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1 Теория чисел

1.1 KTO

```
if (b==0) { x = 1; y = 0; return a; }
    int d = gcd(b,a%b,x,y);
    swap(x,y);
5
   y - = a / b * x;
    return d;
7 }
8 int inv(int r, int m) {
    int x, y;
10
    gcd(r,m,x,y);
11
    return (x+m) %m;
12 }
13 int crt(int r, int n, int c, int m) { return r + ((
      c - r) % m + m) * inv(n, m) % m * n; }
```

1.2 Алгоритм Миллера — Рабина

1 int gcd(int a, int b, int &x, int &y) {

```
__int128 one=1;
2 int po(int a, int b, int p)
3 {
4
     int res=1;
     while(b) {if(b & 1) {res=(res*one*a)%p;--b;} else
        {a=(a*one*a)%p;b>>=1;}} return res;
6 }
7 bool chprime(int n) ///miller-rabin
8 {
     if(n==2) return true;
     if(n<=1 || n%2==0) return false;</pre>
11
     int h=n-1; int d=0; while(h%2==0) {h/=2; ++d;}
     for(int a:{2, 3, 5, 7, 11, 13, 17, 19, 23, 29,
       31, 37})
       {
14
       if(a==n) return true;
       int u=po(a,h,n); bool ok=0;
16
       if(u%n==1) continue;
17
       for(int c=0;c<d;++c)</pre>
18
19
         if ((u+1) %n==0) {ok=1;break;}
20
         u = (u * one * u) %n;
21
22
       if(!ok) return false;
23
24
     return true;
25 }
```

2 Графы

2.1 SCC и 2-SAT

Алгоритм ищет сильносвязные компоненты в графе g, если есть путь $i \to j$, то $scc[i] \le scc[j]$

В случае 2- \mathcal{SAT} рёбра $i\Rightarrow j$ и $(j\oplus 1)\Rightarrow (i\oplus 1)$ должны быть добавлены одновременно.

```
1 vector < vector < int >> g(2 * n);
 2 vector < vector < int >> r(g.size());
 3 for (int i = 0; i < g.size(); ++i) {</pre>
    for (int j : g[i]) r[j] push_back(i);
 5 }
 6 vector<int> used(g.size()), tout(g.size());
 7 int time = 0;
 8 auto dfs = [&](auto dfs, int cur) -> void {
     if (used[cur]) return;
10
     used[cur] = 1;
11
     for (int nxt : g[cur]) {
       dfs(dfs, nxt);
13
14
     // used[cur] = 2;
15
     tout[cur] = time++;
16 };
17 for (int i = 0; i < g.size(); ++i) if (!used[i])
dfs(dfs, i);
18 vector<int> ind(g.size());
| 19 iota(ind.begin(), ind.end(), 0);
```

```
20 sort(all(ind), [&](int i, int j){return tout[i] >
      tout[j];});
21 vector<int> scc(g.size(), -1);
22 auto go = [&](auto go, int cur, int color) -> void
    if (scc[cur] != -1) return;
24
     scc[cur] = color;
    for (int nxt : r[cur]) {
25
26
      go(go, nxt, color);
27
28 1:
29 int color = 0;
30 for (int i : ind) {
31
    if (scc[i] == -1) go(go, i, color++);
32 }
33 for (int i = 0; i < g.size() / 2; ++i) {
    if (scc[2 * i] == scc[2 * i + 1]) "IMPOSSIBLE"
34
    if (scc[2 * i] < scc[2 * i + 1]) {</pre>
35
36
      // !i => i, assign i = true
    } else {
37
38
      // i => !i, assign i = false
39
40 }
```

2.2Эйлеров цикл

```
1 vector < vector < pair < int , int >>> g(n); // pair { nxt ,
       idx}
2 vector < pair < int , int >> e(p.size());
3 // build graph
4 vector < int > in(n), out(n);
5 for (auto [u, v] : e) in[v]++, out[u]++;
6 vector < int > used(m), it(n), cycle;
7 auto dfs = [&](auto dfs, int cur) -> void {
    while (true) {
9
       while (it[cur] < g[cur].size() && used[g[cur][</pre>
       it[cur]].second]) it[cur]++;
       if (it[cur] == g[cur].size()) return;
       auto [nxt, idx] = g[cur][it[cur]];
11
       used[idx] = true;
13
       dfs(dfs, nxt);
       cycle.push_back(idx);
14
15
    }
16 };
17 \text{ int } cnt = 0, odd = -1;
18 for (int i = 0; i < n; ++i){
     if (out[i] && odd == -1) odd = i;
19
     if (in[i] != out[i]) {
       if (in[i] + 1 == out[i]) odd = i;
2.1
       if (abs(in[i] - out[i]) > 1) return {}; // must
22
        hold
23
       cnt ++;
24
    }
25 }
26 if (cnt != 0 && cnt != 2) return {}; // must hold
27 // for undirected find odd vertex (and count that #
        of odd is 0 or 2)
28 dfs(dfs, odd);
29 reverse(cycle.begin(), cycle.end()); 30 if (cycle.size() != m) return {};
```

