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Теория чисел

1.1 KTO

```
1 int gcd(int a, int b, int &x, int &y) {
    if (b==0) { x = 1; y = 0; return a; }
    int d = gcd(b,a%b,y,x);
   y - = a / b * x;
    return d;
6 }
7 int inv(int r, int m) {
    int x, y;
     gcd(r,m,x,y);
    return (x+m) %m;
11 }
12 int crt(int r, int n, int c, int m) { return r + ((
       c - r) % m + m) * inv(n, m) % m * n; }
  1.2 Алгоритм Миллера — Рабина
1 __int128 one=1;
2 int po(int a, int b, int p)
3 {
4
     int res=1;
     while(b) {if(b & 1) {res=(res*one*a)%p;--b;} else
        {a=(a*one*a)%p;b>>=1;}} return res;
6 }
7 bool chprime(int n) //miller-rabin
8 {
9
     if(n==2) return true;
10
     if(n<=1 || n%2==0) return false;</pre>
     int h=n-1; int d=0; while (h\%2==0) \{h/=2; ++d; \}
     for(int a:{2, 3, 5, 7, 11, 13, 17, 19, 23, 29,
      31, 37})
13
       {
14
      if(a==n) return true;
       int u=po(a,h,n);bool ok=0;
16
       if(u%n==1) continue;
       for(int c=0;c<d;++c)</pre>
17
18
19
         if ((u+1) %n==0) {ok=1;break;}
20
         u=(u*one*u)%n;
21
22
       if(!ok) return false;
23
24
     return true;
25 }
```

1.3 Алгоритм Берлекэмпа — Месси

https://mzhang2021.github.io/cp-blog/berlekamp-massey/

```
1 template < typename T>
2 vector<T> berlekampMassey(const vector<T> &s) {
    int n = s.size(), l = 0, m = 1;
3
     vector < T > b(n), c(n);
     T ld = b[0] = c[0] = 1;
     for (int i=0; i<n; i++, m++) {</pre>
6
       T d = s[i];
       for (int j=1; j<=1; j++)</pre>
9
        d += c[j] * s[i-j];
10
       if (d == 0) continue;
       vector<T> temp = c;
11
       T coef = d / ld;
       for (int j=m; j < n; j ++) c[j] -= coef * b[j-m];
14
       if (2 * 1 <= i) {</pre>
15
         1 = i + 1 - 1;
         b = temp;
16
         ld = d;
17
         m = 0;
19
       }
     }
     c.resize(1 + 1);
22
     c.erase(c.begin());
23
     for (T &x : c)
24
      x = -x;
25
     return c;
26 }
```

2 Графы

2.1 SCC и 2-SAT

```
Алгоритм ищет сильносвязные компоненты в графе g, если есть путь i \to j, то scc[i] \le scc[j]
В случае 2-S d\mathcal{T} рёбра i \Rightarrow i и (i \oplus 1) \Rightarrow (i \oplus 1) должны быть
```

В случае 2- \mathcal{SAT} рёбра $i\Rightarrow j$ и $(j\oplus 1)\Rightarrow (i\oplus 1)$ должны быть добавлены одновременно.

```
1 vector \langle int \rangle g(2 * n);
2 vector < vector < int >> r(g.size());
3 for (int i = 0; i < g.size(); ++i) {
    for (int j : g[i]) r[j].push_back(i);
5 }
6 vector < int > used(g.size()), tout(g.size());
7 int time = 0;
8 auto dfs = [&](auto dfs, int cur) -> void {
    if (used[cur]) return;
    used[cur] = 1;
    for (int nxt : g[cur]) {
11
12
      dfs(dfs, nxt);
13
14
    // used[cur] = 2;
15
    tout[cur] = time++;
16 };
17 for (int i = 0; i < g.size(); ++i) if (!used[i])
       dfs(dfs, i);
18 vector<int> ind(g.size());
19 iota(ind.begin(), ind.end(), 0);
20 sort(all(ind), [&](int i, int j){return tout[i] >
      tout[j];});
21 vector < int > scc(g.size(), -1);
22 auto go = [&](auto go, int cur, int color) -> void
     if (scc[cur] != -1) return;
24
    scc[cur] = color;
    for (int nxt : r[cur]) {
      go(go, nxt, color);
27
    }
28 };
29 \text{ int color} = 0;
30 for (int i : ind) {
    if (scc[i] == -1) go(go, i, color++);
33 for (int i = 0; i < g.size() / 2; ++i) {
    if (scc[2 * i] == scc[2 * i + 1]) "IMPOSSIBLE"
    if (scc[2 * i] < scc[2 * i + 1]) {</pre>
35
36
      // !i => i, assign i = true
37
    } else {
      // i => !i, assign i = false
38
39
    }
40 }
```

2.2 Эйлеров цикл

```
1 vector < vector < pair < int , int >>> g(n); // pair { nxt ,
      idx }
2 vector<pair<int, int>> e(p.size());
3 // build graph
4 vector < int > in(n), out(n);
5 for (auto [u, v] : e) in[v]++, out[u]++;
6 vector<int> used(m), it(n), cycle;
7 auto dfs = [&](auto dfs, int cur) -> void {
    while (true) {
9
      while (it[cur] < g[cur].size() && used[g[cur][
       it[cur]].second]) it[cur]++;
      if (it[cur] == g[cur].size()) return;
      auto [nxt, idx] = g[cur][it[cur]];
11
       used[idx] = true;
      dfs(dfs, nxt);
13
14
       cycle.push_back(idx);
15
16 };
17 \text{ int } cnt = 0, odd = -1;
18 for (int i = 0; i < n; ++i){
    if (out[i] && odd == -1) odd = i;
19
    if (in[i] != out[i]) {
      if (in[i] + 1 == out[i]) odd = i;
21
22
       if (abs(in[i] - out[i]) > 1) return {}; // must
```

```
23
       cnt++:
24
25 }
26 if (cnt != 0 && cnt != 2) return {}; // must hold
27 // for undirected find odd vertex (and count that #
       of odd is 0 or 2)
28 dfs(dfs, odd);
29 reverse(cycle.begin(), cycle.end());
30 if (cycle.size() != m) return {};
   2.3 Компоненты вершинной двусвязности
 1 int n, m;
 2 \text{ cin } >> \text{ n } >> \text{ m};
 3 vector \langle vector \langle int \rangle \rangle g(n + 1);
int u, v, c; cin >> u >> v >> c;c--;
     col[{u,v}]=col[{v,u}]=c;
     g[u].push_back(v);
 Q
     g[v].push_back(u);
10 }
11 vector <int> used(n + 1);
12 vector <int> newCompWithoutParent(n + 1), h(n + 1),
       up(n + 1);
13 auto findCutPoints = [&] (auto self, int u, int p)
       -> void {
     used[u] = 1;
     up[u] = h[u];
15
     for (int v : g[u]) {
       if (!used[v]) {
18
         h[v] = h[u] + 1;
19
         self(self, v, u);
         up[u] = min(up[u], up[v]);
20
         if (up[v] >= h[u]) {
22
           newCompWithoutParent[v] = 1;
23
24
       }
       else {
26
         up[u] = min(up[u], h[v]);
27
28
    }
29 };
30 for (int u = 1; u <= n; ++u) {
31
    if (!used[u]) {
32
       findCutPoints(findCutPoints, u, u);
33
34 }
35 int ptr = 0;
36 vector <map <int, int> > colors(m);
37 auto markComponents = [&] (auto self, int u, int
       cur) -> void {
38
     used[u] = 1;
     for (int v : g[u]) {
       if (!used[v]) {
40
         if (newCompWithoutParent[v]) {
41
          ptr++;
43
           self(self, v, ptr - 1);
         else
46
           self(self, v, cur);
         }
       else if (h[v] < h[u]) {</pre>
49
         comp[{u,v}] = comp[{v,u}] = cur;
         int c = col[{u,v}];
         colors[cur][u] |= 1 << c;
         colors[cur][v] |= 1 << c;
54
    }
56 };
57 used.assign(n + 1, 0);
58 for (int u = 1; u <= n; ++u) {
    if (!used[u]) {
       markComponents (markComponents, u, -1);
61
62 }
|63 \text{ for (int comp = 0; comp < m; ++comp) }
```

