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# Теория чисел

## 1.1 KTO

```
1 int gcd(int a, int b, int &x, int &y) {
    if (b==0) { x = 1; y = 0; return a; }
    int d = gcd(b,a%b,y,x);
   y - = a / b * x;
    return d;
6 }
7 int inv(int r, int m) {
    int x, y;
     gcd(r,m,x,y);
    return (x+m) %m;
11 }
12 int crt(int r, int n, int c, int m) { return r + ((
       c - r) % m + m) * inv(n, m) % m * n; }
  1.2 Алгоритм Миллера — Рабина
1 __int128 one=1;
2 int po(int a, int b, int p)
3 {
4
     int res=1;
     while(b) {if(b & 1) {res=(res*one*a)%p;--b;} else
        {a=(a*one*a)%p;b>>=1;}} return res;
6 }
7 bool chprime(int n) //miller-rabin
8 {
9
     if(n==2) return true;
10
     if(n<=1 || n%2==0) return false;</pre>
     int h=n-1; int d=0; while (h\%2==0) \{h/=2; ++d; \}
     for(int a:{2, 3, 5, 7, 11, 13, 17, 19, 23, 29,
      31, 37})
13
       {
14
      if(a==n) return true;
       int u=po(a,h,n);bool ok=0;
16
       if(u%n==1) continue;
       for(int c=0;c<d;++c)</pre>
17
18
19
         if ((u+1) %n==0) {ok=1;break;}
20
         u=(u*one*u)%n;
21
22
       if(!ok) return false;
23
24
     return true;
25 }
```

## 1.3 Алгоритм Берлекэмпа — Месси

https://mzhang2021.github.io/cp-blog/berlekamp-massey/

```
1 template < typename T>
2 vector<T> berlekampMassey(const vector<T> &s) {
    int n = s.size(), l = 0, m = 1;
3
     vector < T > b(n), c(n);
     T ld = b[0] = c[0] = 1;
     for (int i=0; i<n; i++, m++) {</pre>
6
       T d = s[i];
       for (int j=1; j<=1; j++)</pre>
9
        d += c[j] * s[i-j];
10
       if (d == 0) continue;
       vector < T> temp = c;
11
       T coef = d / ld;
       for (int j=m; j < n; j ++) c[j] -= coef * b[j-m];
14
       if (2 * 1 <= i) {</pre>
15
         1 = i + 1 - 1;
         b = temp;
16
         ld = d;
17
         m = 0;
19
       }
     }
     c.resize(1 + 1);
22
     c.erase(c.begin());
23
     for (T &x : c)
24
      x = -x;
25
     return c;
26 }
```

# 2 Графы

## 2.1 SCC и 2-SAT

```
Алгоритм ищет сильносвязные компоненты в графе g, если есть путь i \to j, то scc[i] \le scc[j]
В случае 2-SAT рёбра i \Rightarrow j и (i \oplus 1) \Rightarrow (i \oplus 1) должны быть
```

В случае 2- $\mathcal{SAT}$  рёбра  $i\Rightarrow j$  и  $(j\oplus 1)\Rightarrow (i\oplus 1)$  должны быть добавлены одновременно.

```
1 vector \langle int \rangle g(2 * n);
2 vector < vector < int >> r(g.size());
3 for (int i = 0; i < g.size(); ++i) {
    for (int j : g[i]) r[j].push_back(i);
5 }
6 vector < int > used(g.size()), tout(g.size());
7 int time = 0;
8 auto dfs = [&](auto dfs, int cur) -> void {
    if (used[cur]) return;
    used[cur] = 1;
    for (int nxt : g[cur]) {
11
12
      dfs(dfs, nxt);
13
14
    // used[cur] = 2;
15
    tout[cur] = time++;
16 };
17 for (int i = 0; i < g.size(); ++i) if (!used[i])
       dfs(dfs, i);
18 vector<int> ind(g.size());
19 iota(ind.begin(), ind.end(), 0);
20 sort(all(ind), [&](int i, int j){return tout[i] >
      tout[j];});
21 vector < int > scc(g.size(), -1);
22 auto go = [&](auto go, int cur, int color) -> void
     if (scc[cur] != -1) return;
24
    scc[cur] = color;
    for (int nxt : r[cur]) {
      go(go, nxt, color);
27
    }
28 };
29 \text{ int color} = 0;
30 for (int i : ind) {
    if (scc[i] == -1) go(go, i, color++);
33 for (int i = 0; i < g.size() / 2; ++i) {
    if (scc[2 * i] == scc[2 * i + 1]) "IMPOSSIBLE"
    if (scc[2 * i] < scc[2 * i + 1]) {</pre>
35
36
      // !i => i, assign i = true
    } else {
      // i => !i, assign i = false
38
39
    }
40 }
```