xor, and, or-свёртки

3.1 and-свёртка

```
1 vector (int > band (vector (int > a, vector (int > b)
2 {
3
    int n=0:while((1<<n)<a.size()) ++n:</pre>
    a.resize(1<<n);b.resize(1<<n);
    for(int i=0;i<n;++i) for(int mask=0;mask<(1<<n)</pre>
      ; ++ mask) if (mask & (1 << i)) {a [mask - (1 << i)] += a [}
      mask]; a[mask-(1<<i)]%=p;}
    for(int i=0;i<n;++i) for(int mask=0;mask<(1<<n)</pre>
      ; ++ mask) if (mask & (1<<i)) {b[mask-(1<<i)]+=b[
      mask]; b[mask-(1<<i)]%=p;}
    vector < int > c(1 << n,0);</pre>
    for(int mask=0; mask<(1<<n); ++ mask) {c[mask]=a[</pre>
      mask]*b[mask];c[mask]%=p;}
```

```
for(int i=0;i<n;++i) for(int mask=0;mask<(1<<n)</pre>
       ; ++ mask) if (!(mask & (1<<i))) {c[mask] -= c[mask]
       +(1<<i)];c[mask]%=p;}
10
    return c;
11 }
  3.2 от-свёртка
1 vector < int > bor(vector < int > a.vector < int > b)
    int n=0; while((1<<n)<a.size()) ++n;</pre>
    a.resize(1<<n);b.resize(1<<n);
4
    for(int i = 0; i < n; ++i) for(int mask = 0; mask < (1 << n)</pre>
      ; ++mask) if (!(mask & (1<<i))) {a[mask+(1<<i)]+=
       a[mask];a[mask+(1<<ii)]%=p;}
    for(int i=0;i<n;++i) for(int mask=0;mask<(1<<n)</pre>
       ; ++mask) if (!(mask & (1<<i))) {b [mask+(1<<i)]+=
       b[mask];b[mask+(1<<ii)]%=p;}
    vector < int > c(1 << n, 0);
    for(int mask=0; mask<(1<<n); ++ mask) {c[mask]=a[</pre>
       mask]*b[mask];c[mask]%=p;}
     for(int i = 0; i < n; ++i) for(int mask = 0; mask < (1 << n)</pre>
       ; ++ mask) if (mask & (1<<i)) {c[mask] -=c[mask]
       -(1<<i)];c[mask]%=p;}
    return c:
11 }
  3.3 хот-свёртка
1 vector<int> bxor(vector<int> a, vector<int> b)
2 {
3
    assert(p%2==1); int inv2=(p+1)/2;
    int n=0; while((1<<n)<a.size()) ++n;</pre>
    a.resize(1<<n);b.resize(1<<n);
    for(int i=0;i<n;++i) for(int mask=0;mask<(1<<n)</pre>
       ; ++ mask) if (!(mask & (1<<i))) {int u=a[mask], v=
       a[mask+(1<<ii)]; a[mask+(1<<ii)]=(u+v)%p; a[mask]=(
      u-v)%p;}
    for (int i=0:i < n:++i) for (int mask=0:mask < (1 < < n)
       ; ++mask) if (!(mask & (1<<i))) {int u=b[mask], v=
       b [mask+(1<<ii)]; b [mask+(1<<ii)]=(u+v)%p; b [mask]=(
      u-v)%p;}
     vector < int > c(1 << n,0);
    for(int mask=0; mask<(1<<n); ++ mask) {c[mask]=a[</pre>
       mask]*b[mask];c[mask]%=p;}
     for(int i=0;i<n;++i) for(int mask=0;mask<(1<<n)</pre>
      ; ++mask) if (!(mask & (1<<i))) {int u=c[mask], v=
       c[mask+(1<<ii)];c[mask+(1<<ii)]=((v-u)*inv2)%p;c[
       mask] = ((u+v)*inv2)%p;}
    return c:
      Структуры данных
  4.1 Дерево Фенвика
1 int fe[maxn]; /// fenwick tree
2 void pl(int pos,int val) {while(pos<maxn) {fe[pos} } \\
       ] += val; pos | = (pos+1); }}
3 int get(int pos) {int ans=0; while(pos>=0) {ans+=fe[
       pos];pos&=(pos+1);--pos;} return ans;} /// [0,
       pos] - vkluchitelno!!!
4 int get(int l,int r) {return get(r-1)-get(l-1);} //
       / summa na [l.r)
  4.2 Ordered set
```

```
1 #include <ext/pb_ds/assoc_container.hpp>
2 #include <ext/pb_ds/tree_policy.hpp>
4 using namespace __gnu_pbds;
5 using namespace std;
7 using ordered_set = tree<int, null_type, less<>,
      \verb"rb_tree_tag", | | | tree_order_statistics_node_update" |
      >;
```

