

PR 2 Logika Komputasional

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[3] $\exists x. (\text{makanan}(x) \wedge \forall y. (\text{mahasiswa}(y) \rightarrow \text{suka}(y, x)))$

→ Terdapat makanan yang disukai oleh semua mahasiswa

$\forall y. (\text{mahasiswa}(y) \rightarrow \exists x. (\text{makanan}(x) \wedge \text{suka}(y, x)))$

→ Semua mahasiswa menyukai beberapa makanan tertentu

[5] Premis : $\text{kelas}(\text{Jeki}), \text{umur19}(\text{Jeki}), \forall x. (\text{umur19}(x) \rightarrow \text{sim}(x))$

1. $\text{Kelas}(\text{Jeki})$	Premis
2. $\text{umur19}(\text{Jeki})$	Premis
3. $\forall x. (\text{umur19}(x) \rightarrow \text{sim}(x))$	Premis
4. $\text{umur19}(\text{Jeki}) \rightarrow \text{sim}(\text{Jeki})$	UI 3
5. $\text{sim}(\text{Jeki})$	MP 2, 4
6. $\text{kelas}(\text{Jeki}) \wedge \text{sim}(\text{Jeki})$	AI 1, 5
7. $\exists x. (\text{kelas}(x) \wedge \text{sim}(x))$	EG 6

[6] Fakta : $\forall x. (p(x) \rightarrow q(x)) \rightarrow \exists x. (r(x) \wedge s(x))$ Kesimpulan : $\exists x. s(x)$
 $\forall x. (p(x) \rightarrow s(x)) \wedge \forall x. (s(x) \rightarrow q(x))$

1. $\forall x. (p(x) \rightarrow q(x)) \rightarrow \exists x. (r(x) \wedge s(x))$	Premis
2. $\forall x. (p(x) \rightarrow s(x)) \wedge \forall x. (s(x) \rightarrow q(x))$	Premis
3. $\forall x. (p(x) \rightarrow s(x))$	AE 2
4. $\forall x. (s(x) \rightarrow q(x))$	AE 2
5. $p(a) \rightarrow s(a)$	UI 3
6. $s(a) \rightarrow q(a)$	UI 4
7. $p(a) \rightarrow q(a)$	SH 5, 6
8. $(p(a) \rightarrow q(a)) \rightarrow \exists x. (r(x) \wedge s(x))$	UI 1
9. $(p(a) \rightarrow q(a)) \rightarrow (r(b) \wedge s(b))$	EI 8
10. $r(b) \wedge s(b)$	MP 7, 9
11. $s(b)$	AE 10
12. $\exists x (s(x))$	EG 11

$$[9] \forall x [p(x) \rightarrow (\exists y [q(x, y) \wedge \neg r(y)] \wedge \neg \exists y [q(x, y) \wedge q(y, x)] \wedge \forall y [\neg p(y) \rightarrow \neg s(x, y)])]$$

$$I: \forall x [\neg p(x) \vee (\exists y [q(x, y) \wedge \neg r(y)] \wedge \neg \exists y [q(x, y) \wedge q(y, x)] \wedge \forall y [\neg p(y) \vee \neg s(x, y)])]$$

$$N: \forall x [\neg p(x) \vee (\exists y [q(x, y) \wedge \neg r(y)] \wedge \forall y [\neg q(x, y) \vee \neg q(y, x)] \wedge \forall y [\neg p(y) \vee \neg s(x, y)])]$$

$$S: \forall x [\neg p(x) \vee (\exists y [q(x, y) \wedge \neg r(y)] \wedge \forall z [\neg q(x, z) \vee \neg q(z, x)] \wedge \forall w [\neg p(w) \vee \neg s(x, w)])]$$

$$E: \forall x [\neg p(x) \vee (\neg q(x, f(x)) \wedge \neg r(f(x)) \wedge \forall z [\neg q(x, z) \vee \neg q(z, x)] \wedge \forall w [\neg p(w) \vee \neg s(x, w)])]$$

$$A: \neg p(x) \vee (\neg q(x, f(x)) \wedge \neg r(f(x)) \wedge \neg q(x, z) \vee \neg q(z, x) \wedge \neg p(w) \vee \neg s(x, w))$$

$$D: [(\neg p(x) \vee q(x, f(x))) \wedge (\neg p(x) \vee \neg r(f(x))) \wedge (\neg p(x) \vee \neg q(x, z) \vee \neg q(z, x)) \wedge (\neg p(x) \vee \neg p(w) \vee \neg s(x, w))]$$

$$O: \{ \neg p(x), q(x, f(x)) \}$$

$$\{ \neg p(x), \neg r(f(x)) \}$$

$$\{ \neg p(x), \neg q(x, z), \neg q(z, x) \}$$

$$\{ \neg p(x), p(w), \neg s(x, w) \}$$

$$[10] \textcircled{a} \text{color}(\text{tweety}, \text{yellow}) \text{ dan } \text{color}(x, y)$$

$$\text{Compare: color}(\text{tweety}, \text{yellow}), \text{color}(x, y), \{ \}$$

$$\text{compare: color, color, } \{ \}$$

$$\text{result: } \{ \}$$

$$\text{compare: tweety, x, } \{ \}$$

$$\text{result: } \{ \text{tweety} \leftarrow x \}$$

$$\text{compare: yellow, y, } \{ \text{tweety} \leftarrow x \}$$

$$\text{result: } \{ \text{tweety} \leftarrow x, \text{yellow} \leftarrow y \}$$

$$\text{result: } \{ \text{tweety} \leftarrow x, \text{yellow} \leftarrow y \}$$

$$\textcircled{b} \text{color}(\text{tweety}, \text{yellow}) \text{ dan } \text{color}(x, x)$$

