — code vision, parameter names, types).

Тёмная тема отключается в Appearance & Behavior → Appearance.

Чтобы добавить санитайзеры, надо дописать в CMakeLists.txt `set(CMAKE_CXX_FLAGS "-fsanitize=address -fsanitize=undefined")`

2 Теория чисел

2.1 КТО

```
int gcd(int a, int b, int &x, int &y) {
  if (b==0) { x = 1; y = 0; return a; }
  int d = gcd(b,a%b,y,x);
  y-=a/b*x;
  return d;
}
int inv(int r, int m) {
  int x, y;
  gcd(r,m,x,y);
  return (x+m)%m;
}
int crt(int r, int n, int c, int m) { return r + ((c -
     r) % m + m) * inv(n, m) % m * n; }
```

2.2 Алгоритм Миллера — Рабина

```
__int128 one=1;
int po(int a,int b,int p)
{
  int res=1;
  while(b) {if(b & 1) {res=(res*one*a)%p;--b;} else {a
    =(a*one*a)%p;b>>=1;}} return res;
}
bool chprime(int n) ///miller-rabin
{
  if(n==2) return true;
  if(n<=1 || n%2==0) return false;
  int h=n-1;int d=0;while(h%2==0) {h/=2;++d;}
  for(int a:{2, 3, 5, 7, 11, 13, 17, 19, 23, 29, 31,
    37})
    {
    if(a==n) return true;
    int u=po(a,h,n);bool ok=0;
    if(u%n==1) continue;
    for(int c=0;c<d;++c)
      {
      if((u+1)%n==0) {ok=1;break;}
      u=(u*one*u)%n;
    }
    if(!ok) return false;
  }
  return true;
}
```

2.3 Алгоритм Берлекэмпа — Месси

https://mzhang2021.github.io/cp-blog/berlekamp-massey/

```
template<typename T>
vector<T> berlekampMassey(const vector<T> &s) {
  int n = s.size(), l = 0, m = 1;
  vector<T> b(n), c(n);
  T ld = b[0] = c[0] = 1;
  for (int i=0; i<n; i++, m++) {
    T d = s[i];
    for (int j=1; j<=l; j++)
      d += c[j] * s[i-j];
    if (d == 0) continue;
    vector<T> temp = c;
    T coef = d / ld;
    for (int j=m; j<n; j++) c[j] -= coef * b[j-m];
    if (2 * l <= i) {
      l = i + 1 - l;
      b = temp;
      ld = d;
      m = 0;
    }
  }
  c.resize(l + 1);
  c.erase(c.begin());
  for (T &x : c)
    x = -x;
  return c;
}
```

3 Графы

3.1 SCC и 2-SAT

Алгоритм ищет сильносвязные компоненты в графе g, если есть путь $i \to j$, то $scc[i] \le scc[j]$

```
vector<int> find_scc(vector<vector<int>> g) {
  vector<vector<int>> r(g.size());
  for (int i = 0; i < g.size(); ++i) {
    for (int j : g[i]) r[j].push_back(i);
  }
  vector<int> used(g.size()), tout(g.size());
  int time = 0;
  auto dfs = [&](auto dfs, int cur) -> void {
    if (used[cur]) return;
    used[cur] = 1;
    for (int nxt : g[cur]) {
      dfs(dfs, nxt);
    }
    tout[cur] = time++;
  };
  for (int i = 0; i < g.size(); ++i) if (!used[i]) dfs
    (dfs, i);
  vector<int> ind(g.size());
  iota(ind.begin(), ind.end(), 0);
  sort(all(ind), [&](int i, int j){return tout[i] >
    tout[j];});
  vector<int> scc(g.size(), -1);
  auto go = [&](auto go, int cur, int color) -> void {
    if (scc[cur] != -1) return;
    scc[cur] = color;
    for (int nxt : r[cur]) {
      go(go, nxt, color);
    }
  };
  int color = 0;
  for (int i : ind) {
    if (scc[i] == -1) go(go, i, color++);
  }
  return scc;
}
```

Чтобы решать 2-SAT, надо создать граф на $2n$ вершинах, рёбра $i \Rightarrow j$ и $(j \oplus 1) \Rightarrow (i \oplus 1)$ должны быть добавлены одновременно. После этого если `scc[2 * i] = scc[2 * i + 1]`, то решения нет; если `scc[2 * i + 0] < scc[2 * i + 1]`, то присутствует импликация $\neg i \Rightarrow i$, надо назначить $i =$`true`.

3.2 Эйлеров цикл

```
vector<int> euler(vector<vector<pair<int, int>>> g,
    int m, int src) {  // g[cur][i] = pair{nxt, idx}
  int n = g.size();
  vector<int> used(m), it(n), cycle;
  auto dfs = [&](auto dfs, int cur) -> void {
    while (true) {
      while (it[cur] < g[cur].size() && used[g[cur][it
    [cur]].second]) it[cur]++;
      if (it[cur] == g[cur].size()) return;
      auto [nxt, idx] = g[cur][it[cur]];
      used[idx] = true;
      dfs(dfs, nxt);
      cycle.push_back(idx); // or {cur, nxt}
    }
  };
  dfs(dfs, src);
  reverse(cycle.begin(), cycle.end());
  if (cycle.size() != m) return {}; // check that all
    edges are present in the cycle, fail otherwise
  return cycle;
}
```

3.3 Компоненты рёберной двусвязности

```
int n, m;
cin >> n >> m;
vector <vector <int> > g(n + 1);
map <pair <int, int>, int> comp, col;
for (int i = 0; i < m; ++i) {
  int u, v, c; cin >> u >> v >> c;c--;
  col[{u,v}]=col[{v,u}]=c;
  g[u].push_back(v);
  g[v].push_back(u);
}
vector <int> used(n + 1);
vector <int> newCompWithoutParent(n + 1), h(n + 1), up
    (n + 1);
auto findCutPoints = [&] (auto self, int u, int p) ->
    void {
  used[u] = 1;
  up[u] = h[u];
  for (int v : g[u]) {
    if (!used[v]) {
      h[v] = h[u] + 1;
      self(self, v, u);
      up[u] = min(up[u], up[v]);
      if (up[v] >= h[u]) {
        newCompWithoutParent[v] = 1;
      }
    }
    else {
```

```
      up[u] = min(up[u], h[v]);
    }
  }
};
for (int u = 1; u <= n; ++u) {
  if (!used[u]) {
    findCutPoints(findCutPoints, u, u);
  }
}
int ptr = 0;
vector <map <int, int> > colors(m);
auto markComponents = [&] (auto self, int u, int cur)
    -> void {
  used[u] = 1;
  for (int v : g[u]) {
    if (!used[v]) {
      if (newCompWithoutParent[v]) {
        ptr++;
        self(self, v, ptr - 1);
      }
      else {
        self(self, v, cur);
      }
    }
    else if (h[v] < h[u]) {
      comp[{u,v}]=comp[{v,u}]=cur;
      int c = col[{u,v}];
      colors[cur][u] |= 1 << c;
      colors[cur][v] |= 1 << c;
    }
  }
};
used.assign(n + 1, 0);
for (int u = 1; u <= n; ++u) {
  if (!used[u]) {
    markComponents(markComponents, u, -1);
  }
}
for (int comp = 0; comp < m; ++comp) {
  vector <int> cnt(4);
  int tot = 0;
  for (auto [u, mask] : colors[comp]) {
    tot |= mask;
    cnt[bp(mask)]++;
  }
  if (bp(tot)<3) {
    continue;
  }
  if (cnt[2] || cnt[3]>2) {
    cout << "Yes" << endl;
    return;
  }
}
cout << "No" << endl;
```

3.4 DCP offline

```
struct Dsu {
    int n;
    vector<pair<int &, int>> s;
    vector<int> p, sz;
    // other info

    Dsu(int n) : n(n), p(n), sz(n, 1){
        iota(all(p), 0);
    }

    int get(int u) {
        while (u != p[u]) u = p[u];
        return u;
    }

    bool merge(int u, int v) {
        u = get(u), v = get(v);
        if (u == v) return false;
        if (sz[v] < sz[u]) swap(u, v);
        s.app({p[u], p[u]});
        s.app({sz[v], sz[v]});
        // app other info like s.app({comp, comp});
        p[u] = v;
        sz[v] += sz[u];
        return true;
    }

    void rollback(int sz) {
        while (s.size() != sz) {
            s.back().first = s.back().second;
            s.pop_back();
        }
    }
};

struct DcpOffline {
    int n;
    vector<vector<pair<int, int>>> d;

    void addEdgeOnSegment(int l, int r, int a, int b)
    {
        for (l += n, r += n; l < r; l /= 2, r /= 2) {
            if (l & 1) d[l++].app({a, b});
            if (r & 1) d[--r].app({a, b});
        }
    }

    template<typename T>
    void dfs(Dsu &dsu, T act) {
        dfs(1, 0, n, dsu, act);
    }

    template<typename T>
    void dfs(int v, int l, int r, Dsu &dsu, T act) {
        int sz = dsu.s.size();
        for (auto [u, v]: d[v]) {
            dsu.merge(u, v);
        }
        if (l + 1 == r) {
            act(l, dsu);
        } else {
            int m = (l + r) / 2;
            dfs(v * 2, l, m, dsu, act);
            dfs(v * 2 + 1, m, r, dsu, act);
        }
        dsu.rollback(sz);
    }

    DcpOffline(int maxt) : n(2 << __lg(maxt + 1)), d(2
     * n) {}
};
```

