Содержание

1	Настройка CLion	1
2	Теория чисел	1
	2.1 KTO	1
	2.2 Алгоритм Миллера — Рабина	2
	2.3 Алгоритм Берлекэмпа — Месси	2 2
	2.4 Линейное решето 2.5 Алгоритм Шенкса	2
	2.5 Amopulm menkea	2
3	Графы	3
	3.1 <i>SCC</i> и 2- <i>SAT</i>	3
	3.2 Эйлеров цикл	3
	3.3 Компоненты рёберной двусвязности	4
	3.4 DCP offline	4 5
	0.0 Basemennoe napoco teranne	
4	Свёртки	6
	4.1 AND, OR, XOR свёртки	6
	4.2 FFT & co	6
	4.3 Быстрое FFT	7
	4.4 FFT в double'ax	9
5	Структуры данных	9
	5.1 Дерево Фенвика	9
	5.2 Дерево отрезков в точке	9
	5.3 Массовое дерево отрезков	10
	5.4 Битовый бор	11
	5.5 Ordered set	12 12
	5.6 Convex hull trick 5.7 Центроиды	12
	5.8 Дерево Ли Чао	12
	5.9 Min-Kinetic Segment Tree	13
	G	
6	Строковые алгоритмы	13
	6.1 Префикс-функция	13
	6.2 Z-функция 6.3 Алгоритм Манакера	14 14
	6.3 Алгоритм Манакера	14
	6.5 Алгоритм Ахо — Корасик	15
	6.6 Алгоритм Ахо Корасик	15
	6.7 Дерево палиндромов	15
	6.8 Дерево палиндромов	15
7	Потоки	15
′	7.1 Алгоритм Диница	1 5
	7.2 Mincost k-flow	16
8	Гамильтоновы путь и цикл	17
	8.1 Link-cut tree	17
	8.2 Undirected case 8.3 Directed case	17 18
	6.5 Directed case	10
9	Геома	19
	9.1 Примитивы	19
	9.2 Выпуклая оболочка	19
	9.3 Точка внутри многоугольника	19
	9.4 Касательные	20
10	Цепные дроби	20
	10.1 Поиск нижней огибающей, сумма и минимум по модулю .	20
	10.2 Простая рекурсия	21
	D.	0.1
11	Разное	21
	11.1 Компараторы	21 21
	11.2.1 Быстрый ввод	21
	11.2.2 Быстрый аллокатор	21
	11.3 Флаги компияции	21
	11.3.1 Сеточка в vim	21
	11.4 Что сделать на пробном туре	21
	11.5 Хеш файла без комментариев	21

1 Настройка CLion

```
1. B файле CMakeLists.txt дописать строчку add_compile_definitions(LOCAL). Нажать появившуюся опцию в правом верхнем углу enable auto-reload.
```

```
2. Вбить шаблон в main.cpp:
  #ifdef LOCAL
  #define _GLIBCXX_DEBUG
  #endif
  #include<bits/stdc++.h>
  using namespace std;
  #define int long long
  #define app push back
  #define all(x) x.begin(), x.end()
  #ifdef LOCAL
  #define debug(...) [](auto...a){ ((cout << a << ' '</pre>
       ), ...) << endl; }(#__VA_ARGS__, ":",
        _VA_ARGS___)
  #define debugv(v) do { cout << #v << ": "; for (</pre>
       auto x : v) cout << x << ' '; cout << endl; }</pre>
       while(0)
  #else
  #define debug(...)
  #define debugv(v)
  #endif
  int32_t main() {
    cin.tie(0);ios_base::sync_with_stdio(0);
    int n = 2; vector<int> a(n, n);
    debug(n); debugv(a);
  //59124c
  Скомпилировать, чтобы проверить отсутствие опечаток.
3. Запустить терминал (crtl + alt + T)
  $ cd workspace/CLionProjects
```

Далее отключаем подсветку и форматирование в настройках (ctrl+alt+S)

\$ for c in {A..Z}; do cp main.cpp \$c.cpp && echo "
add_executable(\$c \$c.cpp)" >> CMakeLists.txt;

- ullet Editor o Code Style o Formatter o Do not format прописать *
- ullet Editor o Inspections o C/C++ o static analysis tools o CLang-Tidy отключить
- Editor → Inlay Hints → отключаем всё (достаточно первых трёх code vision, parameter names, types).

Тёмная тема отключается в Appearance & Behavior \rightarrow Appearance. Чтобы добавить санитайзеры, надо дописать в CMakeLists.txt set(CMAKE_CXX_FLAGS "-fsanitize=address-fsanitize=undefined")

2 Теория чисел

done

2.1 KTO

```
int gcd(int a, int b, int &x, int &y) {
   if (b==0) { x = 1; y = 0; return a; }
   int d = gcd(b,a%b,y,x);
   y-=a/b*x;
   return d;
}
int inv(int r, int m) {
   int x, y;
   gcd(r,m,x,y);
   return (x+m)%m;
}
int crt(int r, int n, int c, int m) { return r + ((c - r) % m + m) * inv(n, m) % m * n; }
//8ed8ed
```

2.2 Алгоритм Миллера — Рабина

```
int128 one=1;
int po(int a,int b,int p)
{
  int res=1;
  while(b) {if(b & 1) {res=(res*one*a)%p;--b;} else {a
    =(a*one*a)%p;b>>=1;}} return res;
bool chprime(int n) //miller-rabin
  if(n==2) return true;
  if(n<=1 || n%2==0) return false;</pre>
  int h=n-1; int d=0; while (h%2==0) \{h/=2; ++d; \}
  for(int a:{2, 3, 5, 7, 11, 13, 17, 19, 23, 29, 31,
    371)
    if(a==n) return true;
    int u=po(a,h,n);bool ok=0;
    if(u%n==1) continue;
    for(int c=0; c < d; ++c)
      {
      if((u+1)%n==0) {ok=1;break;}
      u=(u*one*u)%n;
    if(!ok) return false;
  return true;
//86b2ed
```

2.3 Алгоритм Берлекэмпа — Месси

https://mzhang2021.github.io/cp-blog/berlekamp-massey/

```
template<typename T>
vector<T> berlekampMassey(const vector<T> &s) {
  int n = s.size(), 1 = 0, m = 1;
  vector<T> b(n), c(n);
  T ld = b[0] = c[0] = 1;
  for (int i=0; i<n; i++, m++) {</pre>
    T d = s[i];
    for (int j=1; j<=1; j++)</pre>
     d += c[j] * s[i-j];
    if (d == 0) continue;
    vector<T> temp = c;
    T coef = d / ld;
    for (int j=m; j<n; j++) c[j] -= coef * b[j-m];</pre>
    if (2 * 1 <= i) {</pre>
      1 = i + 1 - 1;
      b = temp;
      ld = d;
      m = 0;
  }
  c.resize(1 + 1);
  c.erase(c.begin());
  for (T &x : c)
   x = -x;
  return c;
//ff47ae
```

2.4 Линейное решето

```
const int C = 1e7+7;
vi pr, lp(C);
for (int i = 2; i < C; ++i) {
   if (lp[i] == 0) {
      lp[i] = i;
      pr.app(i);
   }
   for (int j = 0; j < (int)pr.size() && pr[j] <= lp[i]
      && pr[j] * i < C; ++j) {
      lp[pr[j] * i] = pr[j];
   }
}
//36b3d1</pre>
```

2.5 Алгоритм Шенкса

```
#define T int
int mod;
int gcd(int a, int b, int &x, int &y) {
 if (b==0) { x = 1; y = 0; return a; }
  int d = gcd(b,a%b,y,x);
 y=a/b*x;
  return d;
int inv(int r, int m) {
  int x, y;
 gcd(r,m,x,y);
 return (x+m)%m;
int crt(int r, int n, int c, int m) { return r + ((c -
     r) % m + m) * inv(n, m) % m * n; }
T inv(T a)
{
  return inv(a, mod);
T mul(T a, T b)
 return (a*b)%mod;
vector<int> rasl(int x)
 vector<int> v;
  if(x==1) {return v;}
  for(int i=2;i*i<=x;++i)</pre>
    if(x%i==0)
    {
      v=rasl(x/i); v.app(i); return v;
    }
  }
  v.app(x);return v;
T po(T a, int b) ///b>=1
  if(b==1) {return a;}
  if(b%2==0)
  {
    T u=po(a,b/2);
    return mul(u,u);
  }
  else
   T u=po(a,b-1);
    return mul(a,u);
T getper(T a, T one, int per, vector<int> v)
  for(int p:v)
  {
    if(po(a,per/p)==one)
      per/=p;
    }
 return per;
vector<pair<int, int> > shanks(T a, vector<T> b, T one,
    int per) ///a^per=1 and b[i]^per=1 /// all right
    numbers in output are equal
 if(b.empty()) {return {};}
  int n=b.size();
 vector<int> vp=rasl(per);
  int pera=getper(a,one,per,vp);per=pera;
  vp=rasl(pera);
 vector<int> have(n,0);
  int cur2=per;T cura=a;T invcura=inv(a);
  int curad=1;
  vector<pair<T,int> > v;
  vector<bool> ok(n,true);
  vector<T> poinvzx;
  for(int p:vp)
  {
```

```
T ca=po(cura,cur2/p);
    if(ca==one) {continue;}
    T invca=po(invcura,cur2/p);
    int step=sqrt(b.size()*p)+2;
    int wee=p/step+2;
    v.clear();poinvzx.clear();
    T zx=one; T invzx=one; T buba=one;
    vector<T> zhe;
    T lu=one;
    for(int i=0;i<step;++i)</pre>
      v.app({zx,i});zhe.app(lu);
      zx=mul(zx,ca);invzx=mul(invzx,invca);buba=mul(
    buba, cura); lu=mul(lu, invcura);
    poinvzx.app(one);
    for(int j=0;j<wee;++j)</pre>
      poinvzx.app(mul(poinvzx.back(),buba));
    sort(all(v));
    for(int i=0;i<n;++i)</pre>
      if(!ok[i]) {continue;}
      T uu=po(b[i],cur2/p);
      bool okkk=false;
      for(int j=0;j<wee;++j)</pre>
        auto it=lower_bound(all(v), make_pair(uu, OLL));
        if(it!=v.end() && (*it).first==uu)
          okkk=true;
          have[i]-=(curad*step*j);
          have[i]+=(curad*(*it).second);
          have[i]%=pera;if(have[i]<0) {have[i]+=pera;}</pre>
          b[i]=mul(b[i],poinvzx[j]);b[i]=mul(b[i],zhe
    [(*it).second]);
          assert(po(b[i],cur2/p)==one);
          break;
        uu=mul(uu,zx);
      }
      if(!okkk) {ok[i]=false;}
    cur2/=p; cura=po(cura,p); invcura=po(invcura,p);
    curad*=p;
  vector<pair<int,int> > res;
  for(int i=0;i<n;++i)</pre>
    if(ok[i] && b[i]==one)
      res.app({(have[i]%pera+pera)%pera,pera});
    }
    else
    {
      res.app({-1,pera});
    }
  }
  return res;
int shanks2(int x, int y, int mod1) ///only for T=long
    long, 0^0 = 1 by default
 mod=mod1;
  vector<int> v=rasl(mod);sort(all(v));
  int per=1;for(int i=0;i<v.size();++i) {if(i==0 || v[</pre>
    i]!=v[i-1]) {per*=(v[i]-1);} else {per*=v[i];}}
  if(y==1 || mod==1) {return 0;}
  int C=61;
  for(int i=1;i<C;++i)</pre>
  {
    if(po(x,i)==y) {return i;}
  if(y==0) {return (-1);}
  T h=po(x,C);
  int lc1=gcd(h, mod); int lc2=gcd(y, mod);
  if(lc1!=lc2) {return (-1);}
  mod/=lc2;T h1=h/lc2;T y1=y/lc2;
  vector<pair<int, int> > s=shanks(x%mod, {mul(y1, inv(h1
```

```
))},1,per);
if(s[0].first!=(-1))
{
   return s[0].first+C;
}
else
{
   return (-1);
}
//a75596
```

3 Графы

3.1 SCC и 2-SAT

```
Алгоритм ищет сильносвязные компоненты в графе q, если есть путь
i \to j, to scc[i] \le scc[j]
vector<int> find_scc(vector<vector<int>> g) {
  vector<vector<int>>> r(g.size());
  for (int i = 0; i < g.size(); ++i) {</pre>
    for (int j : g[i]) r[j].push_back(i);
  vector<int> used(g.size()), tout(g.size());
  int time = 0;
  auto dfs = [&](auto dfs, int cur) -> void {
    if (used[cur]) return;
    used[cur] = 1;
    for (int nxt : g[cur]) {
      dfs(dfs, nxt);
    tout[cur] = time++;
  };
  for (int i = 0; i < g.size(); ++i) if (!used[i]) dfs</pre>
    (dfs, i);
  vector<int> ind(g.size());
  iota(ind.begin(), ind.end(), 0);
  sort(all(ind), [&](int i, int j){return tout[i] >
    tout[j];});
  vector<int> scc(g.size(), -1);
  auto go = [&](auto go, int cur, int color) -> void {
    if (scc[cur] != -1) return;
    scc[cur] = color;
    for (int nxt : r[cur]) {
      go(go, nxt, color);
    }
  };
  int color = 0;
  for (int i : ind) {
    if (scc[i] == -1) go(go, i, color++);
  return scc;
//08f99a
```

Чтобы решать $2\text{-}\mathcal{SAT}$, надо создать граф на 2n вершинах, рёбра $i\Rightarrow j$ и $(j\oplus 1)\Rightarrow (i\oplus 1)$ должны быть добавлены одновременно. После этого если $\sec[2\ *\ i] = \sec[2\ *\ i+1]$, то решения нет; если $\sec[2\ *\ i+0] < \sec[2\ *\ i+1]$, то присутствует импликация $\neg i\Rightarrow i$, надо назначить i=true.