4.3 Дерево отрезков

```
1 template < typename {\tt Data} , typename {\tt Mod} , typename
       UniteData, typename UniteMod, typename Apply>
  struct MassSegmentTree {
3
    int h, n;
    Data zd;
5
    Mod zm;
    vector < Data > data;
     vector < Mod > mod;
     UniteData ud; // Data (Data, Data)
     UniteMod um; // Mod (Mod, Mod);
10
     Apply a; // Data (Data, Mod, int); last argument
11
       is the length of current segment (could be used
        for range += and sum counting, for instance)
12
13
     template < typename I >
14
     {\tt MassSegmentTree(int\ sz,\ Data\ zd,\ Mod\ zm,}
       UniteData ud, UniteMod um, Apply a, I init) : h
       (_{-1}g(sz > 1 ? sz - 1 : 1) + 1), n(1 << h), zm(
       zm), zd(zd), data(2 * n, zd), mod(n, zm), ud(ud
       ), um(um), a(a) {
       for (int i = 0; i < sz; ++i) data[i + n] = init</pre>
       (i);
16
       for (int i = n - 1; i > 0; --i) data[i] = ud(
       data[2 * i], data[2 * i + 1]);
17
18
    {\tt MassSegmentTree(int\ sz,\ Data\ zd,\ Mod\ zm,}
19
       UniteData ud, UniteMod um, Apply a) : h(__lg(sz
       > 1 ? sz - 1 : 1) + 1), n(1 << h), zm(zm), zd(
       zd), data(2 * n, zd), mod(n, zm), ud(ud), um(um)
       ), a(a) {}
2.0
21
     void push(int i) {
       if (mod[i] == zm) return;
23
       apply(2 * i, mod[i]);
       apply(2 * i + 1, mod[i]);
24
       mod[i] = zm;
25
26
27
2.8
     // is used only for apply
     int length(int i) { return 1 << (h - __lg(i)); }</pre>
29
31
     // is used only for descent
32
     int left(int i) {
      int lvl = __lg(i);
34
       return (i & ((1 << lvl) - 1)) * (1 << (h - lvl)
35
36
37
     // is used only for descent
38
     int right(int i) {
39
       int lvl = __lg(i);
       return ((i & ((1 << lvl) - 1)) + 1) * (1 << (h
40
       - lvl));
41
42
43
     template < typename S>
     void apply(int i, S x) {
       data[i] = a(data[i], x, length(i));
45
46
       if (i < n) mod[i] = um(mod[i], x);</pre>
47
48
49
     void update(int i) {
      if (mod[i] != zm) return;
50
51
       data[i] = ud(data[2 * i], data[2 * i + 1]);
52
53
54
     template < typename S>
     void update(int 1, int r, S x) { // [1; r)
56
       1 += n, r += n;
57
       for (int shift = h; shift > 0; --shift) {
         push(1 >> shift);
59
         push((r - 1) >> shift);
60
61
       for (int lf = 1, rg = r; lf < rg; lf /= 2, rg</pre>
        if (lf & 1) apply(lf++, x);
```

```
63
         if (rg & 1) apply(--rg, x);
64
       for (int shift = 1; shift <= h; ++shift) {</pre>
66
         update(1 >> shift);
67
         update((r - 1) >> shift);
68
69
     }
70
71
     Data get(int 1, int r) { // [1; r)
72
       1 += n, r += n;
73
       for (int shift = h; shift > 0; --shift) {
74
         push(1 >> shift);
         push((r - 1) >> shift);
76
77
       Data leftRes = zd, rightRes = zd;
       for (; 1 < r; 1 /= 2, r /= 2) {
  if (1 & 1) leftRes = ud(leftRes, data[1++]);</pre>
80
          if (r & 1) rightRes = ud(data[--r], rightRes)
       return ud(leftRes, rightRes);
83
84
85
     // l \in [0; n) && ok(get(1, 1), 1);
86
     \label{eq:condition} \mbox{// returns last r: ok(get(1, r), r)}
87
     template < typename C>
88
     int lastTrue(int 1, C ok) {
89
       1 += n;
       for (int shift = h; shift > 0; --shift) push(1
       >> shift);
       Data cur = zd;
       do {
         1 >>= __builtin_ctz(1);
         Data with1;
         with1 = ud(cur, data[1]);
96
         if (ok(with1, right(1))) {
97
            cur = with1;
98
            ++1:
         } else {
0.0
           while (1 < n) {
              push(1);
              Data with2;
              with2 = ud(cur, data[2 * 1]);
              if (ok(with2, right(2 * 1))) {
                cur = with2;
                1 = 2 * 1 + 1;
              } else {
                1 = 2 * 1;
           }
11
           return 1 - n;
12
13
       } while (1 & (1 - 1));
14
       return n;
15
     // r \in [0; n) && ok(get(r, r), r);
17
18
     // returns first 1: ok(get(1, r), 1)
19
     template < typename C>
     int firstTrue(int r, C ok) {
21
       r += n;
       for (int shift = h; shift > 0; --shift) push((r
        - 1) >> shift);
       Data cur = zd;
24
       while (r & (r - 1)) {
25
         r >>= __builtin_ctz(r);
26
         Data with1;
         with1 = ud(data[--r], cur);
         if (ok(with1, left(r))) {
28
           cur = with1:
30
         } else {
31
           while (r < n) {
              push(r);
33
              Data with 2;
34
              with2 = ud(data[2 * r + 1], cur);
              if (ok(with2, right(2 * r))) {
                cur = with2;
                r = 2 * r;
38
              } else {
                r = 2 * r + 1;
39
```