3.5 Взвешенное паросочетание

https://judge.yosupo.jp/submission/201334

```
namespace blossom {
#define d(x) (lab[x.u] + lab[x.v] - 2 * e[x.u][x.v].w)
    const int N = 403*2;
    const int inf = 1e18;
    struct Q{ int u, v, w; } e[N][N];
    vector<int> p[N];
    int n, m = 0, id, h, t, lk[N], sl[N], st[N], f[N],
     b[N][N], s[N], ed[N], q[N], lab[N];
    void upd(int u, int v) { if (!sl[v] || d(e[u][v])
    < d(e[sl[v]][v])) sl[v] = u; }
    void ss(int v) {
        sl[v] = 0;
        for (int u = 1; u <= n; ++u) if (e[u][v].w > 0
     && st[u] != v && !s[st[u]]) upd(u, v);
    }
    void ins(int u){ if (u <= n) q[++t] = u; else for
    (int v : p[u]) ins(v); }
    void ch(int u, int w) { st[u] = w; if (u > n) for
    (int v : p[u]) ch(v, w); }
    int gr(int u, int v) {
        if ((v = find(all(p[u]), v) - p[u].begin()) &
    1) {
            reverse(1 + all(p[u]));
            return (int)p[u].size() - v;
        }
        return v;
    }
    void stm(int u, int v) {
        lk[u] = e[u][v].v;
```

```
        if (u <= n) return; Q w = e[u][v];
        int x = b[u][w.u], y = gr(u,x);
        for (int i = 0; i < y; ++i) stm(p[u][i], p[u][
    i^1]);
        stm(x, v); rotate(p[u].begin(), y+all(p[u]));
    }
    void aug(int u, int v) {
        int w = st[lk[u]];stm(u, v);if (!w) return;
        stm(w, st[f[w]]);
        aug(st[f[w]], w);
    }
    int lca(int u, int v) {
        for (id++; u|v; swap(u, v)) {
            if (!u) continue;if(ed[u] == id) return u;
            ed[u] = id; if (u = st[lk[u]]) u = st[f[u
    ]]; // =, not ==
        }
        return 0;
    }
    void add(int u, int a, int v) {
        int x = n + 1; while (x <= m && st[x]) ++x;
        if (x > m) ++m;
        lab[x] = s[x] = st[x] = 0;
        lk[x] = lk[a];
        p[x].clear();
        p[x].push_back(a);
#define op(q) for (int i = q, j = 0; i != a; i=st[f[j
    ]]) p[x].push_back(i), p[x].push_back(j=st[lk[i]])
    , ins(j) // also not ==
        op(u); reverse(1+all(p[x]));op(v);
        ch(x, x); for (int i = 1; i <= m; ++i) e[x][i
    ].w = e[i][x].w = 0;
        fill(b[x]+1, b[x]+n+1, 0);
        for (int u : p[x]) {
            for (int v = 1; v <= m; ++v) if (!e[x][v].
    w || d(e[u][v]) < d(e[x][v])) e[x][v] = e[u][v], e
    [v][x] = e[v][u];
            for (int v = 1; v <= n; ++v) if (b[u][v])
    b[x][v] = u;
        }
        ss(x);
    }
    void ex(int u) {
        for (int x : p[u]) ch(x, x);
        int a = b[u][e[u][f[u]].u], r = gr(u, a);
        for (int i = 0; i < r; i += 2) {
            int x = p[u][i], y = p[u][i + 1];
            f[x] = e[y][x].u; s[x] = 1; s[y] = 0; sl[x
    ] = 0; ss(y); ins(y);
        }
        s[a] = 1; f[a] = f[u];
        for (int i = r + 1; i < p[u].size(); ++i) s[p[
    u][i]] = -1, ss(p[u][i]);
        st[u] = 0;
    }
    bool on(const Q &e) {
        int u = st[e.u], v = st[e.v], a;
        if (s[v] == -1) {
            f[v] = e.u, s[v] = 1, a = st[lk[v]], sl[v]
     = sl[a] = s[a] = 0, ins(a);
        } else if (!s[v]) {
            a = lca(u, v); if (!a) return aug(u, v),
    aug(v, u), 1; else add(u, a, v);
        }
        return 0;
    }
    bool bfs() {
        fill(s+1, s+m+1, -1);fill(sl+1, sl+m+1, 0); //
     s is filled with -1
        h = 1, t = 0; for (int i = 1; i <= m; ++i) if
    (st[i] == i && !lk[i]) f[i] = s[i] = 0, ins(i);
        if (h > t) return 0;
        while (1) {
            while (h <= t) {
                int u = q[h++];
                if (s[st[u]] != 1) {
                    for (int v = 1; v <= n; ++v) if (e
    [u][v].w > 0 && st[u] != st[v]) {
                        if (d(e[u][v])) upd(u, st[v]);
     else if (on(e[u][v])) return 1;
                    }
                }
            }
            int x = inf;
            for (int i = n+1; i <= m; ++i) if (st[i]
    == i && s[i] == 1) x = min(x, lab[i]/2);
            for (int i = 1; i <= m; ++i) if (st[i] ==
    i && sl[i] && s[i] != 1) x = min(x, d(e[sl[i]][i])
    >>s[i]+1);
            for (int i = 1; i <= n; ++i) if (~s[st[i
    ]]) if ((lab[i] += (s[st[i]] * 2 - 1) * x) <=0)
    return 0;
            for (int i = n + 1; i <= m; ++i) if (st[i]
     == i && ~s[st[i]]) lab[i] += (2 - 4 * s[st[i]]) *
     x;
            h = 1, t = 0;
            for (int i = 1; i <= m; ++i) if (st[i] ==
    i && sl[i] && st[sl[i]] != i && !d(e[sl[i]][i]) &&
     on(e[sl[i]][i])) return 1;
            for (int i = n+1; i <= m; ++i) if (st[i]
    == i && s[i] == 1 && !lab[i]) ex(i);
        }
    }

    pair<int, vector<array<int, 2>>> run(int N, vector
    <array<int, 3>> edges) {
        for (auto &[u, v, w] : edges) ++u, ++v;
        fill(ed+1, ed+m+1, 0);
        fill(lk+1, lk+m+1, 0);
        n = m = N;
        id = 0;
        iota(st + 1, st + n + 1, 1);
        int wm = 0, weight = 0;
        for (int i = 1; i <= n; ++i) for (int j = 1; j
     <= n; ++j) e[i][j] = {i,j,0};
        for (auto [u, v, w] : edges) wm = max(wm, e[v
    ][u].w = e[u][v].w = max(e[u][v].w, w));
        for (int i = 1; i <= n; ++i) p[i].clear();
        for (int i = 1; i <= n; ++i) for (int j = 1; j
     <= n; ++j) b[i][j] = i==j?i:0;
        fill_n(lab+1, n, wm); while (bfs());
        vector<array<int, 2>> matching;
        for (int i = 1; i <= n; ++i) if (i < lk[i])
    weight += e[i][lk[i]].w, matching.push_back({i -
    1, lk[i] - 1});
        return {weight, matching};
    }
}
```

4 Свёртки

4.1 AND, OR, XOR свёртки

```
const int p = 998244353;
vector<int> band(vector<int> a,vector<int> b)
{
  int n=0;while((1<<n)<a.size()) ++n;
  a.resize(1<<n);b.resize(1<<n);
  for(int i=0;i<n;++i) for(int mask=0;mask<(1<<n);++
    mask) if(mask & (1<<i)) {a[mask-(1<<i)]+=a[mask];a
    [mask-(1<<i)]%=p;}
  for(int i=0;i<n;++i) for(int mask=0;mask<(1<<n);++
    mask) if(mask & (1<<i)) {b[mask-(1<<i)]+=b[mask];b
    [mask-(1<<i)]%=p;}
  vector<int> c(1<<n,0);
  for(int mask=0;mask<(1<<n);++mask) {c[mask]=a[mask]*
    b[mask];c[mask]%=p;}
  for(int i=0;i<n;++i) for(int mask=0;mask<(1<<n);++
    mask) if(!(mask & (1<<i))) {c[mask]-=c[mask+(1<<i)
    ];c[mask]%=p;}
  return c;
}
vector<int> bor(vector<int> a,vector<int> b)
{
  int n=0;while((1<<n)<a.size()) ++n;
  a.resize(1<<n);b.resize(1<<n);
  for(int i=0;i<n;++i) for(int mask=0;mask<(1<<n);++
    mask) if(!(mask & (1<<i))) {a[mask+(1<<i)]+=a[mask
    ];a[mask+(1<<i)]%=p;}
```

```
  for(int i=0;i<n;++i) for(int mask=0;mask<(1<<n);++
    mask) if(!(mask & (1<<i))) {b[mask+(1<<i)]+=b[mask
    ];b[mask+(1<<i)]%=p;}
  vector<int> c(1<<n,0);
  for(int mask=0;mask<(1<<n);++mask) {c[mask]=a[mask]*
    b[mask];c[mask]%=p;}
  for(int i=0;i<n;++i) for(int mask=0;mask<(1<<n);++
    mask) if(mask & (1<<i)) {c[mask]-=c[mask-(1<<i)];c
    [mask]%=p;}
  return c;
}
vector<int> bxor(vector<int> a,vector<int> b)
{
  assert(p%2==1);int inv2=(p+1)/2;
  int n=0;while((1<<n)<a.size()) ++n;
  a.resize(1<<n);b.resize(1<<n);
  for(int i=0;i<n;++i) for(int mask=0;mask<(1<<n);++
    mask) if(!(mask & (1<<i))) {int u=a[mask],v=a[mask
    +(1<<i)];a[mask+(1<<i)]=(u+v)%p;a[mask]=(u-v)%p;}
  for(int i=0;i<n;++i) for(int mask=0;mask<(1<<n);++
    mask) if(!(mask & (1<<i))) {int u=b[mask],v=b[mask
    +(1<<i)];b[mask+(1<<i)]=(u+v)%p;b[mask]=(u-v)%p;}
  vector<int> c(1<<n,0);
  for(int mask=0;mask<(1<<n);++mask) {c[mask]=a[mask]*
    b[mask];c[mask]%=p;}
  for(int i=0;i<n;++i) for(int mask=0;mask<(1<<n);++
    mask) if(!(mask & (1<<i))) {int u=c[mask],v=c[mask
    +(1<<i)];c[mask+(1<<i)]=((v-u)*inv2)%p;c[mask]=((u
    +v)*inv2)%p;}
  return c;
}
```

4.2 FFT & co

```
typedef long long ll;
const int p=998244353;
int po(int a,int b) {if(b==0) return 1; if(b==1)
    return a; if(b%2==0) {int u=po(a,b/2);return (u*1
    LL*u)%p;} else {int u=po(a,b-1);return (a*1LL*u)%p
    ;}}
int inv(int x) {return po(x,p-2);}
template<int M, int K, int G> struct Fft {
  // 1, 1/4, 1/8, 3/8, 1/16, 5/16, 3/16, 7/16, ...
  int g[1 << (K - 1)];
  Fft() : g() { //if tl constexpr...
    static_assert(K >= 2, "Fft: K >= 2 must hold");
    g[0] = 1;
    g[1 << (K - 2)] = G;
    for (int l = 1 << (K - 2); l >= 2; l >>= 1) {
      g[l >> 1] = (g[l] * 1LL* g[l]) % M;
    }
    assert((g[1]*1LL * g[1]) % M == M - 1);
    for (int l = 2; l <= 1 << (K - 2); l <<= 1) {
      for (int i = 1; i < l; ++i) {
        g[l + i] = (g[l] * 1LL * g[i]) % M;
      }
    }
  }
  void fft(vector<int> &x) const {
    const int n = x.size();
    assert(n <= 1 << K);
    for (int h = __builtin_ctz(n); h--; ) {
      const int l = (1 << h);
      for (int i = 0; i < n >> (h+1); ++i) {
        for (int j = i << (h+1); j < (((i << 1) + 1)
    << h); ++j) {
          const int t = (g[i] * 1LL* x[j | l]) % M;
          x[j | l] = x[j] - t;
          if (x[j|l] < 0) x[j | l] += M;
          x[j]+=t;
          if (x[j] >= M) x[j] -= M;
        }
      }
    }
    for (int i = 0, j = 0; i < n; ++i) {
      if (i < j) std::swap(x[i], x[j]);
      for (int l = n; (l >>= 1) && !((j ^= l) & l); )
    {}
    }
  }
  vector<int> convolution(vector<int> a, vector<int> b
    ) const {
    if(a.empty() || b.empty()) return {};
    for(int& x:a) {x%=p;if(x>=p) x-=p; if(x<0) x+=p;}
    for(int& x:b) {x%=p;if(x>=p) x-=p; if(x<0) x+=p;}
    const int na = a.size(), nb = b.size();
    int n, invN = 1;
    for (n = 1; n < na + nb - 1; n <<= 1) invN = ((
    invN & 1) ? (invN + M) : invN) >> 1;
    vector<int> x(n, 0), y(n, 0);
    std::copy(a.begin(), a.end(), x.begin());
    std::copy(b.begin(), b.end(), y.begin());
    fft(x);
    fft(y);
    for (int i = 0; i < n; ++i) x[i] = (((static_cast<
    long long>(x[i]) * y[i]) % M) * invN) % M;
    std::reverse(x.begin() + 1, x.end());
    fft(x);
    x.resize(na + nb - 1);
    return x;
  }
};
Fft<998244353,23,31> muls;

vector<int> form(vector<int> v,int n)
{
  while(v.size()<n) v.push_back(0);
  while(v.size()>n) v.pop_back();
  return v;
}
vector<int> operator *(vector<int> v1,vector<int> v2)
{
  return muls.convolution(v1,v2);
}
vector<int> operator +(vector<int> v1,vector<int> v2)
{
  while(v2.size()<v1.size()) v2.push_back(0); while(v1
    .size()<v2.size()) v1.push_back(0);
  for(int i=0;i<v1.size();++i) {v1[i]+=v2[i];if(v1[i
    ]>=p) v1[i]-=p; else if(v1[i]<0) v1[i]+=p;}
  return v1;
}
vector<int> operator -(vector<int> v1,vector<int> v2)
{
  int sz=max(v1.size(),v2.size());while(v1.size()<sz)
    v1.push_back(0); while(v2.size()<sz) v2.push_back
    (0);
  for(int i=0;i<sz;++i) {v1[i]-=v2[i];if(v1[i]<0) v1[i
    ]+=p; else if(v1[i]>=p) v1[i]-=p;} return v1;
}
vector<int> trmi(vector<int> v)
{
  for(int i=1;i<v.size();i+=2) {if(v[i]>0) v[i]=p-v[i
    ]; else v[i]=(-v[i]);}
  return v;
}
vector<int> deriv(vector<int> v)
{
  if(v.empty()) return{};
  vector<int> ans(v.size()-1);
  for(int i=1;i<v.size();++i) ans[i-1]=(v[i]*1LL*i)%p;
  return ans;
}
vector<int> integ(vector<int> v)
{
  vector<int> ans(v.size()+1);ans[0]=0;
  for(int i=1;i<v.size();++i) ans[i-1]=(v[i]*1LL*i)%p;
  return ans;
}
vector<int> mul(vector<vector<int> > v)
{
  if(v.size()==1) return v[0];
  vector<vector<int> > v1,v2;for(int i=0;i<v.size()
    /2;++i) v1.push_back(v[i]); for(int i=v.size()/2;i
    <v.size();++i) v2.push_back(v[i]);
  return muls.convolution(mul(v1),mul(v2));
}
vector<int> inv1(vector<int> v,int n)
{
  assert(v[0]!=0);
```

```
  int sz=1;v=form(v,n);vector<int> a={inv(v[0])};
  while(sz<n)
  {
    vector<int> vsz;for(int i=0;i<min(n,2*sz);++i) vsz
    .push_back(v[i]);
    vector<int> b=((vector<int>) {1})-muls.convolution
    (a,vsz);
    for(int i=0;i<sz;++i) assert(b[i]==0);
    b.erase(b.begin(),b.begin()+sz);
    vector<int> c=muls.convolution(b,a);
    for(int i=0;i<sz;++i) a.push_back(c[i]);
    sz*=2;
  }
  return form(a,n);
}
```

