Содержание

1 Теория чисел

1.1 КТО

```
int gcd(int a, int b, int &x, int &y) {
    if (b==0) { x = 1; y = 0; return a; }
    int d = gcd(b,a%b,x,y);
    swap(x,y);
    y-=a/b*x;
    return d;
}
int inv(int r, int m) {
    int x, y;
    gcd(r,m,x,y);
    return (x+m)%m;
}
int crt(int r, int n, int c, int m) { return r + ((
    c - r) % m + m) * inv(n, m) % m * n; }
```

1.2 Алгоритм Миллера — Рабина

```
__int128 one=1;
int po(int a,int b,int p)
{
    int res=1;
    while(b) {if(b & 1) {res=(res*one*a)%p;--b;}
    else {a=(a*one*a)%p;b>>=1;}} return res;
}
bool chprime(int n) ///miller-rabin
{
    if(n==2) return true;
    if(n<=1 || n%2==0) return false;
    int h=n-1;int d=0;while(h%2==0) {h/=2;++d;}
    for(int a:{2, 3, 5, 7, 11, 13, 17, 19, 23, 29,
    31, 37})
        {
        if(a==n) return true;
        int u=po(a,h,n);bool ok=0;
        if(u%n==1) continue;
        for(int c=0;c<d;++c)
            {
            if((u+1)%n==0) {ok=1;break;}
            u=(u*one*u)%n;
        }
        if(!ok) return false;
    }
    return true;
}
```

2 Графы

2.1 $\mathcal{SCC}$ и 2-$\mathcal{SAT}$

Алгоритм ищет сильносвязные компоненты в графе g, если есть путь $i \to j$, то $scc[i] \le scc[j]$

В случае 2-$\mathcal{SAT}$ рёбра $i \Rightarrow j$ и $(j \oplus 1) \Rightarrow (i \oplus 1)$ должны быть добавлены одновременно.

```
vector<vector<int>> g(2 * n);
vector<vector<int>> r(g.size());
for (int i = 0; i < g.size(); ++i) {
    for (int j : g[i]) r[j].push_back(i);
}
vector<int> used(g.size()), tout(g.size());
int time = 0;
auto dfs = [&](auto dfs, int cur) -> void {
    if (used[cur]) return;
    used[cur] = 1;
    for (int nxt : g[cur]) {
        dfs(dfs, nxt);
    }
    // used[cur] = 2;
    tout[cur] = time++;
};
for (int i = 0; i < g.size(); ++i) if (!used[i])
    dfs(dfs, i);
vector<int> ind(g.size());
iota(ind.begin(), ind.end(), 0);
```

```
sort(all(ind), [&](int i, int j){return tout[i] > tout[j];});
vector<int> scc(g.size(), -1);
auto go = [&](auto go, int cur, int color) -> void {
    if (scc[cur] != -1) return;
    scc[cur] = color;
    for (int nxt : r[cur]) {
        go(go, nxt, color);
    }
};
int color = 0;
for (int i : ind) {
    if (scc[i] == -1) go(go, i, color++);
}
for (int i = 0; i < g.size() / 2; ++i) {
    if (scc[2 * i] == scc[2 * i + 1]) "IMPOSSIBLE"
    if (scc[2 * i] < scc[2 * i + 1]) {
        // !i => i, assign i = true
    } else {
        // i => !i, assign i = false
    }
}
```