$$\text{Compare: color}(\text{tweety}, \text{yellow}), \text{color}(x, x), \{ \}$$

$$\text{compare: color, color, } \{ \}$$

$$\text{result: } \{ \}$$

$$\text{compare: tweety, x, } \{ \}$$

$$\text{result: } \{ \text{tweety} \leftarrow x \}$$

$$\text{compare: yellow, x, } \{ \text{tweety} \leftarrow x \}$$

$$\text{result: } \{ \text{tweety} \leftarrow x, \text{yellow} \leftarrow x \}$$

$$\text{result: } \{ \text{tweety} \leftarrow x, \text{yellow} \leftarrow x \}$$

© compare : color(hat(postman), blue), color(hat(y), x), {}

compare : color, color, {}

result : {}

compare : hat, hat, {}

result : {}

compare : postman, y, {}

result : {postman \leftarrow y}

compare : blue, x, {postman \leftarrow y}

result : {postman \leftarrow y, blue \leftarrow x}

result : {postman \leftarrow y, blue \leftarrow x}

④ compare : q(x, x), q(y, f(y)), {}

compare : q, q, {}

result : {}

compare : x, y, {}

result : {x \leftarrow y}

compare : x, f(y), {x \leftarrow y}

compare : y, f(y), {x \leftarrow y}

result : {x \leftarrow y, f(y) \leftarrow y}

result : {x \leftarrow y, f(y) \leftarrow y}

⑤ compare : p(A, x, f(g(y))), p(z, f(z), f(A)), {}

compare : p, p, {}

result : {}

compare : A, z, {}

result : {A \leftarrow z}

compare : x, f(z), {A \leftarrow z}

result : {A \leftarrow z, x \leftarrow f(z)}

compare : f, f, {A \leftarrow z, x \leftarrow f(z)}

result : {A \leftarrow z, x \leftarrow f(z)}

compare : g(y), A, {A \leftarrow z, x \leftarrow f(z)}

compare : g(y), z, {A \leftarrow z, x \leftarrow f(z)}

result : {A \leftarrow z, x \leftarrow f(z), g(y) \leftarrow z}

result : {A \leftarrow z, x \leftarrow f(z), g(y) \leftarrow z}

③ compare : color(hat(postman), blue), color(hat(y), x), {}

compare : color, color, {}

result : {}

compare : hat, hat, {}

result : {}

compare : postman, y, {}

result : {postman \leftarrow y}

compare : blue, x, {postman \leftarrow y}

result : {postman \leftarrow y, blue \leftarrow x}

result : {postman \leftarrow y, blue \leftarrow x}

④ compare : q(x, x), q(y, f(y)), {}

compare : q, q, {}

result : {}

compare : x, y, {}

result : {x \leftarrow y}

compare : x, f(y), {x \leftarrow y}

compare : y, f(y), {x \leftarrow y}

result : {x \leftarrow y, f(y) \leftarrow y}

result : {x \leftarrow y, f(y) \leftarrow y}

⑤ compare : p(A, x, f(g(y))), p(z, f(z), f(A)), {}

compare : p, p, {}

result : {}

compare : A, z, {}

result : {A \leftarrow z}

compare : x, f(z), {A \leftarrow z}

result : {A \leftarrow z, x \leftarrow f(z)}

compare : f, f, {A \leftarrow z, x \leftarrow f(z)}

result : {A \leftarrow z, x \leftarrow f(z)}

compare : g(y), A, {A \leftarrow z, x \leftarrow f(z)}

compare : g(y), z, {A \leftarrow z, x \leftarrow f(z)}

result : {A \leftarrow z, x \leftarrow f(z), g(y) \leftarrow z}

result : {A \leftarrow z, x \leftarrow f(z), g(y) \leftarrow z}

$$\oplus f(x, g(f(a), u)) = f(g(u, v), x)$$

Compare : $f, f, \{\}$

result : $\{\}$

compare : $x, g(u, v), \{\}$

result : $\{x \leftarrow g(u, v)\}$

compare : $g(f(a), u), x, \{x \leftarrow g(u, v)\}$

compare : $g(f(a), u), g(u, v), \{x \leftarrow g(u, v)\}$

compare : $f(a), u, \{x \leftarrow g(u, v)\}$

result : $\{x \leftarrow g(u, v), f(a) \leftarrow u\}$

compare : $u, v, \{x \leftarrow g(u, v), f(a) \leftarrow u\}$

result : $\{x \leftarrow g(u, v), f(a) \leftarrow u, u \leftarrow v\}$

result : $\{x \leftarrow g(u, v), g(u, v) \leftarrow x, f(a) \leftarrow u, u \leftarrow v\}$

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1. $\{ \neg p(x, y), \neg q(x, y, f(x, y)) \}$ Premis
2. $\{ \neg r(y, z), q(a, y, z) \}$ Premis
3. $\{ r(y, z), \neg q(a, y, z) \}$ Premis
4. $\{ p(x, g(x)), q(x, g(x), z) \}$ Premis
5. $\{ \neg r(x, y), \neg q(x, w, z) \}$ Premis

6. $\{ \neg p(x, y), \neg r(y, z) \}$ 1, 2
7. $\{ \neg q(a, x, z), \neg q(x, w, z) \}$ 3, 5
8. $\{ p(x, y), r(y, z) \}$ 3, 4 MGU $\{ g(x) \leftarrow y, a \leftarrow x \}$
9. $\{ \neg r(y, z), r(y, z), \neg q(a, y, z) \}$ 6, 8
10. $\{ \}$ 9