4.3 Быстрое FFT

- Solution based on https://codeforces.com/blog/entry/117947
- Iterative and in-place version.
- Uses signed montgomery
- Optimized to minimize memory usage

```
const int MOD = 998244353;
const long long MOD2 = (long long) MOD * MOD;
const int root = 3;
const int alim = 64; // Bound for using O(n^2)
    polynomial mult

int modpow(int b, int e) {
  int ans = 1;
  for (; e; b = (long long) b * b % MOD, e /= 2)
    if (e & 1) ans = (long long) ans * b % MOD;
  return ans;
}

const int MODinv = 2 - MOD; // pow(-MOD, -1, 2**32)
inline int m_reduce(long long x) {
    int m = x * MODinv;
    return (x>>32) - (((long long) m * MOD) >> 32);
}

const int r2 = modpow(2, 64);
inline int m_transform(int x) {
    return m_reduce((long long)x * r2);
}

inline int m_add(int x, int y) {
    int z = x + y;
    return z < 0 ? z + MOD : z - MOD;
}

inline int m_sub(int x, int y) {
    int z = x - y;
    return z < 0 ? z + MOD : z - MOD;
}

inline int m_mult(int x, int y) {
    return m_reduce((long long) x * y);
}

vector<int> rt = {1};
vector<int> transformed_rt;
vector<int> transformed_rt2;

template<int a>
void transform(vector<int> &P) {
    int m = P.size();
    int n = m / a;

    int size = rt.size();
    while (2 * size < n) {
        rt.resize(n / 2);
        int r = modpow(root, MOD / (4 * size));
        for (int i = 0; i < size; ++i)
            rt[i + size] = (long long) r * rt[i] % MOD
    ;
        size *= 2;
    }

    // For montgomery
    for (int i = transformed_rt.size(); i < rt.size();
     ++i) {
        transformed_rt.resize(rt.size());
        transformed_rt[i] = m_transform(rt[i]);
        transformed_rt2.resize(rt.size());
        transformed_rt2[i] = (unsigned int) MODinv *
    transformed_rt[i];
    }

    int k = n;
    while (k >= 4) k /= 4;

    if (k == 2) {
        int step = n * a;
        int half_step = step / 2;
        for (int j1 = 0; j1 < half_step; ++j1) {
            int j2 = j1 + half_step;

            int diff = m_sub(P[j1], P[j2]);
            P[j1] = m_add(P[j1], P[j2]);
            P[j2] = diff;
        }
        k = n/2;
    } else {
        k = n;
    }

    for (; k > 1; k /= 4) {
        for (int i = 0; i < n/k; ++i) {
            int step = k * a;
            int half_step = step / 2;
            int quarter_step = half_step / 2;

            int R20  = transformed_rt2[2 * i];
            int RR0 = transformed_rt[2 * i];

            int R21 = transformed_rt2[2 * i + 1];
            int RR1 = transformed_rt[2 * i + 1];

            int R2 = transformed_rt2[i];
            int RR = transformed_rt[i];

            int j1 = i * step;
            int j2 = j1 + quarter_step;
            int j3 = j2 + quarter_step;
            int j4 = j3 + quarter_step;

            for (int j = 0; j < quarter_step; ++j, ++
    j1, ++j2, ++j3, ++j4) {
                int z0;
                {
                    int z = P[j3];
                    int m = (unsigned int) R2 * z;
                    z0 = ((long long) z * RR - (long
    long) m * MOD) >> 32;
                }

                int z1;
                {
                    int z = P[j4];
                    int m = (unsigned int) R2 * z;
                    z1 = ((long long) z * RR - (long
    long) m * MOD) >> 32;
                }

                int sum0 = m_add(P[j1], z0);
                int diff0 = m_sub(P[j1], z0);
                int sum1 = P[j2] + z1;
                int diff1 = P[j2] - z1;

                // [sum0, sum1, diff0, diff1]

                int zz0;
                {
                    int z = sum1;
                    int m = (unsigned int) R20 * z;
                    zz0 = ((long long) z * RR0 - (long
```

```
     long) m * MOD) >> 32;
                }

                int zz1;
                {
                    int z = diff1;
                    int m = (unsigned int) R21 * z;
                    zz1 = ((long long) z * RR1 - (long
     long) m * MOD) >> 32;
                }

                P[j1]  = m_add(sum0, zz0);
                P[j2]  = m_sub(sum0, zz0);
                P[j3]  = m_add(diff0, zz1);
                P[j4]  = m_sub(diff0, zz1);
            }
        }
    }

    for (int i = 0; i < m; ++i)
        if (P[i] < 0) P[i] += MOD;
}

template<int a>
void inverse_transform(vector<int> &P) {
    int m = P.size();
    int n = m / a;
    int n_inv = m_transform(modpow(n, MOD - 2));

    vector<int> rev(n);
    for (int i = 1; i < n; ++i) {
        rev[i] = rev[i / 2] / 2 + (i & 1) * n / 2;
    }

    // P = [p * n_inv for p in P]
    for (int i = 0; i < m; ++i)
        P[i] = m_mult(n_inv, P[i]);

    // P = [P[a * rev[i // a] + (i % a)] for i in
    range(m)]
    for (int i = 1; i < n; ++i)
        if (i < rev[i])
            swap_ranges(P.begin() + a * i, P.begin() +
     a * i + a, P.begin() + a * rev[i]);

    // P = [P[-a * (i // a) + (i % a)] for i in range(
    m)]
    for (int i = 1; i < n/2; ++i)
        swap_ranges(P.begin() + a * i, P.begin() + a *
     i + a, P.begin() + a * (n - i));

    transform<a>(P);

    // P = [P[a * rev[i // a] + (i % a)] for i in
    range(m)]
    for (int i = 1; i < n; ++i)
        if (i < rev[i])
            swap_ranges(P.begin() + a * i, P.begin() +
     a * i + a, P.begin() + a * rev[i]);
}

template<int a>
void fast_polymult_mod(vector<int> &P, vector<int> &Q)
     {
    int m = P.size();
    int n = m / a;

    transform<a>(P);
    transform<a>(Q);

    vector<int> &PQ = P;
    for (int i = 0; i < n; ++i) {
        vector<unsigned long long> res(2 * a);
        for (int j = 0; j < a; ++j) {
            if (j >= 10 && j % 9 == 8)
                for (int k = j; k < j + a - 10; ++k)
                    res[k] -= (res[k] >> 63) * 9 *
    MOD2;
            for (int k = 0; k < a; ++k)
                res[j + k] += (long long) P[i * a + j]
     * Q[i * a + k];
        }

        int c = rt[i/2];
        if (i & 1) c = MOD - c;
        for (int j = 0; j < a; ++j)
            PQ[i * a + j] = (res[j] + c * (res[j + a]
    % MOD)) % MOD;
    }

    inverse_transform<a>(PQ);
}

template <size_t... N>
void work(std::index_sequence<N...>, int x, std::
    vector<int>& a, std::vector<int>& b) {
    static void (*ptrs[])(std::vector<int>&, std::
    vector<int>&) = {&fast_polymult_mod<N+1>...};
    ptrs[x - 1](a, b);
}

void fast_polymult(vector<int> &P, vector<int> &Q) {
    int m1 = P.size();
    int m2 = Q.size();
    int res_len = m1 + m2 - 1;

    int b = 1;
    while ((alim << b) < res_len) ++b;
    int a = ((res_len - 1) >> b) + 1;
    int m = a << b;

    P.resize(m);
    Q.resize(m);

    // Call fast_polymult_mod<a>(P, Q);
    work(std::make_index_sequence<alim>{}, a, P, Q);

    P.resize(res_len);
}
```

4.4 FFT в double'ах

```
using cd = complex<double>;
const double PI = acos(-1);

void fft(vector<cd> & a, bool invert) {
  int n = a.size();

  for (int i = 1, j = 0; i < n; i++) {
    int bit = n >> 1;
    for (; j & bit; bit >>= 1)
      j ^= bit;
    j ^= bit;

    if (i < j)
      swap(a[i], a[j]);
  }

  for (int len = 2; len <= n; len <<= 1) {
    double ang = 2 * PI / len * (invert ? -1 : 1);
    cd wlen(cos(ang), sin(ang));
    for (int i = 0; i < n; i += len) {
      cd w(1);
      for (int j = 0; j < len / 2; j++) {
        cd u = a[i+j], v = a[i+j+len/2] * w;
        a[i+j] = u + v;
        a[i+j+len/2] = u - v;
        w *= wlen;
      }
    }
  }

  if (invert) {
    for (cd & x : a)
      x /= n;
  }
}
vector<int> multiply(vector<int> const& a, vector<int>
     const& b) {
```

```
  vector<cd> fa(a.begin(), a.end()), fb(b.begin(), b.
    end());
  int n = 1;
  while (n < a.size() + b.size())
    n <<= 1;
  fa.resize(n);
  fb.resize(n);

  fft(fa, false);
  fft(fb, false);
  for (int i = 0; i < n; i++)
    fa[i] *= fb[i];
  fft(fa, true);

  vector<int> result(n);
  for (int i = 0; i < n; i++)
    result[i] = round(fa[i].real());
  while(!result.empty() && !result.back()) result.
    pop_back();
  return result;
}
```

