Algebric form of:
$$\left(\frac{8-4\sqrt{3}i}{2+6\sqrt{3}i}\right)^{342} = ?$$

$$\left(\frac{8-4\sqrt{3}i}{2+6\sqrt{3}i}\right)^{342} = \left(\frac{(8-4\sqrt{3}i)(2-6\sqrt{3}i)}{(2+6\sqrt{3}i)(2-6\sqrt{3}i)}\right)^{342} =$$

$$= \left(\frac{16-48\sqrt{3}i-8\sqrt{3}i-72}{4+108}\right)^{342} = \left(\frac{-56-56\sqrt{3}i}{112}\right)^{342} =$$

$$= \left(-\frac{1}{2}-\frac{\sqrt{3}}{2}i\right)^{342} = \left(-1\left(\frac{1}{2}+\frac{\sqrt{3}}{2}i\right)\right)^{342} =$$

$$= -1^{342}\left(\frac{1}{2}+\left(\frac{\sqrt{3}}{2}i\right)\right)^{342}\right) = \left(\frac{1}{2}+\frac{\sqrt{3}}{2}i\right)^{342} =$$

$$|z| = \sqrt{Re(z)^2+Im(z)^2}$$

$$z = |z|\left(\frac{Re(z)}{|z|}+\frac{Im(z)}{|z|}i\right) = |z|\left(\cos\varphi+i\sin\varphi\right)$$

$$z^n = |z|^n\left(\cos n\varphi+i\sin n\varphi\right)$$

$$|z| = \sqrt{\left(\frac{1}{2}\right)^2+\left(\frac{\sqrt{3}}{2}\right)^2} = \sqrt{\frac{4}{4}} = 1$$

$$z^{342} = 1^{342}\left(\cos \frac{342}{6}\pi+i\sin \frac{342}{6}\pi\right)$$

$$z^{342} = \cos \frac{399\pi}{6}+i\sin \frac{399\pi}{6}$$

$$z^{342} = \cos \left(\frac{398\pi}{6}+\pi\right)+i\sin \left(\frac{398\pi}{6}+\pi\right)$$

$$z^{342} = \cos \pi+i\sin \pi=-1$$

$$\Rightarrow \left(\frac{8-4\sqrt{3}i}{2+6\sqrt{3}i}\right)^{342} = -1$$