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1 Теория чисел

1.1 КТО

```

1 int gcd(int a, int b, int &x, int &y) {
2     if (b==0) { x = 1; y = 0; return a; }
3     int d = gcd(b, a%b, x, y);
4     swap(x, y);
5     y -= a/b*x;
6     return d;
7 }
8 int inv(int r, int m) {
9     int x, y;
10    gcd(r, m, x, y);
11    return (x+m)%m;
12 }
13 int crt(int r, int n, int c, int m) { return r + ((
    c - r) % m + m) * inv(n, m) % m * n; }
```

1.2 Алгоритм Миллера — Рабина

```

1 __int128 one=1;
2 int po(int a, int b, int p)
3 {
4     int res=1;
5     while(b) {if(b & 1) {res=(res*one*a)%p; --b;} else
        {a=(a*one*a)%p; b>>=1;}} return res;
6 }
7 bool chprime(int n) //miller-rabin
8 {
9     if(n==2) return true;
10    if(n<=1 || n%2==0) return false;
11    int h=n-1; int d=0; while(h%2==0) {h/=2; ++d;}
12    for(int a:{2, 3, 5, 7, 11, 13, 17, 19, 23, 29,
        31, 37})
13    {
14        if(a==n) return true;
15        int u=po(a, h, n); bool ok=0;
16        if(u%n==1) continue;
17        for(int c=0; c<d; ++c)
18        {
19            if((u+1)%n==0) {ok=1; break;}
20            u=(u*one*u)%n;
21        }
22        if(!ok) return false;
23    }
24    return true;
25 }
```

2 Графы

2.1 *SCC* и 2-*SAT*

Алгоритм ищет сильносвязные компоненты в графе g , если есть путь $i \rightarrow j$, то $scc[i] \leq scc[j]$

В случае 2-*SAT* рёбра $i \Rightarrow j$ и $(j \oplus 1) \Rightarrow (i \oplus 1)$ должны быть добавлены одновременно.

```

1 vector<vector<int>> g(2 * n);
2 vector<vector<int>> r(g.size());
3 for (int i = 0; i < g.size(); ++i) {
4     for (int j : g[i]) r[j].push_back(i);
5 }
6 vector<int> used(g.size()), tout(g.size());
7 int time = 0;
8 auto dfs = [&](auto dfs, int cur) -> void {
9     if (used[cur]) return;
10    used[cur] = 1;
11    for (int nxt : g[cur]) {
12        dfs(dfs, nxt);
13    }
14    // used[cur] = 2;
15    tout[cur] = time++;
16 };
17 for (int i = 0; i < g.size(); ++i) if (!used[i])
    dfs(dfs, i);
18 vector<int> ind(g.size());
19 iota(ind.begin(), ind.end(), 0);
```

```

20 sort(all(ind), [&](int i, int j){return tout[i] >
    tout[j];});
21 vector<int> scc(g.size(), -1);
22 auto go = [&](auto go, int cur, int color) -> void
    {
23     if (scc[cur] != -1) return;
24     scc[cur] = color;
25     for (int nxt : r[cur]) {
26         go(go, nxt, color);
27     }
28 };
29 int color = 0;
30 for (int i : ind) {
31     if (scc[i] == -1) go(go, i, color++);
32 }
33 for (int i = 0; i < g.size() / 2; ++i) {
34     if (scc[2 * i] == scc[2 * i + 1]) "IMPOSSIBLE"
35     if (scc[2 * i] < scc[2 * i + 1]) {
36         // !i => i, assign i = true
37     } else {
38         // i => !i, assign i = false
39     }
40 }

```

2.2 Эйлеров цикл

```

1 vector<vector<pair<int, int>>> g(n); // pair{nxt,
    idx}
2 vector<pair<int, int>> e(p.size());
3 // build graph
4 vector<int> in(n), out(n);
5 for (auto [u, v] : e) in[v]++, out[u]++;
6 vector<int> used(m), it(n), cycle;
7 auto dfs = [&](auto dfs, int cur) -> void {
8     while (true) {
9         while (it[cur] < g[cur].size() && used[g[cur][
            it[cur]].second]) it[cur]++;
10        if (it[cur] == g[cur].size()) return;
11        auto [nxt, idx] = g[cur][it[cur]];
12        used[idx] = true;
13        dfs(dfs, nxt);
14        cycle.push_back(idx);
15    }
16 };
17 int cnt = 0, odd = -1;
18 for (int i = 0; i < n; ++i){
19     if (out[i] && odd == -1) odd = i;
20     if (in[i] != out[i]) {
21         if (in[i] + 1 == out[i]) odd = i;
22         if (abs(in[i] - out[i]) > 1) return {}; // must
            hold
23         cnt++;
24     }
25 }
26 if (cnt != 0 && cnt != 2) return {}; // must hold
27 // for undirected find odd vertex (and count that #
    of odd is 0 or 2)
28 dfs(dfs, odd);
29 reverse(cycle.begin(), cycle.end());
30 if (cycle.size() != m) return {};