5 Структуры данных

5.1 Дерево Фенвика

```
int fe[maxn];
void pl(int pos,int val) {while(pos<maxn) {fe[pos]+=
    val;pos|=(pos+1);}}
int get(int pos) {int ans=0;while(pos>=0) {ans+=fe[pos
    ];pos&=(pos+1);--pos;} return ans;} /// [0,pos] -
    vkluchitelno!!!
int get(int l,int r) {return get(r-1)-get(l-1);} ///
    sum of [l,r)
```

5.2 Дерево отрезков в точке

```
template<typename T, typename U>
struct SegmentTree {
    int h, n;
    T neutral;
    U unite;
    vector<T> data;

    template<typename I>
    SegmentTree(int sz, T neutral, U unite, I init) :
    h(__lg(sz) + 1), n(1 << h), neutral(neutral),
    unite(unite), data(2 * n) {
        for (int i = 0; i < sz; ++i) data[i + n] =
    init(i);
        for (int i = n - 1; i > 0; --i) data[i] =
    unite(data[2 * i], data[2 * i + 1]);
    }

    SegmentTree(int sz, T neutral, U unite) : h(__lg(
    sz) + 1), n(1 << h), neutral(neutral), unite(unite
    ), data(2 * n, neutral) {}

    void set(int i, T x) {
        data[i += n] = x;
        for (i /= 2; i > 0; i /= 2) data[i] = unite(
    data[2 * i], data[2 * i + 1]);
    }

    T get(int l, int r) {
        T leftRes = neutral, rightRes = neutral;
        for (l += n, r += n; l < r; l /= 2, r /= 2) {
            if (l & 1) leftRes = unite(leftRes, data[l
    ++]);
            if (r & 1) rightRes = unite(data[--r],
    rightRes);
        }
        return unite(leftRes, rightRes);
    }
    int left(int i) {
        int lvl = __lg(i);
        return (i & ((1 << lvl) - 1)) * (1 << (h - lvl
    ));
    }
    int right(int i) {
        int lvl = __lg(i);
        return ((i & ((1 << lvl) - 1)) + 1) * (1 << (h
     - lvl));
    }

    // l \in [0; n) && ok(get(l, l), l);
    // returns last r: ok(get(l, r), r)
    template<typename C>
    int lastTrue(int l, C ok) {
        T cur = neutral;
        l += n;
        do {
            l >>= __builtin_ctz(l);
            T with1 = unite(cur, data[l]);
            if (ok(with1, right(l))) {
                cur = with1;
                ++l;
            } else {
                while (l < n) {
                    T with2 = unite(cur, data[2 * l]);
                    if (ok(with2, right(2 * l))) {
                        cur = with2;
                        l = 2 * l + 1;
                    } else {
                        l = 2 * l;
                    }
                }
                return l - n;
            }
        } while (l & (l - 1));
        return n;
    }

    // r \in [0; n) && ok(get(r, r), r);
    // returns first l: ok(get(l, r), l)
    template<typename C>
    int firstTrue(int r, C ok) {
        T cur = neutral;
        r += n;
        while (r & (r - 1)) {
            r >>= __builtin_ctz(r);
            T with1 = unite(data[--r], cur);
            if (ok(with1, left(r))) {
                cur = with1;
            } else {
                while (r < n) {
                    T with2 = unite(data[2 * r + 1],
    cur);
                    if (ok(with2, left(2 * r + 1))) {
                        cur = with2;
                        r = 2 * r;
                    } else {
                        r = 2 * r + 1;
                    }
                }
                return r - n + 1;
            }
        }
        return 0;
    }
};

void example () {
  // max
  SegmentTree<int> segtree(n, -(int)1e18,  [](int x,
    int y) { return max(x, y); });

  // sum
  SegmentTree<int> ones(n, 0LL,  [](int x, int y) {
    return x + y; });

  auto left_zero = [&](int r) { // nearest zero
    strictly to the left
    return ones.firstTrue(r, [r](int sum, int l){
    return r - l == sum; }) - 1;
  };
  auto right_zero = [&](int l) { // nearest zero
    strictly to the right
    return ones.lastTrue(l + 1, [l](int sum, int r){
    return r - (l + 1) == sum; });
```

```
  };
}
```

5.3 Массовое дерево отрезков

```
#ifdef LOCAL
int __lg(int x) { return 63 - __builtin_clzll(x); }
#endif

template<typename Data, typename Mod, typename
    UniteData, typename UniteMod, typename Apply>
struct MassSegmentTree {
  int h, n;
  Data zd;
  Mod zm;
  vector<Data> data;
  vector<Mod> mod;

  UniteData ud; // Data (Data, Data)
  UniteMod um; // Mod (Mod, Mod);
  Apply a; // Data (Data, Mod, int); last argument is
    the length of current segment (could be used for
    range += and sum counting, for instance)

  template<typename I>
  MassSegmentTree(int sz, Data zd, Mod zm, UniteData
    ud, UniteMod um, Apply a, I init) : h(__lg(sz > 1
    ? sz - 1 : 1) + 1), n(1 << h), zm(zm), zd(zd),
    data(2 * n, zd), mod(n, zm), ud(ud), um(um), a(a)
    {
    for (int i = 0; i < sz; ++i) data[i + n] = init(i)
    ;
    for (int i = n - 1; i > 0; --i) data[i] = ud(data
    [2 * i], data[2 * i + 1]);
  }

  MassSegmentTree(int sz, Data zd, Mod zm, UniteData
    ud, UniteMod um, Apply a) : h(__lg(sz > 1 ? sz - 1
     : 1) + 1), n(1 << h), zm(zm), zd(zd), data(2 * n,
     zd), mod(n, zm), ud(ud), um(um), a(a) {}

  void push(int i) {
    if (mod[i] == zm) return;
    apply(2 * i, mod[i]);
    apply(2 * i + 1, mod[i]);
    mod[i] = zm;
  }

  // is used only for apply
  int length(int i) { return 1 << (h - __lg(i)); }

  // used only for descent
  int left(int i) {
    int lvl = __lg(i);
    return (i & ((1 << lvl) - 1)) * (1 << (h - lvl));
  }

  // used only for descent
  int right(int i) {
    int lvl = __lg(i);
    return ((i & ((1 << lvl) - 1)) + 1) * (1 << (h -
    lvl));
  }

  template<typename S>
  void apply(int i, S x) {
    data[i] = a(data[i], x, length(i));
    if (i < n) mod[i] = um(mod[i], x);
  }

  void update(int i) {
    if (mod[i] != zm) return;
    data[i] = ud(data[2 * i], data[2 * i + 1]);
  }

  template<typename S>
  void update(int l, int r, S x) { // [l; r)
    l += n, r += n;
    for (int shift = h; shift > 0; --shift) {
      push(l >> shift);
      push((r - 1) >> shift);
    }
    for (int lf = l, rg = r; lf < rg; lf /= 2, rg /=
    2) {
      if (lf & 1) apply(lf++, x);
      if (rg & 1) apply(--rg, x);
    }
    for (int shift = 1; shift <= h; ++shift) {
      update(l >> shift);
      update((r - 1) >> shift);
    }
  }

  Data get(int l, int r) { // [l; r)
    l += n, r += n;
    for (int shift = h; shift > 0; --shift) {
      push(l >> shift);
      push((r - 1) >> shift);
    }
    Data leftRes = zd, rightRes = zd;
    for (; l < r; l /= 2, r /= 2) {
      if (l & 1) leftRes = ud(leftRes, data[l++]);
      if (r & 1) rightRes = ud(data[--r], rightRes);
    }
    return ud(leftRes, rightRes);
  }

  // l \in [0; n) && ok(get(l, l), l);
  // returns last r: ok(get(l, r), r)
  template<typename C>
  int lastTrue(int l, C ok) {
    l += n;
    for (int shift = h; shift > 0; --shift) push(l >>
    shift);
    Data cur = zd;
    do {
      l >>= __builtin_ctz(l);
      Data with1;
      with1 = ud(cur, data[l]);
      if (ok(with1, right(l))) {
        cur = with1;
        ++l;
      } else {
        while (l < n) {
          push(l);
          Data with2;
          with2 = ud(cur, data[2 * l]);
          if (ok(with2, right(2 * l))) {
            cur = with2;
            l = 2 * l + 1;
          } else {
            l = 2 * l;
          }
        }
        return l - n;
      }
    } while (l & (l - 1));
    return n;
  }

  // r \in [0; n) && ok(get(r, r), r);
  // returns first l: ok(get(l, r), l)
  template<typename C>
  int firstTrue(int r, C ok) {
    r += n;
    for (int shift = h; shift > 0; --shift) push((r -
    1) >> shift);
    Data cur = zd;
    while (r & (r - 1)) {
      r >>= __builtin_ctz(r);
      Data with1;
      with1 = ud(data[--r], cur);
      if (ok(with1, left(r))) {
        cur = with1;
      } else {
        while (r < n) {
          push(r);
          Data with2;
          with2 = ud(data[2 * r + 1], cur);
          if (ok(with2, left(2 * r + 1))) {
            cur = with2;
```

```
            r = 2 * r;
          } else {
            r = 2 * r + 1;
          }
        }
        return r - n + 1;
      }
    }
    return 0;
  }
};

void example () {
  // max and +=
  MassSegmentTree segtree(n, 0LL, 0LL,
  [](int x, int y) { return max(x, y); },
  [](int x, int y) { return x + y; },
  [](int x, int y, int len) { return x + y; });

  // sum and +=
  MassSegmentTree segtree(n, 0LL, 0LL,
  [](int x, int y) { return x + y; },
  [](int x, int y) { return x + y; },
  [](int x, int y, int len) { return x + y * len; });

  // sum and assignment
  MassSegmentTree segtree(n, 0LL, -1LL,
  [](int x, int y) { return x + y; },
  [](int x, int y) { return y; },
  [](int x, int y, int len) { return y * len; });
}
```