81

92

3

```
140
             }
141
           }
142
           return r - n + 1;
         }
143
       }
144
145
        return 0;
146
     }
147 };
   4.3.1 Примеры:
     • Взятие максимума и прибавление константы
     1 MassSegmentTree segtree(n, OLL, OLL,
     2 [](int x, int y) { return max(x, y); },
     3 [](int x, int y) { return x + y; },
     4 [](int x, int y, int len) { return x + y; });
     • Взятие суммы и прибавление константы
     1 MassSegmentTree segtree(n, OLL, OLL,
     2 [](int x, int y) { return x + y; },
     3 [](int x, int y) { return x + y; },
     4 [](int x, int y, int len) { return x + y * len;
           });
     • Взятие суммы и присовение
     1 MassSegmentTree segtree(n, OLL, -1LL,
     2 [](int x, int y) { return x + y; },
     3 [](int x, int y) { return y; },
     4 [](int x, int y, int len) { return y * len; });
```

Строковые алгоритмы

5.1Префикс-функция

```
1 vector<int> prefix_function(string s) {
   vector < int > p(s.size());
    for (int i = 1; i < s.size(); ++i) {</pre>
      p[i] = p[i - 1];
5
      while (p[i] && s[p[i]] != s[i]) p[i] = p[p[i] -
6
      p[i] += s[i] == s[p[i]];
   }
    return p;
9 }
```

5.2 Z-функция

```
1 vector <int> z_function (string s) { // z[i] - lcp
      of s and s[i:]
   int n = (int) s.length();
   vector < int > z (n);
   for (int i=1, l=0, r=0; i<n; ++i) {</pre>
    if (i <= r)
     z[i] = min (r-i+1, z[i-1]);
6
    while (i+z[i] < n \&\& s[z[i]] == s[i+z[i]])
     ++z[i];
9
    if (i+z[i]-1 > r)
10
     1 = i, r = i+z[i]-1;
11 }
12
   return z;
13 }
```

Алгоритм Манакера

```
1 vector < int > manacher_odd(const string &s) {
   vector<int> man(s.size(), 0);
   int 1 = 0, r = 0;
3
    int n = s.size();
    for (int i = 1; i < n; i++) {</pre>
     if (i <= r) {</pre>
6
        man[i] = min(r - i, man[l + r - i]);
8
9
      while (i + man[i] + 1 < n && i - man[i] - 1 >=
      0 && s[i + man[i] + 1] == s[i - man[i] - 1]) {
```

```
10
         man[i]++;
12
       if (i + man[i] > r) {
13
         1 = i - man[i];
14
         r = i + man[i];
15
16
     }
17
     return man;
18 }
19 // abacaba : (0 1 0 3 0 1 0)
20 // abbaa : (0 0 0 0 0)
22 vector <int> manacher_even(const string &s) {
23
    assert(s.size());
24
     string t;
     for (int i = 0; i + 1 < s.size(); ++i) {</pre>
26
      t += s[i];
       t += '#';
28
     }
29
     t += s.back();
30
     auto odd = manacher_odd(t);
     vector <int> ans;
31
32
     for (int i = 1; i < odd.size(); i += 2) {</pre>
      ans.push_back((odd[i]+1)/2);
33
34
35
     return ans;
36 }
37 \text{ // abacaba} : (0 0 0 0 0 0)
38 // abbaa : (0 2 0 1)
```