2.2 Эйлеров цикл

```
vector<vector<pair<int, int>>> g(n); // pair{nxt, idx}
vector<pair<int, int>> e(p.size());
// build graph
vector<int> in(n), out(n);
for (auto [u, v] : e) in[v]++, out[u]++;
vector<int> used(m), it(n), cycle;
auto dfs = [&](auto dfs, int cur) -> void {
    while (true) {
        while (it[cur] < g[cur].size() && used[g[cur][it[cur]].second]) it[cur]++;
        if (it[cur] == g[cur].size()) return;
        auto [nxt, idx] = g[cur][it[cur]];
        used[idx] = true;
        dfs(dfs, nxt);
        cycle.push_back(idx);
    }
};
int cnt = 0, odd = -1;
for (int i = 0; i < n; ++i){
    if (out[i] && odd == -1) odd = i;
    if (in[i] != out[i]) {
        if (in[i] + 1 == out[i]) odd = i;
        if (abs(in[i] - out[i]) > 1) return {}; // must hold
        cnt++;
    }
}
if (cnt != 0 && cnt != 2) return {}; // must hold
// for undirected find odd vertex (and count that # of odd is 0 or 2)
dfs(dfs, odd);
reverse(cycle.begin(), cycle.end());
if (cycle.size() != m) return {};
```

3 xor, and, or-свёртки

3.1 and-свёртка

```
vector<int> band(vector<int> a,vector<int> b)
{
    int n=0;while((1<<n)<a.size()) ++n;
    a.resize(1<<n);b.resize(1<<n);
    for(int i=0;i<n;++i) for(int mask=0;mask<(1<<n);++mask) if(mask & (1<<i)) {a[mask-(1<<i)]+=a[mask];a[mask-(1<<i)]%=p;}
    for(int i=0;i<n;++i) for(int mask=0;mask<(1<<n);++mask) if(mask & (1<<i)) {b[mask-(1<<i)]+=b[mask];b[mask-(1<<i)]%=p;}
    vector<int> c(1<<n,0);
    for(int mask=0;mask<(1<<n);++mask) {c[mask]=a[mask]*b[mask];c[mask]%=p;}
    for(int i=0;i<n;++i) for(int mask=0;mask<(1<<n);++mask) if(!(mask & (1<<i))) {c[mask]-=c[mask+(1<<i)];c[mask]%=p;}
    return c;
}
```

3.2 or-свёртка

```
vector<int> bor(vector<int> a,vector<int> b)
{
    int n=0;while((1<<n)<a.size()) ++n;
    a.resize(1<<n);b.resize(1<<n);
    for(int i=0;i<n;++i) for(int mask=0;mask<(1<<n);++mask) if(!(mask & (1<<i))) {a[mask+(1<<i)]+=a[mask];a[mask+(1<<i)]%=p;}
    for(int i=0;i<n;++i) for(int mask=0;mask<(1<<n);++mask) if(!(mask & (1<<i))) {b[mask+(1<<i)]+=b[mask];b[mask+(1<<i)]%=p;}
    vector<int> c(1<<n,0);
    for(int mask=0;mask<(1<<n);++mask) {c[mask]=a[mask]*b[mask];c[mask]%=p;}
    for(int i=0;i<n;++i) for(int mask=0;mask<(1<<n);++mask) if(mask & (1<<i)) {c[mask]-=c[mask-(1<<i)];c[mask]%=p;}
    return c;
}
```

3.3 xor-свёртка

```
vector<int> bxor(vector<int> a,vector<int> b)
{
    assert(p%2==1);int inv2=(p+1)/2;
    int n=0;while((1<<n)<a.size()) ++n;
    a.resize(1<<n);b.resize(1<<n);
    for(int i=0;i<n;++i) for(int mask=0;mask<(1<<n);++mask) if(!(mask & (1<<i))) {int u=a[mask],v=a[mask+(1<<i)];a[mask+(1<<i)]=(u+v)%p;a[mask]=(u-v)%p;}
    for(int i=0;i<n;++i) for(int mask=0;mask<(1<<n);++mask) if(!(mask & (1<<i))) {int u=b[mask],v=b[mask+(1<<i)];b[mask+(1<<i)]=(u+v)%p;b[mask]=(u-v)%p;}
    vector<int> c(1<<n,0);
    for(int mask=0;mask<(1<<n);++mask) {c[mask]=a[mask]*b[mask];c[mask]%=p;}
    for(int i=0;i<n;++i) for(int mask=0;mask<(1<<n);++mask) if(!(mask & (1<<i))) {int u=c[mask],v=c[mask+(1<<i)];c[mask+(1<<i)]=((v-u)*inv2)%p;c[mask]=((u+v)*inv2)%p;}
    return c;
}
```

