

# SESA2024 Astronautics

## Chapter 9: Communications

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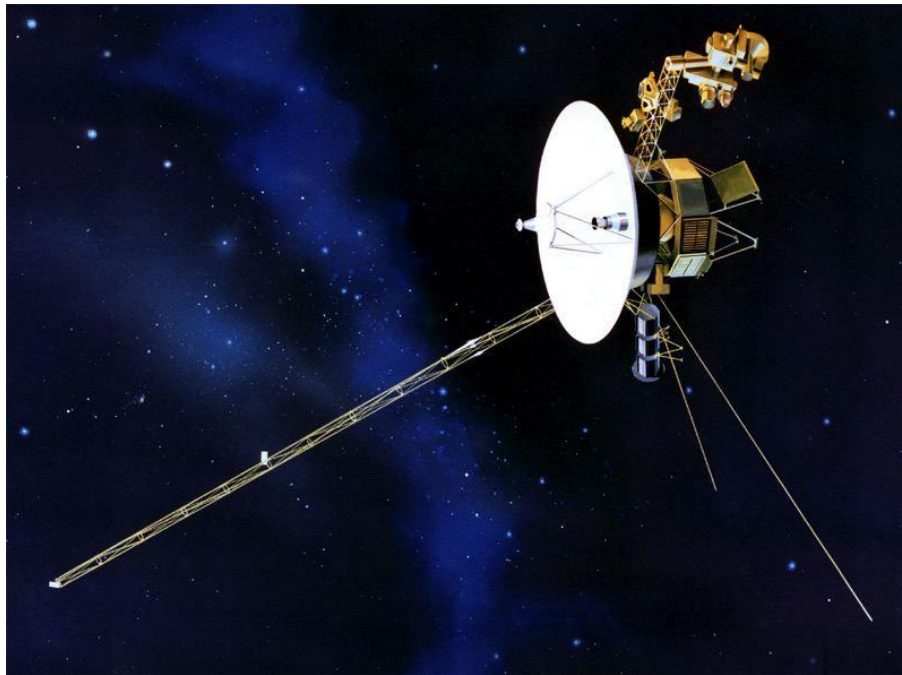
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Example

# The Communications Subsystem

## Function

The function of the communications subsystem is to receive spacecraft operating commands and data from the ground, and to downlink payload and telemetry data to Earth.



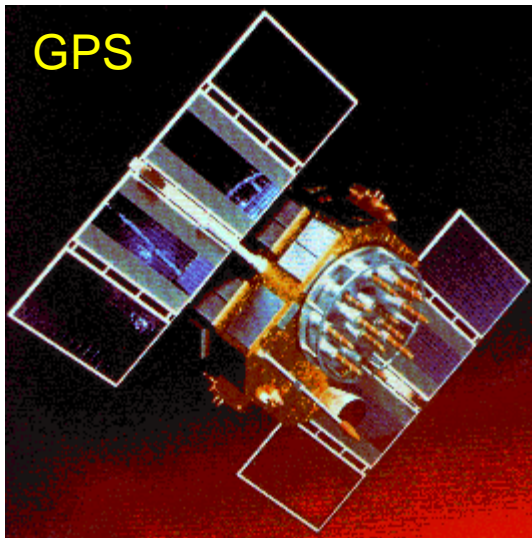
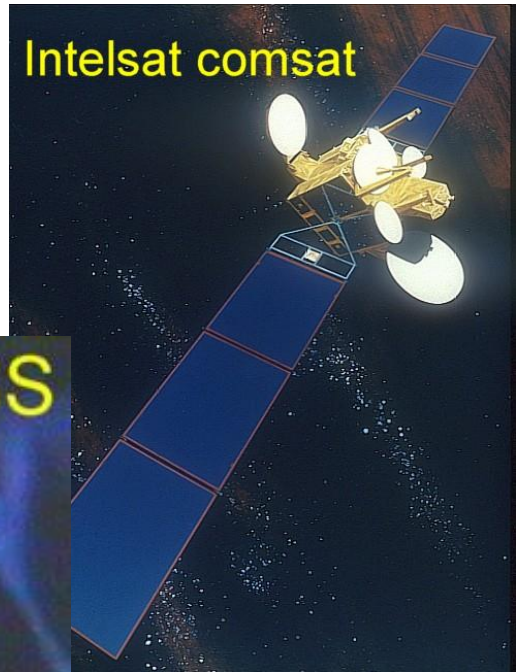
Voyager spacecraft