3.2 Эйлеров цикл

```
vector<int> euler(vector<vector<pair<int, int>>> g,
    int m, int src) { // g[cur][i] = pair{nxt, idx}
  int n = g.size();
 vector<int> used(m), it(n), cycle;
  auto dfs = [&](auto dfs, int cur) -> void {
   while (true) {
     while (it[cur] < g[cur].size() && used[g[cur][it</pre>
    [cur]].second]) it[cur]++;
     if (it[cur] == g[cur].size()) return;
      auto [nxt, idx] = g[cur][it[cur]];
      used[idx] = true;
      dfs(dfs, nxt);
      cycle.push_back(idx); // or {cur, nxt}
   }
  };
  dfs(dfs, src);
  reverse(cycle.begin(), cycle.end());
```

```
if (cycle.size() != m) return {}; // check that all
  edges are present in the cycle, fail otherwise
  return cycle;
}
//f6b9d4
```

3.3 Компоненты рёберной двусвязности

```
int n, m;
cin >> n >> m;
vector \langle \text{vector} \langle \text{int} \rangle \rangle g(n + 1);
map <pair <int, int>, int> comp, col;
for (int i = 0; i < m; ++i) {</pre>
  int u, v, c; cin >> u >> v >> c;c--;
  col[{u,v}]=col[{v,u}]=c;
  g[u].push_back(v);
  g[v].push_back(u);
vector <int> used(n + 1);
vector <int> newCompWithoutParent(n + 1), h(n + 1), up
    (n + 1);
auto findCutPoints = [&] (auto self, int u, int p) ->
    void {
  used[u] = 1;
  up[u] = h[u];
  for (int v : g[u]) {
    if (!used[v]) {
      h[v] = h[u] + 1;
      self(self, v, u);
      up[u] = min(up[u], up[v]);
      if (up[v] >= h[u]) {
        newCompWithoutParent[v] = 1;
    }
    else {
     up[u] = min(up[u], h[v]);
    }
 }
1:
for (int u = 1; u <= n; ++u) {
 if (!used[u]) {
   findCutPoints(findCutPoints, u, u);
 }
}
int ptr = 0;
vector <map <int, int> > colors(m);
auto markComponents = [&] (auto self, int u, int cur)
    -> void {
  used[u] = 1;
  for (int v : g[u]) {
    if (!used[v]) {
      if (newCompWithoutParent[v]) {
        ptr++;
        self(self, v, ptr - 1);
      else {
        self(self, v, cur);
      }
    else if (h[v] < h[u]) {
      comp[{u,v}]=comp[{v,u}]=cur;
      int c = col[{u,v}];
      colors[cur][u] |= 1 << c;
      colors[cur][v] |= 1 << c;
 }
used.assign(n + 1, 0);
for (int u = 1; u \le n; ++u) {
  if (!used[u]) {
   markComponents(markComponents, u, -1);
for (int comp = 0; comp < m; ++comp) {
  vector <int> cnt(4);
  int tot = 0;
  for (auto [u, mask] : colors[comp]) {
    tot |= mask;
    cnt[bp(mask)]++;
  if (bp(tot)<3) {</pre>
```

4

```
continue;
 if (cnt[2] || cnt[3]>2) {
    cout << "Yes" << endl;</pre>
    return;
cout << "No" << endl;</pre>
//01817d
3.4 DCP offline
struct Dsu {
 int n;
  vector<pair<int &, int>> s;
  vector<int> p, sz;
  // other info
  Dsu(int n) : n(n), p(n), sz(n, 1){
   iota(all(p), 0);
  int get(int u) {
    while (u != p[u]) u = p[u];
    return u;
 bool merge(int u, int v) {
    u = get(u), v = get(v);
    if (u == v) return false;
   if (sz[v] < sz[u]) swap(u, v);
    s.app({p[u], p[u]});
    s.app({sz[v], sz[v]});
    // app other info like s.app({comp, comp});
    p[u] = v;
    sz[v] += sz[u];
    return true;
 void rollback(int sz) {
    while (s.size() != sz) {
      s.back().first = s.back().second;
      s.pop_back();
    }
 }
};
struct DcpOffline {
 int n;
 vector<vector<pair<int, int>>> d;
  void addEdgeOnSegment(int 1, int r, int a, int b) {
    for (1 += n, r += n; 1 < r; 1 /= 2, r /= 2) {
      if (1 & 1) d[1++].app({a, b});
      if (r & 1) d[--r].app({a, b});
    }
 }
  template<typename T>
 void dfs(Dsu &dsu, T act) {
    dfs(1, 0, n, dsu, act);
  template<typename T>
  void dfs(int v, int l, int r, Dsu &dsu, T act) {
    int sz = dsu.s.size();
    for (auto [u, v]: d[v]) {
      dsu.merge(u, v);
    if (1 + 1 == r) {
     act(1, dsu);
    } else {
      int m = (1 + r) / 2;
      dfs(v * 2, 1, m, dsu, act);
      dfs(v * 2 + 1, m, r, dsu, act);
    dsu.rollback(sz);
  DcpOffline(int maxt) : n(2 \ll \_lg(maxt + 1)), d(2 *
```

```
};
//3c4e2d
```

void ex(int u) {

for (int x : p[u]) ch(x, x);

int a = b[u][e[u][f[u]].u], r = gr(u, a);

```
3.5 Взвешенное паросочетание
https://judge.yosupo.jp/submission/201334
\#define\ d(x)\ (lab[x.u] + lab[x.v] - 2 * e[x.u][x.v].w)
const int N = 403*2;
const int inf = 1e18;
struct Q{ int u, v, w; } e[N][N];
vector<int> p[N];
int n, m = 0, id, h, t, lk[N], sl[N], st[N], f[N], b[N]
    ][N], s[N], ed[N], q[N], lab[N];
void upd(int u, int v) { if (!sl[v] || d(e[u][v]) < d(</pre>
    e[sl[v]][v])) sl[v] = u; }
void ss(int v) {
 sl[v] = 0;
  for (int u = 1; u \le n; ++u) if (e[u][v].w > 0 && st
    [u] != v \&\& !s[st[u]]) upd(u, v);
void ins(int u){ if (u <= n) q[++t] = u; else for (int</pre>
    v : p[u]) ins(v); }
void ch(int u, int w) { st[u] = w; if (u > n) for (int u) }
    v : p[u]) ch(v, w); }
int gr(int u, int v) {
 if ((v = find(all(p[u]), v) - p[u].begin()) & 1) {
   reverse(1 + all(p[u]));
    return (int)p[u].size() - v;
 return v;
}
void stm(int u, int v) {
 lk[u] = e[u][v].v;
  if (u <= n) return; Q w = e[u][v];</pre>
  int x = b[u][w.u], y = gr(u,x);
  for (int i = 0; i < y; ++i) stm(p[u][i], p[u][i^1]);</pre>
 stm(x, v); rotate(p[u].begin(), y+all(p[u]));
void aug(int u, int v) {
 int w = st[lk[u]];stm(u, v);if (!w) return;
 stm(w, st[f[w]]);
  aug(st[f[w]], w);
int lca(int u, int v) {
  for (id++; u|v; swap(u, v)) {
   if (!u) continue;if(ed[u] == id) return u;
    ed[u] = id; if (u = st[lk[u]]) u = st[f[u]]; // =,
     not ==
 return 0;
//cf1d55
void add(int u, int a, int v) {
 int x = n + 1; while (x \le m \&\& st[x]) ++x;
  if (x > m) ++m;
 lab[x] = s[x] = st[x] = 0;
 lk[x] = lk[a];
 p[x].clear();
 p[x].push back(a);
#define op(q) for (int i = q, j = 0; i != a; i=st[f[j
    ]]) p[x].push_back(i), p[x].push_back(j=st[lk[i]])
    , ins(j) // also not =
  op(u); reverse(1+all(p[x]));op(v);
  ch(x, x); for (int i = 1; i <= m; ++i) e[x][i].w = e
    [i][x].w = 0;
  fill(b[x]+1, b[x]+n+1, 0);
  for (int u : p[x]) {
    for (int v = 1; v <= m; ++v) if (!e[x][v].w || d(e</pre>
    [u][v]) < d(e[x][v])) e[x][v] = e[u][v], e[v][x] =
     e[v][u];
    for (int v = 1; v \le n; ++v) if (b[u][v]) b[x][v]
 1
 ss(x);
```

```
for (int i = 0; i < r; i += 2) {
    int x = p[u][i], y = p[u][i + 1];
    f[x] = e[y][x].u; s[x] = 1; s[y] = 0; sl[x] = 0;
    ss(y); ins(y);
 s[a] = 1; f[a] = f[u];
  for (int i = r + 1; i < p[u].size(); ++i) s[p[u][i]]
    = -1, ss(p[u][i]);
  st[u] = 0;
bool on(const Q &e) {
  int u = st[e.u], v = st[e.v], a;
  if (s[v] == -1) {
    f[v] = e.u, s[v] = 1, a = st[lk[v]], sl[v] = sl[a]
     = s[a] = 0, ins(a);
  } else if (!s[v]) {
    a = lca(u, v); if (!a) return aug(u, v), aug(v, u)
    , 1; else add(u, a, v);
 return 0;
//3f0f1d
bool bfs() {
 fill(s+1, s+m+1, -1); fill(sl+1, sl+m+1, 0); // s is
    filled with -1
  h = 1, t = 0; for (int i = 1; i \le m; ++i) if (st[i]
     == i \&\& !lk[i]) f[i] = s[i] = 0, ins(i);
  if (h > t) return 0;
  while (1) {
    while (h <= t) {</pre>
      int u = q[h++];
      if (s[st[u]] != 1) {
        for (int v = 1; v \le n; ++v) if (e[u][v].w > 0
     && st[u] != st[v]) {
          if (d(e[u][v])) upd(u, st[v]); else if (on(e
    [u][v])) return 1;
        }
      }
    }
    int x = inf;
    for (int i = n+1; i <= m; ++i) if (st[i] == i && s</pre>
    [i] == 1) x = min(x, lab[i]/2);
    for (int i = 1; i <= m; ++i) if (st[i] == i && sl[
    i] && s[i] != 1) x = min(x, d(e[sl[i]][i])>>s[i]
    ]+1);
    for (int i = 1; i <= n; ++i) if (~s[st[i]]) if ((</pre>
    lab[i] += (s[st[i]] * 2 - 1) * x) <=0) return 0;
    for (int i = n + 1; i <= m; ++i) if (st[i] == i &&</pre>
     \sim s[st[i]]) lab[i] += (2 - 4 * s[st[i]]) * x;
    h = 1, t = 0;
    for (int i = 1; i <= m; ++i) if (st[i] == i && sl[</pre>
    i] && st[sl[i]] != i && !d(e[sl[i]][i]) && on(e[sl
    [i]][i])) return 1;
    for (int i = n+1; i <= m; ++i) if (st[i] == i && s
    [i] == 1 \&\& !lab[i]) ex(i);
 }
pair<int, vector<array<int, 2>>> run(int N, vector<</pre>
    array<int, 3>> edges) {
  for (auto &[u, v, w] : edges) ++u, ++v;
  fill(ed+1, ed+m+1, 0);
  fill(lk+1, lk+m+1, 0);
  n = m = N;
  id = 0:
  iota(st + 1, st + n + 1, 1);
  int wm = 0, weight = 0;
  for (int i = 1; i <= n; ++i) for (int j = 1; j <= n;
     ++j) e[i][j] = {i,j,0};
  for (auto [u, v, w] : edges) wm = max(wm, e[v][u].w
    = e[u][v].w = max(e[u][v].w, w));
  for (int i = 1; i <= n; ++i) p[i].clear();</pre>
  for (int i = 1; i <= n; ++i) for (int j = 1; j <= n;
     ++j) b[i][j] = i==j?i:0;
  fill_n(lab+1, n, wm); while (bfs());
  vector<array<int, 2>> matching;
  for (int i = 1; i \le n; ++i) if (i \le lk[i]) weight
    += e[i][lk[i]].w, matching.push_back({i - 1, lk[i]
```

```
- 1});
return {weight, matching};
}
//be682f
```