vector <int> cnt(4);

```
Структуры данных
65
     int tot = 0;
     for (auto [u, mask] : colors[comp]) {
66
       tot |= mask;
                                                                   4.1 Дерево Фенвика
67
68
       cnt[bp(mask)]++;
69
                                                                 1 int fe[maxn]; /// fenwick tree
70
    if (bp(tot)<3) {
                                                                 2 void pl(int pos,int val) {while(pos<maxn) {fe[pos</pre>
71
       continue;
                                                                        ]+=val;pos|=(pos+1);}}
72
                                                                 3 int get(int pos) {int ans=0; while(pos>=0) {ans+=fe[
     if (cnt[2] || cnt[3]>2) {
73
                                                                        pos];pos&=(pos+1);--pos;} return ans;} /// [0,
74
       cout << "Yes" << endl;</pre>
                                                                        pos] - vkluchitelno!!!
75
       return:
                                                                 4 int get(int 1,int r) {return get(r-1)-get(1-1);} //
     }
76
                                                                        / summa na [l,r)
77 }
78 cout << "No" << endl;
                                                                   4.2 Дерево отрезков
                                                                 1 template < typename Data, typename Mod, typename
UniteData, typename UniteMod, typename Apply>
      xor, and, or-свёртки
                                                                   struct MassSegmentTree {
                                                                     int h, n;
                                                                     Data zd;
1 const int p = 998244353;
                                                                     Mod zm:
2 vector<int> band(vector<int> a, vector<int> b)
                                                                     vector < Data > data;
3 {
                                                                     vector < Mod > mod;
4
     int n=0; while((1<<n)<a.size()) ++n;</pre>
     a.resize(1<<n);b.resize(1<<n);
                                                                     UniteData ud; // Data (Data, Data)
                                                                     UniteMod um; // Mod (Mod, Mod);
     for(int i=0;i<n;++i) for(int mask=0;mask<(1<<n)</pre>
6
       ; ++ mask) if(mask & (1<<i)) {a[mask-(1<<i)]+=a[}
                                                                      Apply a; // Data (Data, Mod, int); last argument
       mask]; a [mask - (1 < < i)] % = p;}
                                                                       is the length of current segment (could be used
     \label{for:mask=0} \mbox{for(int i=0;i<n;++i)} \ \ \mbox{for(int mask=0;mask<(1<<n)}
                                                                         for range += and sum counting, for instance)
       ; ++ mask) if (mask & (1<<i)) {b[mask-(1<<i)]+=b[
                                                                12
       mask];b[mask-(1<<i)]%=p;}
                                                                      template < typename I>
8
     vector < int > c(1 << n,0);
                                                                14
                                                                     {\tt MassSegmentTree(int\ sz,\ Data\ zd,\ Mod\ zm,}
                                                                       UniteData ud, UniteMod um, Apply a, I init) : h (__lg(sz > 1 ? sz - 1 : 1) + 1), n(1 << h), zm(
9
     for(int mask=0; mask<(1<<n); ++ mask) {c[mask]=a[</pre>
       mask]*b[mask];c[mask]%=p;}
                                                                        zm), zd(zd), data(2 * n, zd), mod(n, zm), ud(ud
     for(int i=0;i<n;++i) for(int mask=0;mask<(1<<n)</pre>
       ; ++ mask) if(!(mask & (1<<i))) {c[mask]-=c[mask]
                                                                        ), um(um), a(a) {
                                                                        for (int i = 0; i < sz; ++i) data[i + n] = init</pre>
       +(1<<i)]:c[mask]%=p:}
11
                                                                        (i);
     return c;
                                                                        for (int i = n - 1; i > 0; --i) data[i] = ud(
13 vector<int> bor(vector<int> a, vector<int> b)
                                                                        data[2 * i], data[2 * i + 1]);
14 {
                                                                 17
                                                                     }
     int n=0; while((1<<n)<a.size()) ++n;</pre>
15
                                                                 18
16
     a.resize(1<<n);b.resize(1<<n);
                                                                19
                                                                     MassSegmentTree(int sz, Data zd, Mod zm,
                                                                        UniteData ud, UniteMod um, Apply a) : h(__lg(sz
17
     for(int i=0;i<n;++i) for(int mask=0;mask<(1<<n)</pre>
                                                                        > 1 ? sz - 1 : 1) + 1), n(1 << h), zm(zm), zd(
       ; ++ mask) if(!(mask & (1<<i))) {a[mask+(1<<i)]+=
       a[mask]; a[mask+(1<<ii)]%=p;}
                                                                        zd), data(2 * n, zd), mod(n, zm), ud(ud), um(um
     for(int i=0;i<n;++i) for(int mask=0;mask<(1<<n)</pre>
                                                                        ), a(a) {}
       ; ++ mask) if (!(mask & (1<<i))) {b[mask+(1<<i)]+=
                                                                20
       b[mask];b[mask+(1<<ii)]%=p;}
                                                                     void push(int i) {
                                                                       if (mod[i] == zm) return;
     vector < int > c(1 << n,0);
20
     for(int mask=0; mask<(1<<n); ++mask) {c[mask]=a[</pre>
                                                                        apply(2 * i, mod[i]);
                                                                        apply(2 * i + 1, mod[i]);
       mask] * b [mask]; c [mask] % = p;}
                                                                        mod[i] = zm;
                                                                25
     for(int i=0;i<n;++i) for(int mask=0;mask<(1<<n)</pre>
                                                                     }
       ; ++ mask) if (mask & (1<<i)) {c[mask] -= c[mask]
                                                                26
       -(1<<i)];c[mask]%=p;}
                                                                28
                                                                     // is used only for apply
22
     return c;
23 }
                                                                29
                                                                     int length(int i) { return 1 << (h - __lg(i)); }</pre>
24 vector < int > bxor (vector < int > a, vector < int > b)
                                                                30
                                                                31
25 {
                                                                     // is used only for descent
26
     assert(p\%2==1); int inv2=(p+1)/2;
                                                                     int left(int i) {
27
     int n=0; while((1<<n)<a.size()) ++n;</pre>
                                                                33
                                                                       int lvl = __lg(i);
                                                                        return (i & ((1 << lvl) - 1)) * (1 << (h - lvl)
28
     a.resize(1<<n);b.resize(1<<n);
                                                                34
     for(int i=0;i<n;++i) for(int mask=0;mask<(1<<n)</pre>
                                                                       );
                                                                35
       ;++mask) if(!(mask & (1<<i))) {int u=a[mask], v=
       a[mask+(1<<i)]; a[mask+(1<<i)]=(u+v)%p; a[mask]=(
                                                                37
                                                                     // is used only for descent
30
     for(int i=0;i<n;++i) for(int mask=0;mask<(1<<n)</pre>
                                                                     int right(int i) {
                                                                38
       ; ++ mask) if(!(mask & (1<<i))) {int u=b[mask], v=
                                                                39
                                                                        int lvl = __lg(i);
       b[mask+(1<<i)];b[mask+(1<<i)]=(u+v)%p;b[mask]=(
                                                                        return ((i & ((1 << lvl) - 1)) + 1) * (1 << (h
                                                                40
       u-v)%p;}
                                                                        - lvl));
     vector < int > c(1 << n, 0);</pre>
     for(int mask=0; mask<(1<<n); ++mask) {c[mask]=a[</pre>
32
       mask] * b [mask]; c [mask] % = p;}
                                                                     template < typename S>
     for(int i=0;i<n;++i) for(int mask=0;mask<(1<<n)</pre>
                                                                 44
                                                                     void apply(int i, S x) {
       ;++mask) if(!(mask & (1<<i))) {int u=c[mask], v=
                                                                        data[i] = a(data[i], x, length(i));
       c[mask+(1<<i)];c[mask+(1<<i)]=((v-u)*inv2)%p;c[
                                                                        if (i < n) mod[i] = um(mod[i], x);</pre>
       mask]=((u+v)*inv2)%p;}
                                                                 47
34
     return c;
                                                                48
35 }
                                                                      void update(int i) {
```

