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1 Теория чисел

1.1 КТО

```
int gcd(int a, int b, int &x, int &y) {
    if (b==0) { x = 1; y = 0; return a; }
    int d = gcd(b, a%b, y, x);
    y-=a/b*x;
    return d;
}

int inv(int r, int m) {
    int x, y;
    gcd(r, m, x, y);
    return (x+m)%m;
}

int crt(int r, int n, int c, int m) { return r + ((c -
    r) % m + m) * inv(n, m) % m * n; }
```

1.2 Алгоритм Миллера — Рабина

```
__int128 one=1;
int po(int a, int b, int p)
{
    int res=1;
    while(b) {if(b & 1) {res=(res*one*a)%p;--b;} else {a
        =(a*one*a)%p;b>>=1;}} return res;
}

bool chprime(int n) ///miller-rabin
{
    if(n==2) return true;
    if(n<=1 || n%2==0) return false;
    int h=n-1;int d=0;while(h%2==0) {h/=2;++d;}
    for(int a:{2, 3, 5, 7, 11, 13, 17, 19, 23, 29, 31,
        37})
    {
        if(a==n) return true;
        int u=po(a, h, n);bool ok=0;
        if(u%n==1) continue;
        for(int c=0;c<d;++c)
        {
            if((u+1)%n==0) {ok=1;break;}
            u=(u*one*u)%n;
        }
        if(!ok) return false;
    }
    return true;
}
```

1.3 Алгоритм Берлекэмпа — Мессе

<https://mzhang2021.github.io/cp-blog/berlekamp-massey/>

```
template<typename T>
vector<T> berlekampMassey(const vector<T> &s) {
    int n = s.size(), l = 0, m = 1;
    vector<T> b(n), c(n);
    T ld = b[0] = c[0] = 1;
    for (int i=0; i<n; i++, m++) {
        T d = s[i];
        for (int j=1; j<=l; j++)
            d += c[j] * s[i-j];
        if (d == 0) continue;
        vector<T> temp = c;
        T coef = d / ld;
        for (int j=m; j<n; j++) c[j] -= coef * b[j-m];
        if (2 * l <= i) {
            l = i + 1 - l;
            b = temp;
            ld = d;
            m = 0;
        }
    }
    c.resize(l + 1);
    c.erase(c.begin());
    for (T &x : c)
        x = -x;
    return c;
}
```

2 Графы

2.1 SCC и 2-SAT

Алгоритм ищет сильносвязные компоненты в графе g , если есть путь $i \rightarrow j$, то $scc[i] \leq scc[j]$

В случае 2-SAT рёбра $i \Rightarrow j$ и $(j \oplus 1) \Rightarrow (i \oplus 1)$ должны быть добавлены одновременно.

```
vector<vector<int>> g(2 * n);
vector<vector<int>> r(g.size());
for (int i = 0; i < g.size(); ++i) {
    for (int j : g[i]) r[j].push_back(i);
}
vector<int> used(g.size()), tout(g.size());
int time = 0;
auto dfs = [&](auto dfs, int cur) -> void {
    if (used[cur]) return;
    used[cur] = 1;
    for (int nxt : g[cur]) {
        dfs(dfs, nxt);
    }
    // used[cur] = 2;
    tout[cur] = time++;
};
for (int i = 0; i < g.size(); ++i) if (!used[i]) dfs(dfs, i);
vector<int> ind(g.size());
iota(ind.begin(), ind.end(), 0);
sort(all(ind), [&](int i, int j){return tout[i] > tout[j]});
vector<int> scc(g.size(), -1);
auto go = [&](auto go, int cur, int color) -> void {
    if (scc[cur] != -1) return;
    scc[cur] = color;
    for (int nxt : r[cur]) {
        go(go, nxt, color);
    }
};
int color = 0;
for (int i : ind) {
    if (scc[i] == -1) go(go, i, color++);
}
for (int i = 0; i < g.size() / 2; ++i) {
    if (scc[2 * i] == scc[2 * i + 1]) "IMPOSSIBLE"
    if (scc[2 * i] < scc[2 * i + 1]) {
        // !i => i, assign i = true
    } else {
        // i => !i, assign i = false
    }
}
}
```

2.2 Эйлеров цикл

```
vector<int> euler(vector<vector<pair<int, int>>> g) {
    // pair<nxt, idx>
    int n = g.size();
    vector<pair<int, int>> e(p.size());
    // build graph
    vector<int> in(n), out(n);
    for (auto [u, v] : e) in[v]++, out[u]++;
    vector<int> used(m), it(n), cycle;
    auto dfs = [&](auto dfs, int cur) -> void {
        while (true) {
            while (it[cur] < g[cur].size() && used[g[cur][it[cur]].second]) it[cur]++;
            if (it[cur] == g[cur].size()) return;
            auto [nxt, idx] = g[cur][it[cur]];
            used[idx] = true;
            dfs(dfs, nxt);
            cycle.push_back(idx);
        }
    };
    int cnt = 0, odd = -1;
    for (int i = 0; i < n; ++i) {
        if (out[i] && odd == -1) odd = i;
        if (in[i] != out[i]) {
            if (in[i] + 1 == out[i]) odd = i;
        }
    }
}
```

```
if (abs(in[i] - out[i]) > 1) return {}; // must hold
cnt++;
}
if (cnt != 0 && cnt != 2) return {}; // must hold
// for undirected find odd vertex (and count that # of odd is 0 or 2)
dfs(dfs, odd);
reverse(cycle.begin(), cycle.end());
if (cycle.size() != m) return {};
return cycle;
}
```