4 Свёртки

4.1 AND, OR, XOR свёртки

```
vector<int> band(vector<int> a, vector<int> b)
 int n=0; while((1<<n)<a.size()) ++n;</pre>
 a.resize(1<<n);b.resize(1<<n);
  for(int i=0; i< n; ++i) for(int mask=0; mask<(1<< n); ++
    mask) if(mask & (1<<i)) {a[mask-(1<<i)]+=a[mask];a}
    [mask-(1<<i)]%=p;}
  for(int i=0;i<n;++i) for(int mask=0;mask<(1<<n);++</pre>
    mask) if(mask & (1<<i)) {b[mask-(1<<i)]+=b[mask];b}
    [mask-(1<<i)]%=p;}
  vector<int> c(1<<n,0);
  for(int mask=0; mask<(1<< n); ++ mask) {c[mask]=a[mask]*}
    b[mask];c[mask]%=p;}
  for(int i=0;i<n;++i) for(int mask=0;mask<(1<<n);++</pre>
    mask) if(!(mask & (1<<i))) {c[mask]-=c[mask+(1<<i)}
    ];c[mask]%=p;}
  return c;
//807ee0
vector<int> bor(vector<int> a, vector<int> b)
  int n=0; while((1<<n)<a.size()) ++n;</pre>
 a.resize(1<<n);b.resize(1<<n);
  for(int i=0; i< n; ++i) for(int mask=0; mask<(1<< n); ++
    mask) if(!(mask & (1<<i))) {a[mask+(1<<i)]+=a[mask]}
    ];a[mask+(1<<i)]%=p;}
  for(int i=0;i<n;++i) for(int mask=0;mask<(1<<n);++</pre>
    mask) if(!(mask & (1<<i))) {b[mask+(1<<i)]+=b[mask]}
    ];b[mask+(1<<i)]%=p;}
  vector<int> c(1<<n,0);</pre>
  for(int mask=0; mask<(1<< n); ++ mask) {c[mask]=a[mask]*}
   b[mask];c[mask]%=p;}
  for(int i=0;i<n;++i) for(int mask=0;mask<(1<<n);++</pre>
    [mask]%=p;}
 return c;
//07707e
vector<int> bxor(vector<int> a, vector<int> b)
 assert(p%2==1); int inv2=(p+1)/2;
 int n=0; while((1<<n)<a.size()) ++n;</pre>
  a.resize(1<<n); b.resize(1<<n);
 for(int i=0;i<n;++i) for(int mask=0;mask<(1<<n);++</pre>
    mask) if (!(mask & (1 << i)))  {int u=a[mask], v=a[mask]
    +(1<<i)];a[mask+(1<<i)]=(u+v)%p;a[mask]=(u-v)%p;}
  for(int i=0;i<n;++i) for(int mask=0;mask<(1<<n);++</pre>
    mask) if(!(mask & (1<<i))) {int u=b[mask], v=b[mask]</pre>
    +(1<<i)];b[mask+(1<<i)]=(u+v)%p;b[mask]=(u-v)%p;}
  vector < int > c(1 < < n.0):
  for(int mask=0; mask<(1<< n); ++ mask) {c[mask]=a[mask]*}
    b[mask];c[mask]%=p;}
  for(int i=0;i<n;++i) for(int mask=0;mask<(1<<n);++</pre>
    mask) if(!(mask & (1<<i))) {int u=c[mask], v=c[mask]}
    +(1<<i)];c[mask+(1<<i)]=((v-u)*inv2)%p;c[mask]=((u
    +v)*inv2)%p;}
  return c;
}
//20cc50
4.2 FFT & co
```

```
typedef long long 11;
const int p=998244353;
```

```
int po(int a,int b) {if(b==0) return 1; if(b==1)
    return a; if(b%2==0) {int u=po(a,b/2);return (u*1
    LL*u)%p;} else {int u=po(a,b-1); return (a*1LL*u)%p
int inv(int x) {return po(x,p-2);}
template<int M, int K, int G> struct Fft {
  // 1, 1/4, 1/8, 3/8, 1/16, 5/16, 3/16, 7/16, ...
  int g[1 << (K - 1)];</pre>
  Fft() : g() { //if tl constexpr...
    // static_assert(K >= 2, "Fft: K >= 2 must hold");
    q[0] = 1;
    g[1 << (K - 2)] = G;
    for (int 1 = 1 \ll (K - 2); 1 >= 2; 1 >>= 1) {
      g[1 >> 1] = (g[1] * 1LL* g[1]) % M;
    assert((g[1]*1LL * g[1]) % M == M - 1);
    for (int 1 = 2; 1 <= 1 << (K - 2); 1 <<= 1) {
      for (int i = 1; i < 1; ++i) {</pre>
        g[l + i] = (g[l] * 1LL * g[i]) % M;
   }
 }
  void fft(vector<int> &x) const {
    const int n = x.size();
    assert(n \le 1 \le K);
    for (int h = __builtin_ctz(n); h--; ) {
      const int l = (1 \ll h);
      for (int i = 0; i < n >> (h+1); ++i) {
        for (int j = i << (h+1); j < (((i << 1) + 1)
    << h); ++j) {
          const int t = (g[i] * 1LL* x[j | 1]) % M;
          x[j \mid 1] = x[j] - t;
          if (x[j|1] < 0) x[j | 1] += M;
          x[i]+=t;
          if (x[j] >= M) x[j] -= M;
        }
     }
    for (int i = 0, j = 0; i < n; ++i) {
      if (i < j) std::swap(x[i], x[j]);</pre>
      for (int 1 = n; (1 >>= 1) && !((j ^= 1) & 1); )
    { }
    }
  vector<int> convolution(vector<int> a, vector<int> b
    ) const {
    if(a.empty() || b.empty()) return {};
    for(int& x:a) \{x\%=p; if(x>=p) x-=p; if(x<0) x+=p;\}
    for(int& x:b) \{x\%=p; if(x>=p) \ x-=p; if(x<0) \ x+=p;\}
    const int na = a.size(), nb = b.size();
    int n, invN = 1;
    for (n = 1; n < na + nb - 1; n <<= 1) invN = ((
    invN & 1) ? (invN + M) : invN) >> 1;
    vector < int > x(n, 0), y(n, 0);
    std::copy(a.begin(), a.end(), x.begin());
    std::copy(b.begin(), b.end(), y.begin());
    fft(x);
    fft(y);
    for (int i = 0; i < n; ++i) x[i] = (((static_cast<</pre>
    long long>(x[i]) * y[i]) % M) * invN) % M;
    std::reverse(x.begin() + 1, x.end());
    fft(x);
    x.resize(na + nb - 1);
    return x;
 }
Fft<998244353,23,31> muls;
//a1b591
vector<int> form(vector<int> v,int n)
 while(v.size()<n) v.push_back(0);</pre>
 while(v.size()>n) v.pop_back();
  return v;
vector<int> operator *(vector<int> v1, vector<int> v2)
```

return muls.convolution(v1, v2);

6

```
vector<int> operator +(vector<int> v1, vector<int> v2)
  while(v2.size()<v1.size()) v2.push_back(0); while(v1</pre>
    .size()<v2.size()) v1.push_back(0);</pre>
  for(int i=0;i<v1.size();++i) {v1[i]+=v2[i];if(v1[i</pre>
    ]>=p) v1[i]-=p; else if(v1[i]<0) v1[i]+=p;}</pre>
  return v1;
vector<int> operator -(vector<int> v1, vector<int> v2)
  int sz=max(v1.size(), v2.size()); while(v1.size()<sz)</pre>
    v1.push_back(0); while(v2.size()<sz) v2.push_back</pre>
    (0);
  for(int i=0;i<sz;++i) {v1[i]-=v2[i];if(v1[i]<0) v1[i</pre>
    ]+=p; else if(v1[i]>=p) v1[i]-=p;} return v1;
vector<int> trmi(vector<int> v)
  for(int i=1;i<v.size();i+=2) {if(v[i]>0) v[i]=p-v[i
    ]; else v[i]=(-v[i]);}
  return v;
vector<int> deriv(vector<int> v)
  if(v.empty()) return{};
  vector<int> ans(v.size()-1);
  for(int i=1;i<v.size();++i) ans[i-1]=(v[i]*1LL*i)%p;</pre>
  return ans;
}
vector<int> integ(vector<int> v)
  vector<int> ans(v.size()+1);ans[0]=0;
  for(int i=1;i<v.size();++i) ans[i-1]=(v[i]*1LL*i)%p;</pre>
  return ans;
vector<int> mul(vector<vector<int> > v)
  if(v.size()==1) return v[0];
  vector<vector<int> > v1, v2; for(int i=0; i<v.size()</pre>
    /2;++i) v1.push_back(v[i]); for(int i=v.size()/2;i
    <v.size();++i) v2.push_back(v[i]);
  return muls.convolution(mul(v1), mul(v2));
vector<int> inv1(vector<int> v,int n)
  assert(v[0]!=0);
  int sz=1;v=form(v,n);vector<int> a={inv(v[0])};
  while(sz<n)
    vector<int> vsz;for(int i=0;i<min(n,2*sz);++i) vsz</pre>
    .push_back(v[i]);
    vector<int> b=((vector<int>) {1})-muls.convolution
    (a, vsz);
    for(int i=0;i<sz;++i) assert(b[i]==0);</pre>
    b.erase(b.begin(),b.begin()+sz);
    vector<int> c=muls.convolution(b,a);
    for(int i=0;i<sz;++i) a.push_back(c[i]);</pre>
    sz*=2;
  return form(a,n);
//12aa4e
```