```

2.3 Компоненты рёберной двусвязности

```

1 int n, m;
2 cin >> n >> m;
3 vector<vector<int>> g(n + 1);
4 map<pair<int, int>, int> comp, col;
5 for (int i = 0; i < m; ++i) {
6     int u, v, c; cin >> u >> v >> c; c--;
7     col[{u, v}] = col[{v, u}] = c;
8     g[u].push_back(v);
9     g[v].push_back(u);
10 }
11 vector<int> used(n + 1);
12 vector<int> newCompWithoutParent(n + 1), h(n + 1),
    up(n + 1);
13 function<void(int, int)> findCutPoints = [&] (int u
    , int p) {

```

```

14     used[u] = 1;
15     up[u] = h[u];
16     for (int v : g[u]) {
17         if (!used[v]) {
18             h[v] = h[u] + 1;
19             findCutPoints(v, u);
20             up[u] = min(up[u], up[v]);
21             if (up[v] >= h[u]) {
22                 newCompWithoutParent[v] = 1;
23             }
24         }
25         else {
26             up[u] = min(up[u], h[v]);
27         }
28     }
29 };
30 for (int u = 1; u <= n; ++u) {
31     if (!used[u]) {
32         findCutPoints(u, u);
33     }
34 }
35 int ptr = 0;
36 vector<map<int, int>> colors(m);
37 function<void(int, int)> markComponents = [&] (int
    u, int cur) {
38     used[u] = 1;
39     for (int v : g[u]) {
40         if (!used[v]) {
41             if (newCompWithoutParent[v]) {
42                 ptr++;
43                 markComponents(v, ptr - 1);
44             }
45             else {
46                 markComponents(v, cur);
47             }
48         }
49         else if (h[v] < h[u]) {
50             comp[{u, v}] = comp[{v, u}] = cur;
51             int c = col[{u, v}];
52             colors[cur][u] |= 1 << c;
53             colors[cur][v] |= 1 << c;
54         }
55     }
56 };
57 used.assign(n + 1, 0);
58 for (int u = 1; u <= n; ++u) {
59     if (!used[u]) {
60         markComponents(u, -1);
61     }
62 }
63 for (int comp = 0; comp < m; ++comp) {
64     vector<int> cnt(4);
65     int tot = 0;
66     for (auto [u, mask] : colors[comp]) {
67         tot |= mask;
68         cnt[bp(mask)]++;
69     }
70     if (bp(tot) < 3) {
71         continue;
72     }
73     if (cnt[2] || cnt[3] > 2) {
74         cout << "Yes" << endl;
75         return;
76     }
77 }
78 cout << "No" << endl;

```

3 xor, and, or-свёртки

3.1 and-свёртка

```

1 vector<int> band(vector<int> a, vector<int> b)
2 {
3     int n=0; while((1<<n)<a.size()) ++n;
4     a.resize(1<<n); b.resize(1<<n);
5     for(int i=0; i<n; ++i) for(int mask=0; mask<(1<<n)
        ; ++mask) if(mask & (1<<i)) {a[mask-(1<<i)]+=a[
            mask]; a[mask-(1<<i)]%=p;}

```

```

6   for(int i=0;i<n;++i) for(int mask=0;mask<(1<<n)
    ;++mask) if(mask & (1<<i)) {b[mask-(1<<i)]+=b[
    mask];b[mask-(1<<i)]%=p;}
7   vector<int> c(1<<n,0);
8   for(int mask=0;mask<(1<<n);++mask) {c[mask]=a[
    mask]*b[mask];c[mask]%=p;}
9   for(int i=0;i<n;++i) for(int mask=0;mask<(1<<n)
    ;++mask) if(!(mask & (1<<i))) {c[mask]-=c[mask
    +(1<<i)];c[mask]%=p;}
10  return c;
11 }

```

3.2 or-свёртка

```

1 vector<int> bor(vector<int> a,vector<int> b)
2 {
3   int n=0;while((1<<n)<a.size()) ++n;
4   a.resize(1<<n);b.resize(1<<n);
5   for(int i=0;i<n;++i) for(int mask=0;mask<(1<<n)
    ;++mask) if(!(mask & (1<<i))) {a[mask+(1<<i)]+=
    a[mask];a[mask+(1<<i)]%=p;}
6   for(int i=0;i<n;++i) for(int mask=0;mask<(1<<n)
    ;++mask) if(!(mask & (1<<i))) {b[mask+(1<<i)]+=
    b[mask];b[mask+(1<<i)]%=p;}
7   vector<int> c(1<<n,0);
8   for(int mask=0;mask<(1<<n);++mask) {c[mask]=a[
    mask]*b[mask];c[mask]%=p;}
9   for(int i=0;i<n;++i) for(int mask=0;mask<(1<<n)
    ;++mask) if(mask & (1<<i)) {c[mask]-=c[mask
    -(1<<i)];c[mask]%=p;}
10  return c;
11 }