4 Структуры данных

4.1 Дерево Фенвика

```
int fe[maxn]; /// fenwick tree
void pl(int pos,int val) {while(pos<maxn) {fe[pos]+=val;pos|=(pos+1);}}
int get(int pos) {int ans=0;while(pos>=0) {ans+=fe[pos];pos&=(pos+1);--pos;} return ans;} /// [0, pos] - vkluchitelno!!!
int get(int l,int r) {return get(r-1)-get(l-1);} /// summa na [l,r)
```

4.2 Ordered set

```
#include <ext/pb_ds/assoc_container.hpp>
#include <ext/pb_ds/tree_policy.hpp>

using namespace __gnu_pbds;
using namespace std;

using ordered_set = tree<int, null_type, less<>, rb_tree_tag, tree_order_statistics_node_update>;
```

4.3 Дерево отрезков

```
template<typename Data, typename Mod, typename UniteData, typename UniteMod, typename Apply>
struct MassSegmentTree {
    int h, n;
    Data zd;
    Mod zm;
    vector<Data> data;
    vector<Mod> mod;

    UniteData ud; // Data (Data, Data)
    UniteMod um; // Mod (Mod, Mod);
    Apply a; // Data (Data, Mod, int); last argument is the length of current segment (could be used for range += and sum counting, for instance)

    template<typename I>
    MassSegmentTree(int sz, Data zd, Mod zm, UniteData ud, UniteMod um, Apply a, I init) : h(__lg(sz > 1 ? sz - 1 : 1) + 1), n(1 << h), zm(zm), zd(zd), data(2 * n, zd), mod(n, zm), ud(ud), um(um), a(a) {
        for (int i = 0; i < sz; ++i) data[i + n] = init(i);
        for (int i = n - 1; i > 0; --i) data[i] = ud(data[2 * i], data[2 * i + 1]);
    }

    MassSegmentTree(int sz, Data zd, Mod zm, UniteData ud, UniteMod um, Apply a) : h(__lg(sz > 1 ? sz - 1 : 1) + 1), n(1 << h), zm(zm), zd(zd), data(2 * n, zd), mod(n, zm), ud(ud), um(um), a(a) {}

    void push(int i) {
        if (mod[i] == zm) return;
        apply(2 * i, mod[i]);
        apply(2 * i + 1, mod[i]);
        mod[i] = zm;
    }

    // is used only for apply
    int length(int i) { return 1 << (h - __lg(i)); }

    // is used only for descent
    int left(int i) {
        int lvl = __lg(i);
        return (i & ((1 << lvl) - 1)) * (1 << (h - lvl));
    }

    // is used only for descent
    int right(int i) {
        int lvl = __lg(i);
        return ((i & ((1 << lvl) - 1)) + 1) * (1 << (h - lvl));
    }

    template<typename S>
    void apply(int i, S x) {
        data[i] = a(data[i], x, length(i));
        if (i < n) mod[i] = um(mod[i], x);
    }

    void update(int i) {
        if (mod[i] != zm) return;
        data[i] = ud(data[2 * i], data[2 * i + 1]);
    }

    template<typename S>
    void update(int l, int r, S x) { // [l; r)
        l += n, r += n;
        for (int shift = h; shift > 0; --shift) {
            push(l >> shift);
            push((r - 1) >> shift);
        }
        for (int lf = l, rg = r; lf < rg; lf /= 2, rg /= 2) {
            if (lf & 1) apply(lf++, x);
            if (rg & 1) apply(--rg, x);
        }
        for (int shift = 1; shift <= h; ++shift) {
            update(l >> shift);
            update((r - 1) >> shift);
        }
    }

    Data get(int l, int r) { // [l; r)
        l += n, r += n;
        for (int shift = h; shift > 0; --shift) {
            push(l >> shift);
            push((r - 1) >> shift);
        }
        Data leftRes = zd, rightRes = zd;
        for (; l < r; l /= 2, r /= 2) {
            if (l & 1) leftRes = ud(leftRes, data[l++]);
            if (r & 1) rightRes = ud(data[--r], rightRes);
        }
        return ud(leftRes, rightRes);
    }

    // l \in [0; n) && ok(get(l, l), l);
    // returns last r: ok(get(l, r), r)
    template<typename C>
    int lastTrue(int l, C ok) {
        l += n;
        for (int shift = h; shift > 0; --shift) push(l >> shift);
        Data cur = zd;
        do {
            l >>= __builtin_ctz(l);
            Data with1;
            with1 = ud(cur, data[l]);
            if (ok(with1, right(l))) {
                cur = with1;
                ++l;
            } else {
                while (l < n) {
                    push(l);
                    Data with2;
                    with2 = ud(cur, data[2 * l]);
                    if (ok(with2, right(2 * l))) {
                        cur = with2;
                        l = 2 * l + 1;
                    } else {
                        l = 2 * l;
                    }
                }
                return l - n;
            }
        } while (l & (l - 1));
        return n;
    }

    // r \in [0; n) && ok(get(r, r), r);
    // returns first l: ok(get(l, r), l)
    template<typename C>
    int firstTrue(int r, C ok) {
        r += n;
        for (int shift = h; shift > 0; --shift) push((r - 1) >> shift);
        Data cur = zd;
        while (r & (r - 1)) {
            r >>= __builtin_ctz(r);
            Data with1;
            with1 = ud(data[--r], cur);
            if (ok(with1, left(r))) {
                cur = with1;
            } else {
                while (r < n) {
                    push(r);
                    Data with2;
                    with2 = ud(data[2 * r + 1], cur);
                    if (ok(with2, right(2 * r))) {
```

```
                        cur = with2;
                        r = 2 * r;
                    } else {
                        r = 2 * r + 1;
                    }
                }
                return r - n + 1;
            }
        }
        return 0;
    }
};
```