2.3 Компоненты рёберной двусвязности

```
int n, m;
cin >> n >> m;
vector<vector<int>> g(n + 1);
map<pair<int, int>, int> comp, col;
for (int i = 0; i < m; ++i) {
    int u, v, c; cin >> u >> v >> c; c--;
    col[{u, v}] = col[{v, u}] = c;
    g[u].push_back(v);
    g[v].push_back(u);
}
vector<int> used(n + 1);
vector<int> newCompWithoutParent(n + 1), h(n + 1), up(n + 1);
auto findCutPoints = [&](auto self, int u, int p) -> void {
    used[u] = 1;
    up[u] = h[u];
    for (int v : g[u]) {
        if (!used[v]) {
            h[v] = h[u] + 1;
            self(self, v, u);
            up[u] = min(up[u], up[v]);
            if (up[v] >= h[u]) {
                newCompWithoutParent[v] = 1;
            }
        }
        else {
            up[u] = min(up[u], h[v]);
        }
    }
};
for (int u = 1; u <= n; ++u) {
    if (!used[u]) {
        findCutPoints(findCutPoints, u, u);
    }
}
int ptr = 0;
vector<map<int, int>> colors(m);
auto markComponents = [&](auto self, int u, int cur) -> void {
    used[u] = 1;
    for (int v : g[u]) {
        if (!used[v]) {
            if (newCompWithoutParent[v]) {
                ptr++;
                self(self, v, ptr - 1);
            }
            else {
                self(self, v, cur);
            }
        }
        else if (h[v] < h[u]) {
            comp[{u, v}] = comp[{v, u}] = cur;
            int c = col[{u, v}];
            colors[cur][u] |= 1 << c;
            colors[cur][v] |= 1 << c;
        }
    }
};
used.assign(n + 1, 0);
for (int u = 1; u <= n; ++u) {
    if (!used[u]) {
        markComponents(markComponents, u, -1);
    }
}
}
```

```

for (int comp = 0; comp < m; ++comp) {
    vector<int> cnt(4);
    int tot = 0;
    for (auto [u, mask] : colors[comp]) {
        tot |= mask;
        cnt[bp(mask)]++;
    }
    if (bp(tot)<3) {
        continue;
    }
    if (cnt[2] || cnt[3]>2) {
        cout << "Yes" << endl;
        return;
    }
}
cout << "No" << endl;

```

2.4 DCP offline

```

struct Dsu {
    int n;
    vector<pair<int &, int>> s;
    vector<int> p, sz;
    // other info

    Dsu(int n) : n(n), p(n), sz(n, 1) {
        iota(all(p), 0);
    }

    int get(int u) {
        while (u != p[u]) u = p[u];
        return u;
    }

    bool merge(int u, int v) {
        u = get(u), v = get(v);
        if (u == v) return false;
        if (sz[v] < sz[u]) swap(u, v);
        s.app({p[u], p[u]});
        s.app({sz[v], sz[v]});
        // app other info like s.app({comp, comp});
        p[u] = v;
        sz[v] += sz[u];
        return true;
    }

    void rollback(int sz) {
        while (s.size() != sz) {
            s.back().first = s.back().second;
            s.pop_back();
        }
    }
};

struct DcpOffline {
    int n;
    vector<vector<pair<int, int>>> d;

    void addEdgeOnSegment(int l, int r, int a, int b)
    {
        for (l += n, r += n; l < r; l /= 2, r /= 2) {
            if (l & 1) d[l++].app({a, b});
            if (r & 1) d[--r].app({a, b});
        }
    }

    template<typename T>
    void dfs(Dsu &dsu, T act) {
        dfs(1, 0, n, dsu, act);
    }

    template<typename T>
    void dfs(int v, int l, int r, Dsu &dsu, T act) {
        int sz = dsu.s.size();
        for (auto [u, v]: d[v]) {
            dsu.merge(u, v);
        }
        if (l + 1 == r) {
            act(l, dsu);
        } else {
            int m = (l + r) / 2;

```

```

        dfs(v * 2, l, m, dsu, act);
        dfs(v * 2 + 1, m, r, dsu, act);
    }
    dsu.rollback(sz);
}

DcpOffline(int maxt) : n(2 << __lg(maxt + 1)), d(2
    * n) {}
};

```

3 Свёртки

3.1 AND, OR, XOR свёртки

```

const int p = 998244353;
vector<int> band(vector<int> a, vector<int> b)
{
    int n=0; while((1<<n)<a.size()) ++n;
    a.resize(1<<n); b.resize(1<<n);
    for(int i=0; i<n; ++i) for(int mask=0; mask<(1<<n); ++
        mask) if(mask & (1<<i)) {a[mask-(1<<i)]+=a[mask]; a
            [mask-(1<<i)]%=p;}
    for(int i=0; i<n; ++i) for(int mask=0; mask<(1<<n); ++
        mask) if(mask & (1<<i)) {b[mask-(1<<i)]+=b[mask]; b
            [mask-(1<<i)]%=p;}
    vector<int> c(1<<n, 0);
    for(int mask=0; mask<(1<<n); ++mask) {c[mask]=a[mask]*
        b[mask]; c[mask]%=p;}
    for(int i=0; i<n; ++i) for(int mask=0; mask<(1<<n); ++
        mask) if(!(mask & (1<<i))) {c[mask]-=c[mask+(1<<i)
            ]; c[mask]%=p;}
    return c;
}

vector<int> bor(vector<int> a, vector<int> b)
{
    int n=0; while((1<<n)<a.size()) ++n;
    a.resize(1<<n); b.resize(1<<n);
    for(int i=0; i<n; ++i) for(int mask=0; mask<(1<<n); ++
        mask) if(!(mask & (1<<i))) {a[mask+(1<<i)]+=a[mask
            ]; a[mask+(1<<i)]%=p;}
    for(int i=0; i<n; ++i) for(int mask=0; mask<(1<<n); ++
        mask) if(!(mask & (1<<i))) {b[mask+(1<<i)]+=b[mask
            ]; b[mask+(1<<i)]%=p;}
    vector<int> c(1<<n, 0);
    for(int mask=0; mask<(1<<n); ++mask) {c[mask]=a[mask]*
        b[mask]; c[mask]%=p;}
    for(int i=0; i<n; ++i) for(int mask=0; mask<(1<<n); ++
        mask) if(mask & (1<<i)) {c[mask]-=c[mask-(1<<i)]; c
            [mask]%=p;}
    return c;
}

vector<int> bxor(vector<int> a, vector<int> b)
{
    assert(p%2==1); int inv2=(p+1)/2;
    int n=0; while((1<<n)<a.size()) ++n;
    a.resize(1<<n); b.resize(1<<n);
    for(int i=0; i<n; ++i) for(int mask=0; mask<(1<<n); ++
        mask) if(!(mask & (1<<i))) {int u=a[mask], v=a[mask
            +(1<<i)]; a[mask+(1<<i)]=(u+v)%p; a[mask]=(u-v)%p;}
    for(int i=0; i<n; ++i) for(int mask=0; mask<(1<<n); ++
        mask) if(!(mask & (1<<i))) {int u=b[mask], v=b[mask
            +(1<<i)]; b[mask+(1<<i)]=(u+v)%p; b[mask]=(u-v)%p;}
    vector<int> c(1<<n, 0);
    for(int mask=0; mask<(1<<n); ++mask) {c[mask]=a[mask]*
        b[mask]; c[mask]%=p;}
    for(int i=0; i<n; ++i) for(int mask=0; mask<(1<<n); ++
        mask) if(!(mask & (1<<i))) {int u=c[mask], v=c[mask
            +(1<<i)]; c[mask+(1<<i)]=(v-u)*inv2%p; c[mask]=((u
            +v)*inv2)%p;}
    return c;
}