3

```
if (mod[i] != zm) return;
                                                             26
50
                                                                      Data with1;
 51
        data[i] = ud(data[2 * i], data[2 * i + 1]);
                                                                      with1 = ud(data[--r], cur);
 52
                                                             28
                                                                      if (ok(with1, left(r))) {
53
                                                                        cur = with1;
                                                             30
 54
      template < typename S>
                                                                      } else {
 55
      void update(int 1, int r, S x) { // [1; r)
                                                                        while (r < n) {
 56
       1 += n, r += n;
                                                             32
                                                                          push(r);
       for (int shift = h; shift > 0; --shift) {
                                                             33
                                                                          Data with 2;
 58
         push(l >> shift);
                                                             34
                                                                          with2 = ud(data[2 * r + 1], cur);
 59
         push((r - 1) >> shift);
                                                                          if (ok(with2, left(2 * r))) {
60
                                                             36
                                                                            cur = with2;
                                                                            r = 2 * r;
61
        for (int lf = 1, rg = r; lf < rg; lf /= 2, rg</pre>
                                                             37
                                                                          } else {
        /= 2) {
                                                             39
                                                                            r = 2 * r + 1;
62
         if (lf & 1) apply(lf++, x);
63
          if (rg & 1) apply(--rg, x);
                                                             40
                                                                          }
 64
                                                             41
65
        for (int shift = 1; shift <= h; ++shift) {</pre>
                                                             42
                                                                        return r - n + 1;
66
          update(1 >> shift);
                                                             43
67
          update((r - 1) >> shift);
                                                             44
                                                                    }
                                                                    return 0;
68
                                                             45
 69
                                                             46
                                                                  }
                                                             47 };
70
 71
     Data get(int 1, int r) { // [1; r)
       1 += n, r += n;
       for (int shift = h; shift > 0; --shift) {
                                                                4.2.1 Примеры использования
 73
 74
         push(1 >> shift);
                                                                  • Взятие максимума и прибавление константы
 75
          push((r - 1) >> shift);
 76
                                                                 1 MassSegmentTree segtree(n, OLL, OLL,
                                                                 2 [](int x, int y) { return max(x, y); },
 77
       Data leftRes = zd, rightRes = zd;
       for (; 1 < r; 1 /= 2, r /= 2) {
 78
                                                                 3 [](int x, int y) { return x + y; },
                                                                 4 [](int x, int y, int len) { return x + y; });
 79
         if (1 & 1) leftRes = ud(leftRes, data[1++]);
          if (r & 1) rightRes = ud(data[--r], rightRes)
                                                                  • Взятие суммы и прибавление константы
 81
       }
 82
       return ud(leftRes, rightRes);
                                                                 1 MassSegmentTree segtree(n, OLL, OLL,
83
                                                                 2 [](int x, int y) { return x + y; },
 84
                                                                 3 [](int x, int y) { return x + y; },
     // l \in [0; n) && ok(get(1, 1), 1);
 85
                                                                 4 [](int x, int y, int len) { return x + y * len;
86
      // returns last r: ok(get(1, r), r)
      template < typename C>
 88
      int lastTrue(int 1, C ok) {
                                                                  • Взятие суммы и присовение
89
       1 += n;
 90
       for (int shift = h; shift > 0; --shift) push(1
                                                                 1 MassSegmentTree segtree(n, OLL, -1LL,
       >> shift);
                                                                 2 [](int x, int y) { return x + y; },
91
        Data cur = zd;
                                                                 3 [](int x, int y) { return y; },
92
        do {
                                                                 4 [](int x, int y, int len) { return y * len; });
93
         1 >>= __builtin_ctz(1);
          Data with1;
95
          with1 = ud(cur, data[1]);
                                                                4.3 Ordered set
96
          if (ok(with1, right(1))) {
            cur = with1;
                                                              1 #include <ext/pb_ds/assoc_container.hpp>
98
            ++1;
                                                              2 #include <ext/pb_ds/tree_policy.hpp>
99
          } else {
           while (1 < n) {
100
                                                              4 using namespace __gnu_pbds;
101
              push(1);
                                                              5 using namespace std;
              Data with2;
103
              with2 = ud(cur, data[2 * 1]);
                                                              7 using ordered_set = tree<int, null_type, less<>,
104
              if (ok(with2, right(2 * 1))) {
                                                                    rb_tree_tag, tree_order_statistics_node_update
105
                cur = with2;
                1 = 2 * 1 + 1;
106
107
              } else {
108
                1 = 2 * 1;
                                                                4.4 Convex hull trick
109
              }
           }
110
                                                              1 int div_up(int a, int b) { return a/b+((a^b)>0&&a%b
111
           return 1 - n;
                                                                    ); } // divide a by b rounded up
         }
112
                                                                const int LQ = ..., RQ = ...; //leftmost query,
       } while (1 & (1 - 1));
113
                                                                   rightmost query
114
       return n;
                                                              3 int in(ii L, int x) {
115
                                                                    return L.x * x + L.y;
116
                                                              5 }
117
     // r \in [0; n) && ok(get(r, r), r);
                                                              6 struct Hull {
     // returns first 1: ok(get(1, r), 1)
                                                              7 vector <pair <int, int> > lines;
119
     template < typename C>
                                                              8 vector <int> borders;
120
      int firstTrue(int r, C ok) {
                                                              9 void push(ii L) {
121
       r += n;
                                                                    while (lines.size() && in(L,borders.back()) <</pre>
       for (int shift = h; shift > 0; --shift) push((r
                                                                    in(lines.back(),borders.back())) {
         - 1) >> shift);
                                                                        lines.pop_back();
123
       Data cur = zd;
                                                             12
                                                                        borders.pop_back();
124
       while (r & (r - 1)) {
         r >>= __builtin_ctz(r);
                                                                    if (lines.empty()) {
                                                            4
```

```
15
           lines = \{L\};
16
           borders = {LQ};
17
18
       else if (lines.back().x > L.x) {
19
           int x = div_up(L.y - lines.back().y, lines.
       back().x - L.x);
          if (x <= RQ) {
2.0
21
               lines.app(L);
               borders.app(x);
23
24
       }
25 1
26 Hull (){}
27 Hull (vector <ii> a) {
       auto comp = [&] (ii u, ii v) {
          return u.x > v.x || (u.x == v.x && u.y < v.
       y);
30
       };
       sort(all(a), comp);
31
32
       for (auto L : a) {
33
           push(L);
34
35 }
36 int get(int x) {
       int pos = upper_bound(all(borders), x) -
37
       borders.begin();
38
       assert(pos>0);
39
       pos --;
40
       return in(lines[pos],x);
41 }
42 };
       Центроидная декомпозиция
1 vector < int > sz(n), lvl(n, -1);
2 auto dfs = [&](auto dfs, int cur, int prev) -> int
3
       if (lvl[cur] != -1) return 0;
4
       sz[cur] = 1;
       for (auto [nxt, w] : g[cur]) {
           if (nxt != prev) sz[cur] += dfs(dfs, nxt,
6
```

```
8
       return sz[cur];
9 };
10 auto find = [&](auto find, int cur, int prev, int
       tot) -> int {
11
       int bch = -1, bsz = 0;
       for (auto [nxt, w] : g[cur]) {
12
            if (nxt == prev || lvl[nxt] != -1) continue
13
           if (sz[nxt] > bsz) {
14
15
                bch = nxt;
                bsz = sz[nxt];
16
17
           }
18
19
       if (bsz + bsz <= tot) return cur;</pre>
20
       return find(find, bch, cur, tot);
21 1:
22 \text{ dfs(dfs, 0, 0)};
23 auto c = find(find, 0, 0, sz[0]);
24 vector<pair<int, int>> stack{{c, 0}};
25 int ans = INF;
26 while (!stack.empty()) {
27
       auto [centroid, 1] = stack.back();
28
       stack.pop_back();
29
       lvl[centroid] = 1;
       for (auto [nxt, w] : g[centroid]) {
   if (lvl[nxt] != -1) continue;
30
3.1
           dfs(dfs, nxt, centroid);
32
33
            int new_centroid = find(find, nxt, centroid
       , sz[nxt]);
34
           stack.push_back({new_centroid, lvl[centroid
       ] + 1});
35
36
```