4.3.1 Примеры:

- Взятие максимума и прибавление константы

```
MassSegmentTree segtree(n, 0LL, 0LL,
[](int x, int y) { return max(x, y); },
[](int x, int y) { return x + y; },
[](int x, int y, int len) { return x + y; });
```

- Взятие суммы и прибавление константы

```
MassSegmentTree segtree(n, 0LL, 0LL,
[](int x, int y) { return x + y; },
[](int x, int y) { return x + y; },
[](int x, int y, int len) { return x + y * len;
    });
```

- Взятие суммы и присовение

```
MassSegmentTree segtree(n, 0LL, -1LL,
[](int x, int y) { return x + y; },
[](int x, int y) { return y; },
[](int x, int y, int len) { return y * len; });
```

5 Строковые алгоритмы

5.1 Префикс-функция

```
vector<int> prefix_function(string s) {
    vector<int> p(s.size());
    for (int i = 1; i < s.size(); ++i) {
        p[i] = p[i - 1];
        while (p[i] && s[p[i]] != s[i]) p[i] = p[p[
    i] - 1];
        p[i] += s[i] == s[p[i]];
    }
    return p;
}
```

5.2 Z-функция

```
vector<int> z_function (string s) { // z[i] - lcp
    of s and s[i:]
 int n = (int) s.length();
 vector<int> z (n);
 for (int i=1, l=0, r=0; i<n; ++i) {
  if (i <= r)
   z[i] = min (r-i+1, z[i-l]);
  while (i+z[i] < n && s[z[i]] == s[i+z[i]])
   ++z[i];
  if (i+z[i]-1 > r)
   l = i,  r = i+z[i]-1;
 }
 return z;
}
```