```

3.3 xor-свёртка

```

1 vector<int> bxor(vector<int> a,vector<int> b)
2 {
3   assert(p%2==1);int inv2=(p+1)/2;
4   int n=0;while((1<<n)<a.size()) ++n;
5   a.resize(1<<n);b.resize(1<<n);
6   for(int i=0;i<n;++i) for(int mask=0;mask<(1<<n)
    ;++mask) if(!(mask & (1<<i))) {int u=a[mask],v=
    a[mask+(1<<i)];a[mask+(1<<i)]=(u+v)%p;a[mask]=(
    u-v)%p;}
7   for(int i=0;i<n;++i) for(int mask=0;mask<(1<<n)
    ;++mask) if(!(mask & (1<<i))) {int u=b[mask],v=
    b[mask+(1<<i)];b[mask+(1<<i)]=(u+v)%p;b[mask]=(
    u-v)%p;}
8   vector<int> c(1<<n,0);
9   for(int mask=0;mask<(1<<n);++mask) {c[mask]=a[
    mask]*b[mask];c[mask]%=p;}
10  for(int i=0;i<n;++i) for(int mask=0;mask<(1<<n)
    ;++mask) if(!(mask & (1<<i))) {int u=c[mask],v=
    c[mask+(1<<i)];c[mask+(1<<i)]=((v-u)*inv2)%p;c[
    mask]=((u+v)*inv2)%p;}
11  return c;

```

4 Структуры данных

4.1 Дерево Фенвика

```

1 int fe[maxn]; /// fenwick tree
2 void pl(int pos,int val) {while(pos<maxn) {fe[pos
    ]+=val;pos|=(pos+1);}}
3 int get(int pos) {int ans=0;while(pos>=0) {ans+=fe[
    pos];pos&=(pos+1);--pos;} return ans;} /// [0,
    pos] - vkluchitelno!!!
4 int get(int l,int r) {return get(r-1)-get(l-1);} //
    / summa na [l,r]

```

4.2 Ordered set

```

1 #include <ext/pb_ds/assoc_container.hpp>
2 #include <ext/pb_ds/tree_policy.hpp>
3
4 using namespace __gnu_pbds;

```

```

5 using namespace std;
6
7 using ordered_set = tree<int, null_type, less<>,
    rb_tree_tag, tree_order_statistics_node_update
    >;

```

4.3 Дерево отрезков

```

1 template<typename Data, typename Mod, typename
    UniteData, typename UniteMod, typename Apply>
2 struct MassSegmentTree {
3   int h, n;
4   Data zd;
5   Mod zm;
6   vector<Data> data;
7   vector<Mod> mod;
8
9   UniteData ud; // Data (Data, Data)
10  UniteMod um; // Mod (Mod, Mod);
11  Apply a; // Data (Data, Mod, int); last argument
    is the length of current segment (could be used
    for range += and sum counting, for instance)
12
13  template<typename I>
14  MassSegmentTree(int sz, Data zd, Mod zm,
    UniteData ud, UniteMod um, Apply a, I init) : h(
    __lg(sz > 1 ? sz - 1 : 1) + 1), n(1 << h), zm(
    zm), zd(zd), data(2 * n, zd), mod(n, zm), ud(ud
    ), um(um), a(a) {
15    for (int i = 0; i < sz; ++i) data[i + n] = init
    (i);
16    for (int i = n - 1; i > 0; --i) data[i] = ud(
    data[2 * i], data[2 * i + 1]);
17  }
18
19  MassSegmentTree(int sz, Data zd, Mod zm,
    UniteData ud, UniteMod um, Apply a) : h(__lg(sz
    > 1 ? sz - 1 : 1) + 1), n(1 << h), zm(zm), zd(
    zd), data(2 * n, zd), mod(n, zm), ud(ud), um(um
    ), a(a) {}
20
21  void push(int i) {
22    if (mod[i] == zm) return;
23    apply(2 * i, mod[i]);
24    apply(2 * i + 1, mod[i]);
25    mod[i] = zm;
26  }
27
28  // is used only for apply
29  int length(int i) { return 1 << (h - __lg(i)); }
30
31  // is used only for descent
32  int left(int i) {
33    int lvl = __lg(i);
34    return (i & ((1 << lvl) - 1)) * (1 << (h - lvl
    ));
35  }
36
37  // is used only for descent
38  int right(int i) {
39    int lvl = __lg(i);
40    return ((i & ((1 << lvl) - 1)) + 1) * (1 << (h
    - lvl));
41  }
42
43  template<typename S>
44  void apply(int i, S x) {
45    data[i] = a(data[i], x, length(i));
46    if (i < n) mod[i] = um(mod[i], x);
47  }
48
49  void update(int i) {
50    if (mod[i] != zm) return;
51    data[i] = ud(data[2 * i], data[2 * i + 1]);
52  }
53
54  template<typename S>
55  void update(int l, int r, S x) { // [l; r)
56    l += n, r += n;