```

3.2 NTT & co

```

#define int long long
using namespace std;
typedef long long ll;
const int p=998244353;
int po(int a, int b) {if(b==0) return 1; if(b==1)
    return a; if(b%2==0) {int u=po(a, b/2); return (u*u

```

```

LL*u)%p;} else {int u=po(a,b-1);return (a*1LL*u)%p
;}}
int inv(int x) {return po(x,p-2);}
template<int M, int K, int G> struct Fft {
// 1, 1/4, 1/8, 3/8, 1/16, 5/16, 3/16, 7/16, ...
int g[1 << (K - 1)];
Fft() : g() { //if t1 constexpr...
static_assert(K >= 2, "Fft: K >= 2 must hold");
g[0] = 1;
g[1 << (K - 2)] = G;
for (int l = 1 << (K - 2); l >= 2; l >= 1) {
g[l >> 1] = (g[l] * 1LL * g[l]) % M;
}
assert((g[1]*1LL * g[1]) % M == M - 1);
for (int l = 2; l <= 1 << (K - 2); l <= 1) {
for (int i = 1; i < l; ++i) {
g[l + i] = (g[l] * 1LL * g[i]) % M;
}
}
}
}
void fft(vector<int> &x) const {
const int n = x.size();
assert(n <= 1 << K);
for (int h = __builtin_ctz(n); h--;) {
const int l = (1 << h);
for (int i = 0; i < n >> (h+1); ++i) {
for (int j = i << (h+1); j < (((i << 1) + 1)
<< h); ++j) {
const int t = (g[i] * 1LL * x[j | l]) % M;
x[j | l] = x[j] - t;
if (x[j|l] < 0) x[j | l] += M;
x[j]+=t;
if (x[j] >= M) x[j] -= M;
}
}
}
for (int i = 0, j = 0; i < n; ++i) {
if (i < j) std::swap(x[i], x[j]);
for (int l = n; (l >= 1) && !((j ^ 1) & 1); )
{}
}
}
vector<int> convolution(const vector<int> &a, const
vector<int> &b) const {
if(a.empty() || b.empty()) return {};
const int na = a.size(), nb = b.size();
int n, invN = 1;
for (n = 1; n < na + nb - 1; n <= 1) invN = ((
invN & 1) ? (invN + M) : invN) >> 1;
vector<int> x(n, 0), y(n, 0);
std::copy(a.begin(), a.end(), x.begin());
std::copy(b.begin(), b.end(), y.begin());
fft(x);
fft(y);
for (int i = 0; i < n; ++i) x[i] = (((static_cast<
long long>(x[i]) * y[i]) % M) * invN) % M;
std::reverse(x.begin() + 1, x.end());
fft(x);
x.resize(na + nb - 1);
return x;
}
};
Fft<998244353,23,31> muls;
vector<int> form(vector<int> v,int n)
{
while(v.size()<n) v.push_back(0);
while(v.size()>n) v.pop_back();
return v;
}
vector<int> operator *(vector<int> v1,vector<int> v2)
{
return muls.convolution(v1,v2);
}
vector<int> operator +(vector<int> v1,vector<int> v2)
{
while(v2.size()<v1.size()) v2.push_back(0); while(v1
.size()<v2.size()) v1.push_back(0);
for(int i=0;i<v1.size();++i) {v1[i]+=v2[i];if(v1[i]
]>=p) v1[i]-=p; else if(v1[i]<0) v1[i]+=p;}
return v1;
}

```

```

}
vector<int> operator -(vector<int> v1,vector<int> v2)
{
int sz=max(v1.size(),v2.size());while(v1.size()<sz)
v1.push_back(0); while(v2.size()<sz) v2.push_back
(0);
for(int i=0;i<sz;++i) {v1[i]-=v2[i];if(v1[i]<0) v1[i]
]+=p; else if(v1[i]>=p) v1[i]-=p;} return v1;
}
vector<int> trmi(vector<int> v)
{
for(int i=1;i<v.size();i+=2) {if(v[i]>0) v[i]=p-v[i]
]; else v[i]=(-v[i]);}
return v;
}
vector<int> deriv(vector<int> v)
{
if(v.empty()) return{};
vector<int> ans(v.size()-1);
for(int i=1;i<v.size();++i) ans[i-1]=(v[i]*1LL*i)%p;
return ans;
}
vector<int> integ(vector<int> v)
{
vector<int> ans(v.size()+1);ans[0]=0;
for(int i=1;i<v.size();++i) ans[i-1]=(v[i]*1LL*i)%p;
return ans;
}
vector<int> mul(vector<vector<int> > v)
{
if(v.size()==1) return v[0];
vector<vector<int> > v1,v2;for(int i=0;i<v.size()
)/2;++i) v1.push_back(v[i]); for(int i=v.size()/2;i
<v.size();++i) v2.push_back(v[i]);
return muls.convolution(mul(v1),mul(v2));
}
vector<int> invl(vector<int> v,int n)
{
assert(v[0]!=0);
int sz=1;v=form(v,n);vector<int> a={inv(v[0])};
while(sz<n)
{
vector<int> vsz;for(int i=0;i<min(n,2*sz);++i) vsz
.push_back(v[i]);
vector<int> b=((vector<int>) {1})-muls.convolution
(a,vsz);
for(int i=0;i<sz;++i) assert(b[i]==0);
b.erase(b.begin(),b.begin()+sz);
vector<int> c=muls.convolution(b,a);
for(int i=0;i<sz;++i) a.push_back(c[i]);
sz*=2;
}
return form(a,n);
}

```

3.3 старое доброе FFT

```

using cd = complex<double>;
const double PI = acos(-1);

void fft(vector<cd> &a, bool invert) {
int n = a.size();

for (int i = 1, j = 0; i < n; i++) {
int bit = n >> 1;
for (; j & bit; bit >>= 1)
j ^= bit;
j ^= bit;

if (i < j)
swap(a[i], a[j]);
}

for (int len = 2; len <= n; len <= 1) {
double ang = 2 * PI / len * (invert ? -1 : 1);
cd wlen(cos(ang), sin(ang));
for (int i = 0; i < n; i += len) {
cd w(1);
for (int j = 0; j < len / 2; j++) {
cd u = a[i+j], v = a[i+j+len/2] * w;
a[i+j] = u + v;
}
}
}
}

```

```

        a[i+j+len/2] = u - v;
        w *= wlen;
    }
}

if (invert) {
    for (cd & x : a)
        x /= n;
}

vector<int> multiply(vector<int> const& a, vector<int>
    const& b) {
    vector<cd> fa(a.begin(), a.end()), fb(b.begin(), b.
        end());
    int n = 1;
    while (n < a.size() + b.size())
        n <<= 1;
    fa.resize(n);
    fb.resize(n);

    fft(fa, false);
    fft(fb, false);
    for (int i = 0; i < n; i++)
        fa[i] *= fb[i];
    fft(fa, true);

    vector<int> result(n);
    for (int i = 0; i < n; i++)
        result[i] = round(fa[i].real());
    while(!result.empty() && !result.back()) result.
        pop_back();
    return result;
}