5.3 Алгоритм Манакера

```
vector<int> manacher_odd(const string &s) {
    vector<int> man(s.size(), 0);
    int l = 0, r = 0;
    int n = s.size();
    for (int i = 1; i < n; i++) {
        if (i <= r) {
            man[i] = min(r - i, man[l + r - i]);
        }
        while (i + man[i] + 1 < n && i - man[i] - 1
     >= 0 && s[i + man[i] + 1] == s[i - man[i] -
    1]) {
            man[i]++;
        }
        if (i + man[i] > r) {
            l = i - man[i];
            r = i + man[i];
        }
    }
    return man;
}
// abacaba : (0 1 0 3 0 1 0)
// abbaa : (0 0 0 0 0)

vector <int> manacher_even(const string &s) {
    assert(s.size());
    string t;
    for (int i = 0; i + 1 < s.size(); ++i) {
        t += s[i];
        t += '#';
    }
    t += s.back();
    auto odd = manacher_odd(t);
    vector <int> ans;
    for (int i = 1; i < odd.size(); i += 2) {
        ans.push_back((odd[i]+1)/2);
    }
    return ans;
}
// abacaba : (0 0 0 0 0 0)
// abbaa : (0 2 0 1)
```

5.4 Суфмассив

Китайский суффмассив

```
struct SuffixArray {
    vector <int> sa, lcp;
    SuffixArray (string &s, int lim=256) {
        int n = (int)s.size() + 1, k = 0, a, b;
        vector <int> x(s.begin(), s.end() + 1), y(n
    ), ws(max(n, lim)), rank(n);
        sa = lcp = y, iota(sa.begin(), sa.end(), 0)
    ;
        for (int j = 0, p = 0; p < n; j = max(1ll,
    j * 2), lim = p) {
            p = j, iota(y.begin(), y.end(), n - j);
            for (int i = 0; i < n; i++) if (sa[i]
    >= j) y[p++] = sa[i] - j;
            fill(ws.begin(), ws.end(), 0);
            for (int i = 0; i < n; i++) ws[x[i]]++;
            for (int i = 1; i < lim; i++) ws[i] +=
    ws[i - 1];
            for (int i = n; i--; ) sa[--ws[x[y[i
    ]]]] = y[i];
            swap(x, y), p = 1, x[sa[0]] = 0;
            for (int i = 1; i < n; i++) a = sa[i -
    1], b = sa[i], x[b] = (y[a] == y[b] && y[a + j]
     == y[b + j]) ? p - 1 : p++;
        }
        for (int i = 1; i < n; i++) rank[sa[i]] = i
    ;
        for (int i = 0, j; i < n - 1; lcp[rank[i
    ++]]=k)
            for (k && k--, j = sa[rank[i] - 1];
                    s[i + k] == s[j + k]; k++);
    }
};
struct Rmq {
    const int INF = 1e9;
    int n;
    vector<int> rmq;
    Rmq() {}
    void build(const vector<int> &x) {
        assert(x.size() == n);
        for (int i = 0; i < n; ++i) rmq[n + i] = x[
    i];
```

```
        for (int i = n - 1; i > 0; --i) rmq[i] = min(rmq[2 * i], rmq[2 * i + 1]);
    }
    Rmq(int n) : n(n), rmq(2 * n, INF) {}

    void put(int i, int x) {
        rmq[i + n] = min(rmq[i + n], x);
        for (i = (i + n) / 2; i > 0; i /= 2) {
            rmq[i] = min(rmq[i * 2], rmq[i * 2 + 1]);
        }
    }
    int getMin(int l, int r) { //[l;r)
        assert(l < r);
        int res = INF;
        for (l += n, r += n; l < r; l /= 2, r /= 2) {
            if (l & 1) res = min(res, rmq[l++]);
            if (r & 1) res = min(res, rmq[--r]);
        }
        return res;
    }
};

struct Lc {
    vector<int> pos;
    Rmq rmq;
    Lc(string s) : rmq(s.size()) {
        SuffixArray sa(s);
        auto ss = sa.sa;
        ss.erase(ss.begin());

        auto lcp = sa.lcp;
        lcp.erase(lcp.begin());
        lcp.erase(lcp.begin());

        pos.resize(s.size());
        assert(s.size() == ss.size());
        for (int i = 0; i < ss.size(); ++i) {
            pos[ss[i]] = i;
        }
        int n = s.size();
        assert(lcp.size() == n - 1);
        rmq.build(lcp);
    }
    int getLcp(int i, int j) {
        i = pos[i]; j = pos[j];
        if (j < i) {
            swap(i, j);
        }
        if (i == j) {
            return 1e18;
        }
        else {
            return rmq.getMin(i, j);
        }
    }
};
```