```

```

57     for (int shift = h; shift > 0; --shift) {
58         push(l >> shift);
59         push((r - 1) >> shift);
60     }
61     for (int lf = l, rg = r; lf < rg; lf /= 2, rg
62         /= 2) {
63         if (lf & 1) apply(lf++, x);
64         if (rg & 1) apply(--rg, x);
65     }
66     for (int shift = 1; shift <= h; ++shift) {
67         update(l >> shift);
68         update((r - 1) >> shift);
69     }
70 }
71
72 Data get(int l, int r) { // [l; r)
73     l += n, r += n;
74     for (int shift = h; shift > 0; --shift) {
75         push(l >> shift);
76         push((r - 1) >> shift);
77     }
78     Data leftRes = zd, rightRes = zd;
79     for (; l < r; l /= 2, r /= 2) {
80         if (l & 1) leftRes = ud(leftRes, data[l++]);
81         if (r & 1) rightRes = ud(data[--r], rightRes);
82     }
83     return ud(leftRes, rightRes);
84 }
85
86 // l \in [0; n) && ok(get(l, l), l);
87 // returns last r: ok(get(l, r), r)
88 template<typename C>
89 int lastTrue(int l, C ok) {
90     l += n;
91     for (int shift = h; shift > 0; --shift) push(l
92         >> shift);
93     Data cur = zd;
94     do {
95         l >>= __builtin_ctz(l);
96         Data with1;
97         with1 = ud(cur, data[l]);
98         if (ok(with1, right(l))) {
99             cur = with1;
100             ++l;
101         } else {
102             while (l < n) {
103                 push(l);
104                 Data with2;
105                 with2 = ud(cur, data[2 * l]);
106                 if (ok(with2, right(2 * l))) {
107                     cur = with2;
108                     l = 2 * l + 1;
109                 } else {
110                     l = 2 * l;
111                 }
112             }
113             return l - n;
114         } while (l & (l - 1));
115     }
116
117 // r \in [0; n) && ok(get(r, r), r);
118 // returns first l: ok(get(l, r), l)
119 template<typename C>
120 int firstTrue(int r, C ok) {
121     r += n;
122     for (int shift = h; shift > 0; --shift) push((r
123         - 1) >> shift);
124     Data cur = zd;
125     while (r & (r - 1)) {
126         r >>= __builtin_ctz(r);
127         Data with1;
128         with1 = ud(data[--r], cur);
129         if (ok(with1, left(r))) {
130             cur = with1;
131         } else {
132             while (r < n) {
133                 push(r);

```

```

133         Data with2;
134         with2 = ud(data[2 * r + 1], cur);
135         if (ok(with2, right(2 * r))) {
136             cur = with2;
137             r = 2 * r;
138         } else {
139             r = 2 * r + 1;
140         }
141     }
142     return r - n + 1;
143 }
144 }
145 return 0;
146 }
147 };

```

4.3.1 Примеры использования

- Взятие максимума и прибавление константы

```

1 MassSegmentTree segtree(n, 0LL, 0LL,
2 [](int x, int y) { return max(x, y); },
3 [](int x, int y) { return x + y; },
4 [](int x, int y, int len) { return x + y; });

```

- Взятие суммы и прибавление константы

```

1 MassSegmentTree segtree(n, 0LL, 0LL,
2 [](int x, int y) { return x + y; },
3 [](int x, int y) { return x + y; },
4 [](int x, int y, int len) { return x + y * len;
5     });

```

- Взятие суммы и присвоение

```

1 MassSegmentTree segtree(n, 0LL, -1LL,
2 [](int x, int y) { return x + y; },
3 [](int x, int y) { return y; },
4 [](int x, int y, int len) { return y * len; });

```

5 Строковые алгоритмы

5.1 Префикс-функция

```

1 vector<int> prefix_function(string s) {
2     vector<int> p(s.size());
3     for (int i = 1; i < s.size(); ++i) {
4         p[i] = p[i - 1];
5         while (p[i] && s[p[i]] != s[i]) p[i] = p[p[i] -
6             1];
7         p[i] += s[i] == s[p[i]];
8     }
9     return p;

```

5.2 Z-функция

```

1 vector<int> z_function (string s) { // z[i] - lcp
2     of s and s[i:]
3     int n = (int) s.length();
4     vector<int> z (n);
5     for (int i=1, l=0, r=0; i<n; ++i) {
6         if (i <= r)
7             z[i] = min (r-i+1, z[i-l]);
8         while (i+z[i] < n && s[z[i]] == s[i+z[i]])
9             ++z[i];
10        if (i+z[i]-1 > r)
11            l = i, r = i+z[i]-1;
12    }
13    return z;

```

5.3 Алгоритм Манакера

```

1 vector<int> manacher_odd(const string &s) {
2     vector<int> man(s.size(), 0);
3     int l = 0, r = 0;
4     int n = s.size();
5     for (int i = 1; i < n; i++) {
6         if (i <= r) {
7             man[i] = min(r - i, man[l + r - i]);
8         }
9         while (i + man[i] + 1 < n && i - man[i] - 1 >=
10             0 && s[i + man[i] + 1] == s[i - man[i] - 1]) {
11             man[i]++;
12         }
13         if (i + man[i] > r) {
14             l = i - man[i];
15             r = i + man[i];
16         }
17     }
18     return man;
19 }
20 // abacaba : (0 1 0 3 0 1 0)
21 // abbaa : (0 0 0 0 0)
22 vector<int> manacher_even(const string &s) {
23     assert(s.size());
24     string t;
25     for (int i = 0; i + 1 < s.size(); ++i) {
26         t += s[i];
27         t += '#';
28     }
29     t += s.back();
30     auto odd = manacher_odd(t);
31     vector<int> ans;
32     for (int i = 1; i < odd.size(); i += 2) {
33         ans.push_back((odd[i]+1)/2);
34     }
35     return ans;
36 }
37 // abacaba : (0 0 0 0 0 0)
38 // abbaa : (0 2 0 1)