5.4 Битовый бор

```
template<unsigned int sz,typename T=int>
struct binarytrie{
  using Bit=typename conditional<sz<=32,unsigned int,
    unsigned long long>::type;
  struct node{
    T cnt;
    array<int,2>nxt;
    node():cnt(0),nxt({-1,-1}){}
  };
  vector<node>v;
  binarytrie(){v.emplace_back();}
  void insert(Bit x){add(x,1);}
  void erase(Bit x){add(x,-1);}
  void add(Bit x,T k)
  {
    assert(0<=x&&(x>>sz)==0);
    int p=0;
    v[p].cnt+=k;
    for(int i=sz;i--;)
    {
      int j=x>>i&1;
      if(v[p].nxt[j]==-1)
      {
        v[p].nxt[j]=v.size();
        v.emplace_back();
      }
      p=v[p].nxt[j];
      v[p].cnt+=k;
    }
  }
  T count(Bit x,Bit xor_val=0)const//[0,x)
  {
    assert(0<=xor_val&&(xor_val>>sz)==0);
    if(x<0)return 0;
    else if(x>>sz)return v[0].cnt;
    T ret=0;
    int p=0;
    for(int i=sz;i--;)
    {
      int j=x>>i&1,k=xor_val>>i&1;
      if(j==0)p=v[p].nxt[k];
      else
      {
        if(v[p].nxt[k]>=0)ret+=v[v[p].nxt[k]].cnt;
        p=v[p].nxt[!k];
      }
      if(p==-1)break;
    }
    return ret;
  }
  Bit max(Bit xor_val=0)const
  {
    assert(0<=xor_val&&(xor_val>>sz)==0);
    int p=0;
    Bit ret=0;
    if(v[p].cnt==0)return ret;
    for(int i=sz;i--;)
    {
      ret<<=1;
      int k=xor_val>>i&1;
      if(v[p].nxt[!k]>=0&&v[v[p].nxt[!k]].cnt>0)
      {
        p=v[p].nxt[!k];
        ret|=1;
      }
      else p=v[p].nxt[k];
    }
    return ret;
  }
  Bit min(Bit xor_val=0)const
  {
    assert(0<=xor_val&&(xor_val>>sz)==0);
    int p=0;
    Bit ret=0;
    for(int i=sz;i--;)
    {
      ret<<=1;
      int k=xor_val>>i&1;
      if(v[p].nxt[k]>=0&&v[v[p].nxt[k]].cnt>0)p=v[p].
    nxt[k];
      else
      {
        p=v[p].nxt[!k];
        ret|=1;
      }
    }
    return ret;
  }
  Bit find_by_order(T ord,Bit xor_val=0)const
  {
    assert(0<=xor_val&&(xor_val>>sz)==0);
    assert(0<=ord&&ord<v[0].cnt);
    int p=0;
    Bit ret=0;
    for(int i=sz;i--;)
    {
      ret<<=1;
      int k=xor_val>>i&1;
      if(v[p].nxt[k]>=0)
      {
        if(ord>=v[v[p].nxt[k]].cnt)
        {
          ord-=v[v[p].nxt[k]].cnt;
          p=v[p].nxt[!k];
          ret|=1;
        }
        else p=v[p].nxt[k];
      }
      else
      {
        p=v[p].nxt[!k];
        ret|=1;
      }
    }
    return ret;
  }
  T order_of_key(Bit x,Bit xor_val=0)const{return
    count(x,xor_val);}
};
binarytrie<32>bt;
```

5.5 Ordered set

```
#include <ext/pb_ds/assoc_container.hpp>
#include <ext/pb_ds/tree_policy.hpp>

using namespace __gnu_pbds;
```

```
using namespace std;

using ordered_set = tree<int, null_type, less<>,
    rb_tree_tag, tree_order_statistics_node_update>;
```

5.6 Convex hull trick

```
int div_up(int a, int b) { return a/b+((a^b)>0&&a%b);
    } // divide a by b rounded up
const int LQ = ..., RQ = ...; //leftmost query,
    rightmost query
int in(ii L, int x) {
    return L.x * x + L.y;
}
struct Hull {
vector <pair <int, int> > lines;
vector <int> borders;
void push(ii L) {
    while (lines.size() && in(L,borders.back()) < in(
    lines.back(),borders.back())) {
        lines.pop_back();
        borders.pop_back();
    }
    if (lines.empty()) {
        lines = {L};
        borders = {LQ};
    }
    else if (lines.back().x > L.x) {
        int x = div_up(L.y - lines.back().y, lines.
    back().x - L.x);
        if (x <= RQ) {
            lines.app(L);
            borders.app(x);
        }
    }
}
Hull (){}
Hull (vector <ii> a) {
    auto comp = [&] (ii u, ii v) {
        return u.x > v.x || (u.x == v.x && u.y < v.y);
    };
    sort(all(a), comp);
    for (auto L : a) {
        push(L);
    }
}
int get(int x) {
    int pos = upper_bound(all(borders), x) - borders.
    begin();
    assert(pos>0);
    pos--;
    return in(lines[pos],x);
}
};
```

5.7 Центроиды

```
vector<int> sz(n), lvl(n, -1);
auto dfs = [&](auto dfs, int cur, int prev) -> int {
    if (lvl[cur] != -1) return 0;
    sz[cur] = 1;
    for (auto [nxt, w] : g[cur]) {
        if (nxt != prev) sz[cur] += dfs(dfs, nxt, cur)
    ;
    }
    return sz[cur];
};
auto find = [&](auto find, int cur, int prev, int tot)
     -> int {
    int bch = -1, bsz = 0;
    for (auto [nxt, w] : g[cur]) {
        if (nxt == prev || lvl[nxt] != -1) continue;
        if (sz[nxt] > bsz) {
            bch = nxt;
            bsz = sz[nxt];
        }
    }
    if (bsz + bsz <= tot) return cur;
    return find(find, bch, cur, tot);
};
dfs(dfs, 0, 0);
auto c = find(find, 0, 0, sz[0]);
vector<pair<int, int>> stack{{c, 0}};
while (!stack.empty()) {
    auto [centroid, l] = stack.back();
    stack.pop_back();
    lvl[centroid] = l;
    for (auto [nxt, w] : g[centroid]) {
        if (lvl[nxt] != -1) continue;
        dfs(dfs, nxt, centroid);
        int new_centroid = find(find, nxt, centroid,
    sz[nxt]);
        stack.push_back({new_centroid, lvl[centroid] +
     1});
    }
}
```

5.8 Дерево Ли Чао

```
struct Line{
    int a, b;
    Line(){}
    Line (int a, int b) : a(a), b(b) {}
    int get(int x) { return a + b * x;}
};

struct Lichao {
    int n;
    vector <int> x;
    vector <Line> t;
    Lichao(){}
    Lichao (int n, vector<int> x) : n(n), t(n << 2,
    Line(inf, 0)), x(x) {}

    void put(int v, int l, int r, Line L) {
        if (l + 1 == r) {
            if (L.get(x[l]) < t[v].get(x[l])) {
                t[v] = L;
            }
            return;
        }
        int m = (l + r) / 2;
        if (L.get(x[m]) < t[v].get(x[m])) {
            swap(L, t[v]);
        }
        if (L.b > t[v].b) {
            put(2 * v + 1, l, m, L);
        }
        else {
            put(2 * v + 2, m, r, L);
        }
    }

    int get(int v, int l, int r, int i) {
        if (l + 1 == r) {
            return t[v].get(x[l]);
        }
        int m = (l + r) / 2;
        int ans = t[v].get(x[i]);
        if (i < m) {
            ans = min(ans, get(2 * v + 1, l, m, i));
        } else {
            ans = min(ans, get(2 * v + 2, m, r, i));}
        return ans;
    }

    void put(Line L) {
        put(0, 0, n, L);
    }

    int get(int i) {
        return get(0, 0, n, i);
    }
};
```

5.9 Min-Kinetic Segment Tree

I guess the source is https://koosaga.com/307

```
using lint = long long;
const lint inf = 4e18;
const int MAXT = 4100000;
```

```
using pi = array<lint, 2>;

struct line {
    lint A, B;
    int idx;

    lint eval(lint x) { return A * x + B; }

    // returns the x-intercept of intersection "
    strictly" larger than T
    lint cross_after(line &x, lint T) {
        if (x.A == A) {
            return inf;
        }
        lint up = x.B - B;
        lint dn = A - x.A;
        if (dn < 0) {
            dn *= -1;
            up *= -1;
        }
        lint incep = (up <= 0 ? -((-up) / dn) : (up +
    dn - 1) / dn);
        if (incep > T)
            return incep;
        return inf;
    }
};

struct kst { // min kinetic segment tree
    line tree[MAXT];
    lint melt[MAXT], T;
    pi lazy[MAXT];
    int n;

    bool cmp(line &a, line &b) {
        lint l = a.eval(T), r = b.eval(T);
        if (l != r)
            return l > r;
        return a.A > b.A;
    }

    void pull(int p) {
        tree[p] = cmp(tree[2 * p], tree[2 * p + 1]) ?
    tree[2 * p + 1] : tree[2 * p];
        melt[p] = min({melt[2 * p], melt[2 * p + 1],
    tree[2 * p].cross_after(tree[2 * p + 1], 0)});
    }

    void init(int s, int e, int p, vector<line> &l) {
        if (s == e) {
            tree[p] = l[s];
            melt[p] = inf;
            lazy[p] = {0, 0};
            return;
        }
        lazy[p] = {0, 0};
        int m = (s + e) / 2;
        init(s, m, 2 * p, l);
        init(m + 1, e, 2 * p + 1, l);
        pull(p);
    }

    void lazydown(int p) {
        for (int i = 2 * p; i < 2 * p + 2; i++) {
            lazy[i][0] += lazy[p][0];
            lazy[i][1] += lazy[p][1];
            tree[i].B += lazy[p][0] * tree[i].A + lazy
    [p][1];
            melt[i] -= lazy[p][0];
        }
        lazy[p][0] = lazy[p][1] = 0;
    }

    void propagate(int p) {
        if (melt[p] > 0)
            return;
        lazydown(p);
        propagate(2 * p);
        propagate(2 * p + 1);
        pull(p);
    }

    lint query(int s, int e, int ps, int pe, int p =
    1) {
        if (e < ps || pe < s)
            return inf;
        if (s <= ps && pe <= e)
            return tree[p].eval(0);
        int pm = (ps + pe) / 2;
        lazydown(p);
        return min(query(s, e, ps, pm, 2 * p), query(s
    , e, pm + 1, pe, 2 * p + 1));
    }

    void heaten(int s, int e, int ps, int pe, int p,
    lint v) {
        if (e < ps || pe < s)
            return;
        if (s <= ps && pe <= e) {
            lazy[p][0] += v;
            tree[p].B += v * tree[p].A;
            melt[p] -= v;
            propagate(p);
            return;
        }
        lazydown(p);
        int pm = (ps + pe) / 2;
        heaten(s, e, ps, pm, 2 * p, v);
        heaten(s, e, pm + 1, pe, 2 * p + 1, v);
        pull(p);
    }

    void add(int s, int e, int ps, int pe, int p, lint
     v) {
        if (e < ps || pe < s)
            return;
        if (s <= ps && pe <= e) {
            lazy[p][1] += v;
            tree[p].B += v;
            return;
        }
        lazydown(p);
        int pm = (ps + pe) / 2;
        add(s, e, ps, pm, 2 * p, v);
        add(s, e, pm + 1, pe, 2 * p + 1, v);
        pull(p);
    }

    void init(vector<line> &l, lint _T) {
        n = l.size();
        T = _T;
        init(0, n - 1, 1, l);
    }
};
```

6 Строковые алгоритмы

6.1 Префикс-функция

```
vector<int> prefix_function(string s) {
  vector<int> p(s.size());
  for (int i = 1; i < s.size(); ++i) {
    p[i] = p[i - 1];
    while (p[i] && s[p[i]] != s[i]) p[i] = p[p[i] -
    1];
    p[i] += s[i] == s[p[i]];
  }
  return p;
}
```

6.2 Z-функция

```
vector<int> z_function (string s) { // z[i] - lcp of s
     and s[i:]
 int n = (int) s.length();
 vector<int> z (n);
 for (int i=1, l=0, r=0; i<n; ++i) {
  if (i <= r)
   z[i] = min (r-i+1, z[i-l]);
```

```
  while (i+z[i] < n && s[z[i]] == s[i+z[i]])
   ++z[i];
  if (i+z[i]-1 > r)
   l = i,  r = i+z[i]-1;
 }
 return z;
}
```