5.4 Суфмассив

Китайский суффмассив

```
1 struct SuffixArray {
      vector <int> sa, lcp;
     SuffixArray (string &s, int lim=256) {
  int n = (int)s.size() + 1, k = 0, a, b;
 3
 4
 5
        vector \langle int \rangle x(s.begin(), s.end() + 1), y(n),
        ws(max(n, lim)), rank(n);
        sa = lcp = y, iota(sa.begin(), sa.end(), 0);
        for (int j = 0, p = 0; p < n; j = max(111, j *
        2), lim = p) {
         p = j, iota(y.begin(), y.end(), n - j);
          for (int i = 0; i < n; i++) if (sa[i] >= j) y
        [p++] = sa[i] - j;
 10
          fill(ws.begin(), ws.end(), 0);
          for (int i = 0; i < n; i++) ws[x[i]]++;</pre>
          for (int i = 1; i < lim; i++) ws[i] += ws[i -</pre>
 12
         1];
          for (int i = n; i--; ) sa[--ws[x[y[i]]]] = y[
        i];
          swap(x, y), p = 1, x[sa[0]] = 0;
for (int i = 1; i < n; i++) a = sa[i - 1], b</pre>
        = sa[i], x[b] = (y[a] == y[b] && y[a + j] == y[
        b + j]) ? p - 1 : p++;
 16
        }
        for (int i = 1; i < n; i++) rank[sa[i]] = i;</pre>
        for (int i = 0, j; i < n - 1; lcp[rank[i++]]=k)</pre>
 18
          for (k && k--, j = sa[rank[i] - 1];
19
              s[i + k] == s[j + k]; k++);
     }
22 };
23 struct Rmq {
24
     const int INF = 1e9;
25
      int n;
26
      vector<int> rmq;
27
      Rmq() {}
      void build(const vector<int> &x) {
29
        assert(x.size() == n);
30
        for (int i = 0; i < n; ++i) rmq[n + i] = x[i];</pre>
        for (int i = n - 1; i > 0; --i) rmq[i] = min(
        rmq[2 * i], rmq[2 * i + 1]);
 32
      Rmq(int n) : n(n), rmq(2 * n, INF) {}
 33
34
      void put(int i, int x) {
        rmq[i + n] = min(rmq[i + n], x);
36
        for (i = (i + n) / 2; i > 0; i /= 2) {
          rmq[i] = min(rmq[i * 2], rmq[i * 2 + 1]);
138
4
```

```
}
39
40
    }
    int getMin(int 1, int r) { //[1;r)
41
49
       assert(1 < r);
       int res = INF;
43
       for (1 += n, r += n; 1 < r; 1 /= 2, r /= 2) {
44
45
        if (1 & 1) res = min(res, rmq[1++]);
46
         if (r & 1) res = min(res, rmq[--r]);
47
48
       return res;
49
    }
50 }:
52 struct Lc {
    vector < int > pos;
53
    Rmq rmq;
55
    Lc(string s) : rmq(s.size()) {
56
       SuffixArray sa(s);
57
       auto ss = sa.sa:
58
       ss.erase(ss.begin());
59
       auto lcp = sa.lcp;
60
61
       lcp.erase(lcp.begin());
62
       lcp.erase(lcp.begin());
63
64
       pos.resize(s.size());
65
       assert(s.size() == ss.size());
       for (int i = 0; i < ss.size(); ++i) {</pre>
66
        pos[ss[i]] = i;
67
68
69
       int n = s.size();
       assert(lcp.size() == n - 1);
70
71
       rmq.build(lcp);
72
    }
    int getLcp(int i, int j) {
73
74
      i = pos[i]; j = pos[j];
       if (j < i) {</pre>
75
76
        swap(i, j);
77
       }
       if (i == j) {
79
        return 1e18;
80
81
       else {
82
         return rmq.getMin(i, j);
83
84
    }
85 };
```