## 2.2 Эйлеров цикл

```
1 vector < vector < pair < int , int >>> g(n); // pair { nxt ,
      idx }
2 vector<pair<int, int>> e(p.size());
3 // build graph
4 vector < int > in(n), out(n);
5 for (auto [u, v] : e) in[v]++, out[u]++;
6 vector<int> used(m), it(n), cycle;
7 auto dfs = [&](auto dfs, int cur) -> void {
    while (true) {
9
      while (it[cur] < g[cur].size() && used[g[cur][
       it[cur]].second]) it[cur]++;
      if (it[cur] == g[cur].size()) return;
      auto [nxt, idx] = g[cur][it[cur]];
11
       used[idx] = true;
      dfs(dfs, nxt);
13
14
       cycle.push_back(idx);
15
16 };
17 \text{ int } cnt = 0, odd = -1;
18 for (int i = 0; i < n; ++i){
    if (out[i] && odd == -1) odd = i;
19
    if (in[i] != out[i]) {
      if (in[i] + 1 == out[i]) odd = i;
21
22
       if (abs(in[i] - out[i]) > 1) return {}; // must
```

```
23
       cnt++:
24
    }
25 }
26 if (cnt != 0 && cnt != 2) return {}; // must hold
27 // for undirected find odd vertex (and count that #
       of odd is 0 or 2)
28 dfs(dfs, odd);
29 reverse(cycle.begin(), cycle.end());
30 if (cycle.size() != m) return {};
   2.3 Компоненты рёберной двусвязности
 1 int n, m;
 2 \text{ cin } >> \text{ n } >> \text{ m};
 3 vector \langle vector \langle int \rangle \rangle g(n + 1);
int u, v, c; cin >> u >> v >> c;c--;
     col[{u,v}]=col[{v,u}]=c;
     g[u].push_back(v);
 Q
     g[v].push_back(u);
10 }
11 vector <int> used(n + 1);
12 vector <int> newCompWithoutParent(n + 1), h(n + 1),
       up(n + 1);
13 auto findCutPoints = [&] (auto self, int u, int p)
       -> void {
     used[u] = 1;
     up[u] = h[u];
15
     for (int v : g[u]) {
       if (!used[v]) {
17
18
         h[v] = h[u] + 1;
19
         self(self, v, u);
         up[u] = min(up[u], up[v]);
20
         if (up[v] >= h[u]) {
22
           newCompWithoutParent[v] = 1;
23
24
       }
       else {
26
         up[u] = min(up[u], h[v]);
27
28
    }
29 };
30 for (int u = 1; u <= n; ++u) {
    if (!used[u]) {
31
32
       findCutPoints(findCutPoints, u, u);
33
34 }
35 int ptr = 0;
36 vector <map <int, int> > colors(m);
37 auto markComponents = [&] (auto self, int u, int
       cur) -> void {
38
     used[u] = 1;
     for (int v : g[u]) {
       if (!used[v]) {
40
         if (newCompWithoutParent[v]) {
41
          ptr++;
43
           self(self, v, ptr - 1);
         else
46
           self(self, v, cur);
         }
       else if (h[v] < h[u]) {</pre>
49
         comp[{u,v}] = comp[{v,u}] = cur;
         int c = col[{u,v}];
         colors[cur][u] |= 1 << c;
         colors[cur][v] |= 1 << c;
54
    }
56 };
57 used.assign(n + 1, 0);
58 for (int u = 1; u <= n; ++u) {
    if (!used[u]) {
       markComponents (markComponents, u, -1);
61
62 }
|63 \text{ for (int comp = 0; comp < m; ++comp) } 
     vector <int> cnt(4);
```

```
Структуры данных
65
     int tot = 0;
     for (auto [u, mask] : colors[comp]) {
66
       tot |= mask;
                                                                   4.1 Дерево Фенвика
67
68
       cnt[bp(mask)]++;
69
                                                                 1 int fe[maxn]; /// fenwick tree
70
    if (bp(tot)<3) {
                                                                 2 void pl(int pos,int val) {while(pos<maxn) {fe[pos</pre>
71
       continue;
                                                                       ]+=val;pos|=(pos+1);}}
72
                                                                 3 int get(int pos) {int ans=0; while(pos>=0) {ans+=fe[
     if (cnt[2] || cnt[3]>2) {
73
                                                                       pos];pos&=(pos+1);--pos;} return ans;} /// [0,
74
       cout << "Yes" << endl;</pre>
                                                                       pos] - vkluchitelno!!!
75
       return:
                                                                 4 int get(int 1,int r) {return get(r-1)-get(1-1);} //
     }
76
                                                                        / summa na [l,r)
77 }
78 cout << "No" << endl;
                                                                   4.2 Дерево отрезков
                                                                 1 template < typename Data, typename Mod, typename
UniteData, typename UniteMod, typename Apply>
      xor, and, or-свёртки
                                                                   struct MassSegmentTree {
                                                                     int h, n;
                                                                     Data zd;
1 const int p = 998244353;
                                                                     Mod zm:
2 vector<int> band(vector<int> a, vector<int> b)
                                                                     vector < Data > data;
3 {
                                                                     vector < Mod > mod;
4
     int n=0; while((1<<n)<a.size()) ++n;</pre>
     a.resize(1<<n);b.resize(1<<n);
                                                                     UniteData ud; // Data (Data, Data)
                                                                     UniteMod um; // Mod (Mod, Mod);
     for(int i=0;i<n;++i) for(int mask=0;mask<(1<<n)</pre>
6
       ; ++ mask) if(mask & (1<<i)) {a[mask-(1<<i)]+=a[}
                                                                     Apply a; // Data (Data, Mod, int); last argument
       mask];a[mask-(1<<i)]%=p;}
                                                                       is the length of current segment (could be used
     \label{for:mask=0} \mbox{for(int i=0;i<n;++i)} \ \ \mbox{for(int mask=0;mask<(1<<n)}
                                                                        for range += and sum counting, for instance)
       ; ++ mask) if (mask & (1<<i)) {b[mask-(1<<i)]+=b[
                                                                12
       mask];b[mask-(1<<i)]%=p;}
                                                                     template < typename I>
8
     vector < int > c(1 << n,0);
                                                                14
                                                                     {\tt MassSegmentTree(int\ sz,\ Data\ zd,\ Mod\ zm,}
                                                                       UniteData ud, UniteMod um, Apply a, I init) : h (__lg(sz > 1 ? sz - 1 : 1) + 1), n(1 << h), zm(
9
     for(int mask=0; mask<(1<<n); ++ mask) {c[mask]=a[</pre>
       mask]*b[mask];c[mask]%=p;}