6 Потоки

6.1 Алгоритм Диница

6.2 Mincost k-flow

6.2.1 Строим граф

```
struct edge {
    int next, capacity, cost, flow = 0;

    edge() = default;

    edge(int next, int capacity, int cost) : next(next), capacity(capacity), cost(cost) {}

    int rem() const { return capacity - flow; }

    int operator+=(int f) { return flow += f; }

    int operator-=(int f) { return flow -= f; }
};
auto addEdge = [&](auto from, auto next, auto capacity, int cost) {
    g[from].push_back(e.size());
    e.emplace_back(next, capacity, cost);
    g[next].push_back(e.size());
    e.emplace_back(from, 0, -cost);
};
```

Если граф ориентированный, то addEdge вызываем один раз. Если неориентированный, то два, вот так:

```
addEdge(u, v, capacity, cost);
addEdge(v, u, capacity, cost);
```

6.2.2 Запускаем Форда — Беллмана

```
vector<ll> phi(n, 0);
auto fordBellman = [&](int s, int t) {
    phi.assign(n, 0);
    for (int iter = 0; iter < n; ++iter) {
        bool changed = false;
        for (int u = 0; u < n; ++u) {
            for (auto index : g[u]) {
                auto edge = e[index];
                if (edge.rem() > 0 && phi[edge.next] > phi[u] + edge.cost) {
                    phi[edge.next] = phi[u] + edge.cost;
                    changed = true;
                }
            }
        }
        if (!changed) break;
    }
};
fordBellman(s, t);
```

6.2.3 Ищем кратчайший путь Дейкстрой с потенциалами

```
vector<ll> dist;
vector<int> from;
vector<bool> cnt;
auto dijkstra = [&](int s, int t) {
    dist.assign(n, 1e18);
    from.assign(n, -1);
    cnt.assign(n, false);
    dist[s] = 0;
    for (int i = 1; i < n; ++i) {
        int cur = find(cnt.begin(), cnt.end(), false) - cnt.begin();
        for (int j = 0; j < n; ++j) {
            if (!cnt[j] && dist[j] < dist[cur]) cur = j;
        }
        cnt[cur] = true;
        for (int index : g[cur]) {
            auto &edge = e[index];
            if (edge.rem() == 0) continue;
            ll weight = edge.cost + phi[cur] - phi[edge.next];
            if (dist[edge.next] > dist[cur] + weight) {
                dist[edge.next] = dist[cur] + weight;
                from[edge.next] = cur;
            }
        }
    }
    if (dist[t] == (ll) 1e18) return -1LL;
    ll cost = 0;
    for (int p = t; p != s; p = from[p]) {
        for (auto index : g[from[p]]) {
            auto &edge = e[index];
            ll weight = edge.cost + phi[from[p]] - phi[edge.next];
            if (edge.rem() > 0 && edge.next == p && dist[edge.next] == dist[from[p]] + weight) {
                edge += 1;
```

```
                e[index ^ 1] -= 1;
                cost += edge.cost;
                break;
            }
        }
    }
    for (int i = 0; i < n; ++i) {
        phi[i] += dist[i];
    }
    return cost;
};
ll cost = 0;
for (int flow = 0; flow < k; ++flow) {
    ll a = dijkstra(s, t);
    if (a == -1) {
        cout << "-1\n";
        return;
    }
    cost += a;
}
```