6.3 Алгоритм Манакера

```
vector<int> manacher_odd(const string &s) {
  vector<int> man(s.size(), 0);
  int l = 0, r = 0;
  int n = s.size();
  for (int i = 1; i < n; i++) {
    if (i <= r) {
      man[i] = min(r - i, man[l + r - i]);
    }
    while (i + man[i] + 1 < n && i - man[i] - 1 >= 0
    && s[i + man[i] + 1] == s[i - man[i] - 1]) {
      man[i]++;
    }
    if (i + man[i] > r) {
      l = i - man[i];
      r = i + man[i];
    }
  }
  return man;
}
// abacaba : (0 1 0 3 0 1 0)
// abbaa : (0 0 0 0 0)

vector <int> manacher_even(const string &s) {
  assert(s.size());
  string t;
  for (int i = 0; i + 1 < s.size(); ++i) {
    t += s[i];
    t += '#';
  }
  t += s.back();
  auto odd = manacher_odd(t);
  vector <int> ans;
  for (int i = 1; i < odd.size(); i += 2) {
    ans.push_back((odd[i]+1)/2);
  }
  return ans;
}
// abacaba : (0 0 0 0 0 0)
// abbaa : (0 2 0 1)


  auto pal = [&] (int i, int from, int len) {
    if (len == 0) {
        return true;
    }
    int m = len/2;
    if (len & 1) {
        return o[i][from + m] >= m;
    }
    else {
        return e[i][from + m - 1] >= m;
    }
};
```

6.4 Суфмассив

Переработанный китайский суффмассив

```
const int inf = 1e9;
struct rmq {
  int n;
  vector<int> a;
  void build(const vector<int> &x) {
    assert(x.size() == n);
    for (int i = 0; i < n; ++i) a[n + i] = x[i];
    for (int i = n - 1; i > 0; --i) a[i] = min(a[2 * i
    ], a[2 * i + 1]);
  }
  rmq(int n) : n(n), a(2 * n, inf) {}
  void put(int i, int x) {
    a[i + n] = min(a[i + n], x);
    for (i = (i + n) / 2; i > 0; i /= 2) {
      a[i] = min(a[i * 2], a[i * 2 + 1]);
    }
  }
  int getMin(int l, int r) { //[l;r)
    assert(l < r);
    int res = inf;
    for (l += n, r += n; l < r; l /= 2, r /= 2) {
      if (l & 1) res = min(res, a[l++]);
      if (r & 1) res = min(res, a[--r]);
    }
    return res;
  }
};
template <typename T>
vector <int> SA(const T &a) {
    int m = *max_element(all(a)) + 1, n = a.size();
    vector <int> sa(n), nsa(n), pre(max(n, m)), x(a.
    begin(), a.end()), y(n);
    for (int e : x) pre[e]++;
    for (int i = 1; i < m; ++i) pre[i] += pre[i - 1];
    for (int i = 0; i < n; ++i) sa[--pre[x[i]]]=i;
    int dif = 1;
    y[sa.front()]=0;
    for (int i = 1; i < n; ++i) {
        dif += x[sa[i]]!=x[sa[i-1]];
        y[sa[i]] = dif - 1;
    }
    x = y;
    for (int h = 1; dif < n; h *= 2) {
        fill(all(pre), 0);
        for (int e : x) pre[e]++;
        for (int i = 1; i < dif; ++i) pre[i] += pre[i
    - 1];
        for (int t = n; t--; ) {
            int i = sa[t];
            if (i>=h) {
                nsa[--pre[x[i-h]]]=i-h;
            }
            else if (i + 1 != h) {
                nsa[--pre[x[i-h+n+1]]]=i-h+n+1;
            }
        }
        nsa[--pre[x[n - h]]]=n-h;
        sa = nsa;
        auto getr = [&] (int i) {
            if (i + h < n) {
                return x[i + h];
            }
            else {
                return x[i + h - n - 1];
            }
        };
        dif = 1;
        y[sa.front()]=0;
        for (int i = 1; i < n; ++i) {
            if (x[sa[i]]!=x[sa[i-1]] || sa[i-1]+h==n)
    {
                dif++;
            }
            else {
                dif += getr(sa[i]) != getr(sa[i-1]);
            }
            y[sa[i]]=dif-1;
        }
        x = y;
    }
    return sa;
}

template <typename T>
struct suar {
    vector <int> sa, lcp, pos; rmq t;
    suar (const T &a) : t((int)a.size() - 1) {
        sa = SA(a);
        int n = (int)a.size(), k = 0;
        lcp.resize(n - 1);
        pos.resize(n);
        for (int i = 0; i < n; ++i) pos[sa[i]] = i;
        for (int i = 0; i < n; ++i) {
            if (pos[i]+1<n) {
```

```
                int j = sa[pos[i]+1];
                while (i+k<n&&j+k<n&&a[i+k]==a[j+k])k
    ++;
                lcp[pos[i]]=k;
            }
            if (k) {
                k--;
            }
        }
        t.build(lcp);
    }
    int getLcp(int i, int j) {
        i = pos[i]; j = pos[j];
        if (j < i) {
          swap(i, j);
        }
        if (i == j) {
          return inf;
        }
        else {
          return t.getMin(i, j);
        }
    }
};
```

6.5 Алгоритм Ахо — Корасик

6.6 Алгоритм Ахо Корасик

```
struct node{
  int next[alpha] = {}, link[alpha] = {};
  int suf = 0;
  ll visited = 0, ans = 0;
  vector<int> term;
  node() {}
};

vector<node> mem;

int get_next(int nd, char c) {
  if (!mem[nd].next[c - a]) { mem[nd].next[c - a] =
    mem.size(); mem.emplace_back(); }
  return mem[nd].next[c - a];
}

void find(string s, vector<string> t) {
  mem.reserve(1e6 + 100);mem.clear();
  mem.emplace_back();mem.emplace_back();
  // 0th element is nullptr, 1st is the root
  int q = t.size();
  for (int j = 0; j < q; ++j) {
    int cur = 1;
    for (char c : ts[j]) cur = get_next(cur, c);
    mem[cur].term.push_back(j);
  }
  vector<int> bfs_order;
  queue<int> bfs;
  {
      node &root = mem[1];
      root.suf = 1;
      for (char c = a; c < a + alpha; ++c) {
          root.link[c - a] = (root.next[c - a] ? root.
    next[c - a] : 1);
      }
      bfs.push(1);
  }
  while (!bfs.empty()) {
    int cur_idx = bfs.front();
    bfs.pop();
    node &cur = mem[cur_idx];
    bfs_order.push_back(cur_idx);
    for (char c = a; c < a + alpha; ++c) {
      int nxt_idx = cur.next[c - a];
      if (!nxt_idx) continue;
      node &nxt = mem[nxt_idx];
      nxt.suf = (cur_idx == 1 ? 1 : mem[cur.suf].link[
    c - a]);
      for (char c = a; c < a + alpha; ++c) {
        nxt.link[c - a] = (nxt.next[c - a] ? nxt.next[
    c - a] : mem[nxt.suf].link[c - a]);
      }
      bfs.push(nxt_idx);
    }
  }
  // do something
}
```

6.7 Дерево палиндромов

6.8 Дерево палиндромов

```
struct palindromic{
  int n;
  vector<int> p, suf{0, 0}, len{-1, 0};
  vector<array<int, alpha>> to{{}, {}};
  int sz = 2;

  palindromic(const string &s) : n(s.size()), p(n + 1,
     1) {
    suf.reserve(n);
    len.reserve(n);
    for (int i = 0; i < n; ++i) {
      auto check = [&](int l) { return i > l && s[i]
    == s[i - l - 1]; };
      int par = p[i];
      while (!check(len[par])) par = suf[par];
      if (to[par][s[i] - a]) {
        p[i + 1] = to[par][s[i] - a];
        continue;
      }
      p[i + 1] = sz++;
      to[par][s[i] - a] = p[i + 1];
      to.emplace_back();
      len.emplace_back(len[par] + 2);
      do {
        par = suf[par];
      } while (!check(len[par]));
      int link = to[par][s[i] - a];
      if (link == p[i + 1]) link = 1;
      suf.emplace_back(link);
    }
  }
};
```

7 Потоки

7.1 Алгоритм Диница

```
#define pb push_back
struct Dinic{
struct edge{
  int to, flow, cap;
};

const static int N = 555; //count of vertices

vector<edge> e;
vector<int> g[N + 7];
int dp[N + 7];
int ptr[N + 7];

void clear(){
  for (int i = 0; i < N + 7; i++) g[i].clear();
  e.clear();
}

void addEdge(int a, int b, int cap){
  g[a].pb(e.size());
  e.pb({b, 0, cap});
  g[b].pb(e.size());
  e.pb({a, 0, 0});
}

int minFlow, start, finish;

bool bfs(){
  for (int i = 0; i < N; i++) dp[i] = -1;
  dp[start] = 0;
  vector<int> st;
  int uk = 0;
  st.pb(start);
```

```
  while(uk < st.size()){
    int v = st[uk++];
    for (int to : g[v]){
      auto ed = e[to];
      if (ed.cap - ed.flow >= minFlow && dp[ed.to] ==
    -1){
        dp[ed.to] = dp[v] + 1;
        st.pb(ed.to);
      }
    }
  }
  return dp[finish] != -1;
}

int dfs(int v, int flow){
  if (v == finish) return flow;
  for (; ptr[v] < g[v].size(); ptr[v]++){
    int to = g[v][ptr[v]];
    edge ed = e[to];
    if (ed.cap - ed.flow >= minFlow && dp[ed.to] == dp
    [v] + 1){
      int add = dfs(ed.to, min(flow, ed.cap - ed.flow)
    );
      if (add){
        e[to].flow += add;
        e[to ^ 1].flow -= add;
        return add;
      }
    }
  }
  return 0;
}

int dinic(int start, int finish){
  Dinic::start = start;
  Dinic::finish = finish;
  int flow = 0;
  for (minFlow = (1 << 30); minFlow; minFlow >>= 1){
    while(bfs()){
      for (int i = 0; i < N; i++) ptr[i] = 0;
      while(int now = dfs(start, (int)2e9 + 7)) flow
    += now;
    }
  }
  return flow;
}
} dinic;
```

7.2 Mincost k-flow

```
struct edge {
  int next, capacity, cost, flow = 0;

  edge() = default;

  edge(int next, int capacity, int cost) : next(next),
     capacity(capacity), cost(cost) {}

  int rem() const { return capacity - flow; }

  int operator+=(int f) { return flow += f; }

  int operator-=(int f) { return flow -= f; }
};
auto addEdge = [&](auto from, auto next, auto capacity
    , int cost) {
  g[from].push_back(e.size());
  e.emplace_back(next, capacity, cost);
  g[next].push_back(e.size());
  e.emplace_back(from, 0, -cost);
};
/* in case of undirected graph use this:
addEdge(u, v, capacity, cost);
addEdge(v, u, capacity, cost);
*/
vector<ll> phi(n, 0);
auto fordBellman = [&](int s, int t) {
  phi.assign(n, 0);
  for (int iter = 0; iter < n; ++iter) {
    bool changed = false;
    for (int u = 0; u < n; ++u) {
      for (auto index : g[u]) {
        auto edge = e[index];
        if (edge.rem() > 0 && phi[edge.next] > phi[u]
    + edge.cost) {
          phi[edge.next] = phi[u] + edge.cost;
          changed = true;
        }
      }
    }
    if (!changed) break;
  }
};
fordBellman(s, t);
// now shortest path using dijkstra with potentials
vector<ll> dist;
vector<int> from;
vector<bool> cnt;
auto dijkstra = [&](int s, int t) {
  dist.assign(n, 1e18);
  from.assign(n, -1);
  cnt.assign(n, false);
  dist[s] = 0;
  set <pair <int, int> > se;
  se.insert({0, s});
  while ((int)(se.size())) {
    int cur = se.begin()->y;
    se.erase(se.begin());
    cnt[cur] = true;
    for (int index : g[cur]) {
      auto &edge = e[index];
      if (edge.rem() == 0) continue;
      ll weight = edge.cost + phi[cur] - phi[edge.next
    ];
      if (dist[edge.next] > dist[cur] + weight) {
        se.erase({dist[edge.next], edge.next});
        dist[edge.next] = dist[cur] + weight;
        se.insert({dist[edge.next], edge.next});
        from[edge.next] = cur;
      }
    }
  }
  if (dist[t] == (ll) 1e18) return -1LL;
  ll cost = 0;
  for (int p = t; p != s; p = from[p]) {
    for (auto index : g[from[p]]) {
      auto &edge = e[index];
      ll weight = edge.cost + phi[from[p]] - phi[edge.
    next];
      if (edge.rem() > 0 && edge.next == p && dist[
    edge.next] == dist[from[p]] + weight) {
        edge += 1;
        e[index ^ 1] -= 1;
        cost += edge.cost;
        break;
      }
    }
  }
  for (int i = 0; i < n; ++i) {
    phi[i] += dist[i];
  }
  return cost;
};
ll cost = 0;
for (int flow = 0; flow < k; ++flow) {
  ll a = dijkstra(s, t);
  if (a == -1) {
    cout << "-1\n";
    return;
  }
  cost += a;
}
// now recover answer
auto findPath = [&](int s, int t) {
  vector<int> ans;
  int cur = s;
  while (cur != t) {
    for (auto index : g[cur]) {
      auto &edge = e[index];
      if (edge.flow <= 0) continue;
      edge -= 1;
```

```
      e[index ^ 1] += 1;
      ans.push_back(index / 4);
// index / 4 because each edge has 4 copies
      cur = edge.next;
      break;
    }
  }
  return ans;
};
for (int flow = 0; flow < k; ++flow) {
  auto p = findPath(s, t);
  cout << p.size() << ' ';
  for (int x : p) cout << x + 1 << ' ';
  cout << '\n';
}
```