                                                                       zm), zd(zd), data(2 * n, zd), mod(n, zm), ud(ud
     for(int i=0;i<n;++i) for(int mask=0;mask<(1<<n)</pre>
       ; ++ mask) if(!(mask & (1<<i))) {c[mask]-=c[mask]
                                                                       ), um(um), a(a) {
                                                                       for (int i = 0; i < sz; ++i) data[i + n] = init</pre>
       +(1<<i)]:c[mask]%=p:}
11
                                                                       (i);
     return c;
                                                                        for (int i = n - 1; i > 0; --i) data[i] = ud(
13 vector<int> bor(vector<int> a, vector<int> b)
                                                                       data[2 * i], data[2 * i + 1]);
14 {
                                                                17
                                                                     }
     int n=0; while((1<<n)<a.size()) ++n;</pre>
15
                                                                18
16
     a.resize(1<<n);b.resize(1<<n);
                                                                19
                                                                     MassSegmentTree(int sz, Data zd, Mod zm,
                                                                       UniteData ud, UniteMod um, Apply a) : h(__lg(sz
17
     for(int i=0;i<n;++i) for(int mask=0;mask<(1<<n)</pre>
                                                                        > 1 ? sz - 1 : 1) + 1), n(1 << h), zm(zm), zd(
       ; ++ mask) if (!(mask & (1<<i))) {a[mask+(1<<i)]+=
       a[mask]; a[mask+(1<<ii)]%=p;}
                                                                       zd), data(2 * n, zd), mod(n, zm), ud(ud), um(um
     for(int i=0;i<n;++i) for(int mask=0;mask<(1<<n)</pre>
                                                                       ), a(a) {}
       ; ++ mask) if (!(mask & (1<<i))) {b[mask+(1<<i)]+=
                                                                20
       b[mask];b[mask+(1<<ii)]%=p;}
                                                                     void push(int i) {
                                                                       if (mod[i] == zm) return;
     vector < int > c(1 << n,0);
20
     for(int mask=0; mask<(1<<n); ++mask) {c[mask]=a[</pre>
                                                                        apply(2 * i, mod[i]);
                                                                       apply(2 * i + 1, mod[i]);
       mask] * b [mask]; c [mask] % = p;}
                                                                       mod[i] = zm;
                                                                25
     for(int i=0;i<n;++i) for(int mask=0;mask<(1<<n)</pre>
                                                                     }
       ; ++ mask) if (mask & (1<<i)) {c[mask] -= c[mask]
                                                                26
       -(1<<i)];c[mask]%=p;}
                                                                28
                                                                     // is used only for apply
22
     return c;
23 }
                                                                29
                                                                     int length(int i) { return 1 << (h - __lg(i)); }</pre>
24 vector < int > bxor (vector < int > a, vector < int > b)
                                                                30
                                                                31
25 {
                                                                     // is used only for descent
26
     assert(p\%2==1); int inv2=(p+1)/2;
                                                                     int left(int i) {
27
     int n=0; while((1<<n)<a.size()) ++n;</pre>
                                                                33
                                                                       int lvl = __lg(i);
                                                                        return (i & ((1 << lvl) - 1)) * (1 << (h - lvl)
28
     a.resize(1<<n);b.resize(1<<n);
                                                                34
     for(int i=0;i<n;++i) for(int mask=0;mask<(1<<n)</pre>
                                                                       );
                                                                35
       ;++mask) if(!(mask & (1<<i))) {int u=a[mask], v=
       a[mask+(1<<i)]; a[mask+(1<<i)]=(u+v)%p; a[mask]=(
                                                                37
                                                                     // is used only for descent
30
     for(int i=0;i<n;++i) for(int mask=0;mask<(1<<n)</pre>
                                                                     int right(int i) {
                                                                38
       ; ++ mask) if(!(mask & (1<<i))) {int u=b[mask], v=
                                                                39
                                                                       int lvl = __lg(i);
       b[mask+(1<<i)];b[mask+(1<<i)]=(u+v)%p;b[mask]=(
                                                                       return ((i & ((1 << lvl) - 1)) + 1) * (1 << (h
                                                                40
       u-v)%p;}
                                                                        - lvl));
     vector < int > c(1 << n, 0);</pre>
     for(int mask=0; mask<(1<<n); ++mask) {c[mask]=a[</pre>
32
       mask] * b [mask]; c [mask] % = p;}
                                                                     template < typename S>
     for(int i=0;i<n;++i) for(int mask=0;mask<(1<<n)</pre>
                                                                44
                                                                     void apply(int i, S x) {
       ;++mask) if(!(mask & (1<<i))) {int u=c[mask], v=
                                                                       data[i] = a(data[i], x, length(i));
       c[mask+(1<<i)];c[mask+(1<<i)]=((v-u)*inv2)%p;c[
                                                                       if (i < n) mod[i] = um(mod[i], x);</pre>
       mask]=((u+v)*inv2)%p;}
                                                                47
34
     return c;
                                                                48
35 }
                                                                     void update(int i) {
```