# The Communications Subsystem

## Spacecraft

Spacecraft with a predominantly communications payload include:

- Comsats
- Navigation satellites
- Tracking and data relay satellites



# The Communications Subsystem

## The Decibel

- The dB is a commonly used unit in communications link analysis to express power level ratios

e.g. 
$$(P_R / P_T)_{dB} = 10 \log_{10} (P_R / P_T)$$

- We can also express power levels relative to 1 Watt (dBW)

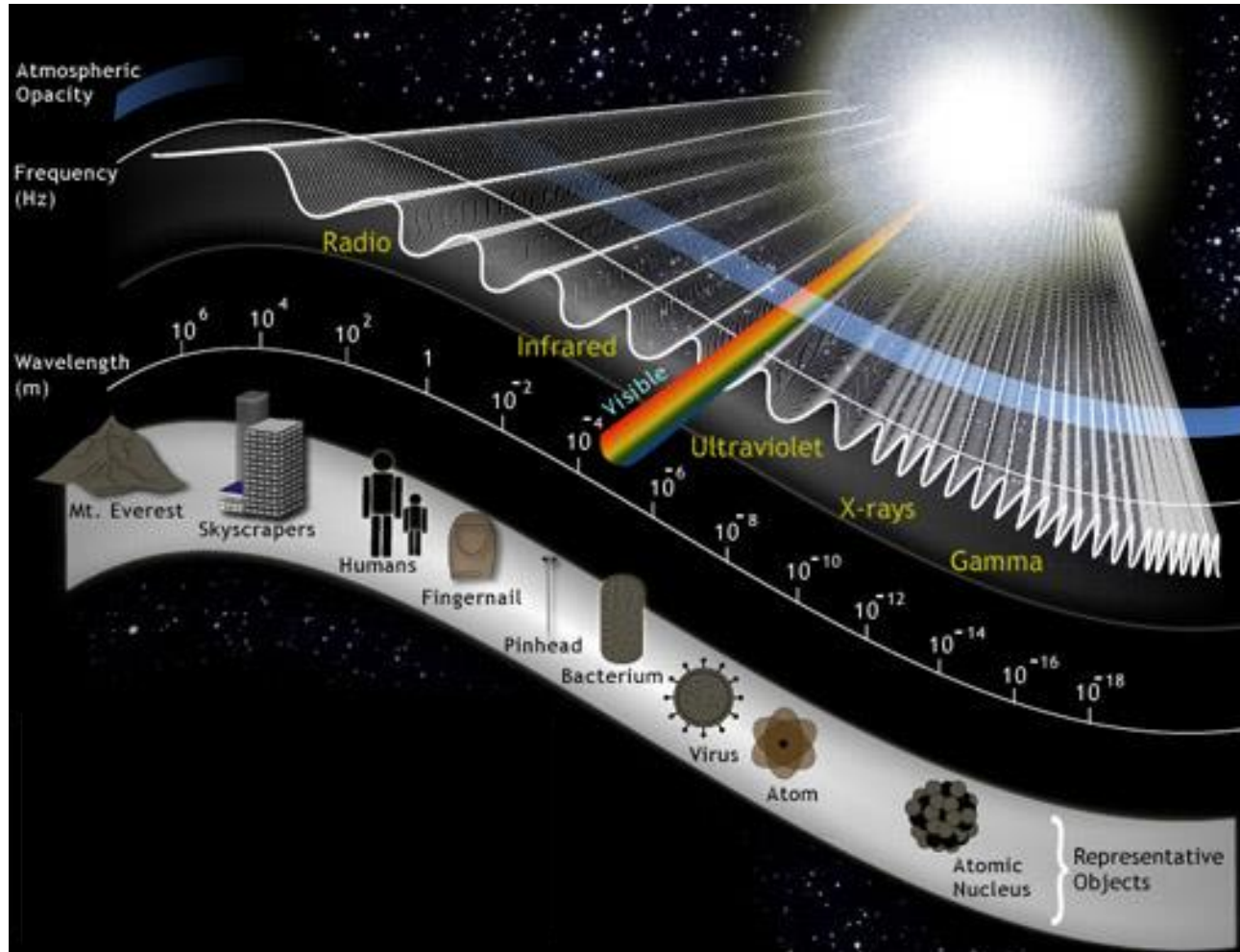
$$(P_T)_{dBW} = 10 \log_{10} (P_T / 1 \text{ Watt})$$