```

4 Структуры данных

4.1 Дерево Фенвика

```

int fe[maxn];
void pl(int pos, int val) {while(pos<maxn) {fe[pos]+=
    val;pos|=(pos+1);}}
int get(int pos) {int ans=0;while(pos>=0) {ans+=fe[pos
    ];pos&=(pos+1);--pos;} return ans;} /// [0,pos] -
    vkluchitelno!!!
int get(int l, int r) {return get(r-1)-get(l-1);} ///
    sum of [l,r]

```

4.2 Дерево отрезков

```

#ifdef LOCAL
int __lg(int x) { return 63 - __builtin_clzll(x); }
#endif

template<typename Data, typename Mod, typename
    UniteData, typename UniteMod, typename Apply>
struct MassSegmentTree {
    int h, n;
    Data zd;
    Mod zm;
    vector<Data> data;
    vector<Mod> mod;

    UniteData ud; // Data (Data, Data)
    UniteMod um; // Mod (Mod, Mod);
    Apply a; // Data (Data, Mod, int); last argument is
        the length of current segment (could be used for
        range += and sum counting, for instance)

    template<typename I>
    MassSegmentTree(int sz, Data zd, Mod zm, UniteData
        ud, UniteMod um, Apply a, I init) : h(__lg(sz > 1
        ? sz - 1 : 1) + 1), n(1 << h), zm(zm), zd(zd),
        data(2 * n, zd), mod(n, zm), ud(ud), um(um), a(a)
        {
            for (int i = 0; i < sz; ++i) data[i + n] = init(i)
                ;
            for (int i = n - 1; i > 0; --i) data[i] = ud(data
                [2 * i], data[2 * i + 1]);
        }
}

```

```

MassSegmentTree(int sz, Data zd, Mod zm, UniteData
    ud, UniteMod um, Apply a) : h(__lg(sz > 1 ? sz - 1
    : 1) + 1), n(1 << h), zm(zm), zd(zd), data(2 * n,
    zd), mod(n, zm), ud(ud), um(um), a(a) {}

```

```

void push(int i) {
    if (mod[i] == zm) return;
    apply(2 * i, mod[i]);
    apply(2 * i + 1, mod[i]);
    mod[i] = zm;
}

// is used only for apply
int length(int i) { return 1 << (h - __lg(i)); }

// is used only for descent
int left(int i) {
    int lvl = __lg(i);
    return (i & ((1 << lvl) - 1)) * (1 << (h - lvl));
}

// is used only for descent
int right(int i) {
    int lvl = __lg(i);
    return ((i & ((1 << lvl) - 1)) + 1) * (1 << (h -
        lvl));
}

template<typename S>
void apply(int i, S x) {
    data[i] = a(data[i], x, length(i));
    if (i < n) mod[i] = um(mod[i], x);
}

void update(int i) {
    if (mod[i] != zm) return;
    data[i] = ud(data[2 * i], data[2 * i + 1]);
}

template<typename S>
void update(int l, int r, S x) { // [l; r)
    l += n, r += n;
    for (int shift = h; shift > 0; --shift) {
        push(l >> shift);
        push((r - 1) >> shift);
    }
    for (int lf = l, rg = r; lf < rg; lf /= 2, rg /=
        2) {
        if (lf & 1) apply(lf++, x);
        if (rg & 1) apply(--rg, x);
    }
    for (int shift = 1; shift <= h; ++shift) {
        update(l >> shift);
        update((r - 1) >> shift);
    }
}

Data get(int l, int r) { // [l; r)
    l += n, r += n;
    for (int shift = h; shift > 0; --shift) {
        push(l >> shift);
        push((r - 1) >> shift);
    }
    Data leftRes = zd, rightRes = zd;
    for (; l < r; l /= 2, r /= 2) {
        if (l & 1) leftRes = ud(leftRes, data[l++]);
        if (r & 1) rightRes = ud(data[--r], rightRes);
    }
    return ud(leftRes, rightRes);
}

// l \in [0; n) && ok(get(l, l), l);
// returns last r: ok(get(l, r), r)
template<typename C>
int lastTrue(int l, C ok) {
    l += n;
    for (int shift = h; shift > 0; --shift) push(l >>
        shift);
    Data cur = zd;
}

```

```

do {
    l >>= __builtin_ctz(l);
    Data with1;
    with1 = ud(cur, data[l]);
    if (ok(with1, right(l))) {
        cur = with1;
        ++l;
    } else {
        while (l < n) {
            push(l);
            Data with2;
            with2 = ud(cur, data[2 * l]);
            if (ok(with2, right(2 * l))) {
                cur = with2;
                l = 2 * l + 1;
            } else {
                l = 2 * l;
            }
        }
        return l - n;
    }
} while (l & (l - 1));
return n;
}

// r \in [0; n) && ok(get(r, r), r);
// returns first l: ok(get(l, r), l)
template<typename C>
int firstTrue(int r, C ok) {
    r += n;
    for (int shift = h; shift > 0; --shift) push((r - 1) >> shift);
    Data cur = zd;
    while (r & (r - 1)) {
        r >>= __builtin_ctz(r);
        Data with1;
        with1 = ud(data[--r], cur);
        if (ok(with1, left(r))) {
            cur = with1;
        } else {
            while (r < n) {
                push(r);
                Data with2;
                with2 = ud(data[2 * r + 1], cur);
                if (ok(with2, right(2 * r))) {
                    cur = with2;
                    r = 2 * r;
                } else {
                    r = 2 * r + 1;
                }
            }
            return r - n + 1;
        }
    }
    return 0;
}

void example () {
    // max and +=
    MassSegmentTree segtree(n, 0LL, 0LL,
    [](int x, int y) { return max(x, y); },
    [](int x, int y) { return x + y; },
    [](int x, int y, int len) { return x + y; });

    // sum and +=
    MassSegmentTree segtree(n, 0LL, 0LL,
    [](int x, int y) { return x + y; },
    [](int x, int y) { return x + y; },
    [](int x, int y, int len) { return x + y * len; });

    // sum and assignment
    MassSegmentTree segtree(n, 0LL, -1LL,
    [](int x, int y) { return x + y; },
    [](int x, int y) { return y; },
    [](int x, int y, int len) { return y * len; });
}