```

5.4 Суфмассив

Китайский суфмассив

```

1 struct SuffixArray {
2     vector<int> sa, lcp;
3     SuffixArray(string &s, int lim=256) {
4         int n = (int)s.size() + 1, k = 0, a, b;
5         vector<int> x(s.begin(), s.end() + 1), y(n),
6             ws(max(n, lim)), rank(n);
7         sa = lcp = y, iota(sa.begin(), sa.end(), 0);
8         for (int j = 0, p = 0; p < n; j = max(1ll, j *
9             2), lim = p) {
10             p = j, iota(y.begin(), y.end(), n - j);
11             for (int i = 0; i < n; i++) if (sa[i] >= j) y
12                 [p++] = sa[i] - j;
13             fill(ws.begin(), ws.end(), 0);
14             for (int i = 0; i < n; i++) ws[x[i]]++;
15             for (int i = 1; i < lim; i++) ws[i] += ws[i -
16                 1];
17             for (int i = n; i--;) sa[--ws[x[y[i]]]] = y[i];
18             swap(x, y), p = 1, x[sa[0]] = 0;
19             for (int i = 1; i < n; i++) a = sa[i - 1], b
20                 = sa[i], x[b] = (y[a] == y[b] && y[a + j] == y[
21                     b + j]) ? p - 1 : p++;
22             for (int i = 1; i < n; i++) rank[sa[i]] = i;
23             for (int i = 0, j; i < n - 1; lcp[rank[i++]] = k)
24                 for (k && k--, j = sa[rank[i] - 1];
25                     s[i + k] == s[j + k]; k++);
26         }
27     }
28 };
29 struct Rmq {
30     const int INF = 1e9;
31     int n;
32     vector<int> rmq;
33     Rmq() {}

```

```

28 void build(const vector<int> &x) {
29     assert(x.size() == n);
30     for (int i = 0; i < n; ++i) rmq[n + i] = x[i];
31     for (int i = n - 1; i > 0; --i) rmq[i] = min(
32         rmq[2 * i], rmq[2 * i + 1]);
33 }
34 Rmq(int n) : n(n), rmq(2 * n, INF) {}
35 void put(int i, int x) {
36     rmq[i + n] = min(rmq[i + n], x);
37     for (i = (i + n) / 2; i > 0; i /= 2) {
38         rmq[i] = min(rmq[i * 2], rmq[i * 2 + 1]);
39     }
40 }
41 int getMin(int l, int r) { //[l;r)
42     assert(l < r);
43     int res = INF;
44     for (l += n, r += n; l < r; l /= 2, r /= 2) {
45         if (l & 1) res = min(res, rmq[l++]);
46         if (r & 1) res = min(res, rmq[--r]);
47     }
48     return res;
49 }
50 };
51 struct Lc {
52     vector<int> pos;
53     Rmq rmq;
54     Lc(string s) : rmq(s.size()) {
55         SuffixArray sa(s);
56         auto ss = sa.sa;
57         ss.erase(ss.begin());
58         auto lcp = sa.lcp;
59         lcp.erase(lcp.begin());
60         lcp.erase(lcp.begin());
61         pos.resize(s.size());
62         assert(s.size() == ss.size());
63         for (int i = 0; i < ss.size(); ++i) {
64             pos[ss[i]] = i;
65         }
66         int n = s.size();
67         assert(lcp.size() == n - 1);
68         rmq.build(lcp);
69     }
70     int getLcp(int i, int j) {
71         i = pos[i]; j = pos[j];
72         if (j < i) {
73             swap(i, j);
74         }
75         if (i == j) {
76             return 1e18;
77         }
78         else {
79             return rmq.getMin(i, j);
80         }
81     }
82 };
83 };
84 };
85 };

```

5.5 Алгоритм Ахо — Корасик

```

1 struct node{
2     node *next[26] = {}, *link[26] = {};
3     node *suf = nullptr;
4     vector<int> term;
5     int visited = 0;
6     node() {}
7     node *get_next(char c) {
8         if (next[c - 'a'] == nullptr) next[c - 'a'] =
9             new node();
10        return next[c - 'a'];
11    }
12 };
13 node *root = new node();
14 for (int i = 0; i < s.size(); ++i) {
15     node *cur = root;
16     for (char c : s[i]) cur = cur->get_next(c);
17     cur->term.push_back(i);