6 Потоки

6.1 Алгоритм Диница

```
1 #define pb push_back
2 struct Dinic{
3 struct edge{
4
    int to, flow, cap;
5 };
7 const static int N = 555; //count of vertices
9 vector<edge> e;
10 vector \langle int \rangle g[N + 7];
11 int dp[N + 7];
12 int ptr[N + 7];
14 void clear(){
15 for (int i = 0; i < N + 7; i++) g[i].clear();
    e.clear();
17 }
18
19 void addEdge(int a, int b, int cap){
   g[a].pb(e.size());
2.0
21
    e.pb({b, 0, cap});
    g[b].pb(e.size());
23
    e.pb({a, 0, 0});
25
26 int minFlow, start, finish;
```

```
28 bool bfs(){
29
     for (int i = 0; i < N; i++) dp[i] = -1;
     dp[start] = 0;
     vector < int > st;
     int uk = 0;
32
33
     st.pb(start);
34
     while(uk < st.size()){</pre>
       int v = st[uk++];
       for (int to : g[v]){
36
        auto ed = e[to];
38
         if (ed.cap - ed.flow >= minFlow && dp[ed.to]
       == -1){
39
           dp[ed.to] = dp[v] + 1;
           st.pb(ed.to);
40
41
42
     }
43
44
     return dp[finish] != -1;
45 }
46
47 int dfs(int v, int flow){
    if (v == finish) return flow;
48
49
     for (; ptr[v] < g[v].size(); ptr[v]++){</pre>
       int to = g[v][ptr[v]];
       edge ed = e[to];
       if (ed.cap - ed.flow >= minFlow && dp[ed.to] ==
       dp[v] + 1){
         int add = dfs(ed.to, min(flow, ed.cap - ed.
       flow));
54
         if (add) {
           e[to].flow += add;
           e[to ^ 1].flow -= add;
           return add;
58
         }
59
       }
60
     }
61
     return 0;
62 }
64 int dinic(int start, int finish){
    Dinic::start = start;
66
     Dinic::finish = finish;
67
     int flow = 0;
68
     for (minFlow = (1 << 30); minFlow; minFlow >>= 1)
69
       while(bfs()){
         for (int i = 0; i < N; i++) ptr[i] = 0;</pre>
         while(int now = dfs(start, (int)2e9 + 7))
       flow += now:
72
       }
73
     }
74
     return flow;
75 }
76 } dinic;
   6.2 Mincost k-flow
   6.2.1 Строим граф
 1 struct edge {
     int next, capacity, cost, flow = 0;
 3
     edge() = default;
 5
 6
     edge(int next, int capacity, int cost) : next(
      next), capacity(capacity), cost(cost) {}
     int rem() const { return capacity - flow; }
10
     int operator+=(int f) { return flow += f; }
     int operator -=(int f) { return flow -= f; }
12
13 };
14 auto addEdge = [\&](auto from, auto next, auto
       capacity, int cost) {
15
     g[from].push_back(e.size());
     e.emplace_back(next, capacity, cost);
17
     g[next].push_back(e.size());
18
     e.emplace_back(from, 0, -cost);
19 };
```

41 42

43 }:

return cost;