```

4.3 Битовый бор

```
template<unsigned int sz, typename T=int>
```

```

struct binarytrie{
    using Bit=typename conditional<sz<=32,unsigned int,
    unsigned long long>::type;
    struct node{
        T cnt;
        array<int, 2>nxt;
        node():cnt(0),nxt({-1,-1}){}
    };
    vector<node>v;
    binarytrie(){v.emplace_back();}
    void insert(Bit x){add(x,1);}
    void erase(Bit x){add(x,-1);}
    void add(Bit x,T k)
    {
        assert(0<=x&&(x>>sz)==0);
        int p=0;
        v[p].cnt+=k;
        for(int i=sz;i--;)
        {
            int j=x>>i&1;
            if(v[p].nxt[j]==-1)
            {
                v[p].nxt[j]=v.size();
                v.emplace_back();
            }
            p=v[p].nxt[j];
            v[p].cnt+=k;
        }
    }
    T count(Bit x, Bit xor_val=0) const//[0, x)
    {
        assert(0<=xor_val&&(xor_val>>sz)==0);
        if(x<0) return 0;
        else if(x>>sz) return v[0].cnt;
        T ret=0;
        int p=0;
        for(int i=sz;i--;)
        {
            int j=x>>i&1, k=xor_val>>i&1;
            if(j==0)p=v[p].nxt[k];
            else
            {
                if(v[p].nxt[k]>=0)ret+=v[v[p].nxt[k]].cnt;
                p=v[p].nxt[!k];
            }
            if(p==-1)break;
        }
        return ret;
    }
    Bit max(Bit xor_val=0) const
    {
        assert(0<=xor_val&&(xor_val>>sz)==0);
        int p=0;
        Bit ret=0;
        if(v[p].cnt==0) return ret;
        for(int i=sz;i--;)
        {
            ret<=1;
            int k=xor_val>>i&1;
            if(v[p].nxt[!k]>=0&&v[v[p].nxt[!k]].cnt>0)
            {
                p=v[p].nxt[!k];
                ret|=1;
            }
            else p=v[p].nxt[k];
        }
        return ret;
    }
    Bit min(Bit xor_val=0) const
    {
        assert(0<=xor_val&&(xor_val>>sz)==0);
        int p=0;
        Bit ret=0;
        for(int i=sz;i--;)
        {
            ret<=1;
            int k=xor_val>>i&1;
            if(v[p].nxt[k]>=0&&v[v[p].nxt[k]].cnt>0)p=v[p].nxt[k];
            else

```

```

    {
        p=v[p].nxt[!k];
        ret|=1;
    }
    return ret;
}
Bit find_by_order(T ord, Bit xor_val=0) const
{
    assert(0<=xor_val&&(xor_val>>sz)==0);
    assert(0<=ord&&ord<v[0].cnt);
    int p=0;
    Bit ret=0;
    for(int i=sz; i--;)
    {
        ret<|=1;
        int k=xor_val>>i&1;
        if(v[p].nxt[k]>=0)
        {
            if(ord>=v[v[p].nxt[k]].cnt)
            {
                ord-=v[v[p].nxt[k]].cnt;
                p=v[p].nxt[!k];
                ret|=1;
            }
            else p=v[p].nxt[k];
        }
        else
        {
            p=v[p].nxt[!k];
            ret|=1;
        }
    }
    return ret;
}
T order_of_key(Bit x, Bit xor_val=0) const {return
    count(x, xor_val);}
};
binarytrie<32>bt;

```

4.4 Ordered set

```

#include <ext/pb_ds/assoc_container.hpp>
#include <ext/pb_ds/tree_policy.hpp>

using namespace __gnu_pbds;
using namespace std;

using ordered_set = tree<int, null_type, less<>,
    rb_tree_tag, tree_order_statistics_node_update>;

```

4.5 Convex hull trick

```

int div_up(int a, int b) { return a/b+((a^b)>0&&a%b);
} // divide a by b rounded up
const int LQ = ..., RQ = ...; //leftmost query,
    rightmost query
int in(ii L, int x) {
    return L.x * x + L.y;
}
struct Hull {
    vector <pair <int, int> > lines;
    vector <int> borders;
    void push(ii L) {
        while (lines.size() && in(L, borders.back()) < in(
            lines.back(), borders.back())) {
            lines.pop_back();
            borders.pop_back();
        }
        if (lines.empty()) {
            lines = {L};
            borders = {LQ};
        }
        else if (lines.back().x > L.x) {
            int x = div_up(L.y - lines.back().y, lines.
                back().x - L.x);
            if (x <= RQ) {
                lines.app(L);
                borders.app(x);
            }
        }
    }
}

```

```

    }
}
Hull () {}
Hull (vector <ii> a) {
    auto comp = [&](ii u, ii v) {
        return u.x > v.x || (u.x == v.x && u.y < v.y);
    };
    sort(all(a), comp);
    for (auto L : a) {
        push(L);
    }
}
int get(int x) {
    int pos = upper_bound(all(borders), x) - borders.
        begin();
    assert(pos>0);
    pos--;
    return in(lines[pos], x);
}
};

```

4.6 Центроиды

```

vector<int> sz(n), lvl(n, -1);
auto dfs = [&](auto dfs, int cur, int prev) -> int {
    if (lvl[cur] != -1) return 0;
    sz[cur] = 1;
    for (auto [nxt, w] : g[cur]) {
        if (nxt != prev) sz[cur] += dfs(dfs, nxt, cur);
    }
    return sz[cur];
};
auto find = [&](auto find, int cur, int prev, int tot)
    -> int {
    int bch = -1, bsz = 0;
    for (auto [nxt, w] : g[cur]) {
        if (nxt == prev || lvl[nxt] != -1) continue;
        if (sz[nxt] > bsz) {
            bch = nxt;
            bsz = sz[nxt];
        }
    }
    if (bsz + bsz <= tot) return cur;
    return find(find, bch, cur, tot);
};
dfs(dfs, 0, 0);
auto c = find(find, 0, 0, sz[0]);
vector<pair<int, int>> stack{{c, 0}};
int ans = INF;
while (!stack.empty()) {
    auto [centroid, l] = stack.back();
    stack.pop_back();
    lvl[centroid] = l;
    for (auto [nxt, w] : g[centroid]) {
        if (lvl[nxt] != -1) continue;
        dfs(dfs, nxt, centroid);
        int new_centroid = find(find, nxt, centroid,
            sz[nxt]);
        stack.push_back({new_centroid, lvl[centroid] +
            1});
    }
}

```

5 Строковые алгоритмы

5.1 Префикс-функция

```

vector<int> prefix_function(string s) {
    vector<int> p(s.size());
    for (int i = 1; i < s.size(); ++i) {
        p[i] = p[i - 1];
        while (p[i] && s[p[i]] != s[i]) p[i] = p[p[i] -
            1];
        p[i] += s[i] == s[p[i]];
    }
    return p;
}