```

```

17 }
18 vector<node*> bfs_order;
19 queue<node*> bfs;
20 root->suf = root;
21 for (char c = 'a'; c <= 'z'; ++c) root->link[c - 'a']
    = (root->next[c - 'a'] ? root->next[c - 'a']
      : root);
22 bfs.push(root);
23 while (!bfs.empty()) {
24     node *cur = bfs.front();
25     bfs_order.push_back(cur);
26     bfs.pop();
27     for (char c = 'a'; c <= 'z'; ++c) {
28         node *nxt = cur->next[c - 'a'];
29         if (!nxt) continue;
30         nxt->suf = (cur == root ? cur : cur->suf->link[
            c - 'a']);
31         for (char c = 'a'; c <= 'z'; ++c) nxt->link[c -
            'a'] = (nxt->next[c - 'a'] ? nxt->next[c - 'a']
              : nxt->suf->link[c - 'a']);
32         bfs.push(nxt);
33     }
34 }
35 node *cur = root;
36 for (char c : t) {
37     cur = cur->link[c - 'a'];
38     cur->visited++;
39 }
40 vector<int> count(n);
41 for (int i = bfs_order.size() - 1; i >= 0; --i) {
42     node *cur = bfs_order[i];
43     for (int idx : cur->term) count[idx] = cur->
        visited;
44     cur->suf->visited += cur->visited;
45 }

```

6 Поток

6.1 Алгоритм Диница

```

1 #define pb push_back
2 struct Dinic{
3     struct edge{
4         int to, flow, cap;
5     };
6
7     const static int N = 555; //count of vertices
8
9     vector<edge> e;
10    vector<int> g[N + 7];
11    int dp[N + 7];
12    int ptr[N + 7];
13
14    void clear(){
15        for (int i = 0; i < N + 7; i++) g[i].clear();
16        e.clear();
17    }
18
19    void addEdge(int a, int b, int cap){
20        g[a].pb(e.size());
21        e.pb({b, 0, cap});
22        g[b].pb(e.size());
23        e.pb({a, 0, 0});
24    }
25
26    int minFlow, start, finish;
27
28    bool bfs(){
29        for (int i = 0; i < N; i++) dp[i] = -1;
30        dp[start] = 0;
31        vector<int> st;
32        int uk = 0;
33        st.pb(start);
34        while(uk < st.size()){
35            int v = st[uk++];
36            for (int to : g[v]){
37                auto ed = e[to];
38                if (ed.cap - ed.flow >= minFlow && dp[ed.to]
                    == -1){

```

```

39                    dp[ed.to] = dp[v] + 1;
40                    st.pb(ed.to);
41                }
42            }
43        }
44        return dp[finish] != -1;
45    }
46
47    int dfs(int v, int flow){
48        if (v == finish) return flow;
49        for (; ptr[v] < g[v].size(); ptr[v]++){
50            int to = g[v][ptr[v]];
51            edge ed = e[to];
52            if (ed.cap - ed.flow >= minFlow && dp[ed.to] ==
                dp[v] + 1){
53                int add = dfs(ed.to, min(flow, ed.cap - ed.
                    flow));
54                if (add){
55                    e[to].flow += add;
56                    e[to ^ 1].flow -= add;
57                    return add;
58                }
59            }
60        }
61        return 0;
62    }
63
64    int dinic(int start, int finish){
65        Dinic::start = start;
66        Dinic::finish = finish;
67        int flow = 0;
68        for (minFlow = (1 << 30); minFlow; minFlow >>= 1)
69            {
70                while(bfs()){
71                    for (int i = 0; i < N; i++) ptr[i] = 0;
72                    while(int now = dfs(start, (int)2e9 + 7))
73                        flow += now;
74                }
75            }
76        return flow;
77    }
78 }
79 } dinic;

```

6.2 Mincost k-flow

6.2.1 Строим граф

```

1 struct edge {
2     int next, capacity, cost, flow = 0;
3
4     edge() = default;
5
6     edge(int next, int capacity, int cost) : next(
            next), capacity(capacity), cost(cost) {}
7
8     int rem() const { return capacity - flow; }
9
10    int operator+=(int f) { return flow += f; }
11
12    int operator-=(int f) { return flow -= f; }
13 };
14 auto addEdge = [&](auto from, auto next, auto
    capacity, int cost) {
15     g[from].push_back(e.size());
16     e.emplace_back(next, capacity, cost);
17     g[next].push_back(e.size());
18     e.emplace_back(from, 0, -cost);
19 };

```

Если граф ориентированный, то addEdge вызываем один раз. Если неориентированный, то два, вот так:

```

1 addEdge(u, v, capacity, cost);
2 addEdge(v, u, capacity, cost);

```

6.2.2 Запускаем Форда — Беллмана

```

1 vector<ll> phi(n, 0);
2 auto fordBellman = [&](int s, int t) {
3     phi.assign(n, 0);

```

```

4  for (int iter = 0; iter < n; ++iter) {
5      bool changed = false;
6      for (int u = 0; u < n; ++u) {
7          for (auto index : g[u]) {
8              auto edge = e[index];
9              if (edge.rem() > 0 && phi[edge.next] > phi[
u] + edge.cost) {
10                 phi[edge.next] = phi[u] + edge.cost;
11                 changed = true;
12             }
13         }
14     }
15     if (!changed) break;
16 }
17 };
18 fordBellman(s, t);