4.3 Быстрое FFT

- Solution based on https://codeforces.com/blog/entry/117947
- Iterative and in-place version.
- Uses signed montgomery
- Optimized to minimize memory usage

```
const int MOD = 998244353;
const long long MOD2 = (long long) MOD * MOD;
const int root = 3;
const int alim = 64; // Bound for using O(n^2)
    polynomial mult
```

```
int modpow(int b, int e) {
  int ans = 1;
  for (; e; b = (long long) b * b % MOD, e /= 2)
    if (e & 1) ans = (long long) ans * b % MOD;
  return ans;
const int MODinv = 2 - MOD; // pow(-MOD, -1, 2**32)
inline int m_reduce(long long x) {
 int m = x * MODinv;
  return (x>>32) - (((long long) m * MOD) >> 32);
const int r2 = modpow(2, 64);
inline int m_transform(int x) {
 return m_reduce((long long)x * r2);
inline int m_add(int x, int y) {
 int z = x + y;
  return z < 0 ? z + MOD : z - MOD;
inline int m_sub(int x, int y) {
 int z = x - y;
  return z < 0 ? z + MOD : z - MOD;
}
inline int m_mult(int x, int y) {
 return m_reduce((long long) x * y);
vector<int> rt = {1};
vector<int> transformed_rt;
vector<int> transformed_rt2;
template<int a>
void transform(vector<int> &P) {
  int m = P.size();
  int n = m / a;
  int size = rt.size();
 while (2 * size < n) {</pre>
    rt.resize(n / 2);
    int r = modpow(root, MOD / (4 * size));
    for (int i = 0; i < size; ++i)</pre>
      rt[i + size] = (long long) r * rt[i] % MOD;
    size *= 2;
  // For montgomery
  for (int i = transformed_rt.size(); i < rt.size();</pre>
    ++i) {
    transformed rt.resize(rt.size());
    transformed_rt[i] = m_transform(rt[i]);
    transformed_rt2.resize(rt.size());
    transformed_rt2[i] = (unsigned int) MODinv *
    transformed_rt[i];
 }
  int k = n;
 while (k >= 4) k /= 4;
  if (k == 2) {
    int step = n * a;
    int half_step = step / 2;
    for (int j1 = 0; j1 < half_step; ++j1) {</pre>
      int j2 = j1 + half_step;
      int diff = m_sub(P[j1], P[j2]);
      P[j1] = m_add(P[j1], P[j2]);
      P[j2] = diff;
    k = n/2;
  } else {
    k = n;
  for (; k > 1; k /= 4) {
    for (int i = 0; i < n/k; ++i) {
```

```
int step = k * a;
      int half_step = step / 2;
      int quarter_step = half_step / 2;
      int R20 = transformed_rt2[2 * i];
      int RR0 = transformed_rt[2 * i];
      int R21 = transformed_rt2[2 * i + 1];
      int RR1 = transformed_rt[2 * i + 1];
      int R2 = transformed_rt2[i];
      int RR = transformed_rt[i];
      int j1 = i * step;
      int j2 = j1 + quarter_step;
      int j3 = j2 + quarter_step;
      int j4 = j3 + quarter_step;
      for (int j = 0; j < quarter_step; ++j, ++j1, ++</pre>
    j2, ++j3, ++j4) {
        int z0;
        {
          int z = P[j3];
          int m = (unsigned int) R2 * z;
          z0 = ((long long) z * RR - (long long) m *
    MOD) >> 32:
       }
        int z1;
        {
          int z = P[j4];
          int m = (unsigned int) R2 * z;
          z1 = ((long long) z * RR - (long long) m *
    MOD) >> 32;
       }
        int sum0 = m_add(P[j1], z0);
        int diff0 = m_sub(P[j1], z0);
        int sum1 = P[j2] + z1;
        int diff1 = P[j2] - z1;
        // [sum0, sum1, diff0, diff1]
        int zz0;
          int z = sum1;
          int m = (unsigned int) R20 * z;
          zz0 = ((long long) z * RR0 - (long long) m *
     MOD) >> 32:
       }
        int zz1;
          int z = diff1;
          int m = (unsigned int) R21 * z;
          zz1 = ((long long) z * RR1 - (long long) m *
     MOD) >> 32;
        P[j1] = m_add(sum0, zz0);
        P[j2] = m_sub(sum0, zz0);
        P[j3]
              = m_add(diff0, zz1);
        P[j4] = m_sub(diff0, zz1);
      }
   }
 for (int i = 0; i < m; ++i)
    if (P[i] < 0) P[i] += MOD;
template<int a>
void inverse transform(vector<int> &P) {
  int m = P.size();
  int n = m / a;
 int n_inv = m_transform(modpow(n, MOD - 2));
 vector<int> rev(n);
  for (int i = 1; i < n; ++i) {</pre>
   rev[i] = rev[i / 2] / 2 + (i & 1) * n / 2;
```

```
}
  // P = [p * n_inv for p in P]
  for (int i = 0; i < m; ++i)
    P[i] = m_mult(n_inv, P[i]);
 // P = [P[a * rev[i // a] + (i % a)] for i in range(
   m)]
  for (int i = 1; i < n; ++i)
   if (i < rev[i])</pre>
     swap_ranges(P.begin() + a * i, P.begin() + a * i
     + a, P.begin() + a * rev[i]);
  // P = [P[-a * (i // a) + (i % a)] for i in range(m)
  for (int i = 1; i < n/2; ++i)
    swap_ranges(P.begin() + a * i, P.begin() + a * i +
     a, P.begin() + a * (n - i);
 transform<a>(P);
  // P = [P[a * rev[i // a] + (i % a)] for i in range(
  for (int i = 1; i < n; ++i)
    if (i < rev[i])</pre>
      swap_ranges(P.begin() + a * i, P.begin() + a * i
     + a, P.begin() + a * rev[i]);
template<int a>
void fast_polymult_mod(vector<int> &P, vector<int> &Q)
  int m = P.size();
  int n = m / a;
 transform<a>(P);
 transform<a>(0);
 vector<int> &PQ = P;
 for (int i = 0; i < n; ++i) {</pre>
    vector<unsigned long long> res(2 * a);
    for (int j = 0; j < a; ++j) {
      if (j >= 10 && j % 9 == 8)
        for (int k = j; k < j + a - 10; ++k)
         res[k] -= (res[k] >> 63) * 9 * MOD2;
      for (int k = 0; k < a; ++k)
        res[j + k] += (long long) P[i * a + j] * Q[i *
     a + k;
    }
    int c = rt[i/2];
    if (i \& 1) c = MOD - c;
    for (int j = 0; j < a; ++j)
      PQ[i * a + j] = (res[j] + c * (res[j + a] % MOD)
    ) % MOD;
  inverse_transform<a>(PQ);
}
template <size_t... N>
void work(std::index_sequence<N...>, int x, std::
    vector<int>& a, std::vector<int>& b) {
  static void (*ptrs[])(std::vector<int>&, std::vector
    <int>&) = {&fast_polymult_mod<N+1>...};
 ptrs[x - 1](a, b);
void fast_polymult(vector<int> &P, vector<int> &Q) {
 int m1 = P.size();
  int m2 = Q.size();
 int res_len = m1 + m2 - 1;
 int b = 1;
 while ((alim << b) < res_len) ++b;</pre>
 int a = ((res_len - 1) >> b) + 1;
 int m = a << b;</pre>
 P.resize(m);
  Q.resize(m);
```

```
// Call fast_polymult_mod<a>(P, Q);
work(std::make_index_sequence<alim>{}, a, P, Q);
P.resize(res_len);
}
//239b3e
```

4.4 FFT B double'ax

```
using cd = complex<double>;
const double PI = acos(-1);
void fft(vector<cd> & a, bool invert) {
  int n = a.size();
  for (int i = 1, j = 0; i < n; i++) {
    int bit = n >> 1;
    for (; j & bit; bit >>= 1)
      j ^= bit;
    j ^= bit;
    if (i < j)</pre>
      swap(a[i], a[j]);
  }
  for (int len = 2; len <= n; len <<= 1) {</pre>
    double ang = 2 * PI / len * (invert ? -1 : 1);
    cd wlen(cos(ang), sin(ang));
    for (int i = 0; i < n; i += len) {</pre>
      cd w(1);
      for (int j = 0; j < len / 2; j++) {
        cd u = a[i+j], v = a[i+j+len/2] * w;
        a[i+j] = u + v;
        a[i+j+len/2] = u - v;
        w *= wlen;
      }
    }
  }
  if (invert) {
    for (cd & x : a)
      x /= n;
  }
vector<int> multiply(vector<int> const& a, vector<int>
     const& b) {
  vector<cd> fa(a.begin(), a.end()), fb(b.begin(), b.
   end());
  int n = 1;
  while (n < a.size() + b.size())</pre>
   n <<= 1:
  fa.resize(n);
  fb.resize(n);
  fft(fa, false);
  fft(fb, false);
  for (int i = 0; i < n; i++)</pre>
    fa[i] *= fb[i];
  fft(fa, true);
  vector<int> result(n);
  for (int i = 0; i < n; i++)</pre>
    result[i] = round(fa[i].real());
  while(!result.empty() && !result.back()) result.
    pop_back();
  return result;
//35d9d0
```

5 Структуры данных

5.1 Дерево Фенвика

```
int fe[maxn];
void pl(int pos,int val) {while(pos<maxn) {fe[pos]+=
    val;pos|=(pos+1);}
int get(int pos) {int ans=0;while(pos>=0) {ans+=fe[pos
    ];pos&=(pos+1);--pos;} return ans;} /// [0,pos] -
    vkluchitelno!!!
```

```
int get(int 1,int r) {return get(r-1)-get(l-1);} ///
    sum of [1,r)

//2991a1
```

```
5.2 Дерево отрезков в точке
template<typename T, typename U>
struct SegmentTree {
  int h, n;
 T neutral;
 U unite;
 vector<T> data;
 template<typename I>
 SegmentTree(int sz, T neutral, U unite, I init) : h(
     lg(sz) + 1), n(1 << h), neutral(neutral), unite(</pre>
    unite), data(2 * n) {
    for (int i = 0; i < sz; ++i) data[i + n] = init(i)</pre>
    for (int i = n - 1; i > 0; --i) data[i] = unite(
    data[2 * i], data[2 * i + 1]);
 SegmentTree(int sz, T neutral, U unite) : h(__lg(sz)
     + 1), n(1 << h), neutral(neutral), unite(unite),
    data(2 * n, neutral) {}
 void set(int i, T x) {
    data[i += n] = x;
    for (i /= 2; i > 0; i /= 2) data[i] = unite(data[2
     * i], data[2 * i + 1]);
 T get(int 1, int r) {
    T leftRes = neutral, rightRes = neutral;
    for (1 += n, r += n; 1 < r; 1 /= 2, r /= 2) {
      if (1 & 1) leftRes = unite(leftRes, data[1++]);
      if (r & 1) rightRes = unite(data[--r], rightRes)
    return unite(leftRes, rightRes);
  int left(int i) {
    int lvl = __lg(i);
    return (i & ((1 << lvl) - 1)) * (1 << (h - lvl));</pre>
  int right(int i) {
    int lvl = __lg(i);
    return ((i & ((1 << lvl) - 1)) + 1) * (1 << (h -
  }
  // 1 \in [0; n) \&\& ok(get(1, 1), 1);
  // returns last r: ok(get(l, r), r)
  template<typename C>
  int lastTrue(int 1, C ok) {
    T cur = neutral;
    1 += n;
    do {
      1 >>= __builtin_ctz(1);
      T with1 = unite(cur, data[1]);
      if (ok(with1, right(l))) {
        cur = with1;
        ++1;
      } else {
        while (1 < n) {</pre>
          T with2 = unite(cur, data[2 * 1]);
          if (ok(with2, right(2 * 1))) {
            cur = with2;
            1 = 2 * 1 + 1;
          } else {
            1 = 2 * 1;
          }
        return 1 - n;
    } while (1 & (1 - 1));
    return n;
```

```
// r \in [0; n) && ok(get(r, r), r);
  // returns first 1: ok(get(1, r), 1)
  template<typename C>
  int firstTrue(int r, C ok) {
   T cur = neutral;
   r += n;
    while (r & (r - 1)) {
     r >>= __builtin_ctz(r);
T with1 = unite(data[--r], cur);
      if (ok(with1, left(r))) {
        cur = with1:
      } else {
        while (r < n) {
          T with2 = unite(data[2 * r + 1], cur);
          if (ok(with2, left(2 * r + 1))) {
            cur = with2;
            r = 2 * r;
          } else {
            r = 2 * r + 1;
          }
        return r - n + 1;
      }
    }
   return 0;
 }
}:
//64190d
5.3 Массовое дерево отрезков
//#ifdef LOCAL
//int __lg(int x) { return 63 - __builtin_clzll(x); }
//#endif
template<typename Data, typename Mod, typename
   UniteData, typename UniteMod, typename Apply>
struct MassSegmentTree {
 int h, n;
 Data zd;
 Mod zm;
 vector<Data> data;
  vector<Mod> mod;
 UniteData ud; // Data (Data, Data)
 UniteMod um; // Mod (Mod, Mod);
 Apply a; // Data (Data, Mod, int); last argument is
    the length of current segment (could be used for
    range += and sum counting, for instance)
  template<typename I>
 MassSegmentTree(int sz, Data zd, Mod zm, UniteData
    ud, UniteMod um, Apply a, I init) : h(__lg(sz) +
    1), n(1 \ll h), zm(zm), zd(zd), data(2 * n, zd),
    mod(n, zm), ud(ud), um(um), a(a) {
   for (int i = 0; i < sz; ++i) data[i + n] = init(i)</pre>
    for (int i = n - 1; i > 0; --i) data[i] = ud(data
    [2 * i], data[2 * i + 1]);
 {\tt MassSegmentTree(int\ sz,\ Data\ zd,\ Mod\ zm,\ UniteData}
    ud, UniteMod um, Apply a) : h(\underline{lg(sz)} + 1), n(1
    << h), zm(zm), zd(zd), data(2 * n, zd), mod(n, zm)
    , ud(ud), um(um), a(a) {}
 void push(int i) {
    if (mod[i] == zm) return;
    apply(2 * i, mod[i]);
    apply(2 * i + 1, mod[i]);
   mod[i] = zm;
```