```

5.2 Z-функция


```
vector<int> z_function (string s) { // z[i] - lcp of s
    and s[i:]
    int n = (int) s.length();
    vector<int> z (n);
    for (int i=1, l=0, r=0; i<n; ++i) {
        if (i <= r)
            z[i] = min (r-i+1, z[i-l]);
        while (i+z[i] < n && s[z[i]] == s[i+z[i]])
            ++z[i];
        if (i+z[i]-1 > r)
            l = i, r = i+z[i]-1;
    }
    return z;
}
```

5.3 Алгоритм Манакера

```
vector<int> manacher_odd(const string &s) {
    vector<int> man(s.size(), 0);
    int l = 0, r = 0;
    int n = s.size();
    for (int i = 1; i < n; i++) {
        if (i <= r) {
            man[i] = min(r - i, man[l + r - i]);
        }
        while (i + man[i] + 1 < n && i - man[i] - 1 >= 0
            && s[i + man[i] + 1] == s[i - man[i] - 1]) {
            man[i]++;
        }
        if (i + man[i] > r) {
            l = i - man[i];
            r = i + man[i];
        }
    }
    return man;
}
// abacaba : (0 1 0 3 0 1 0)
// abbaa : (0 0 0 0 0)
```

```
vector<int> manacher_even(const string &s) {
    assert(s.size());
    string t;
    for (int i = 0; i + 1 < s.size(); ++i) {
        t += s[i];
        t += '#';
    }
    t += s.back();
    auto odd = manacher_odd(t);
    vector<int> ans;
    for (int i = 1; i < odd.size(); i += 2) {
        ans.push_back((odd[i]+1)/2);
    }
    return ans;
}
// abacaba : (0 0 0 0 0 0)
// abbaa : (0 2 0 1)
```

5.4 Суфмассив

Переработанный китайский суффмассив

```
const int inf = 1e9;
struct rmq {
    int n;
    vector<int> a;
    void build(const vector<int> &x) {
        assert(x.size() == n);
        for (int i = 0; i < n; ++i) a[n + i] = x[i];
        for (int i = n - 1; i > 0; --i) a[i] = min(a[2 * i
            ], a[2 * i + 1]);
    }
    rmq(int n) : n(n), a(2 * n, inf) {}
    void put(int i, int x) {
        a[i + n] = min(a[i + n], x);
        for (i = (i + n) / 2; i > 0; i /= 2) {
            a[i] = min(a[i * 2], a[i * 2 + 1]);
        }
    }
    int getMin(int l, int r) { //[l;r)
        assert(l < r);
        int res = inf;
        for (l += n, r += n; l < r; l /= 2, r /= 2) {
```

```
            if (l & 1) res = min(res, a[l++]);
            if (r & 1) res = min(res, a[--r]);
        }
        return res;
    }
};
template <typename T>
vector<int> SA(const T &a) {
    int m = *max_element(all(a)) + 1, n = a.size();
    vector<int> sa(n), nsa(n), pre(max(n, m)), x(a.
        begin(), a.end()), y(n);
    for (int e : x) pre[e]++;
    for (int i = 1; i < m; ++i) pre[i] += pre[i - 1];
    for (int i = 0; i < n; ++i) sa[--pre[x[i]]]=i;
    int dif = 1;
    y[sa.front()]=0;
    for (int i = 1; i < n; ++i) {
        dif += x[sa[i]]!=x[sa[i-1]];
        y[sa[i]] = dif - 1;
    }
    x = y;
    for (int h = 1; dif < n; h *= 2) {
        fill(all(pre), 0);
        for (int e : x) pre[e]++;
        for (int i = 1; i < dif; ++i) pre[i] += pre[i
            - 1];
        for (int t = n; t--;) {
            int i = sa[t];
            if (i>=h) {
                nsa[--pre[x[i-h]]]=i-h;
            }
            else if (i + 1 != h) {
                nsa[--pre[x[i-h+n+1]]]=i-h+n+1;
            }
        }
        nsa[--pre[x[n - h]]]=n-h;
        sa = nsa;
        auto getr = [&] (int i) {
            if (i + h < n) {
                return x[i + h];
            }
            else {
                return x[i + h - n - 1];
            }
        };
        dif = 1;
        y[sa.front()]=0;
        for (int i = 1; i < n; ++i) {
            if (x[sa[i]]!=x[sa[i-1]] || sa[i-1]+h==n)
                dif++;
            else {
                dif += getr(sa[i]) != getr(sa[i-1]);
            }
            y[sa[i]]=dif-1;
        }
        x = y;
    }
    return sa;
}
```

```
template <typename T>
struct suar {
    vector<int> sa, lcp, pos; rmq t;
    suar(const T &a) : t((int)a.size() - 1) {
        sa = SA(a);
        int n = (int)a.size(), k = 0;
        lcp.resize(n - 1);
        pos.resize(n);
        for (int i = 0; i < n; ++i) pos[sa[i]] = i;
        for (int i = 0; i < n; ++i) {
            if (pos[i]+1<n) {
                int j = sa[pos[i]+1];
                while (i+k<n&&j+k<n&&a[i+k]==a[j+k])k
                    ++;
                lcp[pos[i]]=k;
            }
            if (k) {
                k--;
            }
        }
    }
};
```



```

    }
    }
    t.build(lcp);
}
int getLcp(int i, int j) {
    i = pos[i]; j = pos[j];
    if (j < i) {
        swap(i, j);
    }
    if (i == j) {
        return inf;
    }
    else {
        return t.getMin(i, j);
    }
}
};

```

5.5 Алгоритм Ахо — Корасик

5.6 Алгоритм Ахо Корасик

```

struct node{
    int next[alpha] = {}, link[alpha] = {};
    int suf = 0;
    ll visited = 0, ans = 0;
    vector<int> term;
    node() {}
};

vector<node> mem;

int get_next(int nd, char c) {
    if (!mem[nd].next[c - a]) { mem[nd].next[c - a] =
        mem.size(); mem.emplace_back(); }
    return mem[nd].next[c - a];
}

void find(string s, vector<string> t) {
    mem.reserve(1e6 + 100); mem.clear();
    mem.emplace_back(); mem.emplace_back();
    // 0th element is nullptr, 1st is the root
    int q = t.size();
    for (int j = 0; j < q; ++j) {
        int cur = 1;
        for (char c : ts[j]) cur = get_next(cur, c);
        mem[cur].term.push_back(j);
    }
    vector<int> bfs_order;
    queue<int> bfs;
    {
        node &root = mem[1];
        root.suf = 1;
        for (char c = a; c < a + alpha; ++c) {
            root.link[c - a] = (root.next[c - a] ? root.
next[c - a] : 1);
        }
        bfs.push(1);
    }
    while (!bfs.empty()) {
        int cur_idx = bfs.front();
        bfs.pop();
        node &cur = mem[cur_idx];
        bfs_order.push_back(cur_idx);
        for (char c = a; c < a + alpha; ++c) {
            int nxt_idx = cur.next[c - a];
            if (!nxt_idx) continue;
            node &nxt = mem[nxt_idx];
            nxt.suf = (cur_idx == 1 ? 1 : mem[cur.suf].link[
c - a]);
            for (char c = a; c < a + alpha; ++c) {
                nxt.link[c - a] = (nxt.next[c - a] ? nxt.next[
c - a] : mem[nxt.suf].link[c - a]);
            }
            bfs.push(nxt_idx);
        }
    }
    // do something
}