45 for (int flow = 0; flow < k; ++flow) {

 $44 \ 11 \ cost = 0;$

```
Если граф ориентированный, то addEdge вызываем один раз. Если
                                                              46
                                                                   ll a = dijkstra(s, t);
                                                                   if (a == -1) {
   неориентированный, то два, вот так:
                                                                     cout << " -1\n";
 1 addEdge(u, v, capacity, cost);
                                                              49
                                                                     return;
2 addEdge(v, u, capacity, cost);
                                                                   }
                                                              50
                                                              51
                                                                   cost += a;
                                                              52 }
  6.2.2 Запускаем Форда — Беллмана
1 vector<11> phi(n, 0);
                                                                 6.2.4 Восстанавливаем ответ
2 auto fordBellman = [&](int s, int t) {
    phi.assign(n, 0);
                                                               1 auto findPath = [&](int s, int t) {
     for (int iter = 0; iter < n; ++iter) {</pre>
                                                                  vector < int > ans:
       bool changed = false;
                                                                   int cur = s;
6
       for (int u = 0; u < n; ++u) {</pre>
                                                                   while (cur != t) {
                                                               4
         for (auto index : g[u]) {
                                                                     for (auto index : g[cur]) {
           auto edge = e[index];
                                                                       auto &edge = e[index];
9
           if (edge.rem() > 0 && phi[edge.next] > phi[
                                                                       if (edge.flow <= 0) continue;</pre>
       u] + edge.cost) {
                                                                       edge -= 1;
10
             phi[edge.next] = phi[u] + edge.cost;
                                                                       e[index ^ 1] += 1;
             changed = true;
11
                                                                       ans.push_back(index / 4);
                                                              10
                                                              11 // index / 4 because each edge has 4 copies
         }
                                                                       cur = edge.next;
       }
14
                                                              13
                                                                       break;
15
       if (!changed) break;
                                                              14
    }
16
                                                                   }
17 };
                                                              16
                                                                   return ans;
18 fordBellman(s, t):
                                                              17 };
                                                              18 for (int flow = 0; flow < k; ++flow) {
                                                              19
                                                                   auto p = findPath(s, t);
  6.2.3 Ищем кратчайший путь Дейкстрой с потенциалами
                                                                   cout << p.size() << ', ';
                                                              20
                                                                   for (int x : p) cout << x + 1 << ', ';</pre>
1 vector<11> dist;
                                                              22
                                                                   cout << '\n';
2 vector < int > from;
3 vector < bool > cnt;
4 auto dijkstra = [&](int s, int t) {
     dist.assign(n, 1e18);
                                                                     FFT & co
    from.assign(n, -1);
cnt.assign(n, false);
                                                                 7.1 NTT & co
     dist[s] = 0;
9
     for (int i = 1; i < n; ++i) {</pre>
       int cur = find(cnt.begin(), cnt.end(), false) -
10
                                                               1 typedef long long 11;
                                                               2 const int p=998244353;
        cnt.begin();
                                                               3 int po(int a, int b) {if(b==0) return 1; if(b==1)
11
       for (int j = 0; j < n; ++j) {
        if (!cnt[j] && dist[j] < dist[cur]) cur = j;</pre>
                                                                     return a; if(b%2==0) {int u=po(a,b/2); return (u
12
13
                                                                     *1LL*u) %p;} else {int u=po(a,b-1); return (a*1LL
                                                                     *u)%p;}}
14
       cnt[cur] = true;
15
       for (int index : g[cur]) {
                                                               4 int inv(int x) {return po(x,p-2);}
         auto &edge = e[index];
                                                               5 template <\! int M , int K , int G> struct Fft {
                                                                  // 1, 1/4, 1/8, 3/8, 1/16, 5/16, 3/16, 7/16, ...
17
         if (edge.rem() == 0) continue;
18
         ll weight = edge.cost + phi[cur] - phi[edge.
                                                                   int g[1 << (K - 1)];</pre>
                                                                   Fft(\bar{)}: g() { //if tl constexpr...}
       nextl:
19
         if (dist[edge.next] > dist[cur] + weight) {
                                                               9
                                                                     static_assert(K >= 2, "Fft: K >= 2 must hold");
20
           dist[edge.next] = dist[cur] + weight;
                                                                     g[0] = 1;
           from[edge.next] = cur;
                                                                     g[1 << (K - 2)] = G;
21
                                                              11
22
         }
                                                              12
                                                                     for (int 1 = 1 << (K - 2); 1 >= 2; 1 >>= 1) {
       }
23
                                                                       g[l >> 1] = (static_cast < long long > (g[l]) * g
24
    }
                                                                     [1]) % M;
25
     if (dist[t] == (11) 1e18) return -1LL;
                                                              14
26
                                                                     assert((static_cast < long long > (g[1]) * g[1]) %
     11 cost = 0:
     for (int p = t; p != s; p = from[p]) {
27
                                                                     M == M - 1);
       for (auto index : g[from[p]]) {
                                                                     for (int 1 = 2; 1 <= 1 << (K - 2); 1 <<= 1) {
29
         auto &edge = e[index];
                                                                       for (int i = 1; i < 1; ++i) {</pre>
                                                                         g[l + i] = (static_cast < long long > (g[l]) *
30
         ll weight = edge.cost + phi[from[p]] - phi[
                                                                     g[i]) % M;
       edge.next];
                                                              19
31
         if (edge.rem() > 0 && edge.next == p && dist[
                                                                       }
       edge.next] == dist[from[p]] + weight) {
                                                              20
           edge += 1;
e[index ^ 1] -= 1;
                                                              21
                                                              22
                                                                   void fft(vector<int> &x) const {
33
                                                              23
34
           cost += edge.cost;
                                                                     const int n = x.size();
                                                              24
                                                                     assert(!(n & (n - 1)) && n <= 1 << K);
35
           break;
36
         }
                                                                     for (int h = __builtin_ctz(n); h--; ) {
                                                              26
                                                                       const int 1 = 1 << h;</pre>
37
                                                                       for (int i = 0; i < n >> 1 >> h; ++i) {
                                                              27
38
39
     for (int i = 0; i < n; ++i) {</pre>
                                                              28
                                                                         for (int j = i << 1 << h; j < ((i << 1) +
      phi[i] += dist[i];
40
                                                                     1) << h; ++j) {
```

29

30

]) * x[j | 1]) % M;

const int t = (static_cast < long long > (g[i

if ((x[j | 1] = x[j] - t) < 0) x[j | 1]