5

5 Строковые алгоритмы

5.1 Префикс-функция

```
1 vector<int> prefix_function(string s) {
    vector < int > p(s.size());
    for (int i = 1; i < s.size(); ++i) {</pre>
3
      p[i] = p[i - 1];
4
       while (p[i] && s[p[i]] != s[i]) p[i] = p[p[i] -
       17:
      p[i] += s[i] == s[p[i]];
    return p;
9 }
  5.2 Z-функция
1 vector \langle int \rangle z_function (string s) { // z[i] - lcp
      of s and s[i:]
   int n = (int) s.length();
3 vector<int> z (n);
   for (int i=1, l=0, r=0; i<n; ++i) {</pre>
    if (i <= r)</pre>
     z[i] = min (r-i+1, z[i-1]);
    while (i+z[i] < n && s[z[i]] == s[i+z[i]])
     ++z[i];
   if (i+z[i]-1 > r)
10
     l = i, r = i+z[i]-1;
   }
   return z:
13 }
   5.3 Алгоритм Манакера
1 vector<int> manacher_odd(const string &s) {
     vector < int > man(s.size(), 0);
    int 1 = 0, r = 0;
4
     int n = s.size();
    for (int i = 1; i < n; i++) {</pre>
      if (i <= r) {</pre>
         man[i] = min(r - i, man[l + r - i]);
9
       while (i + man[i] + 1 < n && i - man[i] - 1 >=
       0 && s[i + man[i] + 1] == s[i - man[i] - 1]) {
        man [i]++:
      if (i + man[i] > r) {
13
         1 = i - man[i];
14
         r = i + man[i];
    }
16
    return man;
18 }
19 // abacaba : (0 1 0 3 0 1 0)
20 // abbaa : (0 0 0 0 0)
22 vector <int> manacher_even(const string &s) {
23
    assert(s.size());
24
     string t;
    for (int i = 0; i + 1 < s.size(); ++i) {</pre>
26
      t += s[i];
       t += '#';
27
28
    }
29
    t += s.back();
    auto odd = manacher_odd(t);
30
31
     vector <int> ans;
32
    for (int i = 1; i < odd.size(); i += 2) {</pre>
33
       ans.push_back((odd[i]+1)/2);
34
    return ans;
35
36 }
37 // abacaba : (0 0 0 0 0 0)
38 // abbaa : (0 2 0 1)
40 auto pal = [&] (int 1, int len) {
41
       if (len & 1) {
           int m = 1 + len/2;
42
           return odd[m] >= len/2;
44
45
       else
46
           int m = 1 + len/2 - 1;
           return even[m] >= len/2;
```