6.2.4 Восстанавливаем ответ

```
auto findPath = [&](int s, int t) {
    vector<int> ans;
    int cur = s;
    while (cur != t) {
        for (auto index : g[cur]) {
            auto &edge = e[index];
            if (edge.flow <= 0) continue;
            edge -= 1;
            e[index ^ 1] += 1;
            ans.push_back(index / 4);
// index / 4 because each edge has 4 copies
            cur = edge.next;
            break;
        }
    }
    return ans;
};
for (int flow = 0; flow < k; ++flow) {
    auto p = findPath(s, t);
    cout << p.size() << ' ';
    for (int x : p) cout << x + 1 << ' ';
    cout << '\n';
}
```

7 FFT & co

7.1 NTT & co

```
typedef long long ll;
const int p=998244353;
int po(int a,int b) {if(b==0) return 1; if(b==1)
    return a; if(b%2==0) {int u=po(a,b/2);return (u
    *1LL*u)%p;} else {int u=po(a,b-1);return (a*1LL
    *u)%p;}}
int inv(int x) {return po(x,p-2);}
template<int M, int K, int G> struct Fft {
  // 1, 1/4, 1/8, 3/8, 1/16, 5/16, 3/16, 7/16, ...
  int g[1 << (K - 1)];
  Fft() : g() { //if tl constexpr...
    static_assert(K >= 2, "Fft: K >= 2 must hold");
    g[0] = 1;
    g[1 << (K - 2)] = G;
    for (int l = 1 << (K - 2); l >= 2; l >>= 1) {
      g[l >> 1] = (static_cast<long long>(g[l]) * g
    [l]) % M;
    }
    assert((static_cast<long long>(g[1]) * g[1]) %
    M == M - 1);
    for (int l = 2; l <= 1 << (K - 2); l <<= 1) {
      for (int i = 1; i < l; ++i) {
        g[l + i] = (static_cast<long long>(g[l]) *
    g[i]) % M;
      }
    }
  }
  void fft(vector<int> &x) const {
    const int n = x.size();
    assert(!(n & (n - 1)) && n <= 1 << K);
    for (int h = __builtin_ctz(n); h--; ) {
      const int l = 1 << h;
      for (int i = 0; i < n >> 1 >> h; ++i) {
        for (int j = i << 1 << h; j < ((i << 1) +
    1) << h; ++j) {
          const int t = (static_cast<long long>(g[i
    ]) * x[j | l]) % M;
          if ((x[j | l] = x[j] - t) < 0) x[j | l]
    += M;
          if ((x[j] += t) >= M) x[j] -= M;
        }
      }
    }
    for (int i = 0, j = 0; i < n; ++i) {
      if (i < j) std::swap(x[i], x[j]);
      for (int l = n; (l >>= 1) && !((j ^= l) & l);
     ) {}
    }
  }
  vector<int> convolution(const vector<int> &a,
    const vector<int> &b) const {
    if(a.empty() || b.empty()) return {};
    const int na = a.size(), nb = b.size();
    int n, invN = 1;
    for (n = 1; n < na + nb - 1; n <<= 1) invN = ((
    invN & 1) ? (invN + M) : invN) >> 1;
    vector<int> x(n, 0), y(n, 0);
    std::copy(a.begin(), a.end(), x.begin());
    std::copy(b.begin(), b.end(), y.begin());
    fft(x);
    fft(y);
    for (int i = 0; i < n; ++i) x[i] = (((
    static_cast<long long>(x[i]) * y[i]) % M) *
    invN) % M;
    std::reverse(x.begin() + 1, x.end());
    fft(x);
    x.resize(na + nb - 1);
    return x;
  }
};
Fft<998244353,23,31> muls;
vector<int> form(vector<int> v,int n)
{
    while(v.size()<n) v.push_back(0);
    while(v.size()>n) v.pop_back();
    return v;
}
vector<int> operator *(vector<int> v1,vector<int>
    v2)
{
    return muls.convolution(v1,v2);
}