e.g.

$$P_T = 42.3 \text{ dBW} \Rightarrow P_T = 16.98 \text{ kW}$$

# The Communications Subsystem

## Transmission

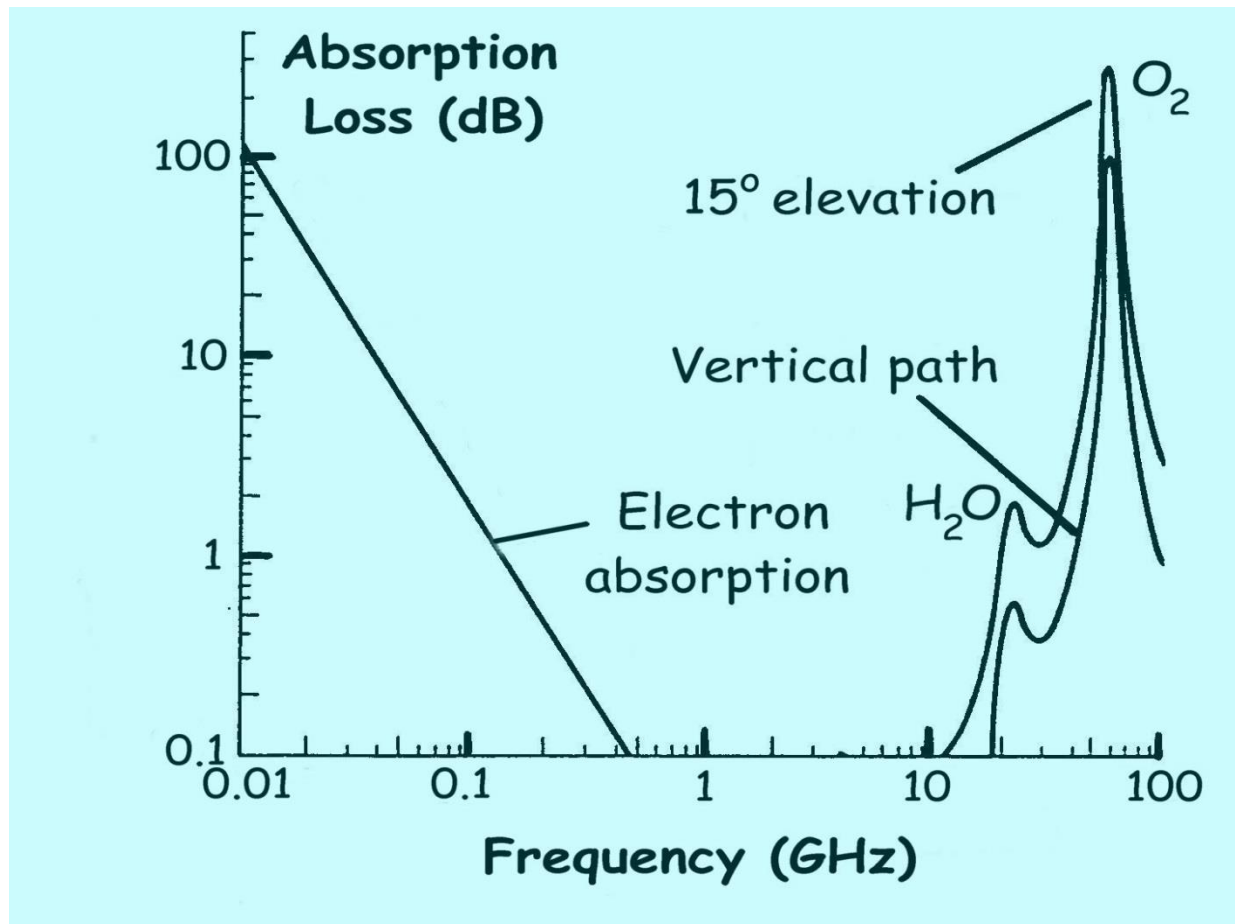


The communications system uses focused microwave beams to send and receive data.