```

6.2.3 Ищем кратчайший путь Дейкстры с потенциалами

```

1  vector<ll> dist;
2  vector<int> from;
3  vector<bool> cnt;
4  auto dijkstra = [&](int s, int t) {
5      dist.assign(n, 1e18);
6      from.assign(n, -1);
7      cnt.assign(n, false);
8      dist[s] = 0;
9      for (int i = 1; i < n; ++i) {
10         int cur = find(cnt.begin(), cnt.end(), false) -
cnt.begin();
11         for (int j = 0; j < n; ++j) {
12             if (!cnt[j] && dist[j] < dist[cur]) cur = j;
13         }
14         cnt[cur] = true;
15         for (int index : g[cur]) {
16             auto &edge = e[index];
17             if (edge.rem() == 0) continue;
18             ll weight = edge.cost + phi[cur] - phi[edge.
next];
19             if (dist[edge.next] > dist[cur] + weight) {
20                 dist[edge.next] = dist[cur] + weight;
21                 from[edge.next] = cur;
22             }
23         }
24     }
25     if (dist[t] == (ll) 1e18) return -1LL;
26     ll cost = 0;
27     for (int p = t; p != s; p = from[p]) {
28         for (auto index : g[from[p]]) {
29             auto &edge = e[index];
30             ll weight = edge.cost + phi[from[p]] - phi[
edge.next];
31             if (edge.rem() > 0 && edge.next == p && dist[
edge.next] == dist[from[p]] + weight) {
32                 edge += 1;
33                 e[index ^ 1] -= 1;
34                 cost += edge.cost;
35                 break;
36             }
37         }
38     }
39     for (int i = 0; i < n; ++i) {
40         phi[i] += dist[i];
41     }
42     return cost;
43 };
44 ll cost = 0;
45 for (int flow = 0; flow < k; ++flow) {
46     ll a = dijkstra(s, t);
47     if (a == -1) {
48         cout << "-1\n";
49         return;
50     }
51     cost += a;
52 }

```

6.2.4 Восстанавливаем ответ

```

1  auto findPath = [&](int s, int t) {
2      vector<int> ans;
3      int cur = s;
4      while (cur != t) {
5          for (auto index : g[cur]) {
6              auto &edge = e[index];
7              if (edge.flow <= 0) continue;
8              edge -= 1;
9              e[index ^ 1] += 1;
10             ans.push_back(index / 4);
11         }
12         // index / 4 because each edge has 4 copies
13         cur = edge.next;
14         break;
15     }
16     return ans;
17 };
18 for (int flow = 0; flow < k; ++flow) {
19     auto p = findPath(s, t);
20     cout << p.size() << ' ';
21     for (int x : p) cout << x + 1 << ' ';
22     cout << '\n';
23 }

```

7 FFT & co

7.1 NTT & co

```

1  typedef long long ll;
2  const int p=998244353;
3  int po(int a,int b) {if(b==0) return 1; if(b==1)
return a; if(b%2==0) {int u=po(a,b/2);return (u
*1LL*u)%p;} else {int u=po(a,b-1);return (a*1LL
*u)%p;}}
4  int inv(int x) {return po(x,p-2);}
5  template<int M, int K, int G> struct Fft {
6      // 1, 1/4, 1/8, 3/8, 1/16, 5/16, 3/16, 7/16, ...
7      int g[1 << (K - 1)];
8      Fft() : g() { //if t1 constexpr...
9          static_assert(K >= 2, "Fft: K >= 2 must hold");
10         g[0] = 1;
11         g[1 << (K - 2)] = G;
12         for (int l = 1 << (K - 2); l >= 2; l >>= 1) {
13             g[l >> 1] = (static_cast<long long>(g[l]) * g
[l]) % M;
14         }
15         assert((static_cast<long long>(g[l]) * g[l]) %
M == M - 1);
16         for (int l = 2; l <= 1 << (K - 2); l <= 1) {
17             for (int i = 1; i < l; ++i) {
18                 g[l + i] = (static_cast<long long>(g[l]) *
g[i]) % M;
19             }
20         }
21     }
22     void fft(vector<int> &x) const {
23         const int n = x.size();
24         assert(!(n & (n - 1)) && n <= 1 << K);
25         for (int h = __builtin_ctz(n); h--;) {
26             const int l = 1 << h;
27             for (int i = 0; i < n >> 1 >> h; ++i) {
28                 for (int j = i << 1 << h; j < ((i << 1) +
1) << h; ++j) {
29                     const int t = (static_cast<long long>(g[i
]) * x[j | l]) % M;
30                     if ((x[j | l] = x[j] - t) < 0) x[j | l]
+= M;
31                     if ((x[j] += t) >= M) x[j] -= M;
32                 }
33             }
34         }
35         for (int i = 0, j = 0; i < n; ++i) {
36             if (i < j) std::swap(x[i], x[j]);
37             for (int l = n; (l >>= 1) && !((j ^= 1) & 1);
) {}
38         }
39     }
40     vector<int> convolution(const vector<int> &a,
const vector<int> &b) const {