48

return inf;

```
}
49 };
                                                                         }
                                                                         else {
                                                             63
                                                                           return t.getMin(i, j);
   5.4 Суфмассив
                                                             65
                                                                     }
  Переработанный китайский суффмассив
                                                             66 };
 1 const int inf = 1e9;
2 struct rmq {
                                                                     Алгоритм Ахо — Корасик
    int n;
     vector<int> a:
                                                              1 struct node{
     void build(const vector<int> &x) {
                                                                 int next[alpha] = {}, link[alpha] = {};
       assert(x.size() == n);
       for (int i = 0; i < n; ++i) a[n + i] = x[i];</pre>
                                                                   int suf = 0:
                                                                  11 \text{ visited} = 0, \text{ ans} = 0;
       for (int i = n - 1; i > 0; --i) a[i] = min(a[2
8
       * i], a[2 * i + 1]);
                                                                   vector<int> term;
                                                                  node() {}
9
    }
                                                              7 };
10
     rmq(int n) : n(n), a(2 * n, inf) {}
     void put(int i, int x) {
11
                                                              9 vector < node > mem;
12
       a[i + n] = min(a[i + n], x);
                                                              10
13
       for (i = (i + n) / 2; i > 0; i /= 2) {
                                                              11 int get_next(int nd, char c) {
         a[i] = min(a[i * 2], a[i * 2 + 1]);
14
                                                                  if (!mem[nd].next[c - a]) { mem[nd].next[c - a] =
16
    }
                                                                     mem.size(); mem.emplace_back(); }
                                                                   return mem[nd].next[c - a];
     int getMin(int 1, int r) { //[1;r)
17
                                                              14 }
      assert(1 < r);
19
       int res = inf:
                                                              16 void find(string s, vector<string> t) {
20
       for (1 += n, r += n; 1 < r; 1 /= 2, r /= 2) {
                                                                   mem.reserve(1e6 + 100); mem.clear();
21
         if (1 & 1) res = min(res, a[1++]);
                                                                   mem.emplace_back(); mem.emplace_back();
22
         if (r & 1) res = min(res, a[--r]);
                                                                  // 0th element is nullptr, 1st is the root
                                                              19
23
                                                              20
                                                                   int q = t.size();
24
       return res;
                                                              21
                                                                   for (int j = 0; j < q; ++j) {
25
    }
                                                                     int cur = 1;
26 };
27 template <typename T>
                                                              23
                                                                     for (char c : ts[j]) cur = get_next(cur, c);
                                                              24
                                                                     mem[cur].term.push_back(j);
28 struct suar {
                                                              25
29
       vector <int> sa, lcp, rank; rmg t;
       suar (T s, int lim=256) : t((int)s.size() - 1)
                                                              26
                                                                   vector<int> bfs_order;
30
                                                              27
                                                                   queue < int > bfs;
       \{ // \text{ s must be nonempty, } 0 < \text{s[i]} < \text{lim!} 
                                                              28
           int n = (int)s.size() + 1, k = 0, a, b; s.
                                                              29
                                                                       node &root = mem[1];
       app(0);
32
           vector <int> x(s.begin(), s.end()), y(n),
                                                                       root.suf = 1;
       ws(max(n, lim)); rank.resize(n);
                                                              31
                                                                       for (char c = a; c < a + alpha; ++c) {</pre>
                                                                           root.link[c - a] = (root.next[c - a] ?
33
           sa = lcp = y, iota(sa.begin(), sa.end(), 0)
                                                                     root.next[c - a] : 1);
           for (int j = 0, p = 0; p < n; j = max(111,</pre>
34
                                                              34
                                                                       bfs.push(1);
       j * 2), lim = p) {
               p = j, iota(y.begin(), y.end(), n - j);
                                                              36
                                                                   while (!bfs.empty()) {
36
               for (int i = 0; i < n; i++) if (sa[i]</pre>
                                                                     int cur_idx = bfs.front();
       >= j) y[p++] = sa[i] - j;
                                                              38
                                                                     bfs.pop();
37
               fill(ws.begin(), ws.end(), 0);
                                                                     node &cur = mem[cur_idx];
38
                for (int i = 0; i < n; i++) ws[x[i]]++;</pre>
                                                              40
                                                                     bfs_order.push_back(cur_idx);
39
                for (int i = 1; i < lim; i++) ws[i] +=</pre>
                                                                     for (char c = a; c < a + alpha; ++c) {</pre>
       ws[i - 1];
                                                                       int nxt_idx = cur.next[c - a];
                                                              42
40
               for (int i = n; i--; ) sa[--ws[x[y[i
                                                                       if (!nxt_idx) continue;
       ]]]] = y[i];
                                                                       node &nxt = mem[nxt_idx];
41
                swap(x, y), p = 1, x[sa[0]] = 0;
                                                                       nxt.suf = (cur_idx == 1 ? 1 : mem[cur.suf].
               for (int i = 1; i < n; i++) a = sa[i -</pre>
42
                                                                     link[c - a]);
       1], b = sa[i], x[b] = (y[a] == y[b] && y[a + j]
                                                                       for (char c = a; c < a + alpha; ++c) {</pre>
          y[b + j]) ? p - 1 : p++;
                                                                         nxt.link[c - a] = (nxt.next[c - a] ? nxt.
43
                                                                     next[c - a] : mem[nxt.suf].link[c - a]);
           for (int i = 1; i < n; i++) rank[sa[i]] = i</pre>
44
                                                                       bfs.push(nxt_idx);
45
           for (int i = 0, j; i < n - 1; lcp[rank[i</pre>
       ++]]=k)
46
               for (k && k--, j = sa[rank[i] - 1];
                    s[i + k] == s[j + k]; k++);
                                                              52
                                                                   // do something
47
                                                              53 }
           sa.erase(sa.begin()); lcp.erase(lcp.begin()
48
       ); lcp.erase(lcp.begin());
                                                                5.6 Дерево палиндромов
49
           t.build(lcp);
50
           for (auto &e : rank) {
                                                              1 struct palindromic{
               e - - ;
52
                                                                  int n;
53
                                                                   vector < int > p, suf{0, 0}, len{-1, 0};
                                                                  vector < array < int , alpha >> to {{}};
54
       int getLcp(int i, int j) {
55
           i = rank[i]; j = rank[j];
                                                                   int sz = 2;
           if (j < i) {
57
             swap(i, j);
                                                              7
                                                                   palindromic(const string &s) : n(s.size()), p(n +
58
                                                                     1, 1) {
                                                              8
           if (i == j) {
                                                                     suf.reserve(n);
                                                             6
```

```
9
       len.reserve(n);
10
       for (int i = 0; i < n; ++i) {</pre>
        auto check = [&](int 1) { return i > 1 && s[i
11
       ] == s[i - 1 - 1]; };
12
         int par = p[i];
         while (!check(len[par])) par = suf[par];
13
         if (to[par][s[i] - a]) {
14
         p[i + 1] = to[par][s[i] - a];
16
           continue;
         }
17
18
         p[i + 1] = sz++;
         to[par][s[i] - a] = p[i + 1];
19
20
         to.emplace_back();
21
         len.emplace_back(len[par] + 2);
22
         do {
23
          par = suf[par];
         } while (!check(len[par]));
24
         int link = to[par][s[i] - a];
         if (link == p[i + 1]) link = 1;
27
         suf.emplace_back(link);
28
29
    }
30 };
```