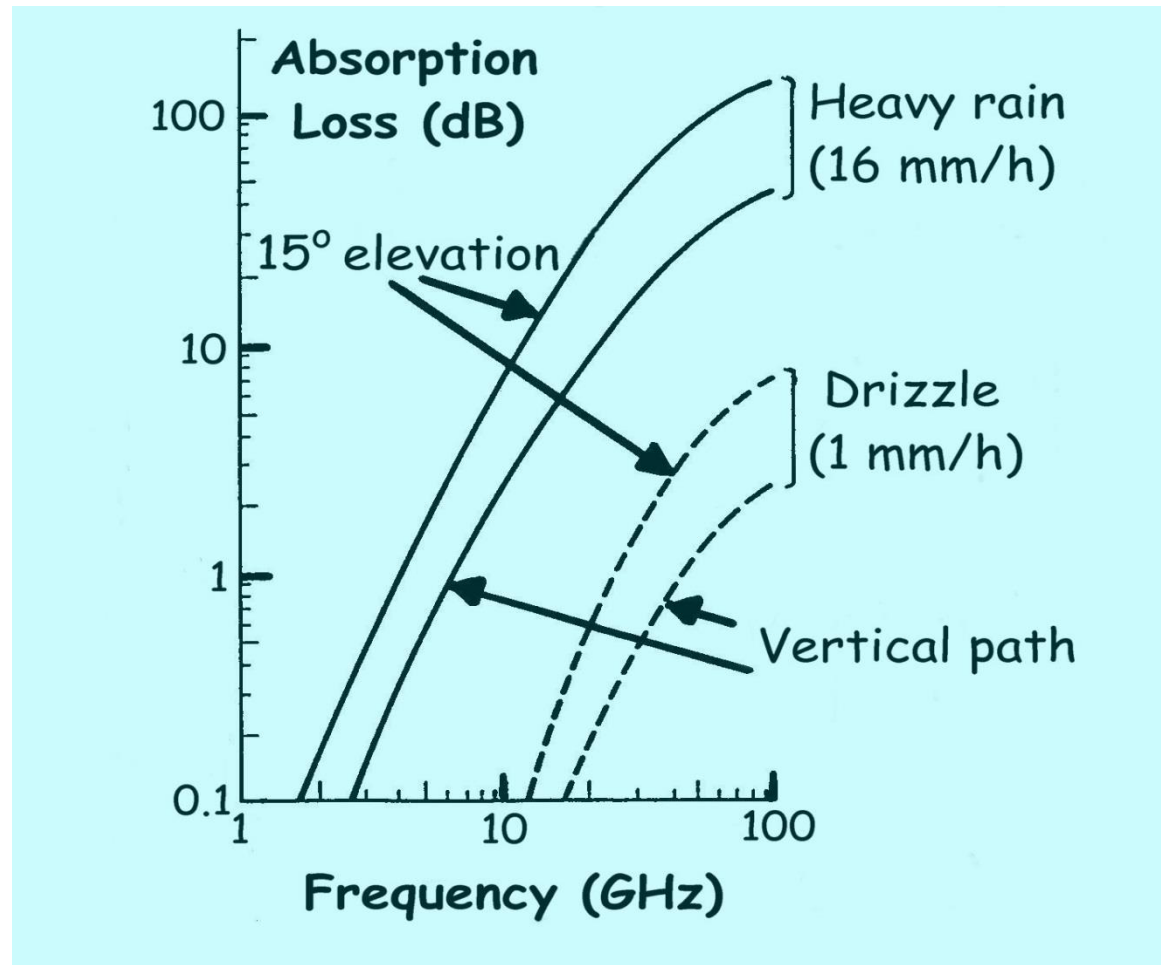
# Atmospheric Windows

Atmospheric and Ionospheric Absorption (fairly constant)



# Atmospheric Windows

Absorption due to rain (highly variable)





# Atmospheric Windows

## Frequency Bands

- Satellite frequency bands are allocated by the ITU (International Telecommunications Union)

<b>Usage</b>	<b>Downlink (GHz)</b>	<b>Uplink (GHz)</b>
<b>TT&amp;C*</b>	0.137 – 0.138	1.427 – 1.429
<b>Fixed comms</b>		
- C-Band	3.7 – 4.2	5.925 – 7.075
- K-Band	10.7 – 12.2	14.0 – 14.5
<b>Mobile comms</b>		
Maritime (L-Band)	1.530 – 1.544	1.627 – 1.646