vector<int> operator +(vector<int> v1,vector<int>
    v2)
{
    while(v2.size()<v1.size()) v2.push_back(0);
    while(v1.size()<v2.size()) v1.push_back(0);
    for(int i=0;i<v1.size();++i) {v1[i]+=v2[i];if(
    v1[i]>=p) v1[i]-=p; else if(v1[i]<0) v1[i]+=p;}
    return v1;
}
vector<int> operator -(vector<int> v1,vector<int>
    v2)
{
    int sz=max(v1.size(),v2.size());while(v1.size()
    <sz) v1.push_back(0); while(v2.size()<sz) v2.
    push_back(0);
    for(int i=0;i<sz;++i) {v1[i]-=v2[i];if(v1[i]<0)
     v1[i]+=p; else if(v1[i]>=p) v1[i]-=p;} return
    v1;
}
vector<int> trmi(vector<int> v)
{
    for(int i=1;i<v.size();i+=2) {if(v[i]>0) v[i]=p
    -v[i]; else v[i]=(-v[i]);}
    return v;
}
```

```
84 vector<int> deriv(vector<int> v)
85 {
86     if(v.empty()) return{};
87     vector<int> ans(v.size()-1);
88     for(int i=1;i<v.size();++i) ans[i-1]=(v[i]*1LL*
       i)%p;
89     return ans;
90 }
91 vector<int> integ(vector<int> v)
92 {
93     vector<int> ans(v.size()+1);ans[0]=0;
94     for(int i=1;i<v.size();++i) ans[i-1]=(v[i]*1LL*
       i)%p;
95     return ans;
96 }
97 vector<int> mul(vector<vector<int> > v)
98 {
99     if(v.size()==1) return v[0];
100    vector<vector<int> > v1,v2;for(int i=0;i<v.size
       ()/2;++i) v1.push_back(v[i]); for(int i=v.size
       ()/2;i<v.size();++i) v2.push_back(v[i]);
101    return muls.convolution(mul(v1),mul(v2));
102 }
103 vector<int> inv1(vector<int> v,int n)
104 {
105    assert(v[0]!=0);
106    int sz=1;v=form(v,n);vector<int> a={inv(v[0])};
107    while(sz<n)
108    {
109        vector<int> vsz;for(int i=0;i<min(n,2*sz)
       ;++i) vsz.push_back(v[i]);
110        vector<int> b=((vector<int>) {1})-muls.
       convolution(a,vsz);
111        for(int i=0;i<sz;++i) assert(b[i]==0);
112        b.erase(b.begin(),b.begin()+sz);
113        vector<int> c=muls.convolution(b,a);
114        for(int i=0;i<sz;++i) a.push_back(c[i]);
115        sz*=2;
116    }
117    return form(a,n);
118 }
119 vector<int> inv(vector<int> v,int n)
120 {
121    v=form(v,n);assert(v[0]!=0);if(v.size()==1) {
       return {inv(v[0])};} vector<int> v1=trmi(v);
122    vector<int> a=v1*v;a=form(a,2*n);
123    vector<int> b((n+1)/2);for(int i=0;i<b.size()
       ;++i) b[i]=a[2*i];
124    vector<int> ans1=inv(b,b.size());vector<int>
       ans2(n);for(int i=0;i<n;++i) {if(i%2==0) ans2[i
       ]=ans1[i/2]; else ans2[i]=0;}
125    return form(v1*ans2,n);
126 }
127 vector<int> operator/(vector<int> a,vector<int> b)
128 {
129    while(!a.empty() && a.back()==0) a.pop_back();
       while(!b.empty() && b.back()==0) b.pop_back();
130    int n=a.size();int m=b.size();if(n<m) return
       {};
131    reverse(a.begin(),a.end());reverse(b.begin(),b.
       end());vector<int> ans=a*inv(b,n-m+1);while(ans
       .size()>n-m+1) ans.pop_back();
132    reverse(ans.begin(),ans.end());while(!ans.empty
       () && ans.back()==0) ans.pop_back();return ans;
133 }
134 vector<int> operator%(vector<int> a,vector <int> b)
135 {
136    vector<int> ans=a-b*(a/b);while(!ans.empty() &&
        ans.back()==0) ans.pop_back(); return ans;
137 }
```