if ((x[j] += t) >= M) x[j] -= M;

```
32
           }
33
         }
34
       }
35
       for (int i = 0, j = 0; i < n; ++i) {
         if (i < j) std::swap(x[i], x[j]);</pre>
36
37
         for (int 1 = n; (1 >>= 1) && !((j ^= 1) & 1);
        ) {}
38
       }
39
     }
40
     vector<int> convolution(const vector<int> &a,
       const vector<int> &b) const {
41
       if(a.empty() || b.empty()) return {};
42
       const int na = a.size(), nb = b.size();
       int n, invN = 1;
43
44
       for (n = 1; n < na + nb - 1; n <<= 1) invN = ((</pre>
       invN & 1) ? (invN + M) : invN) >> 1;
       vector < int > x(n, 0), y(n, 0);
45
46
       std::copy(a.begin(), a.end(), x.begin());
47
       std::copy(b.begin(), b.end(), y.begin());
48
       fft(x):
49
       fft(y);
       for (int i = 0; i < n; ++i) x[i] = (((</pre>
50
       static_cast<long long>(x[i]) * y[i]) % M) *
       invN) % M;
51
       std::reverse(x.begin() + 1, x.end());
52
       fft(x);
53
       x.resize(na + nb - 1):
54
       return x;
55
56 };
57 Fft < 998244353,23,31 > muls;
58 vector<int> form(vector<int> v,int n)
59 {
60
       while (v.size()<n) v.push_back(0);
       while(v.size()>n) v.pop_back();
61
62
       return v;
63 }
64 vector <int> operator *(vector <int> v1, vector <int>
       v2)
65 f
66
       return muls.convolution(v1.v2):
67
68 vector <int> operator +(vector <int> v1, vector <int>
69 {
70
       while (v2.size() < v1.size()) v2.push_back(0);</pre>
       while(v1.size()<v2.size()) v1.push_back(0);</pre>
71
       for (int i=0; i < v1.size(); ++i) {v1[i]+=v2[i]; if(</pre>
       v1[i]>=p) v1[i]-=p; else if(v1[i]<0) v1[i]+=p;}
72
       return v1;
73 }
74 vector < int > operator - (vector < int > v1, vector < int >
75 {
76
       int sz=max(v1.size(), v2.size()); while(v1.size()
       <sz) v1.push_back(0); while(v2.size()<sz) v2.</pre>
       push_back(0);
77
       for(int i=0;i<sz;++i) {v1[i]-=v2[i];if(v1[i]<0)</pre>
        v1[i]+=p; else if(v1[i]>=p) v1[i]-=p;} return
       v1:
78 }
79 vector < int > trmi (vector < int > v)
80 {
       for(int i=1;i<v.size();i+=2) {if(v[i]>0) v[i]=p
81
       -v[i]; else v[i]=(-v[i]);}
82
       return v;
83 }
84 vector <int> deriv(vector <int> v)
85 {
86
       if(v.empty()) return{};
87
       vector < int > ans(v.size()-1);
88
       for (int i=1; i < v. size(); ++i) ans[i-1] = (v[i] *1LL*
       i)%p;
89
       return ans;
90
91 vector < int > integ(vector < int > v)
92 {
93
       vector < int > ans(v.size()+1); ans[0]=0;
       for(int i=1;i<v.size();++i) ans[i-1]=(v[i]*1LL*</pre>
94
       i)%p;
```

```
95
       return ans;
96 }
97 vector<int> mul(vector<vector<int> > v)
98 {
99
       if(v.size()==1) return v[0];
       vector<vector<int> > v1,v2;for(int i=0;i<v.size</pre>
00
       ()/2;++i) v1.push_back(v[i]); for(int i=v.size
       ()/2;i<v.size();++i) v2.push_back(v[i]);
0.1
       return muls.convolution(mul(v1),mul(v2));
102 }
03 vector<int> inv1(vector<int> v,int n)
04 {
05
       assert(v[0]!=0);
06
       int sz=1; v=form(v,n); vector < int > a = {inv(v[0])};
       while(sz<n)
0.8
            vector < int > vsz; for (int i = 0; i < min(n, 2*sz)</pre>
       ;++i) vsz.push_back(v[i]);
           vector<int> b=((vector<int>) {1})-muls.
       convolution(a.vsz):
            for(int i=0;i<sz;++i) assert(b[i]==0);</pre>
            b.erase(b.begin(),b.begin()+sz);
12
13
            vector < int > c = muls.convolution(b,a);
14
            for(int i=0;i<sz;++i) a.push_back(c[i]);</pre>
            sz*=2:
16
17
       return form(a,n);
18 }
19 vector<int> inv(vector<int> v,int n)
20 {
       v=form(v,n);assert(v[0]!=0);if(v.size()==1) {
       return {inv(v[0])};} vector<int> v1=trmi(v);
22
       vector < int > a = v1 * v; a = form(a, 2*n);
       vector<int> b((n+1)/2); for(int i=0; i<b.size()</pre>
       ;++i) b[i]=a[2*i];
24
       vector<int> ans1=inv(b,b.size());vector<int>
       ans2(n); for(int i=0; i<n; ++i) {if(i%2==0) ans2[i
       \exists = ans1[i/2]: else ans2[i]=0:
       return form(v1*ans2,n);
26 F
27 vector<int> operator/(vector<int> a,vector<int> b)
28 {
29
       while(!a.empty() && a.back()==0) a.pop_back();
       while(!b.empty() && b.back() == 0) b.pop_back();
30
       int n=a.size();int m=b.size();if(n<m) return</pre>
       {}:
       reverse(a.begin(),a.end()); reverse(b.begin(),b.
       end()); vector < int > ans = a * inv(b, n-m+1); while (ans
       .size()>n-m+1) ans.pop_back();
32
       reverse(ans.begin(),ans.end()); while(!ans.empty
       () && ans.back()==0) ans.pop_back(); return ans;
33 1
34 vector<int> operator%(vector<int> a, vector <int> b)
35 {
36
       vector<int> ans=a-b*(a/b); while(!ans.empty() &&
        ans.back() == 0) ans.pop_back(); return ans;
l37 1
```