// is used only for apply

// used only for descent
int left(int i) {

int lvl = __lg(i);

int length(int i) { return 1 << (h - __lg(i)); }</pre>

```
return (i & ((1 << lvl) - 1)) * (1 << (h - lvl));</pre>
// used only for descent
int right(int i) {
  int lvl = __lg(i);
  return ((i & ((1 << lvl) - 1)) + 1) * (1 << (h -
  lv1));
template<typename S>
void apply(int i, S x) {
  data[i] = a(data[i], x, length(i));
  if (i < n) mod[i] = um(mod[i], x);
void update(int i) {
  if (mod[i] != zm) return;
  data[i] = ud(data[2 * i], data[2 * i + 1]);
template<typename S>
void update(int 1, int r, S x) { // [1; r)
  1 += n, r += n;
  for (int shift = h; shift > 0; --shift) {
    push(1 >> shift);
    push((r - 1) >> shift);
  for (int lf = 1, rg = r; lf < rg; lf /= 2, rg /=</pre>
  2) {
    if (lf & 1) apply(lf++, x);
    if (rg & 1) apply(--rg, x);
  for (int shift = 1; shift <= h; ++shift) {</pre>
    update(1 >> shift);
    update((r - 1) >> shift);
Data get(int 1, int r) { // [1; r)
  1 += n, r += n;
  for (int shift = h; shift > 0; --shift) {
    push(1 >> shift);
    push((r - 1) >> shift);
  Data leftRes = zd, rightRes = zd;
  for (; 1 < r; 1 /= 2, r /= 2) {
    if (1 & 1) leftRes = ud(leftRes, data[1++]);
    if (r & 1) rightRes = ud(data[--r], rightRes);
  return ud(leftRes, rightRes);
}
// 1 \in [0; n) \&\& ok(get(1, 1), 1);
// returns last r: ok(get(l, r), r)
template<typename C>
int lastTrue(int 1, C ok) {
  1 += n;
  for (int shift = h; shift > 0; --shift) push(l >>
  shift);
  Data cur = zd;
  do {
    1 >>= __builtin_ctz(1);
    Data with1;
    with1 = ud(cur, data[1]);
    if (ok(with1, right(1))) {
      cur = with1;
      ++1;
    } else {
      while (1 < n) {
        push(1);
        Data with2;
        with2 = ud(cur, data[2 * 1]);
        if (ok(with2, right(2 * 1))) {
          cur = with2;
          1 = 2 * 1 + 1;
        } else {
          1 = 2 * 1;
      }
```

```
return 1 - n;
    } while (1 & (1 - 1));
    return n;
  // r \in [0; n) && ok(get(r, r), r);
  // returns first 1: ok(get(1, r), 1)
  template<typename C>
  int firstTrue(int r, C ok) {
    r += n:
    for (int shift = h; shift > 0; --shift) push((r -
    1) >> shift);
    Data cur = zd;
    while (r & (r - 1)) {
      r >>= __builtin_ctz(r);
      Data with1;
      with1 = ud(data[--r], cur);
      if (ok(with1, left(r))) {
        cur = with1;
      } else {
        while (r < n) {
          push(r);
          Data with2;
          with 2 = ud(data[2 * r + 1], cur);
          if (ok(with2, left(2 * r + 1))) {
            cur = with2:
            r = 2 * r;
          } else {
            r = 2 * r + 1;
        }
        return r - n + 1;
    }
    return 0;
};
//7a7099
```

5.4 Битовый бор

```
template<unsigned int sz,typename T=int>
struct binarytrie{
 using Bit=typename conditional<sz<=32,unsigned int,
    unsigned long long>::type;
  struct node{
   T cnt;
   array<int,2>nxt;
   node():cnt(0),nxt({-1,-1}){}
 };
 vector<node>v;
 binarytrie(){v.emplace_back();}
 void insert(Bit x){add(x,1);}
  void erase(Bit x) {add(x,-1);}
  void add(Bit x,T k)
    assert(0 \le x \& (x >> sz) == 0);
    int p=0;
   v[p].cnt+=k;
    for(int i=sz;i--;)
      int j=x>>i&1;
      if(v[p].nxt[j]==-1)
        v[p].nxt[j]=v.size();
        v.emplace_back();
      p=v[p].nxt[j];
      v[p].cnt+=k;
    }
 T count(Bit x,Bit xor_val=0)const//[0,x)
   assert(0<=xor val&&(xor val>>sz)==0);
    if(x<0)return 0;</pre>
    else if(x>>sz)return v[0].cnt;
    T ret=0;
    int p=0;
    for(int i=sz;i--;)
```

```
int j=x>>i&1,k=xor_val>>i&1;
    if(j==0)p=v[p].nxt[k];
    else
    {
      if(v[p].nxt[k] \ge 0) ret += v[v[p].nxt[k]].cnt;
      p=v[p].nxt[!k];
    if(p==-1)break;
  }
  return ret;
Bit max(Bit xor_val=0)const
{
  assert(0 \le xor_val & (xor_val >> sz) == 0);
  int p=0;
  Bit ret=0;
  if(v[p].cnt==0)return ret;
  for(int i=sz:i--:)
    ret<<=1;
    int k=xor_val>>i&1;
    if(v[p].nxt[!k] \ge 0\&v[v[p].nxt[!k]].cnt>0)
      p=v[p].nxt[!k];
      ret|=1;
    }
    else p=v[p].nxt[k];
  return ret;
Bit min(Bit xor_val=0)const
  assert(0 <= xor_val&&(xor_val>>sz)==0);
  int p=0;
  Bit ret=0;
  for(int i=sz;i--;)
    ret<<=1;
    int k=xor_val>>i&1;
    if(v[p].nxt[k] \ge 0\&v[v[p].nxt[k]].cnt > 0)p=v[p].
  nxt[k];
    else
    {
      p=v[p].nxt[!k];
      ret |=1;
  }
  return ret;
Bit find_by_order(T ord,Bit xor_val=0)const
  assert(0 <= xor_val && (xor_val >> sz) == 0);
  assert(0<=ord&&ord<v[0].cnt);
  int p=0;
  Bit ret=0;
  for(int i=sz;i--;)
    ret<<=1;
    int k=xor_val>>i&1;
    if(v[p].nxt[k]>=0)
    {
      if(ord>=v[v[p].nxt[k]].cnt)
      {
        ord-=v[v[p].nxt[k]].cnt;
        p=v[p].nxt[!k];
        ret|=1;
      else p=v[p].nxt[k];
    }
    else
    {
      p=v[p].nxt[!k];
      ret|=1;
    }
  }
  return ret;
T order_of_key(Bit x,Bit xor_val=0)const{return
  count(x,xor_val);}
```

using ordered_set = tree<int, null_type, less<>,

rb_tree_tag, tree_order_statistics_node_update>;

```
};
binarytrie<32>bt;
//0b3855
5.5 Ordered set

#include <ext/pb_ds/assoc_container.hpp>
#include <ext/pb_ds/tree_policy.hpp>
using namespace __gnu_pbds;
```

//f589b9 **5.6 Convex hull trick**

using namespace std;

```
int div_up(int a, int b) { return a/b+((a^b)>0&&a%b);
    } // divide a by b rounded up
const int LQ = ..., RQ = ...; //leftmost query,
   rightmost query
int in(ii L, int x) {
 return L.x * x + L.y;
struct Hull {
vector <pair <int, int> > lines;
vector <int> borders;
void push(ii L) {
 while (lines.size() && in(L,borders.back()) < in(</pre>
    lines.back(),borders.back())) {
    lines.pop_back();
   borders.pop_back();
 if (lines.empty()) {
   lines = \{L\};
   borders = {LQ};
 else if (lines.back().x > L.x) {
    int x = div_up(L.y - lines.back().y, lines.back().
    x - L.x);
    if (x \le RQ) {
      lines.app(L);
      borders.app(x);
 }
Hull (){}
Hull (vector <ii> a) {
 auto comp = [&] (ii u, ii v) {
   return u.x > v.x || (u.x == v.x && u.y < v.y);</pre>
 1:
  sort(all(a), comp);
 for (auto L : a) {
   push(L);
 }
int get(int x) {
 int pos = upper_bound(all(borders), x) - borders.
   begin();
 assert(pos>0);
 pos--;
 return in(lines[pos],x);
};
//04555a
```

5.7 Центроиды

```
vector<int> sz(n), lvl(n, -1);
auto dfs = [&](auto dfs, int cur, int prev) -> int {
  if (lvl[cur] != -1) return 0;
  sz[cur] = 1;
  for (auto [nxt, w] : g[cur]) {
    if (nxt != prev) sz[cur] += dfs(dfs, nxt, cur);
  }
  return sz[cur];
};
```

```
auto find = [&](auto find, int cur, int prev, int tot)
     -> int {
  int bch = -1, bsz = 0:
  for (auto [nxt, w] : g[cur]) {
    if (nxt == prev || lvl[nxt] != -1) continue;
    if (sz[nxt] > bsz) {
      bch = nxt;
      bsz = sz[nxt];
    }
  if (bsz + bsz <= tot) return cur;</pre>
 return find(find, bch, cur, tot);
dfs(dfs, 0, 0);
auto c = find(find, 0, 0, sz[0]);
vector<pair<int, int>> stack{{c, 0}};
while (!stack.empty()) {
  auto [centroid, 1] = stack.back();
  stack.pop_back();
  lvl[centroid] = 1;
  for (auto [nxt, w] : g[centroid]) {
    if (lvl[nxt] != -1) continue;
    dfs(dfs, nxt, centroid);
    int new_centroid = find(find, nxt, centroid, sz[
    nxtl);
    stack.push_back({new_centroid, lvl[centroid] + 1})
  }
//0e1e52
5.8 Дерево Ли Чао
struct Line{
 int a, b;
 Line(){}
 Line (int a, int b) : a(a), b(b) {}
  int get(int x) { return a + b * x;}
struct Lichao {
 int n;
  vector <int> x;
  vector <Line> t;
 Lichao(){}
 Lichao (int n, vector\langle int \rangle x) : n(n), t(n \langle \langle 2 \rangle, Line
    (inf, 0)), x(x) {}
 void put(int v, int 1, int r, Line L) {
    if (1 + 1 == r) {
      if (L.get(x[1]) < t[v].get(x[1])) {</pre>
        t[v] = L;
      }
      return;
    }
    int m = (1 + r) / 2;
    if (L.get(x[m]) < t[v].get(x[m])) {
      swap(L, t[v]);
    if (L.b > t[v].b) {
      put(2 * v + 1, 1, m, L);
    }
    else {
      put(2 * v + 2, m, r, L);
  int get(int v, int l, int r, int i) {
    if (1 + 1 == r) {
     return t[v].get(x[1]);
    int m = (1 + r) / 2;
    int ans = t[v].get(x[i]);
    if (i < m) {
      ans = min(ans, get(2 * v + 1, 1, m, i));
    } else {
      ans = min(ans, get(2 * v + 2, m, r, i));}
    return ans;
```

```
void put(Line L) {
   put(0, 0, n, L);
}
int get(int i) {
   return get(0, 0, n, i);
};
//99f5fa
```

```
5.9 Min-Kinetic Segment Tree
I guess the source is https://koosaga.com/307
using lint = long long;
const lint inf = 4e18;
const int MAXT = 4100000;
using pi = array<lint, 2>;
struct line {
 lint A, B;
 int idx;
 lint eval(lint x) { return A * x + B; }
  // returns the x-intercept of intersection "strictly
   " larger than T
  lint cross_after(line &x, lint T) {
   if (x.A == A) {
     return inf;
   lint up = x.B - B;
   lint dn = A - x.A;
    if (dn < 0) {
     dn *= -1;
     up *= -1;
   lint incep = (up \le 0 ? -((-up) / dn) : (up + dn -
    1) / dn);
    if (incep > T)
     return incep;
    return inf;
 }
};
struct kst { // min kinetic segment tree
  line tree[MAXT];
 lint melt[MAXT], T;
 pi lazy[MAXT];
 bool cmp(line &a, line &b) {
    lint l = a.eval(T), r = b.eval(T);
    if (1 != r)
      return 1 > r;
   return a.A > b.A;
 }
 void pull(int p) {
    tree[p] = cmp(tree[2 * p], tree[2 * p + 1]) ? tree
    [2 * p + 1] : tree[2 * p];
   melt[p] = min(\{melt[2 * p], melt[2 * p + 1], tree)
    [2 * p].cross_after(tree[2 * p + 1], 0)});
  void init(int s, int e, int p, vector<line> &1) {
    if (s == e) {
      tree[p] = l[s];
      melt[p] = inf;
      lazy[p] = \{0, 0\};
   lazy[p] = {0, 0};
    int m = (s + e) / 2;
    init(s, m, 2 * p, 1);
   init(m + 1, e, 2 * p + 1, 1);
   pull(p);
 void lazydown(int p) {
```

```
for (int i = 2 * p; i < 2 * p + 2; i++) {
      lazy[i][0] += lazy[p][0];
      lazy[i][1] += lazy[p][1];
      tree[i].B += lazy[p][0] * tree[i].A + lazy[p
    ][1];
      melt[i] -= lazy[p][0];
    lazy[p][0] = lazy[p][1] = 0;
 void propagate(int p) {
    if (melt[p] > 0)
      return;
    lazydown(p);
    propagate(2 * p);
    propagate(2 * p + 1);
   pull(p);
 lint query(int s, int e, int ps, int pe, int p = 1)
    if (e < ps || pe < s)</pre>
      return inf;
    if (s <= ps && pe <= e)
     return tree[p].eval(0);
    int pm = (ps + pe) / 2;
    lazydown(p);
    return min(query(s, e, ps, pm, 2 * p), query(s, e,
     pm + 1, pe, 2 * p + 1));
 void heaten(int s, int e, int ps, int pe, int p,
    lint v) {
    if (e < ps || pe < s)</pre>
      return;
    if (s <= ps && pe <= e) {</pre>
      lazy[p][0] += v;
      tree[p].B += v * tree[p].A;
      melt[p] -= v;
      propagate(p);
      return;
    lazydown(p);
    int pm = (ps + pe) / 2;
    heaten(s, e, ps, pm, 2 * p, v);
    heaten(s, e, pm + 1, pe, 2 * p + 1, v);
    pull(p);
 void add(int s, int e, int ps, int pe, int p, lint v
    if (e < ps || pe < s)</pre>
      return;
    if (s <= ps && pe <= e) {
      lazy[p][1] += v;
      tree[p].B += v;
      return:
    lazydown(p);
    int pm = (ps + pe) / 2;
    add(s, e, ps, pm, 2 * p, v);
    add(s, e, pm + 1, pe, 2 * p + 1, v);
    pull(p);
 void init(vector<line> &1, lint _T) {
   n = 1.size();
    T = _T;
    init(0, n - 1, 1, 1);
 }
};
//66f9a9
```