6 Потоки

6.1 Алгоритм Диница

```
1 #define pb push_back
2 struct Dinic{
3 struct edge{
    int to, flow, cap;
5 };
7 const static int N = 555; //count of vertices
9 vector<edge> e;
10 vector \langle int \rangle g[N + 7];
11 int dp[N + 7];
12 int ptr[N + 7];
13
14 \text{ void clear()} \{
   for (int i = 0; i < N + 7; i++) g[i].clear();</pre>
15
16
     e.clear();
17 1
18
19 void addEdge(int a, int b, int cap){
   g[a].pb(e.size());
2.1
     e.pb({b, 0, cap});
     g[b].pb(e.size());
     e.pb({a, 0, 0});
24 1
26 int minFlow, start, finish;
28 bool bfs(){
   for (int i = 0; i < N; i++) dp[i] = -1;</pre>
29
30
    dp[start] = 0;
31
    vector < int > st:
32
    int uk = 0;
     st.pb(start);
34
     while(uk < st.size()){</pre>
35
      int v = st[uk++];
       for (int to : g[v]){
        auto ed = e[to];
37
         if (ed.cap - ed.flow >= minFlow && dp[ed.to]
38
       == -1){
39
           dp[ed.to] = dp[v] + 1;
40
            st.pb(ed.to);
41
42
       }
44
     return dp[finish] != -1;
45 }
47 int dfs(int v, int flow){
    if (v == finish) return flow;
49
     for (; ptr[v] < g[v].size(); ptr[v]++){</pre>
50
      int to = g[v][ptr[v]];
       edge ed = e[to];
```

```
52
      if (ed.cap - ed.flow >= minFlow && dp[ed.to] ==
        dp[v] + 1){
        int add = dfs(ed.to, min(flow, ed.cap - ed.
       flow));
        if (add){
          e[to].flow += add;
           e[to ^ 1].flow -= add;
           return add;
58
59
      }
60
     }
     return 0;
62 }
63
64 int dinic(int start, int finish){
     Dinic::start = start;
66
     Dinic::finish = finish:
67
     int flow = 0;
68
     for (minFlow = (1 << 30); minFlow; minFlow >>= 1)
69
       while(bfs()){
70
        for (int i = 0; i < N; i++) ptr[i] = 0;</pre>
71
         while(int now = dfs(start, (int)2e9 + 7))
       flow += now;
73
     }
74
     return flow;
75 }
76 } dinic;
   6.2 Mincost k-flow
   6.2.1 Строим граф
 1 struct edge {
    int next, capacity, cost, flow = 0;
 3
     edge() = default:
 5
     edge(int next, int capacity, int cost) : next(
      next), capacity(capacity), cost(cost) {}
     int rem() const { return capacity - flow; }
10
     int operator+=(int f) { return flow += f; }
11
     int operator -=(int f) { return flow -= f; }
12
13 };
g[from].push_back(e.size());
16
     e.emplace_back(next, capacity, cost);
17
     g[next].push_back(e.size());
18
     e.emplace_back(from, 0, -cost);
19 };
   Если граф ориентированный, то addEdge вызываем один раз. Если
   неориентированный, то два, вот так:
 1 addEdge(u, v, capacity, cost);
 2 addEdge(v, u, capacity, cost);
   6.2.2 Запускаем Форда — Беллмана
 1 vector<11> phi(n, 0);
 2 auto fordBellman = [&](int s, int t) {
     phi.assign(n, 0);
     for (int iter = 0; iter < n; ++iter) {</pre>
       bool changed = false;
       for (int u = 0; u < n; ++u) {
 6
         for (auto index : g[u]) {
           auto edge = e[index];
9
           if (edge.rem() > 0 && phi[edge.next] > phi[
       u] + edge.cost) {
10
             phi[edge.next] = phi[u] + edge.cost;
             changed = true;
11
12
        }
13
14
       if (!changed) break;
```

```
14
16 }
                                                                    }
17 };
                                                              15
                                                                  }
18 fordBellman(s, t);
                                                              16
                                                                  return ans;
                                                              17 };
                                                              18 for (int flow = 0; flow \langle k; ++flow \rangle {
  6.2.3 Ищем кратчайший путь Дейкстрой с потенциалами
                                                                 auto p = findPath(s, t);
                                                                   cout << p.size() << '';</pre>
1 vector<11> dist:
                                                                  for (int x : p) cout << x + 1 << ', ';
cout << '\n';</pre>
2 vector<int> from;
                                                              22
3 vector < bool > cnt;
                                                              23 F
4 auto dijkstra = [&](int s, int t) {
    dist.assign(n, 1e18);
    from.assign(n, -1);
                                                                    FFT & co
     cnt.assign(n, false);
     dist[s] = 0;
                                                                 7.1 NTT & co
9
     set <pair <int, int> > se;
     se.insert({0, s});
10
                                                               1 #define int long long
11
     while ((int)(se.size())) {
                                                               2 using namespace std;
      int cur = se.begin()->y;
12
                                                              3 typedef long long 11;
13
       se.erase(se.begin());
                                                               4 const int p=998244353;
       cnt[cur] = true;
14
                                                               5 int po(int a, int b) {if(b==0) return 1; if(b==1)
       for (int index : g[cur]) {
                                                                     return a; if (b\%2==0) {int u=po(a,b/2); return (u
         auto &edge = e[index];
                                                                     *1LL*u)%p;} else {int u=po(a,b-1);return (a*1LL
         if (edge.rem() == 0) continue;
                                                                     *u)%p;}}
         ll weight = edge.cost + phi[cur] - phi[edge.
                                                               6 int inv(int x) {return po(x,p-2);}
       nextl:
                                                               7 template < int M, int K, int G> struct Fft {
19
         if (dist[edge.next] > dist[cur] + weight) {
                                                                  // 1, 1/4, 1/8, 3/8, 1/16, 5/16, 3/16, 7/16, ...
int g[1 << (K - 1)];
           se.erase({dist[edge.next], edge.next});
20
2.1
           dist[edge.next] = dist[cur] + weight;
                                                                   Fft() : g() { //if tl constexpr...
22
           se.insert({dist[edge.next], edge.next});
                                                                     static_assert(K >= 2, "Fft: K >= 2 must hold");
           from[edge.next] = cur;
                                                                     g[0] = 1;
24
                                                                     g[1 << (K - 2)] = G;
25
      }
                                                                     for (int 1 = 1 << (K - 2); 1 >= 2; 1 >>= 1) {
                                                              14
    }
                                                                       g[1 >> 1] = (g[1] * 1LL* g[1]) % M;
27
    if (dist[t] == (11) 1e18) return -1LL;
                                                              16
28
     11 cost = 0;
                                                                     assert((g[1]*1LL * g[1]) % M == M - 1);
29
     for (int p = t; p != s; p = from[p]) {
                                                                     for (int 1 = 2; 1 <= 1 << (K - 2); 1 <<= 1) {
       for (auto index : g[from[p]]) {
30
                                                                       for (int i = 1; i < 1; ++i) {
                                                              19
         auto &edge = e[index];
         11 weight = edge.cost + phi[from[p]] - phi[
                                                              20
                                                                         g[1 + i] = (g[1] * 1LL * g[i]) % M;
32
       edge.next];
                                                              22
                                                                     }
         if (edge.rem() > 0 && edge.next == p && dist[
                                                              23
       edge.next] == dist[from[p]] + weight) {
                                                              24
                                                                   void fft(vector<int> &x) const {
34
           edge += 1;
           e[index ^ 1] -= 1;
                                                              25
                                                                     const int n = x.size();
35
                                                              26
                                                                     assert(n <= 1 << K);
           cost += edge.cost;
36
                                                                     for (int h = __builtin_ctz(n); h--; ) {
  const int l = (1 << h);</pre>
                                                              27
           break;
                                                              28
         }
38
                                                              29
                                                                       for (int i = 0; i < n >> (h+1); ++i) {
39
      }
                                                                         for (int j = i << (h+1); j < (((i << 1) +
                                                                     1) << h); ++j) {
    for (int i = 0; i < n; ++i) {</pre>
41
                                                              31
                                                                           const int t = (g[i] * 1LL* x[j | 1]) % M;
42
      phi[i] += dist[i];
                                                                           x[j | 1] = x[j] - t;
43
                                                                           if (x[j|1] < 0) x[j | 1] += M;
44
    return cost;
                                                                           x[j]+=t;
45 };
                                                                           if (x[j] >= M) x[j] -= M;
46 \ 11 \ cost = 0:
                                                              36