```

```

41     if(a.empty() || b.empty()) return {};
42     const int na = a.size(), nb = b.size();
43     int n, invN = 1;
44     for (n = 1; n < na + nb - 1; n <= 1) invN = ((
45         invN & 1) ? (invN + M) : invN) >> 1;
46     vector<int> x(n, 0), y(n, 0);
47     std::copy(a.begin(), a.end(), x.begin());
48     std::copy(b.begin(), b.end(), y.begin());
49     fft(x);
50     fft(y);
51     for (int i = 0; i < n; ++i) x[i] = (((
52         static_cast<long long>(x[i]) * y[i]) % M) *
53         invN) % M;
54     std::reverse(x.begin() + 1, x.end());
55     fft(x);
56     x.resize(na + nb - 1);
57     return x;
58 }
59 Fft<998244353,23,31> muls;
60 vector<int> form(vector<int> v,int n)
61 {
62     while(v.size()<n) v.push_back(0);
63     while(v.size()>n) v.pop_back();
64     return v;
65 }
66 vector<int> operator *(vector<int> v1,vector<int>
67     v2)
68 {
69     return muls.convolution(v1,v2);
70 }
71 vector<int> operator +(vector<int> v1,vector<int>
72     v2)
73 {
74     while(v2.size()<v1.size()) v2.push_back(0); while
75     (v1.size()<v2.size()) v1.push_back(0);
76     for(int i=0;i<v1.size();++i) {v1[i]+=v2[i];if(v1[
77     i]>=p) v1[i]-=p; else if(v1[i]<0) v1[i]+=p;}
78     return v1;
79 }
80 vector<int> operator -(vector<int> v1,vector<int>
81     v2)
82 {
83     int sz=max(v1.size(),v2.size());while(v1.size()<
84     sz) v1.push_back(0); while(v2.size()<sz) v2.
85     push_back(0);
86     for(int i=0;i<sz;++i) {v1[i]-=v2[i];if(v1[i]<0)
87     v1[i]+=p; else if(v1[i]>=p) v1[i]-=p;} return
88     v1;
89 }
90 vector<int> trmi(vector<int> v)
91 {
92     for(int i=1;i<v.size();i+=2) {if(v[i]>0) v[i]=p-v
93     [i]; else v[i]=(-v[i]);}
94     return v;
95 }
96 vector<int> deriv(vector<int> v)
97 {
98     if(v.empty()) return{};
99     vector<int> ans(v.size()-1);
100    for(int i=1;i<v.size();++i) ans[i-1]=(v[i]*1LL*i
101    %p;
102    return ans;
103 }
104 vector<int> integ(vector<int> v)
105 {
106    vector<int> ans(v.size()+1);ans[0]=0;
107    for(int i=1;i<v.size();++i) ans[i-1]=(v[i]*1LL*i
108    %p;
109    return ans;
110 }
111 vector<int> mul(vector<vector<int> > v)
112 {
113    if(v.size()==1) return v[0];
114    vector<vector<int> > v1,v2;for(int i=0;i<v.size()
115    /2;++i) v1.push_back(v[i]); for(int i=v.size()
116    /2;i<v.size();++i) v2.push_back(v[i]);
117    return muls.convolution(mul(v1),mul(v2));
118 }
119 vector<int> inv1(vector<int> v,int n)
120 {
121    assert(v[0]!=0);
122    int sz=1;v=form(v,n);vector<int> a={inv(v[0])};
123    while(sz<n)
124    {
125        vector<int> vsz;for(int i=0;i<min(n,2*sz);++i)
126        vsz.push_back(v[i]);
127        vector<int> b=((vector<int>) {1})-muls.
128        convolution(a,vsz);
129        for(int i=0;i<sz;++i) assert(b[i]==0);
130        b.erase(b.begin(),b.begin()+sz);
131        vector<int> c=muls.convolution(b,a);
132        for(int i=0;i<sz;++i) a.push_back(c[i]);
133        sz*=2;
134    }
135    return form(a,n);
136 }
137 vector<int> inv(vector<int> v,int n)
138 {
139    v=form(v,n);assert(v[0]!=0);if(v.size()==1) {
140        return {inv(v[0])};} vector<int> v1=trmi(v);
141    vector<int> a=v1*v;a=form(a,2*n);
142    vector<int> b((n+1)/2);for(int i=0;i<b.size();++i)
143    b[i]=a[2*i];
144    vector<int> ans1=inv(b,b.size());vector<int> ans2
145    (n);for(int i=0;i<n;++i) {if(i%2==0) ans2[i]=
146    ans1[i/2]; else ans2[i]=0;}
147    return form(v1*ans2,n);
148 }
149 vector<int> operator/(vector<int> a,vector<int> b)
150 {
151    while(!a.empty() && a.back()==0) a.pop_back();
152    while(!b.empty() && b.back()==0) b.pop_back();
153    int n=a.size();int m=b.size();if(n<m) return {};
154    reverse(a.begin(),a.end());reverse(b.begin(),b.
155    end());vector<int> ans=a*inv(b,n-m+1);while(ans
156    .size()>n-m+1) ans.pop_back();
157    reverse(ans.begin(),ans.end());while(!ans.empty()
158    && ans.back()==0) ans.pop_back();return ans;
159 }
160 vector<int> operator%(vector<int> a,vector<int> b)
161 {
162    vector<int> ans=a-b*(a/b);while(!ans.empty() &&
163    ans.back()==0) ans.pop_back(); return ans;
164 }

```