```

5.7 Дерево палиндромов

5.8 Дерево палиндромов

```

struct palindromic{
    int n;
    vector<int> p, suf{0, 0}, len{-1, 0};
    vector<array<int, alpha>> to{{}, {}};
    int sz = 2;

    palindromic(const string &s) : n(s.size()), p(n + 1,
1) {
        suf.reserve(n);
        len.reserve(n);
        for (int i = 0; i < n; ++i) {
            auto check = [&](int l) { return i > l && s[i]
== s[i - l - 1]; };
            int par = p[i];
            while (!check(len[par])) par = suf[par];
            if (to[par][s[i] - a]) {
                p[i + 1] = to[par][s[i] - a];
                continue;
            }
            p[i + 1] = sz++;
            to[par][s[i] - a] = p[i + 1];
            to.emplace_back();
            len.emplace_back(len[par] + 2);
            do {
                par = suf[par];
            } while (!check(len[par]));
            int link = to[par][s[i] - a];
            if (link == p[i + 1]) link = 1;
            suf.emplace_back(link);
        }
    }
};

```

6 Потоки

6.1 Алгоритм Диница

```

#define pb push_back
struct Dinic{
    struct edge{
        int to, flow, cap;
    };

    const static int N = 555; //count of vertices

    vector<edge> e;
    vector<int> g[N + 7];
    int dp[N + 7];
    int ptr[N + 7];

    void clear(){
        for (int i = 0; i < N + 7; i++) g[i].clear();
        e.clear();
    }

    void addEdge(int a, int b, int cap){
        g[a].pb(e.size());
        e.pb({b, 0, cap});
        g[b].pb(e.size());
        e.pb({a, 0, 0});
    }

    int minFlow, start, finish;

    bool bfs(){
        for (int i = 0; i < N; i++) dp[i] = -1;
        dp[start] = 0;
        vector<int> st;
        int uk = 0;
        st.pb(start);
        while(uk < st.size()){
            int v = st[uk++];
            for (int to : g[v]){
                auto ed = e[to];
                if (ed.cap - ed.flow >= minFlow && dp[ed.to] ==
-1){

```

```

        dp[ed.to] = dp[v] + 1;
        st.pb(ed.to);
    }
}
return dp[finish] != -1;
}

int dfs(int v, int flow){
    if (v == finish) return flow;
    for (; ptr[v] < g[v].size(); ptr[v]++){
        int to = g[v][ptr[v]];
        edge ed = e[to];
        if (ed.cap - ed.flow >= minFlow && dp[ed.to] == dp[v] + 1){
            int add = dfs(ed.to, min(flow, ed.cap - ed.flow));
            if (add){
                e[to].flow += add;
                e[to ^ 1].flow -= add;
                return add;
            }
        }
    }
    return 0;
}

int dinic(int start, int finish){
    Dinic::start = start;
    Dinic::finish = finish;
    int flow = 0;
    for (minFlow = (1 << 30); minFlow; minFlow >>= 1){
        while(bfs()){
            for (int i = 0; i < N; i++) ptr[i] = 0;
            while(int now = dfs(start, (int)2e9 + 7)) flow += now;
        }
    }
    return flow;
}
} dinic;

```

6.2 Mincost k-flow

```

struct edge {
    int next, capacity, cost, flow = 0;

    edge() = default;

    edge(int next, int capacity, int cost) : next(next),
        capacity(capacity), cost(cost) {}

    int rem() const { return capacity - flow; }

    int operator+=(int f) { return flow += f; }

    int operator-=(int f) { return flow -= f; }
};

auto addEdge = [&](auto from, auto next, auto capacity, int cost) {
    g[from].push_back(e.size());
    e.emplace_back(next, capacity, cost);
    g[next].push_back(e.size());
    e.emplace_back(from, 0, -cost);
};

/* in case of undirected graph use this:
addEdge(u, v, capacity, cost);
addEdge(v, u, capacity, cost);
*/

vector<ll> phi(n, 0);
auto fordBellman = [&](int s, int t) {
    phi.assign(n, 0);
    for (int iter = 0; iter < n; ++iter) {
        bool changed = false;
        for (int u = 0; u < n; ++u) {
            for (auto index : g[u]) {
                auto edge = e[index];
                if (edge.rem() > 0 && phi[edge.next] > phi[u] + edge.cost) {
                    phi[edge.next] = phi[u] + edge.cost;
                    changed = true;
                }
            }
        }
    }
}

```

```

    }
}
if (!changed) break;
}
};

fordBellman(s, t);
// now shortest path using dijkstra with potentials
vector<ll> dist;
vector<int> from;
vector<bool> cnt;
auto dijkstra = [&](int s, int t) {
    dist.assign(n, 1e18);
    from.assign(n, -1);
    cnt.assign(n, false);
    dist[s] = 0;
    set<pair<int, int>> se;
    se.insert({0, s});
    while ((int)(se.size())) {
        int cur = se.begin()->y;
        se.erase(se.begin());
        cnt[cur] = true;
        for (int index : g[cur]) {
            auto &edge = e[index];
            if (edge.rem() == 0) continue;
            ll weight = edge.cost + phi[cur] - phi[edge.next];
            if (dist[edge.next] > dist[cur] + weight) {
                se.erase({dist[edge.next], edge.next});
                dist[edge.next] = dist[cur] + weight;
                se.insert({dist[edge.next], edge.next});
                from[edge.next] = cur;
            }
        }
    }
    if (dist[t] == (ll) 1e18) return -1LL;
    ll cost = 0;
    for (int p = t; p != s; p = from[p]) {
        for (auto index : g[from[p]]) {
            auto &edge = e[index];
            ll weight = edge.cost + phi[from[p]] - phi[edge.next];
            if (edge.rem() > 0 && edge.next == p && dist[edge.next] == dist[from[p]] + weight) {
                edge += 1;
                e[index ^ 1] -= 1;
                cost += edge.cost;
                break;
            }
        }
    }
    for (int i = 0; i < n; ++i) {
        phi[i] += dist[i];
    }
    return cost;
};

ll cost = 0;
for (int flow = 0; flow < k; ++flow) {
    ll a = dijkstra(s, t);
    if (a == -1) {
        cout << "-1\n";
        return;
    }
    cost += a;
}

// now recover answer
auto findPath = [&](int s, int t) {
    vector<int> ans;
    int cur = s;
    while (cur != t) {
        for (auto index : g[cur]) {
            auto &edge = e[index];
            if (edge.flow <= 0) continue;
            edge -= 1;
            e[index ^ 1] += 1;
            ans.push_back(index / 4);
            // index / 4 because each edge has 4 copies
            cur = edge.next;
            break;
        }
    }
}