3

```
if (mod[i] != zm) return;
50
 51
        data[i] = ud(data[2 * i], data[2 * i + 1]);
 52
53
 54
      template < typename S>
 55
      void update(int 1, int r, S x) { // [1; r)
 56
       1 += n, r += n;
        for (int shift = h; shift > 0; --shift) {
 58
          push(l >> shift);
 59
          push((r - 1) >> shift);
60
61
        for (int lf = 1, rg = r; lf < rg; lf /= 2, rg</pre>
        /= 2) {
62
         if (lf & 1) apply(lf++, x);
63
          if (rg & 1) apply(--rg, x);
 64
65
        for (int shift = 1; shift <= h; ++shift) {</pre>
66
          update(1 >> shift);
67
          update((r - 1) >> shift);
68
 69
70
 71
      Data get(int 1, int r) { // [1; r)
       1 += n, r += n;
        for (int shift = h; shift > 0; --shift) {
 73
 74
          push(1 >> shift);
 75
          push((r - 1) >> shift);
 76
 77
        Data leftRes = zd, rightRes = zd;
 78
        for (; 1 < r; 1 /= 2, r /= 2) {</pre>
 79
         if (1 & 1) leftRes = ud(leftRes, data[1++]);
          if (r & 1) rightRes = ud(data[--r], rightRes)
 81
        }
 82
        return ud(leftRes, rightRes);
83
 84
      // l \in [0; n) && ok(get(1, 1), 1);
 85
      // returns last r: ok(get(1, r), r)
86
      template < typename C>
 88
      int lastTrue(int 1, C ok) {
89
       1 += n;
 90
        for (int shift = h; shift > 0; --shift) push(1
        >> shift);
91
        Data cur = zd;
92
        do f
93
          1 >>= __builtin_ctz(1);
          Data with1;
95
          with1 = ud(cur, data[1]);
96
          if (ok(with1, right(1))) {
            cur = with1;
98
            ++1;
99
          } else {
            while (1 < n) {
100
1.01
              push(1);
              Data with2;
103
              with2 = ud(cur, data[2 * 1]);
104
              if (ok(with2, right(2 * 1))) {
105
                cur = with2;
                1 = 2 * 1 + 1;
106
107
              } else {
108
                1 = 2 * 1;
109
              }
            }
110
111
            return 1 - n;
          }
112
       } while (1 & (1 - 1));
113
114
       return n;
115
116
117
      // r \in [0; n) && ok(get(r, r), r);
      // returns first 1: ok(get(1, r), 1)
119
      template < typename C>
120
      int firstTrue(int r, C ok) {
121
       r += n;
        for (int shift = h; shift > 0; --shift) push((r
         - 1) >> shift);
123
        Data cur = zd;
124
        while (r & (r - 1)) {
         r >>= __builtin_ctz(r);
                                                             4
```

```
26
         Data with1;
         with1 = ud(data[--r], cur);
28
         if (ok(with1, left(r))) {
           cur = with1;
30
         } else {
           while (r < n) {
             push(r);
33
             Data with 2;
34
             with2 = ud(data[2 * r + 1], cur);
             if (ok(with2, right(2 * r))) {
36
               cur = with2;
               r = 2 * r;
37
             } else {
39
               r = 2 * r + 1;
40
             }
41
42
           return r - n + 1;
43
         }
44
       }
       return 0;
45
46
     }
47 };
   4.2.1 Примеры использования
    • Взятие максимума и прибавление константы
    1 MassSegmentTree segtree(n, OLL, OLL,
    2 [](int x, int y) { return max(x, y); },
    3 [](int x, int y) { return x + y; },
    4 [](int x, int y, int len) { return x + y; });
    • Взятие суммы и прибавление константы
    1 MassSegmentTree segtree(n, OLL, OLL,
    2 [](int x, int y) { return x + y; },
    3 [](int x, int y) { return x + y; },
    4 [](int x, int y, int len) { return x + y * len;
    • Взятие суммы и присовение
    1 MassSegmentTree segtree(n, OLL, -1LL,
    2 [](int x, int y) { return x + y; },
    3 [](int x, int y) { return y; },
    4 [](int x, int y, int len) { return y * len; });
   4.3 Ordered set
 1 #include <ext/pb_ds/assoc_container.hpp>
 2 #include <ext/pb_ds/tree_policy.hpp>
 4 using namespace __gnu_pbds;
 5 using namespace std;
 7 using ordered_set = tree<int, null_type, less<>,
       rb_tree_tag, tree_order_statistics_node_update
   4.4 Convex hull trick
 1 11 div_up(11 a, 11 b) { return a/b+((a^b)>0&&a%b);
       } // divide a by b rounded up
 3 struct Line {
 4
      11 k, b;
       Line() : k(), b() {}
 6
       Line (ll _k, ll _b) : k(_k), b(_b) {}
 9
       ll getVal(ll x) {
10
           return k * x + b;
11
12 };
13 struct Hull {
       vector<Line> lines;
14
       vector<1l> borders;
16
```

```
St. Petersburg State University (Ushakov, Turevskii, Danilevich)
17
       Hull() : lines(), borders() {}
18
19
       void addLine(Line L) {
20
           while(!lines.empty()) {
                if (lines.back().getVal(borders.back())
21
        >= L.getVal(borders.back())) {
22
                     lines.pop_back();
23
                    borders.pop_back();
24
                } else break;
25
26
            if (lines.empty()) {
2.7
                lines.push_back(L);
                borders.push_back(OLL); //leftmost
       query
29
30
            if (lines.back().k <= L.k) return;</pre>
31
            ll x = div_up(L.b - lines.back().b, lines.
32
       back().k - L.k); //must work for negative!
33
           lines.push_back(L);
34
            borders.push_back(x);
35
36
       ll getMinVal(ll x) {
       int pos = upper_bound(borders.begin(),
borders.end(), x) - borders.begin();
38
           if (pos == 0) throw;
39
           pos - - ;
40
            return lines[pos].getVal(x);
41
42 1:
   4.5 Центроидная декомпозиция
1 vector \langle int \rangle sz(n), lvl(n, -1);
2 auto dfs = [&](auto dfs, int cur, int prev) -> int
       if (lvl[cur] != -1) return 0;
4
       sz[cur] = 1;
       for (auto [nxt, w] : g[cur]) {
            if (nxt != prev) sz[cur] += dfs(dfs, nxt,
6
       cur);
```

```
8
       return sz[cur];
9 };
10 auto find = [&](auto find, int cur, int prev, int
       tot) -> int {
11
       int bch = -1, bsz = 0;
       for (auto [nxt, w] : g[cur]) {
12
            if (nxt == prev | | lvl[nxt] != -1) continue
13
            if (sz[nxt] > bsz) {
14
15
                bch = nxt;
                bsz = sz[nxt];
           }
18
19
       if (bsz + bsz <= tot) return cur;</pre>
2.0
       return find(find, bch, cur, tot);
21 }:
22 dfs(dfs, 0, 0);
23 auto c = find(find, 0, 0, sz[0]);
24 vector<pair<int, int>> stack{{c, 0}};
25 int ans = INF;
26 while (!stack.empty()) {
27
       auto [centroid, 1] = stack.back();
2.8
       stack.pop_back();
29
       lvl[centroid] = 1;
       for (auto [nxt, w] : g[centroid]) {
   if (lvl[nxt] != -1) continue;
30
3.1
           dfs(dfs, nxt, centroid);
33
           int new_centroid = find(find, nxt, centroid
       , sz[nxt]);
34
           stack.push_back({new_centroid, lvl[centroid
       ] + 1});
35
       }
36 }
```

