

$$\begin{aligned}
v_1 &= (-4, 3, 5, -3) \\
v_2 &= (-4, -1, 8, -14) \\
v_3 &= (-1, 1, 1, 0) \\
v_4 &= (-1, -3, 2, \mu - 8) \\
v &= (1, 1, \lambda, 1)
\end{aligned}$$

$$\begin{aligned}
& \begin{array}{c} 1 \\ 1 \end{array} \left( \begin{array}{cccc|c} -4 & -4 & -1 & -1 & 1 \\ 3 & -1 & 1 & -3 & 1 \\ 5 & 8 & 1 & 2 & \lambda \\ -3 & -14 & 0 & \mu - 8 & 1 \end{array} \right) \\
& \rightarrow \begin{array}{c} -4 \\ 1 \\ -3 \end{array} \left( \begin{array}{cccc|c} -4 & -4 & -1 & -1 & 1 \\ -1 & -5 & 0 & -4 & 2 \\ 1 & 4 & 0 & 1 & \lambda + 1 \\ -3 & -14 & 0 & \mu - 8 & 1 \end{array} \right) \\
& \rightarrow \begin{array}{c} 16 \\ -5 \\ 1 \end{array} \left( \begin{array}{cccc|c} 0 & 16 & -1 & 15 & -7 \\ -1 & -5 & 0 & -4 & 2 \\ 0 & -1 & 0 & -3 & \lambda + 3 \\ 0 & 1 & 0 & \mu + 4 & -5 \end{array} \right) \\
& \rightarrow \left( \begin{array}{cccc|c} 0 & 0 & -1 & -33 & 16\lambda + 41 \\ -1 & 0 & 0 & 11 & -5\lambda - 13 \\ 0 & -1 & 0 & -3 & \lambda + 3 \\ 0 & 0 & 0 & \mu + 1 & \lambda - 2 \end{array} \right) \begin{array}{l} -1 \\ -1 \\ -1 \end{array}
\end{aligned}$$

$$\left| \begin{array}{rcl} x_3 & + & 33x_4 = -16\lambda - 41 \\ x_1 & + & -11x_4 = 5\lambda + 13 \\ x_2 & + & 3x_4 = -\lambda - 3 \\ & & (\mu + 1)x_4 = \lambda - 2 \end{array} \right.$$

$$\mathbf{1} \quad \mu = -1$$

$$\mathbf{1.1} \quad \lambda = 2$$

$$\left| \begin{array}{rcl} x_3 & + & 33x_4 = -16\lambda - 41 \\ x_1 & + & -11x_4 = 5\lambda + 13 \\ x_2 & + & 3x_4 = -\lambda - 3 \\ & & 0x_4 = 0 \end{array} \right.$$

$$\rightarrow \left| \begin{array}{rcl} x_3 & + & 33x_4 = -16\lambda - 41 \\ x_1 & + & -11x_4 = 5\lambda + 13 \\ x_2 & + & 3x_4 = -\lambda - 3 \end{array} \right.$$

$$x_4 = p$$

$$\left| \begin{array}{rcl} x_3 & + & 33p = -16\lambda - 41 \\ x_1 & + & -11p = 5\lambda + 13 \\ x_2 & + & 3p = -\lambda - 3 \end{array} \right.$$

$$\rightarrow \left| \begin{array}{rcl} x_3 & = & -16\lambda - 41 - 33p \\ x_1 & = & 5\lambda + 13 + 11p \\ x_2 & = & -\lambda - 3 - 3p \end{array} \right.$$

## 1.2 $\lambda \neq 2$

$$\left| \begin{array}{rcl} x_3 & + & 33x_4 = -16\lambda - 41 \\ x_1 & + & -11x_4 = 5\lambda + 13 \\ x_2 & + & 3x_4 = -\lambda - 3 \\ & & 0x_4 = \lambda - 2 \end{array} \right.$$

## 2 $\mu \neq -1$

### 2.1 $\lambda = 2$

$$\left| \begin{array}{rcl} x_3 & + & 33x_4 = -16\lambda - 41 \\ x_1 & + & -11x_4 = 5\lambda + 13 \\ x_2 & + & 3x_4 = -\lambda - 3 \\ & & (\mu + 1)x_4 = 0 \end{array} \right.$$

$$\rightarrow \left| \begin{array}{rcl} x_3 & = & -16\lambda - 41 \\ x_1 & = & 5\lambda + 13 \\ x_2 & = & -\lambda - 3 \\ x_4 & = & 0 \end{array} \right.$$

### 2.2 $\lambda \neq 2$

$$\left| \begin{array}{rcl} x_3 & + & 33x_4 = -16\lambda - 41 \\ x_1 & + & -11x_4 = 5\lambda + 13 \\ x_2 & + & 3x_4 = -\lambda - 3 \\ & & (\mu + 1)x_4 = \lambda - 2 \end{array} \right.$$

$$\rightarrow \left| \begin{array}{rcl} x_3 & = & \frac{-(16\lambda+41)(\mu+1)-33(\lambda-2)}{\mu+1} \\ x_1 & = & \frac{(5\lambda+13)(\mu+1)+11(\lambda-2)}{-(\lambda+3)(\mu+1)-3(\lambda-2)} \\ x_2 & = & \frac{\mu+1}{\lambda-2} \\ x_4 & = & \frac{\lambda-2}{\mu+1} \end{array} \right.$$

$$\rightarrow \left\{ \begin{array}{lcl} x_3 & = & \frac{-(16\lambda\mu+40\lambda+41\mu-25)}{\mu+1} \\ x_1 & = & \frac{5\lambda\mu+16\lambda+13\mu-9}{\mu+1} \\ x_2 & = & \frac{-(\lambda\mu+4\lambda+3\mu-3)}{\mu+1} \\ x_4 & = & \frac{\lambda-2}{\mu+1} \end{array} \right.$$