$$\lim_{n \to \infty} \frac{2n^3 + 3n + 5}{-3n^3 + 4n + 7}$$

$$\lim_{n\to\infty} \frac{\frac{n^3}{n^2} (2 + \frac{3}{n^2} + \frac{5}{n^3})}{\frac{n^3}{n^3} (-3 + \frac{4}{n^2} + \frac{7}{n^3})}$$

$$\lim_{n\to\infty} \frac{2 + \frac{3}{n^2} + \frac{5}{n^3}}{-3 + \frac{4}{n^2} + \frac{7}{n^3}}$$

$$\lim_{n\to\infty} \frac{2+\frac{3}{n^2}+\frac{5}{n^3}}{-3+\frac{4}{2}+\frac{7}{3}}$$

$$\lim_{n\to\infty} \frac{2+3\frac{1}{n}\frac{1}{n}+5\frac{1}{n}\frac{1}{n}\frac{1}{n}}{-3+4\frac{1}{n}\frac{1}{n}+7\frac{1}{n}\frac{1}{n}\frac{1}{n}}$$

$$\frac{1}{n} \to 0 \implies \lim_{n \to \infty} \frac{2+3\times 0+5\times 0}{-3+4\times 0+7\times 0}$$

$$\implies \lim_{n \to \infty} \frac{2n^3 + 3n + 5}{-3n^3 + 4n + 7} = \frac{-2}{3}$$