# Строковые алгоритмы

# Префикс-функция

```
1 vector<int> prefix_function(string s) {
```

4

vector < int > a;

void build(const vector<int> &x) {

```
vector < int > p(s.size());
3
     for (int i = 1; i < s.size(); ++i) {</pre>
      p[i] = p[i - 1];
4
       while (p[i] && s[p[i]] != s[i]) p[i] = p[p[i] -
5
       1];
6
      p[i] += s[i] == s[p[i]];
    }
    return p;
9 }
  5.2 Z-функция
1 vector <int> z_function (string s) { // z[i] - lcp
      of s and s[i:]
   int n = (int) s.length();
   vector < int > z (n);
4 for (int i=1, l=0, r=0; i<n; ++i) {
    if (i <= r)</pre>
     z[i] = min (r-i+1, z[i-1]);
    while (i+z[i] < n && s[z[i]] == s[i+z[i]])
     ++z[i];
9
    if (i+z[i]-1 > r)
10
     l = i, r = i+z[i]-1;
   }
11
12
   return z;
13 }
  5.3 Алгоритм Манакера
1 vector<int> manacher_odd(const string &s) {
     vector < int > man(s.size(), 0);
3
     int 1 = 0, r = 0;
     int n = s.size();
     for (int i = 1; i < n; i++) {</pre>
      if (i <= r) {</pre>
7
        man[i] = min(r - i, man[1 + r - i]);
9
       while (i + man[i] + 1 < n && i - man[i] - 1 >=
       0 && s[i + man[i] + 1] == s[i - man[i] - 1]) {
10
        man[i]++;
      if (i + man[i] > r) {
12
13
        1 = i - man[i];
14
         r = i + man[i];
16
    }
17
     return man;
18 }
19 // abacaba : (0 1 0 3 0 1 0)
20 // abbaa : (0 0 0 0 0)
22 vector <int> manacher_even(const string &s) {
23
    assert(s.size());
24
     string t;
     for (int i = 0; i + 1 < s.size(); ++i) {</pre>
26
      t += s[i];
27
       t += '#';
28
    }
29
    t += s.back();
30
     auto odd = manacher_odd(t);
31
     vector <int> ans;
    for (int i = 1; i < odd.size(); i += 2) {</pre>
32
33
       ans.push_back((odd[i]+1)/2);
34
35
     return ans;
36 }
37 // abacaba : (0 0 0 0 0 0)
38 // abbaa : (0 2 0 1)
  5.4 Суфмассив
  Переработанный китайский суффмассив
1 const int inf = 1e9;
2 struct rmq {
3
    int n:
```

```
6
       assert(x.size() == n);
       for (int i = 0; i < n; ++i) a[n + i] = x[i];</pre>
       for (int i = n - 1; i > 0; --i) a[i] = min(a[2
8
                                                                4
       * i], a[2 * i + 1]);
                                                                5
9
                                                                6
10
     rmq(int n) : n(n), a(2 * n, inf) {}
11
     void put(int i, int x) {
       a[i + n] = min(a[i + n], x);
12
       for (i = (i + n) / 2; i > 0; i /= 2) {
                                                                10
         a[i] = min(a[i * 2], a[i * 2 + 1]);
14
                                                                12
16
     }
17
     int getMin(int 1, int r) { //[1;r)
18
       assert(1 < r):
19
       int res = inf;
                                                                15
       for (1 += n, r += n; 1 < r; 1 /= 2, r /= 2) {</pre>
         if (1 & 1) res = min(res, a[1++]);
21
                                                                17
22
         if (r & 1) res = min(res, a[--r]);
                                                                18
23
                                                                19
24
       return res;
                                                               20
25
                                                                21
26 1:
27 template <typename T>
                                                               23
                                                                24
28 struct suar {
                                                               25
29
       vector <int> sa, lcp, rank; rmq t;
30
       suar (T s, int lim=256) : t((int)s.size() - 1)
                                                               26
       { // s must be nonempty, 0 < s[i] < lim!
                                                                27
           int n = (int)s.size() + 1, k = 0, a, b; s.
                                                               28
31
       app(0);
                                                                29
32
                                                                30
           vector <int> x(s.begin(), s.end()), y(n),
       ws(max(n, lim)); rank.resize(n);
           sa = lcp = y, iota(sa.begin(), sa.end(), 0)
34
           for (int j = 0, p = 0; p < n; j = max(111,</pre>
       j * 2), lim = p) {
                                                               34
35
                p = j, iota(y.begin(), y.end(), n - j);
36
                for (int i = 0; i < n; i++) if (sa[i]</pre>
                                                                36
       >= j) y[p++] = sa[i] - j;
37
                fill(ws.begin(), ws.end(), 0);
                                                                38
                for (int i = 0; i < n; i++) ws[x[i]]++;
for (int i = 1; i < lim; i++) ws[i] +=</pre>
39
                                                                40
       ws[i - 1];
                                                                42
40
                for (int i = n; i--; ) sa[--ws[x[y[i
       ]]]] = y[i];
41
                swap(x, y), p = 1, x[sa[0]] = 0;
                for (int i = 1; i < n; i++) a = sa[i -</pre>
42
       1], b = sa[i], x[b] = (y[a] == y[b] && y[a + j]
        == y[b + j]) ? p - 1 : p++;
43
            for (int i = 1; i < n; i++) rank[sa[i]] = i</pre>
44
45
           for (int i = 0, j; i < n - 1; lcp[rank[i</pre>
       ++]]=k)
                                                                50
                for (k && k--, j = sa[rank[i] - 1];
46
                                                               51
47
                    s[i + k] == s[j + k]; k++);
                                                               52
            sa.erase(sa.begin()); lcp.erase(lcp.begin()
       ); lcp.erase(lcp.begin());
49
           t.build(lcp);
50
            for (auto &e : rank) {
51
                e--;
53
       }
                                                                4
54
       int getLcp(int i, int j) {
           i = rank[i]; j = rank[j];
56
           if (j < i) {</pre>
                                                                7
57
             swap(i, j);
58
59
           if (i == j) {
                                                                9
60
             return inf;
61
                                                                11
            else {
62
63
             return t.getMin(i, j);
                                                                12
64
65
       }
                                                               14
66 };
                                                               16
                                                               17
        Алгоритм Ахо — Корасик
                                                               18
```

```
1 struct node{
```

```
int next[alpha] = {}, link[alpha] = {};
    int suf = 0;
    11 visited = 0. ans = 0:
    vector<int> term;
    node() {}
7 };
9 vector < node > mem;
11 int get_next(int nd, char c) {
    if (!mem[nd].next[c - a]) { mem[nd].next[c - a] =
       mem.size(); mem.emplace_back(); }
    return mem[nd].next[c - a];
14 }
16 void find(string s, vector<string> t) {
    mem.reserve(1e6 + 100); mem.clear();
    mem.emplace_back(); mem.emplace_back();
    // Oth element is nullptr, 1st is the root
    int q = t.size();
    for (int j = 0; j < q; ++ j) {
      int cur = 1;
      for (char c : ts[j]) cur = get_next(cur, c);
      mem[cur].term.push_back(j);
    vector<int> bfs_order;
    queue < int > bfs;
        node &root = mem[1];
        root.suf = 1;
        for (char c = a; c < a + alpha; ++c) {</pre>
            root.link[c - a] = (root.next[c - a] ?
      root.next[c - a] : 1);
        bfs.push(1);
    }
    while (!bfs.empty()) {
      int cur idx = bfs.front():
      bfs.pop();
      node &cur = mem[cur_idx];
      bfs_order.push_back(cur_idx);
       for (char c = a; c < a + alpha; ++c) {</pre>
        int nxt_idx = cur.next[c - a];
        if (!nxt_idx) continue;
        node &nxt = mem[nxt_idx];
        nxt.suf = (cur_idx == 1 ? 1 : mem[cur.suf].
      link[c - a]);
        for (char c = a; c < a + alpha; ++c) {</pre>
          nxt.link[c - a] = (nxt.next[c - a] ? nxt.
      next[c - a] : mem[nxt.suf].link[c - a]);
        bfs.push(nxt_idx);
    }
    // do something
  5.6 Дерево палиндромов
1 struct palindromic{
    int n;
    vector<int> p, suf{0, 0}, len{-1, 0};
    vector<array<int, alpha>> to{{}};
    int sz = 2;
    palindromic(const string &s) : n(s.size()), p(n +
       1, 1) {
      suf.reserve(n):
      len.reserve(n);
      for (int i = 0; i < n; ++i) {</pre>
        auto check = [&](int 1) { return i > 1 && s[i
      ] == s[i - 1 - 1]; };
        int par = p[i];
        while (!check(len[par])) par = suf[par];
         if (to[par][s[i] - a]) {
          p[i + 1] = to[par][s[i] - a];
           continue;
        p[i + 1] = sz++;
19
         to[par][s[i] - a] = p[i + 1];
        to.emplace_back();
```

6

```
2.1
         len.emplace_back(len[par] + 2);
22
         do {
23
          par = suf[par];
         } while (!check(len[par]));
24
25
         int link = to[par][s[i] - a];
         if (link == p[i + 1]) link = 1;
26
27
         suf.emplace_back(link);
29
    }
30 };
```