6 Строковые алгоритмы

6.1 Префикс-функция

```
vector<int> prefix_function(string s) {
  vector<int> p(s.size());
```

```
for (int i = 1; i < s.size(); ++i) {</pre>
   p[i] = p[i - 1];
    while (p[i] \&\& s[p[i]] != s[i]) p[i] = p[p[i] -
    11:
   p[i] += s[i] == s[p[i]];
 return p;
//c33adc
```

6.2 Z-функция

```
vector<int> z_function (string s) { // z[i] - lcp of s
     and s[i:]
 int n = (int) s.length();
 vector<int> z (n);
 for (int i=1, l=0, r=0; i<n; ++i) {</pre>
 if (i <= r)</pre>
  z[i] = min (r-i+1, z[i-1]);
  while (i+z[i] < n \&\& s[z[i]] == s[i+z[i]])
   ++z[i];
  if (i+z[i]-1 > r)
  1 = i, r = i+z[i]-1;
}
//85d656
```

6.3 Алгоритм Манакера

```
vector<int> manacher_odd(const string &s) {
  vector<int> man(s.size(), 0);
  int 1 = 0, r = 0;
 int n = s.size();
  for (int i = 1; i < n; i++) {</pre>
    if (i <= r) {</pre>
     man[i] = min(r - i, man[l + r - i]);
   while (i + man[i] + 1 < n && i - man[i] - 1 >= 0
    && s[i + man[i] + 1] == s[i - man[i] - 1]) {
     man[i]++;
   if (i + man[i] > r) {
     l = i - man[i];
      r = i + man[i];
   }
 }
  return man;
// abacaba : (0 1 0 3 0 1 0)
// abbaa : (0 0 0 0 0)
vector <int> manacher_even(const string &s) {
 assert(s.size());
 string t;
  for (int i = 0; i + 1 < s.size(); ++i) {</pre>
   t += s[i];
   t += '#';
 t += s.back();
 auto odd = manacher_odd(t);
  vector <int> ans;
 for (int i = 1; i < odd.size(); i += 2) {</pre>
   ans.push_back((odd[i]+1)/2);
 return ans;
// abacaba : (0 0 0 0 0 0)
// abbaa : (0 2 0 1)
  auto pal = [&] (int i, int from, int len) {
    if (len == 0) {
        return true;
    int m = len/2;
    if (len & 1) {
        return o[i][from + m] >= m;
    }
        return e[i][from + m - 1] >= m;
```

```
};
//d74301
```

6.4 Суфмассив

```
Переработанный китайский суффмассив
const int inf = 1e9;
struct rmq {
  int n;
  vector<int> a;
 void build(const vector<int> &x) {
    assert(x.size() == n);
    for (int i = 0; i < n; ++i) a[n + i] = x[i];
    for (int i = n - 1; i > 0; --i) a[i] = min(a[2 * i])
    ], a[2 * i + 1]);
 rmq(int n) : n(n), a(2 * n, inf) {}
 void put(int i, int x) {
    a[i + n] = min(a[i + n], x);
    for (i = (i + n) / 2; i > 0; i /= 2) {
      a[i] = min(a[i * 2], a[i * 2 + 1]);
 int getMin(int 1, int r) { //[1;r)
    assert(l < r);
    int res = inf;
    for (1 += n, r += n; 1 < r; 1 /= 2, r /= 2) {
      if (1 & 1) res = min(res, a[1++]);
      if (r & 1) res = min(res, a[--r]);
    return res;
 }
};
template <typename T>
vector <int> SA(const T &a) {
 int m = *max_element(all(a)) + 1, n = a.size();
  vector \langle int \rangle sa(n), nsa(n), pre(max(n, m)), x(a.
    begin(), a.end()), y(n);
  for (int e : x) pre[e]++;
  for (int i = 1; i < m; ++i) pre[i] += pre[i - 1];</pre>
  for (int i = 0; i < n; ++i) sa[--pre[x[i]]]=i;</pre>
  int dif = 1;
 y[sa.front()]=0;
  for (int i = 1; i < n; ++i) {</pre>
    dif += x[sa[i]]!=x[sa[i-1]];
   y[sa[i]] = dif - 1;
  }
 x = y;
 for (int h = 1; dif < n; h *= 2) {
    fill(all(pre), 0);
    for (int e : x) pre[e]++;
    for (int i = 1; i < dif; ++i) pre[i] += pre[i -</pre>
    for (int t = n; t--; ) {
     int i = sa[t];
      if (i>=h) {
       nsa[--pre[x[i-h]]]=i-h;
      else if (i + 1 != h) {
        nsa[--pre[x[i-h+n+1]]]=i-h+n+1;
    }
    nsa[--pre[x[n - h]]]=n-h;
    auto getr = [&] (int i) {
     if (i + h < n) {
       return x[i + h];
      else {
        return x[i + h - n - 1];
    dif = 1;
    v[sa.front()]=0;
    for (int i = 1; i < n; ++i) {</pre>
      if (x[sa[i]]!=x[sa[i-1]] || sa[i-1]+h==n) {
        dif++;
```

```
else {
        dif += getr(sa[i]) != getr(sa[i-1]);
      y[sa[i]]=dif-1;
   x = y;
  }
  return sa;
template <typename T>
struct suar {
  vector <int> sa, lcp, pos; rmq t;
  suar (const T &a) : t((int)a.size() - 1) {
    sa = SA(a);
    int n = (int)a.size(), k = 0;
    lcp.resize(n - 1);
    pos.resize(n);
    for (int i = 0; i < n; ++i) pos[sa[i]] = i;
    for (int i = 0; i < n; ++i) {</pre>
      if (pos[i]+1<n) {</pre>
        int j = sa[pos[i]+1];
        while (i+k<n&&j+k<n&&a[i+k]==a[j+k])k++;
        lcp[pos[i]]=k;
      if (k) {
        k--;
      }
    t.build(lcp);
  int getLcp(int i, int j) {
    i = pos[i]; j = pos[j];
    if (j < i) {</pre>
      swap(i, j);
    if (i == j) {
      return inf;
    else {
     return t.getMin(i, j);
  }
};
//6327c9
```

6.5 Алгоритм Ахо — Корасик

6.6 Алгоритм Ахо Корасик

```
struct node{
 int next[alpha] = {}, link[alpha] = {};
  int suf = 0;
 11 \text{ visited} = 0, \text{ ans} = 0;
 vector<int> term;
 node() {}
};
vector<node> mem;
int get_next(int nd, char c) {
 if (!mem[nd].next[c - a]) { mem[nd].next[c - a] =
    mem.size(); mem.emplace_back(); }
  return mem[nd].next[c - a];
void find(string s, vector<string> t) {
 mem.reserve(1e6 + 100); mem.clear();
 mem.emplace_back();mem.emplace_back();
  // Oth element is nullptr, 1st is the root
 int q = t.size();
  for (int j = 0; j < q; ++j) {
    int cur = 1;
    for (char c : ts[j]) cur = get_next(cur, c);
   mem[cur].term.push_back(j);
  vector<int> bfs_order;
  queue<int> bfs;
```

```
{
      node &root = mem[1];
      root.suf = 1:
      for (char c = a; c < a + alpha; ++c) {
          root.link[c - a] = (root.next[c - a] ? root.
    next[c - a] : 1);
      bfs.push(1);
 while (!bfs.empty()) {
    int cur_idx = bfs.front();
   bfs.pop();
   node &cur = mem[cur_idx];
   bfs_order.push_back(cur_idx);
    for (char c = a; c < a + alpha; ++c) {
     int nxt_idx = cur.next[c - a];
     if (!nxt_idx) continue;
     node &nxt = mem[nxt_idx];
     nxt.suf = (cur_idx == 1 ? 1 : mem[cur.suf].link[
    c - al);
     for (char c = a; c < a + alpha; ++c) {</pre>
       nxt.link[c - a] = (nxt.next[c - a] ? nxt.next[
    c - a] : mem[nxt.suf].link[c - a]);
     bfs.push(nxt_idx);
   }
  }
  // do something
//23bad7
```

6.7 Дерево палиндромов

6.8 Дерево палиндромов

```
struct palindromic{
 int n;
  vector<int> p, suf{0, 0}, len{-1, 0};
 vector<array<int, alpha>> to{{}, {}};
 int sz = 2;
 palindromic(const string &s) : n(s.size()), p(n + 1,
     1) {
    suf.reserve(n);
    len.reserve(n);
    for (int i = 0; i < n; ++i) {</pre>
     auto check = [&](int 1) { return i > 1 && s[i]
    == s[i - 1 - 1]; \};
      int par = p[i];
      while (!check(len[par])) par = suf[par];
      if (to[par][s[i] - a]) {
       p[i + 1] = to[par][s[i] - a];
        continue;
      p[i + 1] = sz++;
      to[par][s[i] - a] = p[i + 1];
      to.emplace_back();
      len.emplace_back(len[par] + 2);
      do {
       par = suf[par];
      } while (!check(len[par]));
      int link = to[par][s[i] - a];
      if (link == p[i + 1]) link = 1;
      suf.emplace_back(link);
 }
};
//6aecca
```