Aero (L-Band)	1.545 – 1.559	1.647 – 1.660
<b>Navigation</b>		
L-Band	1.535 – 1.560	1.635 – 1.660
<b>Space research§</b>		
S-Band	2.20 – 2.29	2.025 – 2.120
X-Band	7.25 – 7.75	7.9 – 8.4

**\*TT&C** = Tracking, Telemetry & Command

**§** Includes Earth-observation and interplanetary missions

# Encoding, Modulation and Bandwidth

## Digital Encoding

**Space communications are predominantly digital**

➡ Bit Error Rate (BER) becomes the measure of link quality

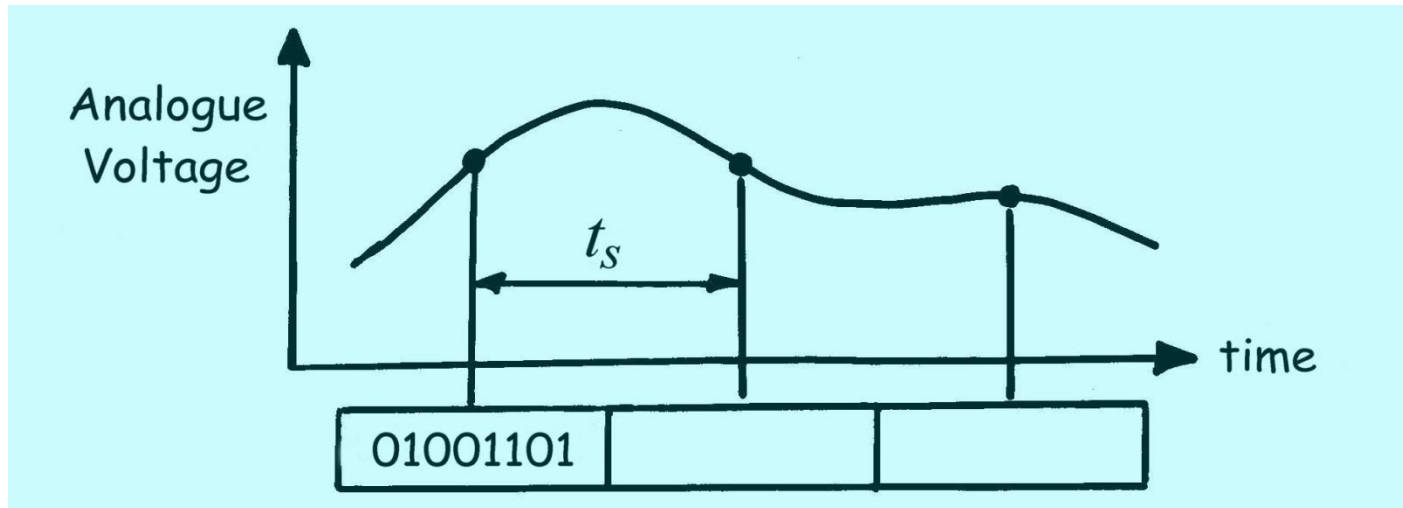
This involves the requirement to convert an analogue signal to a digital bit stream (e.g. telephony)