## 6 Потоки

## 6.1 Алгоритм Диница

```
1 #define pb push_back
2 struct Dinic{
3 struct edge{
    int to, flow, cap;
5 }:
7 const static int N = 555; //count of vertices
9 vector<edge> e;
10 vector < int > g[N + 7];
11 int dp[N + 7];
12 int ptr[N + 7];
13
14 void clear(){
   for (int i = 0; i < N + 7; i++) g[i].clear();</pre>
15
16
    e.clear();
17 }
18
19 void addEdge(int a, int b, int cap){
   g[a].pb(e.size());
2.0
21
    e.pb({b, 0, cap});
    g[b].pb(e.size());
23
    e.pb({a, 0, 0});
24 }
26 int minFlow, start, finish;
27
28 bool bfs(){
   for (int i = 0; i < N; i++) dp[i] = -1;</pre>
29
    dp[start] = 0;
31
    vector<int> st:
32
    int uk = 0;
    st.pb(start);
34
    while(uk < st.size()){</pre>
35
       int v = st[uk++];
       for (int to : g[v]){
36
37
         auto ed = e[to];
         if (ed.cap - ed.flow >= minFlow && dp[ed.to]
       == -1){
39
           dp[ed.to] = dp[v] + 1;
40
           st.pb(ed.to);
41
         }
      }
42
43
    }
44
     return dp[finish] != -1;
46
47 int dfs(int v, int flow){
    if (v == finish) return flow;
     for (; ptr[v] < g[v].size(); ptr[v]++){</pre>
49
50
       int to = g[v][ptr[v]];
       edge ed = e[to];
51
       if (ed.cap - ed.flow >= minFlow && dp[ed.to] ==
52
        dp[v] + 1){
53
         int add = dfs(ed.to, min(flow, ed.cap - ed.
       flow));
         if (add){
55
           e[to].flow += add;
           e[to ^ 1].flow -= add;
56
           return add;
58
         }
59
      }
60
    }
61
     return 0;
62 }
```

```
63
64 int dinic(int start, int finish){
    Dinic::start = start;
66
     Dinic::finish = finish:
67
     int flow = 0;
68
     for (minFlow = (1 << 30); minFlow; minFlow >>= 1)
69
       while(bfs()){
         for (int i = 0; i < N; i++) ptr[i] = 0;</pre>
70
71
         while(int now = dfs(start, (int)2e9 + 7))
       flow += now:
72
       }
     }
73
74
     return flow;
75 }
76 } dinic;
   6.2 Mincost k-flow
   6.2.1 Строим граф
 1 struct edge {
     int next, capacity, cost, flow = 0;
 3
     edge() = default;
 4
 5
 6
     edge(int next, int capacity, int cost) : next(
       next), capacity(capacity), cost(cost) {}
 8
     int rem() const { return capacity - flow; }
     int operator+=(int f) { return flow += f; }
11
12
     int operator -=(int f) { return flow -= f; }
13 };
14 auto addEdge = [&](auto from, auto next, auto
       capacity, int cost) {
15
     g[from].push_back(e.size());
16
     e.emplace_back(next, capacity, cost);
     g[next].push_back(e.size());
18
     e.emplace_back(from, 0, -cost);
19 };
   Если граф ориентированный, то addEdge вызываем один раз. Если
   неориентированный, то два, вот так:
 1 addEdge(u, v, capacity, cost);
 2 addEdge(v, u, capacity, cost);
   6.2.2 Запускаем Форда — Беллмана
 1 vector<11> phi(n, 0);
 2 auto fordBellman = [&](int s, int t) {
     phi.assign(n, 0);
     for (int iter = 0; iter < n; ++iter) {</pre>
 5
       bool changed = false;
 6
       for (int u = 0; u < n; ++u) {</pre>
         for (auto index : g[u]) {
 7
 8
           auto edge = e[index];
 9
           if (edge.rem() > 0 && phi[edge.next] > phi[
       u] + edge.cost) {
10
             phi[edge.next] = phi[u] + edge.cost;
              changed = true;
12
           }
         }
14
15
       if (!changed) break;
16
     }
17 }:
18 fordBellman(s, t);
   6.2.3 Ищем кратчайший путь Дейкстрой с потенциалами
 1 vector<11> dist;
 2 vector<int> from;
 3 vector < bool > cnt;
 4 auto dijkstra = [&](int s, int t) {
     dist.assign(n, 1e18);
     from.assign(n, -1);
```

```
7
     cnt.assign(n, false);
8
     dist[s] = 0;
9
     set <pair <int, int> > se;
     se.insert({0, s});
10
     while ((int)(se.size())) {
      int cur = se.begin()->y;
12
       se.erase(se.begin());
13
       cnt[cur] = true;
14
15
       for (int index : g[cur]) {
         auto &edge = e[index];
16
         if (edge.rem() == 0) continue;
17
         11 weight = edge.cost + phi[cur] - phi[edge.
18
       next];
19
        if (dist[edge.next] > dist[cur] + weight) {
20
           se.erase({dist[edge.next], edge.next});
21
           dist[edge.next] = dist[cur] + weight;
           se.insert({dist[edge.next], edge.next});
22
23
           from[edge.next] = cur;
24
      }
25
26
    if (dist[t] == (11) 1e18) return -1LL;
27
2.8
    11 cost = 0;
     for (int p = t; p != s; p = from[p]) {
       for (auto index : g[from[p]]) {
30
         auto &edge = e[index];
31
         11 weight = edge.cost + phi[from[p]] - phi[
32
       edge.next];
         if (edge.rem() > 0 && edge.next == p && dist[
33
       edge.next] == dist[from[p]] + weight) {
34
           edge += 1;
           e[index ^ 1] -= 1;
35
           cost += edge.cost;
36
37
           break;
38
39
      }
40
41
    for (int i = 0; i < n; ++i) {</pre>
      phi[i] += dist[i];
42
43
44
    return cost:
45 };
46 \ 11 \ cost = 0;
47 for (int flow = 0; flow < k; ++flow) {
   ll a = dijkstra(s, t);
    if (a == -1) {
  cout << "-1\n";
49
50
       return:
    }
52
53
     cost += a;
54 }
  6.2.4 Восстанавливаем ответ
1 auto findPath = [&](int s, int t) {
    vector < int > ans;
3
    int cur = s:
    while (cur != t) {
      for (auto index : g[cur]) {
         auto &edge = e[index];
         if (edge.flow <= 0) continue;</pre>
         edge -= 1;
         e[index ^ 1] += 1;
Q
         ans.push_back(index / 4);
11 // index / 4 because each edge has 4 copies
         cur = edge.next;
12
13
         break:
       }
14
16
    return ans;
17 };
18 for (int flow = 0; flow < k; ++flow) {
    auto p = findPath(s, t);
19
20
     cout << p.size() << '';</pre>
    for (int x : p) cout << x + 1 << ''; cout << '\n';
21
2.2
23
```