7 Потоки

7.1 Алгоритм Диница

```
#define pb push_back
struct Dinic{
struct edge{
   int to, flow, cap;
};
const static int N = 555; //count of vertices
```

```
vector<edge> e;
vector<int> g[N + 7];
int dp[N + 7];
int ptr[N + 7];
void clear(){
  for (int i = 0; i < N + 7; i++) g[i].clear();</pre>
  e.clear();
void addEdge(int a, int b, int cap){
  g[a].pb(e.size());
  e.pb({b, 0, cap});
  g[b].pb(e.size());
  e.pb({a, 0, 0});
int minFlow, start, finish;
bool bfs(){
  for (int i = 0; i < N; i++) dp[i] = -1;
  dp[start] = 0;
  vector<int> st;
  int uk = 0;
  st.pb(start);
  while(uk < st.size()){</pre>
    int v = st[uk++];
    for (int to : g[v]){
     auto ed = e[to];
      if (ed.cap - ed.flow >= minFlow && dp[ed.to] ==
    -1) {
        dp[ed.to] = dp[v] + 1;
        st.pb(ed.to);
    }
  return dp[finish] != -1;
int dfs(int v, int flow){
  if (v == finish) return flow;
  for (; ptr[v] < g[v].size(); ptr[v]++){</pre>
    int to = g[v][ptr[v]];
    edge ed = e[to];
    if (ed.cap - ed.flow >= minFlow && dp[ed.to] == dp
    [v] + 1){}
      int add = dfs(ed.to, min(flow, ed.cap - ed.flow)
    );
      if (add) {
        e[to].flow += add;
        e[to ^ 1].flow -= add;
        return add;
    }
  }
  return 0;
int dinic(int start, int finish){
  Dinic::start = start;
  Dinic::finish = finish;
  int flow = 0;
  for (minFlow = (1 << 30); minFlow; minFlow >>= 1){
    while(bfs()){
      for (int i = 0; i < N; i++) ptr[i] = 0;</pre>
      while(int now = dfs(start, (int)2e9 + 7)) flow
    += now;
    }
  return flow;
} dinic;
//15c079
7.2 Mincost k-flow
struct edge {
  int next, capacity, cost, flow = 0;
  edge() = default;
```

```
edge(int next, int capacity, int cost) : next(next),
     capacity(capacity), cost(cost) {}
  int rem() const { return capacity - flow; }
 int operator+=(int f) { return flow += f; }
 int operator-=(int f) { return flow -= f; }
};
auto addEdge = [&](auto from, auto next, auto capacity
     int cost) {
  g[from].push_back(e.size());
 e.emplace_back(next, capacity, cost);
 g[next].push back(e.size());
  e.emplace_back(from, 0, -cost);
/\star in case of undirected graph use this:
addEdge(u, v, capacity, cost);
addEdge(v, u, capacity, cost);
*/
vector<ll> phi(n, 0);
auto fordBellman = [&](int s, int t) {
 phi.assign(n, 0);
  for (int iter = 0; iter < n; ++iter) {</pre>
    bool changed = false;
    for (int u = 0; u < n; ++u) {
     for (auto index : q[u]) {
        auto edge = e[index];
        if (edge.rem() > 0 && phi[edge.next] > phi[u]
    + edge.cost) {
          phi[edge.next] = phi[u] + edge.cost;
          changed = true;
        1
     }
    if (!changed) break;
 }
};
fordBellman(s, t);
// now shortest path using dijkstra with potentials
vector<ll> dist:
vector<int> from;
vector<bool> cnt;
auto dijkstra = [&](int s, int t) {
  dist.assign(n, 1e18);
  from.assign(n, -1);
  cnt.assign(n, false);
 dist[s] = 0;
  set <pair <int, int> > se;
  se.insert({0, s});
  while ((int)(se.size())) {
    int cur = se.begin()->y;
    se.erase(se.begin());
    cnt[curl = true;
    for (int index : g[cur]) {
      auto &edge = e[index];
      if (edge.rem() == 0) continue;
     ll weight = edge.cost + phi[cur] - phi[edge.next
    1;
     if (dist[edge.next] > dist[cur] + weight) {
        se.erase({dist[edge.next], edge.next});
        dist[edge.next] = dist[cur] + weight;
        se.insert({dist[edge.next], edge.next});
        from[edge.next] = cur;
    }
  }
  if (dist[t] == (11) 1e18) return -1LL;
  11 \cos t = 0;
  for (int p = t; p != s; p = from[p]) {
    for (auto index : g[from[p]]) {
      auto &edge = e[index];
     11 weight = edge.cost + phi[from[p]] - phi[edge.
    next];
      if (edge.rem() > 0 && edge.next == p && dist[
    edge.next] == dist[from[p]] + weight) {
        edge += 1;
        e[index ^ 1] -= 1;
        cost += edge.cost;
        break;
```

```
}
    }
  for (int i = 0; i < n; ++i) {</pre>
   phi[i] += dist[i];
  return cost;
};
11 cost = 0;
for (int flow = 0; flow < k; ++flow) {</pre>
  ll a = dijkstra(s, t);
  if (a == -1) {
    cout << "-1\n";
    return;
  cost += a;
}
// now recover answer
auto findPath = [&](int s, int t) {
  vector<int> ans;
  int cur = s;
  while (cur != t) {
    for (auto index : g[cur]) {
      auto &edge = e[index];
      if (edge.flow <= 0) continue;</pre>
      edge -= 1;
      e[index ^ 1] += 1;
      ans.push_back(index / 4);
// index / 4 because each edge has 4 copies
      cur = edge.next;
      break;
    }
  1
  return ans;
};
for (int flow = 0; flow < k; ++flow) {
 auto p = findPath(s, t);
cout << p.size() << ' ';</pre>
  for (int x : p) cout << x + 1 << ' ';</pre>
  cout << '\n';
//94b9cb
```

8 Гамильтоновы путь и цикл

https://codeforces.com/blog/entry/90513, https://codeforces.com/blog/entry/90743.

8.1 Link-cut tree

namespace LCT {

```
vector<vi> ch;
vi fa, rev;
void init(int n) {
  ch.resize(n + 1);
  fa.resize(n + 1);
  rev.resize(n + 1);
  for (int i = 0; i <= n; i++)</pre>
    ch[i].resize(2),
    ch[i][0] = ch[i][1] = fa[i] = rev[i] = 0;
bool isr(int a)
  return !(ch[fa[a]][0] == a || ch[fa[a]][1] == a);
void pushdown(int a)
{
  if(rev[a])
    rev[ch[a][0]] ^= 1, rev[ch[a][1]] ^= 1;
    swap(ch[a][0], ch[a][1]);
    rev[a] = 0;
  }
void push(int a)
  if(!isr(a)) push(fa[a]);
 pushdown(a);
void rotate(int a)
```

```
int f = fa[a], gf = fa[f];
   int tp = ch[f][1] == a;
   int son = ch[a][tp ^ 1];
   if(!isr(f))
     ch[gf][ch[gf][1] == f] = a;
   fa[a] = gf;
   ch[f][tp] = son;
   if(son) fa[son] = f;
   ch[a][tp ^ 1] = f, fa[f] = a;
 void splay(int a)
   push(a);
   while(!isr(a))
     int f = fa[a], gf = fa[f];
     if(isr(f)) rotate(a);
      {
        int t1 = ch[gf][1] == f, t2 = ch[f][1] == a;
        if(t1 == t2) rotate(f), rotate(a);
        else rotate(a), rotate(a);
   }
 }
 void access(int a)
 {
    int pr = a;
   splay(a);
   ch[a][1] = 0;
   while(1)
     if(!fa[a]) break;
     int u = fa[a];
     splay(u);
     ch[u][1] = a;
     a = u;
   1
   splay(pr);
 }
 void makeroot(int a)
   access(a);
   rev[a] ^= 1;
 void link(int a, int b)
   makeroot(a);
   fa[a] = b;
 void cut(int a, int b)
   makeroot(a);
   access(b);
   fa[a] = 0, ch[b][0] = 0;
 int fdr(int a)
   access(a);
   while(1)
     pushdown(a);
     if (ch[a][0]) a = ch[a][0];
     else {
        splay(a);
        return a;
   }
 }
//647cca
```

8.2 Undirected case

```
#include <bits/stdc++.h>
using namespace std;
namespace hamil {
```

```
template <typename T> bool chkmax(T &x,T y) {return x
  <y?x=y,true:false;}</pre>
template <typename T> bool chkmin(T &x,T y) {return x
  >y?x=y,true:false;}
#define vi vector<int>
#define pb push_back
#define mp make_pair
#define pi pair<int, int>
#define fi first
#define se second
#define 11 long long
using namespace LCT;
vector<vi> used;
unordered_set<int> caneg;
void cut(int a, int b) {
 LCT::cut(a, b);
  for (int s = 0; s < 2; s++) {
    for (int i = 0; i < used[a].size(); i++)</pre>
      if (used[a][i] == b) {
        used[a].erase(used[a].begin() + i);
        break;
    if (used[a].size() == 1) caneg.insert(a);
    swap(a, b);
void link(int a, int b) {
 LCT::link(a, b);
  for (int s = 0; s < 2; s++) {</pre>
    used[a].pb(b);
    if (used[a].size() == 2) caneg.erase(a);
    swap(a, b);
  }
vi work(int n, vector<pi> eg, ll mx_ch = -1) {
  // mx_ch : max number of adding/replacing default
   is (n + 100) * (n + 50)
  // n : number of vertices. 1-indexed.
  // eg: vector<pair<int, int> > storing all the
  edges.
  // return a vector<int> consists of all indices of
   vertices on the path. return empty list if failed
   to find one.
  LCT::init(n);
  if (mx_ch == -1) mx_ch = 111 * (n + 100) * (n +
  50); //default
  used.resize(n + 1);
  caneg.clear();
  for (int i = 1; i <= n; i++) used[i].clear();</pre>
  vector<vi> edges(n + 1);
  for (auto v : eg)
    edges[v.fi].pb(v.se),
    edges[v.se].pb(v.fi);
  for (int i = 1; i <= n; i++)</pre>
    caneg.insert(i);
 mt19937 x(chrono::steady_clock::now().
  time_since_epoch().count());
  int tot = 0;
  while (mx_ch >= 0) {
  // cout << tot << ' ' << mx_ch << endl;
    vector<pi> eg;
    for (auto v : caneg)
      for (auto s : edges[v])
        eg.pb(mp(v, s));
    shuffle(eg.begin(), eg.end(), x);
    if (eg.size() == 0) break;
    for (auto v : eg) {
      mx ch--;
      int a = v.fi, b = v.se;
      if (used[a].size() < used[b].size()) swap(a, b</pre>
      if (used[b].size() >= 2) continue;
      if (x() & 1) continue;
      if (LCT::fdr(a) == LCT::fdr(b)) continue;
      if (used[a].size() < 2 && used[b].size() < 2)</pre>
```

```
tot++;
        if (used[a].size() == 2) {
          int p = used[a][x() % 2];
          cut(a, p);
        link(a, b);
      if (tot == n - 1) {
        vi cur;
        for (int i = 1; i <= n; i++)</pre>
          if (used[i].size() <= 1) {</pre>
            int pl = i, ls = 0;
            while (pl) {
              cur.pb(pl);
              int flag = 0;
              for (auto v : used[pl])
                if (v != ls) {
                   ls = pl;
                  pl = v;
                   flag = 1;
                   break;
              if (!flag) break;
            break:
          }
        return cur;
    //failed to find a path
    return vi();
 }
}
//c35638
8.3 Directed case
namespace hamil {
  template <typename T> bool chkmax(T &x,T y) {return x
    <y?x=y, true:false; }</pre>
  template <typename T> bool chkmin(T &x,T y){return x
    >y?x=y,true:false;}
  #define vi vector<int>
  #define pb push_back
  #define mp make_pair
  #define pi pair<int, int>
  #define fi first
  #define se second
  #define 11 long long
  using namespace LCT;
  vi out, in;
 vi work(int n, vector<pi> eg, ll mx_ch = -1) {
    // mx_ch : max number of adding/replacing default
     is (n + 100) * (n + 50)
    // n : number of vertices. 1-indexed.
    // eg: vector<pair<int, int> > storing all the
    edges.
```

// return a vector<int> consists of all indices of

out.resize(n + 1), in.resize(n + 1);

to find one.

vertices on the path. return empty list if failed

```
if (in[s] == 0) {
            assert(canin.count(s));
            continue:
          }
          else eg.pb(mp(v, s));
      for (auto v : canin)
        for (auto s : to[v])
          eg.pb(mp(s, v));
      shuffle(eg.begin(), eg.end(), x);
      if (eg.size() == 0) break;
      for (auto v : eg) {
        mx_ch--;
        if (in[v.se] && out[v.fi]) continue;
        if (LCT::fdr(v.fi) == LCT::fdr(v.se)) continue
        if (in[v.se] || out[v.fi])
         if (x() & 1) continue;
        if (!in[v.se] && !out[v.fi])
         tot++;
        if (in[v.se]) {
         LCT::cut(in[v.se], v.se);
          canin.insert(v.se);
          canout.insert(in[v.se]);
          out[in[v.se]] = 0;
          in[v.se] = 0;
        if (out[v.fi]) {
          LCT::cut(v.fi, out[v.fi]);
          canin.insert(out[v.fi]);
          canout.insert(v.fi);
          in[out[v.fi]] = 0;
          out[v.fi] = 0;
        LCT::link(v.fi, v.se);
        canin.erase(v.se);
        canout.erase(v.fi);
        in[v.se] = v.fi;
        out[v.fi] = v.se;
      if (tot == n - 1) {
        vi cur:
        for (int i = 1; i <= n; i++)</pre>
          if (!in[i]) {
            int pl = i;
            while (pl) {
             cur.pb(pl),
             pl = out[pl];
           break:
          }
        return cur;
     }
    //failed to find a path
   return vi();
//43ae60
```