8 Гамильтоновы путь и цикл

https://codeforces.com/blog/entry/90513,
https://codeforces.com/blog/entry/90743.

8.1 Link-cut tree

```
namespace LCT {
    vector<vi> ch;
    vi fa, rev;
    void init(int n) {
        ch.resize(n + 1);
        fa.resize(n + 1);
        rev.resize(n + 1);
        for (int i = 0; i <= n; i++)
            ch[i].resize(2),
            ch[i][0] = ch[i][1] = fa[i] = rev[i] = 0;
    }
    bool isr(int a)
    {
        return !(ch[fa[a]][0] == a || ch[fa[a]][1] ==
    a);
    }
    void pushdown(int a)
    {
        if(rev[a])
        {
            rev[ch[a][0]] ^= 1, rev[ch[a][1]] ^= 1;
            swap(ch[a][0], ch[a][1]);
            rev[a] = 0;
        }
    }
    void push(int a)
    {
        if(!isr(a)) push(fa[a]);
        pushdown(a);
    }
    void rotate(int a)
    {
        int f = fa[a], gf = fa[f];
        int tp = ch[f][1] == a;
        int son = ch[a][tp ^ 1];
        if(!isr(f))
            ch[gf][ch[gf][1] == f] = a;
        fa[a] = gf;

        ch[f][tp] = son;
        if(son) fa[son] = f;

        ch[a][tp ^ 1] = f, fa[f] = a;
    }
    void splay(int a)
    {
        push(a);
        while(!isr(a))
        {
            int f = fa[a], gf = fa[f];
            if(isr(f)) rotate(a);
            else
            {
                int t1 = ch[gf][1] == f, t2 = ch[f][1]
     == a;
                if(t1 == t2) rotate(f), rotate(a);
                else rotate(a), rotate(a);
            }
        }
    }
    void access(int a)
    {
        int pr = a;
        splay(a);
        ch[a][1] = 0;
        while(1)
        {
            if(!fa[a]) break;
            int u = fa[a];
            splay(u);
            ch[u][1] = a;
            a = u;
        }
        splay(pr);
    }
    void makeroot(int a)
    {
        access(a);
        rev[a] ^= 1;
    }
    void link(int a, int b)
    {
        makeroot(a);
        fa[a] = b;
    }
    void cut(int a, int b)
    {
        makeroot(a);
        access(b);
        fa[a] = 0, ch[b][0] = 0;
    }
    int fdr(int a)
    {
        access(a);
        while(1)
        {
            pushdown(a);
            if (ch[a][0]) a = ch[a][0];
            else {
                splay(a);
                return a;
            }
        }
    }
}
```

8.2 Undirected case

```
#include <bits/stdc++.h>
using namespace std;
namespace hamil {
    template <typename T> bool chkmax(T &x,T y){return
     x<y?x=y,true:false;}
    template <typename T> bool chkmin(T &x,T y){return
     x>y?x=y,true:false;}
    #define vi vector<int>
    #define pb push_back
    #define mp make_pair
    #define pi pair<int, int>
    #define fi first
    #define se second
    #define ll long long
    using namespace LCT;
    vector<vi> used;
    unordered_set<int> caneg;
    void cut(int a, int b) {
      LCT::cut(a, b);
      for (int s = 0; s < 2; s++) {
        for (int i = 0; i < used[a].size(); i++)
          if (used[a][i] == b) {
            used[a].erase(used[a].begin() + i);
            break;
          }
        if (used[a].size() == 1) caneg.insert(a);
        swap(a, b);
      }
    }
    void link(int a, int b) {
```

```
    LCT::link(a, b);
    for (int s = 0; s < 2; s++) {
      used[a].pb(b);
      if (used[a].size() == 2) caneg.erase(a);
      swap(a, b);
    }
  }
    vi work(int n, vector<pi> eg, ll mx_ch = -1) {
        // mx_ch : max number of adding/replacing
    default is (n + 100) * (n + 50)
        // n : number of vertices. 1-indexed.
        // eg: vector<pair<int, int> > storing all the
     edges.
        // return a vector<int> consists of all
    indices of vertices on the path. return empty list
     if failed to find one.

        LCT::init(n);
        if (mx_ch == -1) mx_ch = 1ll * (n + 100) * (n
    + 50); //default
        used.resize(n + 1);
        caneg.clear();
        for (int i = 1; i <= n; i++) used[i].clear();

        vector<vi> edges(n + 1);
        for (auto v : eg)
            edges[v.fi].pb(v.se),
            edges[v.se].pb(v.fi);

        for (int i = 1; i <= n; i++)
            caneg.insert(i);

        mt19937 x(chrono::steady_clock::now().
    time_since_epoch().count());
        int tot = 0;
        while (mx_ch >= 0) {
        //    cout << tot << ' ' << mx_ch << endl;
            vector<pi> eg;
            for (auto v : caneg)
                for (auto s : edges[v])
                    eg.pb(mp(v, s));

            shuffle(eg.begin(), eg.end(), x);
            if (eg.size() == 0) break;
            for (auto v : eg) {
                mx_ch--;
                int a = v.fi, b = v.se;
                if (used[a].size() < used[b].size())
    swap(a, b);
                if (used[b].size() >= 2) continue;
                if (x() & 1) continue;
                if (LCT::fdr(a) == LCT::fdr(b))
    continue;
                if (used[a].size() < 2 && used[b].size
    () < 2)
                  tot++;
                if (used[a].size() == 2) {
                  int p = used[a][x() % 2];
                  cut(a, p);
                }
                link(a, b);
            }
            if (tot == n - 1) {
                vi cur;
                for (int i = 1; i <= n; i++)
                    if (used[i].size() <= 1) {
                        int pl = i, ls = 0;
                        while (pl) {
                            cur.pb(pl);
                            int flag = 0;
                            for (auto v : used[pl])
                              if (v != ls) {
                                ls = pl;
                                pl = v;
                                flag = 1;
                                break;
                }
              if (!flag) break;
                        }
                        break;
                    }
                return cur;
            }
        }
        //failed to find a path
        return vi();
    }
}
```

8.3 Directed case

```
namespace hamil {
    template <typename T> bool chkmax(T &x,T y){return
     x<y?x=y,true:false;}
    template <typename T> bool chkmin(T &x,T y){return
     x>y?x=y,true:false;}
    #define vi vector<int>
    #define pb push_back
    #define mp make_pair
    #define pi pair<int, int>
    #define fi first
    #define se second
    #define ll long long
    using namespace LCT;
    vi out, in;
    vi work(int n, vector<pi> eg, ll mx_ch = -1) {
        // mx_ch : max number of adding/replacing
    default is (n + 100) * (n + 50)
        // n : number of vertices. 1-indexed.
        // eg: vector<pair<int, int> > storing all the
     edges.
        // return a vector<int> consists of all
    indices of vertices on the path. return empty list
     if failed to find one.
        out.resize(n + 1), in.resize(n + 1);
        LCT::init(n);
        for (int i = 0; i <= n; i++) in[i] = out[i] =
    0;
        if (mx_ch == -1) mx_ch = 1ll * (n + 100) * (n
    + 50); //default
        vector<vi> from(n + 1), to(n + 1);
        for (auto v : eg)
            from[v.fi].pb(v.se),
            to[v.se].pb(v.fi);
        unordered_set<int> canin, canout;
        for (int i = 1; i <= n; i++)
            canin.insert(i),
            canout.insert(i);
        mt19937 x(chrono::steady_clock::now().
    time_since_epoch().count());
        int tot = 0;
        while (mx_ch >= 0) {
        //    cout << tot << ' ' << mx_ch << endl;
            vector<pi> eg;
            for (auto v : canout)
                for (auto s : from[v])
                    if (in[s] == 0) {
                        assert(canin.count(s));
                        continue;
                    }
                    else eg.pb(mp(v, s));
            for (auto v : canin)
                for (auto s : to[v])
                    eg.pb(mp(s, v));
            shuffle(eg.begin(), eg.end(), x);
            if (eg.size() == 0) break;
            for (auto v : eg) {
                mx_ch--;
                if (in[v.se] && out[v.fi]) continue;
                if (LCT::fdr(v.fi) == LCT::fdr(v.se))
    continue;
                if (in[v.se] || out[v.fi])
                    if (x() & 1) continue;
                if (!in[v.se] && !out[v.fi])
                    tot++;
                if (in[v.se]) {
                    LCT::cut(in[v.se], v.se);
                    canin.insert(v.se);
                    canout.insert(in[v.se]);
                    out[in[v.se]] = 0;
                    in[v.se] = 0;
```

```
                }
                if (out[v.fi]) {
                    LCT::cut(v.fi, out[v.fi]);
                    canin.insert(out[v.fi]);
                    canout.insert(v.fi);
                    in[out[v.fi]] = 0;
                    out[v.fi] = 0;
                }
                LCT::link(v.fi, v.se);
                canin.erase(v.se);
                canout.erase(v.fi);
                in[v.se] = v.fi;
                out[v.fi] = v.se;
            }
            if (tot == n - 1) {
                vi cur;
                for (int i = 1; i <= n; i++)
                    if (!in[i]) {
                        int pl = i;
                        while (pl) {
                            cur.pb(pl),
                            pl = out[pl];
                        }
                        break;
                    }
                return cur;
            }
        }
        //failed to find a path
        return vi();
    }
}
```