## 7 FFT & co

## 7.1 NTT & co

```
1 #define int long long
 2 using namespace std;
 3 typedef long long 11;
 4 const int p=998244353;
 5 int po(int a, int b) {if(b==0) return 1; if(b==1)
       return a; if(b%2==0) {int u=po(a,b/2); return (u
       *1LL*u)%p;} else {int u=po(a,b-1);return (a*1LL
       *u)%p;}}
 6 int inv(int x) {return po(x,p-2);}
7 template < int M, int K, int G> struct Fft {
8  // 1, 1/4, 1/8, 3/8, 1/16, 5/16, 3/16, 7/16, ...
     int g[1 << (K - 1)];</pre>
10
     Fft() : g() { //if tl constexpr...
       static_assert(K >= 2, "Fft: K >= 2 must hold");
       g[0] = 1;
12
       g[1 << (K - 2)] = G;
14
        for (int 1 = 1 << (K - 2); 1 >= 2; 1 >>= 1) {
          g[1 >> 1] = (g[1] * 1LL* g[1]) % M;
16
17
       assert((g[1]*1LL * g[1]) % M == M - 1);
       for (int 1 = 2; 1 <= 1 << (K - 2); 1 <<= 1) {
18
         for (int i = 1; i < 1; ++i) {</pre>
           g[1 + i] = (g[1] * 1LL * g[i]) % M;
21
         7.
22
     }
23
24
     void fft(vector<int> &x) const {
25
       const int n = x.size();
26
       assert(n <= 1 << K);
       for (int h = __builtin_ctz(n); h--; ) {
  const int l = (1 << h);</pre>
27
28
29
          for (int i = 0; i < n >> (h+1); ++i) {
           for (int j = i << (h+1); j < (((i << 1) +
30
       1) << h); ++j) {
              const int t = (g[i] * 1LL* x[j | 1]) % M;
              x[j | 1] = x[j] - t;
              if (x[j|1] < 0) x[j | 1] += M;</pre>
              x[j]+=t;
              if (x[j] >= M) x[j] -= M;
35
           }
36
         }
37
38
       }
39
        for (int i = 0, j = 0; i < n; ++i) {
         if (i < j) std::swap(x[i], x[j]);</pre>
41
         for (int 1 = n; (1 >>= 1) && !((j ^= 1) & 1);
        ) {}
42
43
     }
44
     vector < int > convolution (const vector < int > &a,
       const vector <int> &b) const {
45
       if(a.empty() || b.empty()) return {};
       const int na = a.size(), nb = b.size();
       int n, invN = 1;
47
48
       for (n = 1; n < na + nb - 1; n <<= 1) invN = ((</pre>
       invN & 1) ? (invN + M) : invN) >> 1;
       vector < int > x(n, 0), y(n, 0);
49
       std::copy(a.begin(), a.end(), x.begin());
51
       std::copy(b.begin(), b.end(), y.begin());
       fft(x);
       fft(y);
54
       for (int i = 0; i < n; ++i) x[i] = (((
       static_cast<long long>(x[i]) * y[i]) % M) *
       invN) % M;
55
       std::reverse(x.begin() + 1, x.end());
56
       fft(x);
       x.resize(na + nb - 1);
57
58
       return x;
59
60 };
61 Fft < 998244353,23,31 > muls;
62 vector < int > form (vector < int > v, int n)
63 {
64
     while(v.size()<n) v.push_back(0);</pre>
65
     while(v.size()>n) v.pop_back();
66
     return v;
67 }
```

```
68 vector <int> operator *(vector <int> v1, vector <int>
 69 {
                                                                  8
 70
      return muls.convolution(v1, v2);
                                                                  Q
                                                                           ^= bit;
 72 vector<int> operator +(vector<int> v1, vector<int>
                                                                  11
                                                                  12
 73 {
                                                                  13
      while(v2.size()<v1.size()) v2.push_back(0); while</pre>
 74
                                                                  14
        (v1.size() < v2.size()) v1.push_back(0);
                                                                  15
      for(int i=0;i<v1.size();++i) {v1[i]+=v2[i];if(v1[</pre>
 75
                                                                  16
        i]>=p) v1[i]-=p; else if(v1[i]<0) v1[i]+=p;}
 76
      return v1;
 77 }
                                                                  19
 78 vector<int> operator -(vector<int> v1, vector<int>
                                                                  20
        v2)
 79 {
                                                                  22
 80
      int sz=max(v1.size(), v2.size()); while(v1.size()
        sz) v1.push_back(0); while(v2.size() < sz) v2.
                                                                 24
        push_back(0);
                                                                 25
      for(int i=0;i<sz;++i) {v1[i]-=v2[i];if(v1[i]<0)</pre>
                                                                  26
        v1[i]+=p; else if(v1[i]>=p) v1[i]-=p;} return
                                                                 27
                                                                           }
                                                                 28
                                                                        }
                                                                  29
 82 }
 83 vector<int> trmi(vector<int> v)
                                                                  30
 84 {
                                                                  31
 85
      for(int i=1;i<v.size();i+=2) {if(v[i]>0) v[i]=p-v
                                                                  32
        [i]; else v[i]=(-v[i]);}
                                                                 33
                                                                           x /= n;
 86
      return v;
                                                                  34
 87 }
                                                                  35 }
 88 vector<int> deriv(vector<int> v)
 89 {
90
      if(v.empty()) return{};
91
      vector<int> ans(v.size()-1);
                                                                        b.end());
 92
      for(int i=1;i<v.size();++i) ans[i-1]=(v[i]*1LL*i)</pre>
                                                                  38
                                                                       int n = 1;
        %p;
                                                                  39
93
      return ans;
                                                                  40
                                                                        n <<= 1;
94 }
95 vector < int > integ(vector < int > v)
 96 {
97
      vector < int > ans(v.size()+1); ans[0]=0;
                                                                  44
98
      for(int i=1;i<v.size();++i) ans[i-1]=(v[i]*1LL*i)</pre>
                                                                  46
        %p;
99
      return ans;
100 }
                                                                  48
101 vector < int > mul(vector < vector < int > v)
102 {
103
      if(v.size() == 1) return v[0];
104
      vector < vector < int > > v1, v2; for (int i=0; i < v. size ()</pre>
                                                                  52
        /2;++i) v1.push_back(v[i]); for(int i=v.size()
        /2; i < v. size(); ++i) v2.push_back(v[i]);
105
      return muls.convolution(mul(v1), mul(v2));
                                                                  54
106
                                                                  55 }
107 vector<int> inv1(vector<int> v,int n)
108 {
109
      assert(v[0]!=0);
                                                                        Геома
110
      int sz=1; v=form(v,n); vector <int> a={inv(v[0])};
111
      while (sz<n)
112
      {
        vector < int > vsz; for (int i = 0; i < min(n, 2*sz); ++i)</pre>
113
        vsz.push_back(v[i]);
114
        vector < int > b = ((vector < int >) {1}) - muls.
                                                                  3
        convolution(a, vsz);
                                                                  4
        for (int i=0; i < sz; ++i) assert(b[i]==0);</pre>
116
        b.erase(b.begin(),b.begin()+sz);
                                                                  5
117
        vector < int > c = muls.convolution(b,a);
118
        for(int i=0;i<sz;++i) a.push_back(c[i]);</pre>
119
        sz*=2:
                                                                  8
120
      }
                                                                  9
121
      return form(a,n):
                                                                  10
                                                                             }
122 }
    7.2 старое доброе FFT
                                                                  14
 1 using cd = complex < double >;
 2 const double PI = acos(-1);
                                                                  15
                                                                  16
 3
                                                                         }:
 4 void fft(vector < cd > & a, bool invert) {
                                                                  17
                                                                         auto lowert = [&](Point p) { //first vertex in
```