47 for (int flow = 0; flow < k; ++flow) {
                                                                       }
    11 a = dijkstra(s, t);
    if (a == -1) {
                                                              38
49
                                                                     for (int i = 0, j = 0; i < n; ++i) {
      cout << "-1\n";
50
                                                                       if (i < j) std::swap(x[i], x[j]);</pre>
                                                              40
51
       return:
                                                                       for (int 1 = n; (1 >>= 1) && !((j ^= 1) & 1);
    3.
52
                                                                      ) {}
     cost += a;
                                                              42
                                                                     }
54 }
                                                                   }
                                                              43
                                                              44
                                                                   vector < int > convolution (const vector < int > &a,
  6.2.4 Восстанавливаем ответ
                                                                     const vector <int> &b) const {
                                                                     if(a.empty() || b.empty()) return {};
1 auto findPath = [&](int s, int t) {
                                                              46
                                                                     const int na = a.size(), nb = b.size();
                                                                     int n, invN = 1;
    vector < int > ans;
                                                              47
                                                                     for (n = 1; n < na + nb - 1; n <<= 1) invN = ((</pre>
    int cur = s:
                                                              48
3
     while (cur != t) {
                                                                     invN & 1) ? (invN + M) : invN) >> 1;
       for (auto index : g[cur]) {
                                                                     vector < int > x(n, 0), y(n, 0);
6
         auto &edge = e[index];
                                                                     std::copy(a.begin(), a.end(), x.begin());
         if (edge.flow <= 0) continue;</pre>
                                                                     std::copy(b.begin(), b.end(), y.begin());
         edge -= 1;
                                                              52
                                                                     fft(x);
         e[index ^ 1] += 1;
9
                                                                     fft(y);
         ans.push_back(index / 4);
                                                              54
                                                                     for (int i = 0; i < n; ++i) x[i] = (((</pre>
                                                                     static_cast<long long>(x[i]) * y[i]) % M) *
11 // index / 4 because each edge has 4 copies
12
         cur = edge.next;
                                                                     invN) % M;
         break:
                                                                     std::reverse(x.begin() + 1, x.end());
```

```
120
        fft(x);
 56
 57
        x.resize(na + nb - 1);
 58
        return x;
 59
     }
 60 };
 61 Fft < 998244353,23,31 > muls:
 62 vector<int> form(vector<int> v,int n)
 63 {
      while(v.size()<n) v.push_back(0);</pre>
 64
 65
      while(v.size()>n) v.pop_back();
 66
      return v;
 67 ]
                                                                  5
 68 vector <int> operator *(vector <int> v1, vector <int>
                                                                  6
        v2)
 69 {
                                                                  8
      return muls.convolution(v1, v2);
                                                                  9
 71 }
 72 vector <int> operator +(vector <int> v1, vector <int>
        v2)
 73 {
      while(v2.size()<v1.size()) v2.push_back(0); while</pre>
                                                                  14
        (v1.size()<v2.size()) v1.push_back(0);
      for(int i=0;i<v1.size();++i) {v1[i]+=v2[i];if(v1[</pre>
                                                                  16
        i]>=p) v1[i]-=p; else if(v1[i]<0) v1[i]+=p;}
                                                                  17
 76
      return v1:
                                                                  18
 77 }
                                                                  19
 78 vector < int > operator - (vector < int > v1, vector < int >
                                                                  20
        v2)
                                                                  21
 79 {
                                                                  22
 80
      int sz=max(v1.size(), v2.size()); while(v1.size()
                                                                  23
        sz) v1.push_back(0); while(v2.size()<sz) v2.
                                                                  24
        push_back(0);
                                                                  25
      for(int i=0;i<sz;++i) {v1[i]-=v2[i];if(v1[i]<0)</pre>
 81
        v1[i]+=p; else if(v1[i]>=p) v1[i]-=p;} return
                                                                  27
                                                                  28
 82 }
                                                                  29
                                                                       }
 83 vector<int> trmi(vector<int> v)
                                                                  30
 84 {
      for(int i=1;i<v.size();i+=2) {if(v[i]>0) v[i]=p-v
                                                                  32
        [i]; else v[i]=(-v[i]);}
                                                                  33
 86
      return v:
                                                                  34
 87 1
                                                                  35 }
 88 vector<int> deriv(vector<int> v)
 89 {
 90
      if(v.empty()) return{};
                                                                  37
 91
      vector < int > ans(v.size()-1);
 92
      for(int i=1;i<v.size();++i) ans[i-1]=(v[i]*1LL*i)</pre>
                                                                  38
        %p;
 93
      return ans:
 94 }
 95 vector<int> integ(vector<int> v)
 96 {
      vector < int > ans(v.size()+1);ans[0]=0;
 97
                                                                  44
      for(int i=1;i<v.size();++i) ans[i-1]=(v[i]*1LL*i)</pre>
 98
        %p;
 99
      return ans;
100 }
101 vector<int> mul(vector<vector<int> > v)
102 {
      if(v.size()==1) return v[0];
103
      vector < vector < int > > v1, v2; for (int i=0; i < v.size()</pre>
        /2;++i) v1.push_back(v[i]); for(int i=v.size()
        /2;i<v.size();++i) v2.push_back(v[i]);</pre>
      return muls.convolution(mul(v1), mul(v2));
                                                                  54
106 }
                                                                  55 }
107 vector < int > inv1 (vector < int > v, int n)
108 {
109
      assert(v[0]!=0):
110
      int sz=1; v=form(v,n); vector < int > a = { inv(v[0]) };
      while (sz<n)
111
119
      {
113
        vector<int> vsz;for(int i=0;i<min(n,2*sz);++i)</pre>
        vsz.push_back(v[i]);
                                                                  2
114
        vector < int > b = ((vector < int >) {1}) - muls.
        convolution(a, vsz);
                                                                  4
115
        for(int i=0;i<sz;++i) assert(b[i]==0);</pre>
        b.erase(b.begin(),b.begin()+sz);
116
                                                                  5
117
        vector < int > c = muls.convolution(b,a);
                                                                  6
118
        for(int i=0;i<sz;++i) a.push_back(c[i]);</pre>
                                                                  7
119
        sz*=2;
                                                                 9
```

```
return form(a,n);
  7.2 старое доброе FFT
1 using cd = complex < double >;
2 const double PI = acos(-1);
  void fft(vector < cd > & a, bool invert) {
    int n = a.size():
    for (int i = 1, j = 0; i < n; i++) {
      int bit = n >> 1;
      for (; j & bit; bit >>= 1)
        j ^= bit;
      j ^= bit;
      if (i < i)
        swap(a[i], a[j]);
    for (int len = 2; len <= n; len <<= 1) {</pre>
      double ang = 2 * PI / len * (invert ? -1 : 1);
      cd wlen(cos(ang), sin(ang));
      for (int i = 0; i < n; i += len) {</pre>
        cd w(1);
        for (int j = 0; j < len / 2; j++) {</pre>
          cd u = a[i+j], v = a[i+j+len/2] * w;
          a[i+j] = u + v;
          a[i+j+len/2] = u - v;
           w *= wlen;
    if (invert) {
      for (cd & x : a)
        x /= n;
36 vector<int> multiply(vector<int> const& a, vector<
     int > const& b) {
    vector < cd> fa(a.begin(), a.end()), fb(b.begin(),
     b.end());
    int n = 1;
    while (n < a.size() + b.size())</pre>
     n <<= 1;
    fa.resize(n);
    fb.resize(n):
    fft(fa, false);
    fft(fb, false);
    for (int i = 0; i < n; i++)</pre>
      fa[i] *= fb[i];
    fft(fa, true);
    vector<int> result(n);
    for (int i = 0; i < n; i++)</pre>
      result[i] = round(fa[i].real());
    while(!result.empty() && !result.back()) result.
      pop_back();
    return result;
      Геома
  8.1 Касательные
      auto max = [&] (auto cmp) {
          int k = 0:
           for (int lg = 18; lg >= 0; --lg) {
               int i = k + (1 << lg), j = k - (1 << lg)
               i = (i % n + n) % n;
               j = (j \% n + n) \% n;
               array<int, 3> ind{i, j, k};
```