9 Геома

9.1 Примитивы

```
struct Point {
    int x, y;
    Point(){}
    Point (int x_, int y_) {
        x = x_; y = y_;
    }
    Point operator + (Point p) {
        return Point(x+p.x,y+p.y);
    }
    Point operator - (Point p) {
        return Point(x - p.x, y - p.y);
    }
    int operator * (Point p) {
        return x * p.y - y * p.x;
    }
    int operator % (Point p) {
        return x * p.x + y * p.y;
    }
    bool operator < (Point v) {
        return (*this) * v > 0;
    }
    bool operator > (Point v) {
        return v < (*this);
    };
    bool operator <= (Point v) {
        return (*this) * v >= 0;
    }
};
bool line(Point a, Point b, Point c) {
    return (b-a)*(c-b)==0;
}
bool ord(Point a, Point p, Point b) {
    return (p - a)%(p - b)<0;
}

int hp(Point a) {
    if (a.y == 0) return a.x >= 0;
    return a.y > 0;
}

bool comp(Point a, Point b) {
    if (hp(a) != hp(b)) return hp(a) < hp(b);
    return a.x * b.y - a.y * b.x > 0;
}
```

9.2 Выпуклая оболочка

```
using pt = pair<int, int>;
#define x first
#define y second

int cross(pt p, pt q) {
    return p.x * q.y - p.y * q.x;
}
int scalar(pt p, pt q) {
    return p.x * q.x + p.y * q.y;
}
pt operator-(pt a, pt b) { return {a.x - b.x, a.y - b.
    y}; }
vector<pt> convex(vector<pt> a) {
    sort(all(a));
    if (a.size() == 2 && a[0] == a[1]) return {a[0]};
    if (a.size() <= 1) return a;
    vector<pt> h;
    for (int t = 0; t < 2; ++t) {
        int sz = h.size() - t;
        for (auto p: a) {
            while (h.size() >= sz + 2 && cross(p - h.
    end()[-1], h.end()[-2] - h.end()[-1]) <= 0) h.
    pop_back();
            h.push_back(p);
        }
        reverse(all(a));
    }
    return h; // h is circular: h.front() == h.back()
}
```

9.3 Точка внутри многоугольника

```
    auto inT = [&] (Point a, Point b, Point c, Point p
    ) {
        a = a-p; b = b-p; c = c-p;
        return abs(a*b)+abs(b*c)+abs(c*a) == abs(a*b+b
    *c+c*a);
    };
    auto inP = [&] (Point p) { //a must be in
    counterclockwise order!
        int l = 1, r = n - 1;
        while (l < r - 1) {
            int m = (l + r) / 2;
            if ((a[m] - a[0]) < (p - a[0])) {
                l = m;
            }
            else {
                r = m;
            }
        }
        return inT(a[l], a[0], a[r], p);
    };
```

9.4 Касательные

```
    auto max = [&] (auto cmp) {
        int k = 0;
        for (int lg = 18; lg >= 0; --lg) {
            int i = k + (1 << lg), j = k - (1 << lg);
            i = (i % n + n) % n;
            j = (j % n + n) % n;
            array<int, 3> ind{i, j, k};
            sort(all(ind), cmp);
            k = ind[2];
        }
        return k;
    };
    auto uppert = [&](Point p) { //last vertex in
    counterclockwise order about p
        auto cmp = [&] (int i, int j) {return (a[i] -
    p) < (a[j] - p); };
        return max(cmp);
    };
    auto lowert = [&](Point p) { //first vertex in
    counterclockwise order about p
        auto cmp = [&] (int i, int j) {return (a[i] -
    p) > (a[j] - p); };
```

```
        return max(cmp);
    };
    auto uppertinf = [&](Point p) { //upper tangent
    line parallel to vector p
        swap(p.x, p.y);
        p.x = -p.x;
        auto cmp = [&] (int i, int j) { return a[i] %
    p < a[j] % p; };
        return max(cmp);
    };
    auto lowertinf = [&](Point p) { //lower tangent
    line parallel to vector p
        swap(p.x, p.y);
        p.x = -p.x;
        auto cmp = [&] (int i, int j) { return a[i] %
    p > a[j] % p; };
        return max(cmp);
    };
```

10 Цепные дроби

https://cp-algorithms.com/algebra/continued-fractions.html

10.1 Поиск нижней огибающей, сумма и минимум по модулю

```
int floor(int a, int b) {
  return a / b - ((a ^ b) < 0 && a % b);
}
vector<int> decompose(int p, int q) {
  vector<int> f;
  while (q != 0) {
    f.push_back(floor(p, q));
    p -= q * f.back();
    swap(p, q);
  }
  return f;
}

using matrix = array<int, 4>;

matrix operator*(matrix a, matrix b) {
  matrix c{0,0,0,0};
  for (int i = 0; i < 2; ++i) {
    for (int j = 0; j < 2; ++j) {
      for (int k = 0; k < 2; ++k) {
        c[2 * i + k] += a[2 * i + j] * b[2 * j + k];
      }
    }
  }
  return c;
}

#define x first
#define y second

// computes lower convex hull for 0 <= x <= N, 0 <= y
    <= (ax + b) / c
vector<pair<int, int>> lower_convex_hull(int a, int b,
     int c, int n) {
  matrix m = {1, 0, 0, 1};
  auto f = decompose(a, c);
  vector<pair<int, int>> conv{{1, 0}, {0, 1}};
  for (int x : f) {
    m = m * matrix{x, 1, 1, 0};
    conv.emplace_back(m[2], m[0]);
    if (m[2] > n) break; // there should be one (if
    any) with .x > n
  }
  auto diff = [&](int x, int y) {
    return c * y - a * x;
  };
  int x = 0, y = b / c;
  vector<pair<int, int>> res{{x, y}};
  int i;
  for (i = 2; i + 1 < conv.size(); i += 2) {
    while (diff(x + conv[i + 1].x, y + conv[i + 1].y)
    <= b) {
      int t = 1 + (diff(x + conv[i - 1].x, y + conv[i
    - 1].y) - b - 1) / abs(diff(conv[i].x, conv[i].y))
    ;
      auto [dx, dy] = tuple{conv[i - 1].x + t * conv[i
    ].x, conv[i - 1].y + t * conv[i].y};
      int k = (n - x) / dx;
      if (k == 0) break;
      if (diff(dx, dy)) k = min(k, (b - diff(x, y)) /
    diff(dx, dy));
      x += k * dx, y += k * dy;
      res.push_back({x, y});
    }
  }
  if (i >= conv.size()) i -= 2;
  for (; i > 0; i -= 2) {
    auto [dx1, dy1] = conv[i];
    if (x + dx1 > n) continue;
    x += dx1, y += dy1;
    if (i + 1 < conv.size()) {
      auto [dx2, dy2] = conv[i + 1];
      int k = (n - x) / dx2;
      x += k * dx2;
      y += k * dy2;
    }
    res.emplace_back(x, y);
    int k = (n - x) / dx1;
    if (k == 0) continue;
    x += k * dx1;
    y += k * dy1;
    res.emplace_back(x, y);
  }
  return res;
}

// number of (x, y) under pq line such that p.x <= x <
     q.x && 0 < y
int area(auto p, auto q) {
  int integers = gcd(q.x - p.x, q.y - p.y);
  return ((p.y + q.y - 1) * (q.x - p.x + 1) + integers
     + 1) / 2 - q.y;
}

// sum of (ax + b) / c for 0 <= x < n
int get_area(int a, int b, int c, int n) { // SUM (ax
    + b) / c for 0 <= x <= n
  auto ch = lower_convex_hull(a, b, c, n + 1);
  int sum = 0;
  for (int i = 0; i + 1 < ch.size(); ++i) {
    sum += area(ch[i], ch[i + 1]);
  }
  return sum;
}

// min of (ax + b) % c for 0 <= x <= n
int get_min(int a, int b, int c, int n) {
  auto ch = lower_convex_hull(a, b, c, n);
  // in fact, here we need only the last point of the
     first half of the algo (that is going up)
  int mn = c;
  for (auto [x, y] : ch) mn = min(mn, (a * x + b) % c)
    ;
  return mn;
}
```

10.2 Простая рекурсия

Число точек $(x, y) : 0 \leqslant x < n, 0 < y \leqslant (kx + b)/d$. То есть $\sum_{x=0}^{n-1} \lfloor \frac{kx+b}{d} \rfloor$.

```
int cnt (int n, int k, int b, int d)
{
    if (k == 0) return (b / d) * n;
    if (k >= d || b >= d) {
        return (k / d) * n * (n - 1) / 2 + (b / d) * n
     + cnt(n, k % d, b % d, d);
    }
    return cnt((k * n + b) / d, d, (k * n + b) % d, k)
    ;
}
```

11 Разное

11.1 Компараторы

```
bool cmp1(int x, int y) { return x > y; }

struct cmp2{
    bool operator()(int x, int y) const { return x > y
    ; }
};

int32_t main() {
    set<int, decltype(cmp1)*> s1({1, 2, 3}, cmp1);
    for (int x : s1) cout << x << ' '; cout << '\n';
    set<int, cmp2> s2({4, 5, 6});
    for (int x : s2) cout << x << ' '; cout << '\n';
    auto cmp3 = [&](int x, int y) { return x > y; };
    set<int, decltype(cmp3)> s3({7, 8, 9}, cmp3); //
    second cmp3 could be omitted if cmp3 = [](...) {
    ... }
    for (int x : s3) cout << x << ' '; cout << '\n';

    vector<int> v{3, 2, 1};
    cout << lower_bound(all(v), 2, cmp1) - v.begin()
    << '\n';
    cout << lower_bound(all(v), 2, cmp2()) - v.begin()
     << '\n';
    cout << lower_bound(all(v), 2, cmp3) - v.begin()
    << '\n';
}
```

11.2 Трюки от Сергея Копелиовича

11.2.1 Быстрый ввод

https://acm.math.spbu.ru/~sk1/algo/input-output/fread_write.cpp.html

```
const int buf_size = 4096;

int getChar() {
    static char buf[buf_size];
    static int len = 0, pos = 0;
    if (pos == len)
        pos = 0, len = fread(buf, 1, buf_size, stdin);
    if (pos == len)
        return -1;
    return buf[pos++];
}

int readChar() {
    while (1) {
        int c = getChar();
        if (c > 32) return c;
    }
}

int readInt() {
    int s = 1, c = readChar(), x = 0;
    if (c == '-')
        s = -1, c = getChar();
    while (isdigit(c))
        x = x * 10 + c - '0', c = getChar();
    return s * x;
}
```

https://acm.math.spbu.ru/~sk1/algo/memory.cpp.html

11.2.2 Быстрый аллокатор

```
const int MAX_MEM = 1e8;
int mpos = 0;
char mem[MAX_MEM];
inline void * operator new (size_t n) {
  assert((mpos += n) <= MAX_MEM);
  return (void *)(mem + mpos - n);
}
void operator delete (void *) noexcept { } // must
    have!
void operator delete (void *, size_t) noexcept { } //
    must have!
```

11.3 Флаги компияции

```
-DLOCAL -Wall -Wextra -pedantic -Wshadow -Wformat=2
-Wfloat-equal -Wconversion -Wlogical-op -Wshift-
overflow=2 -Wduplicated-cond -Wcast-qual -Wcast-
align -D_GLIBCXX_DEBUG -D_GLIBCXX_DEBUG_PEDANTIC
-D_FORTIFY_SOURCE=2 -fsanitize=address -
fsanitize=undefined -fno-sanitize-recover -fstack-
protector -std=c++2a
```

11.3.1 Сеточка в vim

https://codeforces.com/blog/entry/122540

```
i|<esc>25A   |<esc>
o+<esc>25A---+<esc>
Vky35Pdd
```

11.4 Что сделать на пробном туре

- Убедиться, что работают все IDE. Разобраться, как настраивать в них LOCAL.
- В системе ML — это ML или RE?
- Максимальный размер файла
- Можно посмотреть на время работы серверов позапускав Флойда — Варшалла
- Посмотреть, насколько быстр быстрый ввод