Algebric form of: 
$$\left(\frac{8-4\sqrt{3}i}{2+6\sqrt{3}i}\right)^{342} = ?$$

$$\left(\frac{8-4\sqrt{3}i}{2+6\sqrt{3}i}\right)^{342} = \left(\frac{(8-4\sqrt{3}i)(2-6\sqrt{3}i)}{(2+6\sqrt{3}i)(2-6\sqrt{3}i)}\right)^{342} =$$

$$= \left(\frac{16-48\sqrt{3}i-8\sqrt{3}i-72}{4+108}\right)^{342} = \left(\frac{-56-56\sqrt{3}i}{112}\right)^{342} = \left(-\frac{1}{2}-\frac{\sqrt{3}}{2}i\right)^{342}$$

$$|z| = \sqrt{Re(z)^2 + Im(z)^2}$$

$$z = |z| \left(\frac{Re(z)}{|z|} + \frac{Im(z)}{|z|}i\right) = |z| (\cos\varphi + i\sin\varphi)$$

$$z^n = |z|^n (\cos n\varphi + i\sin n\varphi)$$

$$|z| = \sqrt{\left(\frac{1}{2}\right)^2 + \left(\frac{\sqrt{3}}{2}\right)^2} = \sqrt{\frac{4}{4}} = 1$$

$$z = 1 \left(\cos\frac{5}{3}\pi + i\sin\frac{5}{3}\pi\right)$$

$$z^{342} = 1^{342} \left(\cos\frac{342}{3}\pi + i\sin\frac{342}{3}\pi\right)$$

$$z^{342} = \cos 560\pi + i\sin 560\pi$$

$$z^{342} = \cos 0\pi + i\sin 0\pi = 1$$

$$\Rightarrow \left(\frac{8-4\sqrt{3}i}{2+6\sqrt{3}i}\right)^{342} = 1$$