sort(all(ind), cmp);

```
9
               k = ind[2]:
10
           }
11
           return k:
19
       }:
13
       auto uppert = [&](Point p) { //last vertex in
       counterclockwise order about p
14
           auto cmp = [&] (int i, int j) {return (a[i]
        - p) < (a[j] - p); };
           return max(cmp);
16
       };
17
       auto lowert = [&](Point p) { //first vertex in
       counterclockwise order about p
          auto cmp = [&] (int i, int j) {return (a[i]
18
        - p) > (a[j] - p); };
19
           return max(cmp);
20
       auto uppertinf = [&](Point p) { //upper tangent
2.1
        line parallel to vector p
           swap(p.x, p.y);
2.3
           p.x = -p.x;
24
           auto cmp = [&] (int i, int j) { return a[i]
        % p < a[j] % p; };
25
           return max(cmp);
26
       };
2.7
       auto lowertinf = [&](Point p) { //lower tangent
        line parallel to vector p
28
           swap(p.x, p.y);
29
           p.x = -p.x;
           auto cmp = [&] (int i, int j) { return a[i]
30
        % p > a[j] % p; };
3.1
           return max(cmp);
32
```

8.2 Примитивы

```
1 struct Point {
       int x, y
3
       Point(){}
       Point (int x_, int y_) {
           x = x_{-}; y = y_{-};
5
       }
       Point operator + (Point p) {
           return Point(x+p.x,y+p.y);
9
10
       Point operator - (Point p) {
11
           return Point(x - p.x, y - p.y);
13
       int operator * (Point p) {
14
            return x * p.y - y * p.x;
15
16
       int operator % (Point p) {
           return x * p.x + y * p.y;
18
19
       bool operator < (Point v) {</pre>
20
           return (*this) * v > 0;
21
22
       bool operator > (Point v) {
23
           return v < (*this);</pre>
2.4
25
       bool operator <= (Point v) {</pre>
26
           return (*this) * v >= 0;
27
28 l:
29 bool line(Point a, Point b, Point c) {
30
       return (b-a)*(c-b)==0;
31 }
32 bool ord(Point a, Point p, Point b) {
33
       return (p - a)\%(p - b) < 0;
34 }
```

8.3 Точка нестрого внутри выпуклости

```
auto inT = [&] (Point a, Point b, Point c,
Point p) {
    a = a-p; b = b-p; c = c-p;
    return abs(a*b)+abs(b*c)+abs(c*a) == abs(a*b+b*c+c*a);
};
auto inP = [&] (Point p) { //a must be in counterclockwise order!
    int l = 1, r = n - 1;
```

9 Разное

9.1 Флаги компияции

```
-DLOCAL -Wall -Wextra -pedantic -Wshadow -Wformat=2
-Wfloat-equal -Wconversion -Wlogical-op -Wshift-overflow=2
-Wduplicated-cond -Wcast-qual -Wcast-align -D_GLIBCXX_DEBUG
-D_GLIBCXX_DEBUG_PEDANTIC -D_FORTIFY_SOURCE=2
-fsanitize=address -fsanitize=undefined -fno-sanitize-recover
-fstack-protector -std=c++2a
```

9.1.1 Сеточка в vim

https://codeforces.com/blog/entry/122540

```
1 i | <esc>25A | <esc>
2 o+<esc>25A---+<esc>
3 Vky35Pdd
```

9.2 Что сделать на пробном туре

- Убедиться, что работаеют все IDE. Разобраться, как настраивать в них LOCAL.
- В системе ML это ML или RE?
- Максимальный размер файла
- Можно посмотреть на время работы серверов позапускав Флойда — Варшалла

9.3 Шаблон

```
1 #include < bits / stdc++.h>
 3 using namespace std;
 5 #define int long long
 6 #define app push_back
 7 \text{ #define all(x)} \text{ x.begin(), x.end()}
 8 #ifdef LOCAL
 9 #define debug(...) [](auto...a){ ((cout << a <<
        ' '), ...) << endl; }(#__VA_ARGS__, ":",
        __VA_ARGS__)
10 #else
11 #define debug(...)
12 #endif
13
14 int32_t main() {
15
        cin.tie(0); ios_base::sync_with_stdio(0);
16 }
...
```