**PCM (Pulse Code Modulation)** is a commonly used encoding technique (which is not actually a modulation method!)

# Encoding, Modulation and Bandwidth

## Digital Encoding

Example: Estimate the digital data rate of an analogue telephone signal using PCM.



- Signal is sampled every  $t_s$  seconds, and encoded as an 8 bit word (giving  $2^8 = 256$  discrete levels)
- Sampling frequency  $f_s = t_s^{-1}$  (Hz)

# Encoding, Modulation and Bandwidth

## Digital Encoding

- Maximum frequency in a human voice  $\sim 3,400$  Hz
- For good quality reproduction we require  $f_s \geq 2 f_{\max}$  (Nyquist)
- Therefore  $f_s = 8$  kHz
- Hence bit rate for one-way telephone circuit is

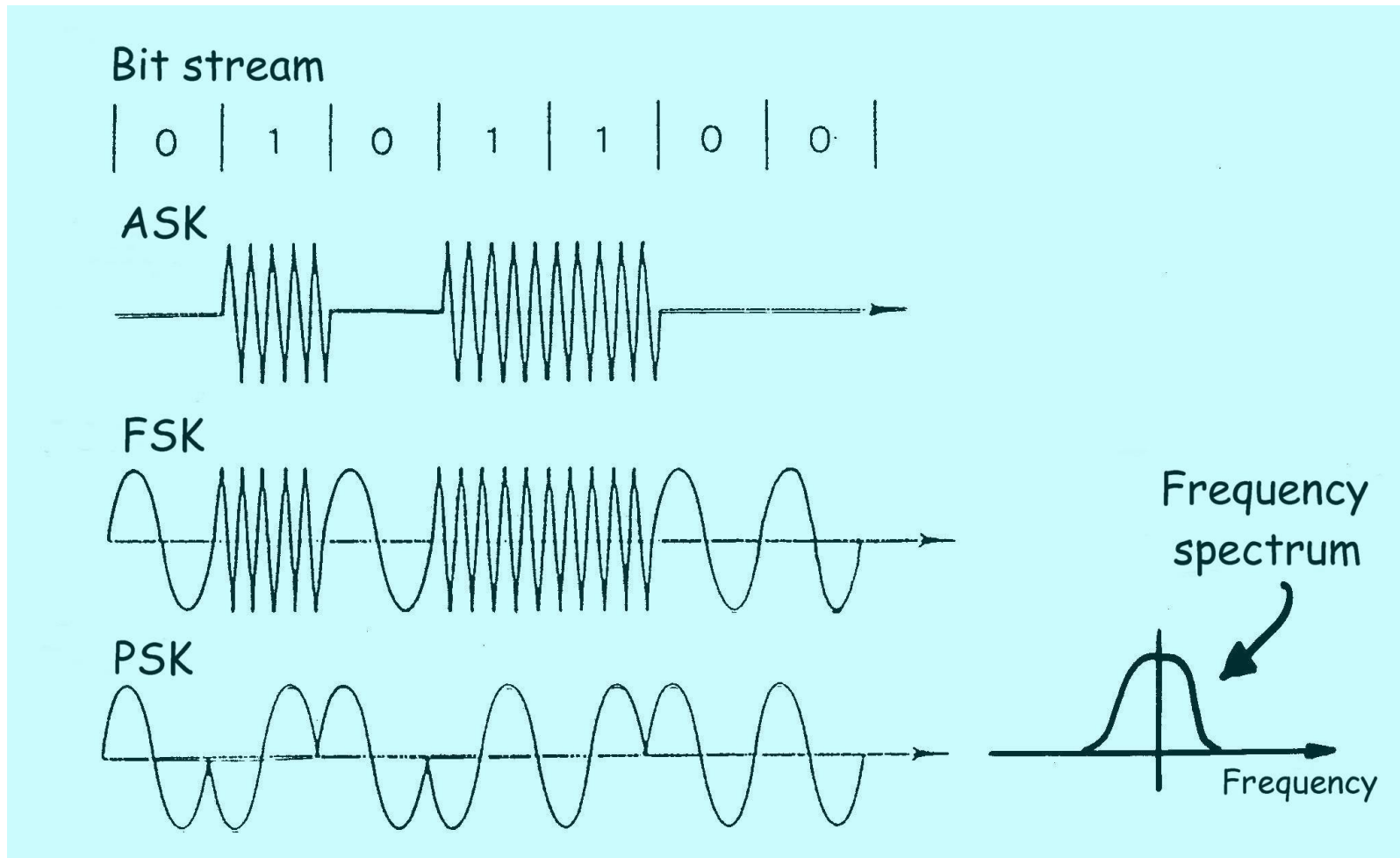
$$R_b = 8000(8) = 64 \text{ kbps}$$

## Digital Modulation Techniques

- **The carrier wave** is modulated to carry digital information using:
  - **ASK** (Amplitude Shift Keying)
  - **FSK** (Frequency Shift keying), or
  - **PSK** (Phase Shift Keying)

# Encoding, Modulation and Bandwidth

## Digital Modulation Techniques



# Encoding, Modulation and Bandwidth

## Digital Modulation Techniques

- **PSK is the most widely used** form of digital modulation