```

```

    }
    return ans;
};
for (int flow = 0; flow < k; ++flow) {
    auto p = findPath(s, t);
    cout << p.size() << ' ';
    for (int x : p) cout << x + 1 << ' ';
    cout << '\n';
}

```

7 Геометрия

7.1 Прimitives

```

struct Point {
    int x, y;
    Point(){}
    Point (int x_, int y_) {
        x = x_; y = y_;
    }
    Point operator + (Point p) {
        return Point(x+p.x,y+p.y);
    }
    Point operator - (Point p) {
        return Point(x - p.x, y - p.y);
    }
    int operator * (Point p) {
        return x * p.y - y * p.x;
    }
    int operator % (Point p) {
        return x * p.x + y * p.y;
    }
    bool operator < (Point v) {
        return (*this) * v > 0;
    }
    bool operator > (Point v) {
        return v < (*this);
    };
    bool operator <= (Point v) {
        return (*this) * v >= 0;
    }
};

bool line(Point a, Point b, Point c) {
    return (b-a)*(c-b)==0;
}

bool ord(Point a, Point p, Point b) {
    return (p - a)%(p - b)<0;
}

}

7.2 Выпуклая оболочка

using pt = pair<int, int>;
#define x first
#define y second

int cross(pt p, pt q) {
    return p.x * q.y - p.y * q.x;
}

int scalar(pt p, pt q) {
    return p.x * q.x + p.y * q.y;
}

pt operator-(pt a, pt b) { return {a.x - b.x, a.y - b.y}; }

vector<pt> convex(vector<pt> a) {
    sort(all(a));
    if (a.size() == 2 && a[0] == a[1]) return {a[0]};
    if (a.size() <= 1) return a;
    vector<pt> h;
    for (int t = 0; t < 2; ++t) {
        int sz = h.size() - t;
        for (auto p: a) {
            while (h.size() >= sz + 2 && cross(p - h.
end()[1], h.end()[2] - h.end()[1]) <= 0) h.
pop_back();
            h.push_back(p);
        }
        reverse(all(a));
    }
    return h; // h is circular: h.front() == h.back()
}

```

7.3 Точка внутри многоугольника

```

auto inT = [&] (Point a, Point b, Point c, Point p
) {
    a = a-p; b = b-p; c = c-p;
    return abs(a*b)+abs(b*c)+abs(c*a) == abs(a*b+b
*c+c*a);
};

auto inP = [&] (Point p) { //a must be in
counterclockwise order!
    int l = 1, r = n - 1;
    while (l < r - 1) {
        int m = (l + r) / 2;
        if ((a[m] - a[0]) < (p - a[0])) {
            l = m;
        }
        else {
            r = m;
        }
    }
    return inT(a[l], a[0], a[r], p);
};

```

7.4 Касательные

```

auto max = [&] (auto cmp) {
    int k = 0;
    for (int lg = 18; lg >= 0; --lg) {
        int i = k + (1 << lg), j = k - (1 << lg);
        i = (i % n + n) % n;
        j = (j % n + n) % n;
        array<int, 3> ind{i, j, k};
        sort(all(ind), cmp);
        k = ind[2];
    }
    return k;
};

auto uppert = [&] (Point p) { //last vertex in
counterclockwise order about p
    auto cmp = [&] (int i, int j) {return (a[i] -
p) < (a[j] - p); };
    return max(cmp);
};

auto lowert = [&] (Point p) { //first vertex in
counterclockwise order about p
    auto cmp = [&] (int i, int j) {return (a[i] -
p) > (a[j] - p); };
    return max(cmp);
};

auto uppertinf = [&] (Point p) { //upper tangent
line parallel to vector p
    swap(p.x, p.y);
    p.x = -p.x;
    auto cmp = [&] (int i, int j) { return a[i] %
p < a[j] % p; };
    return max(cmp);
};

auto lowertinf = [&] (Point p) { //lower tangent
line parallel to vector p
    swap(p.x, p.y);
    p.x = -p.x;
    auto cmp = [&] (int i, int j) { return a[i] %
p > a[j] % p; };
    return max(cmp);
};

```

8 Разное

8.1 Флаги компиляции

```

-DLOCAL -Wall -Wextra -pedantic -Wshadow -Wformat=2
-Wfloat-equal -Wconversion -Wlogical-op -Wshift-
overflow=2 -Wduplicated-cond -Wcast-qual -Wcast-
align -D_GLIBCXX_DEBUG -D_GLIBCXX_DEBUG_PEDANTIC
-D_FORTIFY_SOURCE=2 -fsanitize=address -
fsanitize=undefined -fno-sanitize-recover -fstack-
protector -std=c++2a

```

8.1.1 Сеточка в vim

<https://codeforces.com/blog/entry/122540>

```
i|<esc>25A    |<esc>
o+<esc>25A---+<esc>
Vky35Pdd
```

8.2 Что сделать на пробном туре

- Убедиться, что работают все IDE. Разобраться, как настраивать в них LOCAL.
- В системе ML — это ML или RE?
- Максимальный размер файла
- Можно посмотреть на время работы серверов позапусков Флойда — Варшалла

8.3 Шаблон

```
#ifdef LOCAL
#define _GLIBCXX_DEBUG
#endif
#include<bits/stdc++.h>

using namespace std;

#define int long long
#define app push_back
#define all(x) x.begin(), x.end()
#ifdef LOCAL
#define debug(...) [](auto...a){ ((cout << a << ' '
    ), ...) << endl; }(__VA_ARGS__, ":",
    __VA_ARGS__)
#define debugv(v) do { cout << #v << ": "; for (
    auto x : v) cout << x << ' '; cout << endl; }
    while(0)
#else
#define debug(...)
#define debugv(v)
#endif

int32_t main() {
    cin.tie(0);ios_base::sync_with_stdio(0);
}
```