int n = a.size():

```
for (int i = 1, j = 0; i < n; i++) {</pre>
      int bit = n >> 1;
      for (; j & bit; bit >>= 1)
        j ^= bit;
      if (i < j)
        swap(a[i], a[j]);
    for (int len = 2; len <= n; len <<= 1) {</pre>
      double ang = 2 * PI / len * (invert ? -1 : 1);
       cd wlen(cos(ang), sin(ang));
       for (int i = 0; i < n; i += len) {</pre>
        cd w(1);
         for (int j = 0; j < len / 2; j++) {</pre>
           cd u = a[i+j], v = a[i+j+len/2] * w;
          a[i+j] = u + v;
           a[i+j+len/2] = u - v;
           w *= wlen;
    if (invert) {
      for (cd & x : a)
36 vector<int> multiply(vector<int> const& a, vector<
     int > const & b) {
    vector < cd > fa(a.begin(), a.end()), fb(b.begin(),
    while (n < a.size() + b.size())</pre>
    fa.resize(n):
    fb.resize(n);
    fft(fa, false);
    fft(fb, false);
    for (int i = 0; i < n; i++)</pre>
     fa[i] *= fb[i];
    fft(fa, true);
     vector<int> result(n);
    for (int i = 0; i < n; i++)</pre>
      result[i] = round(fa[i].real());
     while(!result.empty() && !result.back()) result.
      pop_back();
    return result;
  8.1 Касательные
       auto max = [&] (auto cmp) {
          int k = 0;
           for (int lg = 18; lg >= 0; --lg) {
               int i = k + (1 << lg), j = k - (1 << lg)
               i = (i \% n + n) \% n;
               j = (j \% n + n) \% n;
               array<int, 3> ind{i, j, k};
               sort(all(ind), cmp);
               k = ind[2];
           return k;
       auto uppert = [&](Point p) { //last vertex in
       counterclockwise order about p
          auto cmp = [&] (int i, int j) {return (a[i]
         p) < (a[j] - p); };
           return max(cmp);
```

counterclockwise order about p

9

```
18
           auto cmp = [&] (int i, int j) {return (a[i]
        - p) > (a[j] - p); };
19
           return max(cmp);
20
       }:
21
       auto uppertinf = [&](Point p) { //upper tangent
        line parallel to vector p
22
           swap(p.x, p.y);
23
           p.x = -p.x;
           auto cmp = [&] (int i, int j) { return a[i]
2.4
        % p < a[j] % p; };
25
           return max(cmp);
26
       auto lowertinf = [&](Point p) { //lower tangent
        line parallel to vector \mathbf{p}
2.8
           swap(p.x, p.y);
           p.x = -p.x;
           auto cmp = [&] (int i, int j) { return a[i]
30
        % p > a[j] % p; };
31
           return max(cmp);
       }:
32
```

## 8.2 Примитивы

```
1 struct Point {
       int x, y;
3
       Point(){}
4
       Point (int x_, int y_) {
           x = x_{-}; y = y_{-};
       Point operator + (Point p) {
           return Point(x+p.x,y+p.y);
9
10
       Point operator - (Point p) {
           return Point(x - p.x, y - p.y);
12
13
       int operator * (Point p) {
           return x * p.y - y * p.x;
       }
15
16
       int operator % (Point p) {
17
           return x * p.x + y * p.y;
       }
18
19
       bool operator < (Point v) {</pre>
20
           return (*this) * v > 0;
2.1
       }
       bool operator > (Point v) {
23
           return v < (*this);</pre>
24
25
       bool operator <= (Point v) {</pre>
26
           return (*this) * v >= 0;
27
28 };
29 bool line(Point a, Point b, Point c) {
       return (b-a)*(c-b)==0;
31 }
32 bool ord(Point a, Point p, Point b) {
33
       return (p - a) %(p - b) <0;
34 }
```

## 8.3 Точка нестрого внутри выпуклости

```
1
       auto inT = [&] (Point a, Point b, Point c,
       Point p) {
           a = a-p; b = b-p; c = c-p;
           return abs(a*b)+abs(b*c)+abs(c*a) == abs(a*
3
      b+b*c+c*a):
5
       auto inP = [&] (Point p) { //a must be in
       counterclockwise order!
           int 1 = 1, r = n - 1;
           while (1 < r - 1) {
               int m = (1 + r) / 2;
9
               if ((a[m] - a[0]) < (p - a[0])) {</pre>
10
                   1 = m;
               }
12
               else {
                   r = m;
           }
15
16
           return inT(a[1], a[0], a[r], p);
      }:
```

## 9 Разное

#### 9.1 Флаги компияции

```
-DLOCAL -Wall -Wextra -pedantic -Wshadow -Wformat=2
-Wfloat-equal -Wconversion -Wlogical-op -Wshift-overflow=2
-Wduplicated-cond -Wcast-qual -Wcast-align -D_GLIBCXX_DEBUG
-D_GLIBCXX_DEBUG_PEDANTIC -D_FORTIFY_SOURCE=2
-fsanitize=address -fsanitize=undefined -fno-sanitize-recover
-fstack-protector -std=c++2a
```

#### 9.1.1 Сеточка в vim

https://codeforces.com/blog/entry/122540

```
1 i | <esc>25A | <esc>2 o+<esc>25A---+<esc>3 Vky35Pdd
```

## 9.2 Что сделать на пробном туре

- Убедиться, что работаеют все IDE. Разобраться, как настраивать в них LOCAL.
- В системе ML это ML или RE?
- Максимальный размер файла
- Можно посмотреть на время работы серверов позапускав Флойда — Варшалла

#### 9.3 Шаблон

```
1 #include < bits / stdc++.h>
3 using namespace std;
5 #define int long long
6 #define app push_back
7 #define all(x) x.begin(), x.end()
8 #ifdef LOCAL
9 #define debug(...) [](auto...a){ ((cout << a <<
       ' '), ...) << endl; }(#__VA_ARGS__, ":",
      __VA_ARGS__)
10 #else
11 #define debug(...)
12 #endif
13
14 int32_t main() {
15
       cin.tie(0);ios_base::sync_with_stdio(0);
16 }
```