9 Геома

9.1 Примитивы

```
struct Point {
  int x, y;
  Point(){}
  Point (int x_, int y_) {
    x = x_; y = y_;
}
  Point operator + (Point p) {
    return Point(x+p.x,y+p.y);
}
  Point operator - (Point p) {
    return Point(x - p.x, y - p.y);
}
  int operator * (Point p) {
    return x * p.y - y * p.x;
}
  int operator % (Point p) {
    return x * p.x + y * p.y;
}
```

```
bool operator < (Point v) {</pre>
   return (*this) * v > 0;
  bool operator > (Point v) {
   return v < (*this);</pre>
  bool operator <= (Point v) {</pre>
   return (*this) * v >= 0;
} :
bool line(Point a, Point b, Point c) {
 return (b-a)*(c-b)==0;
bool ord(Point a, Point p, Point b) {
 return (p - a)%(p - b)<0;
int hp(Point a) {
  if (a.y == 0) return a.x >= 0;
  return a.y > 0;
bool comp(Point a, Point b) {
  if (hp(a) != hp(b)) return hp(a) < hp(b);
  return a.x * b.y - a.y * b.x > 0;
//a48b68
9.2 Выпуклая оболочка
using pt = pair<int, int>;
#define x first
#define y second
int cross(pt p, pt q) {
```

```
return p.x * q.y - p.y * q.x;
int scalar(pt p, pt q) {
 return p.x * q.x + p.y * q.y;
pt operator-(pt a, pt b) { return {a.x - b.x, a.y - b.
   y}; }
vector<pt> convex(vector<pt> a) {
  sort(all(a));
  if (a.size() == 2 && a[0] == a[1]) return {a[0]};
  if (a.size() <= 1) return a;</pre>
 vector<pt> h;
 for (int t = 0; t < 2; ++t) {
    int sz = h.size() - t;
    for (auto p: a) {
     while (h.size() >= sz + 2 \&\& cross(p - h.end()
    [-1], h.end()[-2] - h.end()[-1]) <= 0) h.pop_back
    ();
     h.push_back(p);
    }
    reverse(all(a));
 return h; // h is circular: h.front() == h.back()
//110bb5
```

9.3 Точка внутри многоугольника

```
auto inT = [&] (Point a, Point b, Point c, Point p) {
    a = a-p; b = b-p; c = c-p;
    return abs(a*b)+abs(b*c)+abs(c*a) == abs(a*b+b*c+c*a
    );
};
auto inP = [&] (Point p) { //a must be in
    counterclockwise order!
    int l = 1, r = n - 1;
    while (1 < r - 1) {
        int m = (1 + r) / 2;
        if ((a[m] - a[0]) < (p - a[0])) {
            1 = m;
        }
        else {
            r = m;
        }
}</pre>
```

```
}
return inT(a[l], a[0], a[r], p);
};
//lcd0cf
```

9.4 Касательные

```
auto max = [&] (auto cmp) {
 int k = 0;
  for (int lg = 18; lg >= 0; --lg) {
    int i = k + (1 << lg), j = k - (1 << lg);
    i = (i % n + n) % n;
    j = (j % n + n) % n;
    array<int, 3> ind{i, j, k};
   sort(all(ind), cmp);
   k = ind[2];
 return k;
};
auto uppert = [&](Point p) { //last vertex in
    counterclockwise order about p
  auto cmp = [&] (int i, int j) {return (a[i] - p) < (</pre>
    a[i] - p); };
 return max(cmp);
auto lowert = [&](Point p) { //first vertex in
    counterclockwise order about p
  auto cmp = [&] (int i, int j) {return (a[i] - p) > (
    a[j] - p); };
 return max(cmp);
}:
auto uppertinf = [&](Point p) { //upper tangent line
   parallel to vector p
 swap(p.x, p.y);
 p.x = -p.x;
 auto cmp = [&] (int i, int j) { return a[i] % p < a[</pre>
   j] % p; };
 return max(cmp);
};
auto lowertinf = [&](Point p) { //lower tangent line
   parallel to vector p
 swap(p.x, p.y);
 p.x = -p.x;
 auto cmp = [&] (int i, int j) { return a[i] % p > a[
    j] % p; };
  return max(cmp);
```

10 Цепные дроби

//90f89d

https://cp-algorithms.com/algebra/continued-fractions.html

10.1 Поиск нижней огибающей, сумма и минимум по модулю

```
int floor(int a, int b) {
  return a / b - ((a ^ b) < 0 && a % b);</pre>
vector<int> decompose(int p, int q) {
  vector<int> f;
  while (q != 0) {
    f.push_back(floor(p, q));
    p -= q * f.back();
    swap(p, q);
  }
  return f;
using matrix = array<int, 4>;
matrix operator*(matrix a, matrix b) {
 matrix c\{0,0,0,0\};
  for (int i = 0; i < 2; ++i) {
    for (int j = 0; j < 2; ++j) {
      for (int k = 0; k < 2; ++k) {
        c[2 * i + k] += a[2 * i + j] * b[2 * j + k];
```

```
}
 return c;
#define x first
#define y second
// computes lower convex hull for 0 <= x <= N, 0 <= y
    \leq (ax + b) / c
vector<pair<int, int>> lower_convex_hull(int a, int b,
     int c, int n) {
 matrix m = \{1, 0, 0, 1\};
 auto f = decompose(a, c);
  vector<pair<int, int>> conv{{1, 0}, {0, 1}};
  for (int x : f) {
    m = m * matrix{x, 1, 1, 0};
    conv.emplace_back(m[2], m[0]);
   if (m[2] > n) break; // there should be one (if
    any) with .x > n
 auto diff = [\&] (int x, int y) {
   return c * y - a * x;
  };
  int x = 0, y = b / c;
  vector<pair<int, int>> res{{x, y}};
  int i:
  for (i = 2; i + 1 < conv.size(); i += 2) {</pre>
    while (diff(x + conv[i + 1].x, y + conv[i + 1].y)
    \leq b) {
     int t = 1 + (diff(x + conv[i - 1].x, y + conv[i
    - 1].y) - b - 1) / abs(diff(conv[i].x, conv[i].y))
     auto [dx, dy] = tuple{conv[i - 1].x + t * conv[i
    ].x, conv[i - 1].y + t * conv[i].y};
      int k = (n - x) / dx;
      if (k == 0) break;
      if (diff(dx, dy)) k = min(k, (b - diff(x, y)) /
    diff(dx, dy));
     x += k * dx, y += k * dy;
      res.push_back({x, y});
    }
  }
  if (i >= conv.size()) i -= 2;
  for (; i > 0; i -= 2) {
    auto [dx1, dy1] = conv[i];
    if (x + dx1 > n) continue;
    x += dx1, y += dy1;
    if (i + 1 < conv.size()) {</pre>
      auto [dx2, dy2] = conv[i + 1];
      int k = (n - x) / dx2;
     x += k * dx2;
     y += k * dy2;
    res.emplace_back(x, y);
    int k = (n - x) / dx1;
    if (k == 0) continue;
    x += k * dx1;
    y += k * dy1;
    res.emplace_back(x, y);
  return res;
// number of (x, y) under pq line such that p.x <= x <
     q.x && 0 < y
int area(auto p, auto q) {
  int integers = gcd(q.x - p.x, q.y - p.y);
  return ((p.y + q.y - 1) * (q.x - p.x + 1) + integers
     + 1) / 2 - q.y;
}
// sum of (ax + b) / c for 0 <= x < n
int get_area(int a, int b, int c, int n) { // SUM (ax
    + b) / c for 0 <= x <= n
  auto ch = lower_convex_hull(a, b, c, n + 1);
  int sum = 0;
  for (int i = 0; i + 1 < ch.size(); ++i) {
    sum += area(ch[i], ch[i + 1]);
```

```
return sum;
}

// min of (ax + b) % c for 0 <= x <= n
int get_min(int a, int b, int c, int n) {
  auto ch = lower_convex_hull(a, b, c, n);
  // in fact, here we need only the last point of the
    first half of the algo (that is going up)
  int mn = c;
  for (auto [x, y] : ch) mn = min(mn, (a * x + b) % c)
    ;
  return mn;
}
//87941e</pre>
```

10.2 Простая рекурсия

```
Число точек (x,y):0\leqslant x< n,0< y\leqslant (kx+b)/d. To ects \sum_{x=0}^{n-1}\lfloor\frac{kx+b}{d}\rfloor. int cnt (int n, int k, int b, int d) { if (k=0) return (b/d) * n; if (k>=d\mid |b>=d) { return (k/d) * n * (n-1)/2 + (b/d) * n + cnt(n,k % d, b % d, d); } return cnt((k*n+b)/d,d,(k*n+b) % d, k); } //11a6a0
```

11 Разное

11.1 Компараторы

```
bool cmp1(int x, int y) { return x > y; }
struct cmp2{
    bool operator()(int x, int y) const { return x > y
    ; }
};
int32_t main() {
    set<int, decltype(cmp1)*> s1({1, 2, 3}, cmp1);
for (int x : s1) cout << x << ' '; cout << '\n';</pre>
    set<int, cmp2> s2({4, 5, 6});
    for (int x : s2) cout << x << ' '; cout << '\n';</pre>
    auto cmp3 = [\&] (int x, int y) { return x > y; };
    set<int, decltype(cmp3)> s3({7, 8, 9}, cmp3); //
    second cmp3 could be omitted if cmp3 = [](...) {
     ...}
    for (int x : s3) cout << x << ' '; cout << ' \setminus n';
    vector<int> v{3, 2, 1};
    cout << lower_bound(all(v), 2, cmp1) - v.begin();</pre>
    cout << lower_bound(all(v),2,cmp2()) - v.begin();</pre>
    cout << lower_bound(all(v), 2, cmp3) - v.begin();</pre>
```

11.2 Трюки от Сергея Копелиовича

11.2.1 Быстрый ввод

//adea08

https://acm.math.spbu.ru/~sk1/algo/input-output

```
const int buf_size = 4096;
int getChar() {
    static char buf[buf_size];
    static int len = 0, pos = 0;
    if (pos == len)
        pos = 0, len = fread(buf, 1, buf_size, stdin);
    if (pos == len)
        return -1;
    return buf[pos++];
}
int readChar() {
    while (1) {
```

```
int c = getChar();
  if (c > 32) return c;
}

int readInt() {
  int s = 1, c = readChar(), x = 0;
  if (c == '-')
    s = -1, c = getChar();
  while (isdigit(c))
    x = x * 10 + c - '0', c = getChar();
  return s * x;
}

//dc0a77
```

https://acm.math.spbu.ru/~sk1/algo/memory.cpp.html

11.2.2 Быстрый аллокатор

```
const int MAX_MEM = 1e8;
int mpos = 0;
char mem[MAX_MEM];
inline void * operator new (size_t n) {
   assert((mpos += n) <= MAX_MEM);
   return (void *)(mem + mpos - n);
}
void operator delete (void *) noexcept { } // must
   have!
void operator delete (void *, size_t) noexcept { } //
   must have!</pre>
```

//8726b1

11.3 Флаги компияции

-DLOCAL -Wall -Wextra -pedantic -Wshadow -Wformat=2 -Wfloat-equal -Wconversion -Wlogical-op -Wshift-overflow=2 -Wduplicated-cond -Wcast-qual -Wcast-align -D_GLIBCXX_DEBUG -D_GLIBCXX_DEBUG_PEDANTIC -D_FORTIFY_SOURCE=2 -fsanitize=address -fsanitize=undefined -fno-sanitize-recover -fstack-protector -std=c++2a

11.3.1 Сеточка в vim

https://codeforces.com/blog/entry/122540

```
i|<esc>25A |<esc>
o+<esc>25A---+<esc>
Vky35Pdd
```

11.4 Что сделать на пробном туре

- Послать клар
- Распечатать что-то
- Получить ML (stack & heap)
- Максимальный размер отправляемого файла?
- Убедиться, что чекер регистронезависимый (yes/YES)
- Позапускать Флойда Варшалла
- Посмотреть, насколько быстр быстрый ввод
- Перебить что-то, проверить хеш
- Проверить санитайзеры

11.5 Хеш файла без комментариев

Хеш файла, игнорирующий переводы строк и комментарии:

```
$ cpp -dD -P -fpreprocessed "$filename" | tr -d '[:
    space:]' | md5sum | cut -c-6
```