- **Information transmission** requires frequency bandwidth. This is illustrated by Shannon's Law:

$$R_{\max} = B \log_2 \left( 1 + \frac{S}{N} \right) \quad (\text{bps}) \quad (9.1)$$

where  $R_{\max}$  is the maximum data rate (bps),

$B$  is the channel bandwidth (Hz), and  $S/N$  is the signal-to-noise power ratio



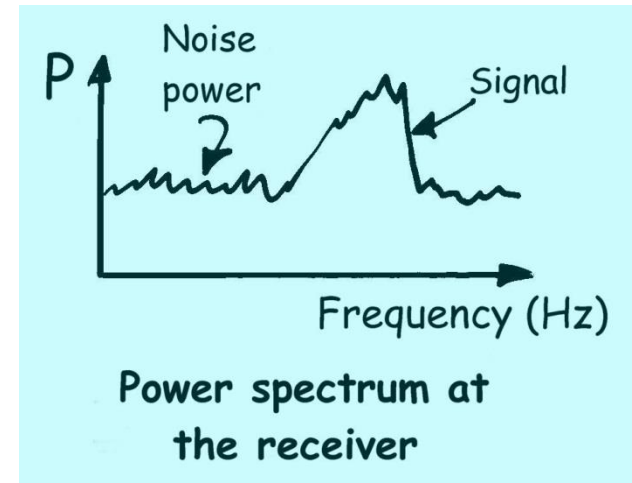
# Noise

- **Noise** is any unwanted interference with the signal:

- We must be able to recover the signal in a noisy environment
- The effectiveness of the link is characterised by the signal-to-noise ratio (related to the BER)

- **Sources of noise** include

- Atmospheric emission and scattering
- The Sun, Earth and galactic sources
- Lightning
- Artificial sources (cars, electrical machinery, etc.)
- Internal electronic/microwave devices



# Noise

- **Sources are characterised** by an equivalent noise temperature  $T$  (K) so that the noise power  $N$  within a bandwidth  $B$  (Hz) is given by

$$N = kTB \quad (\text{W}) \quad (9.2)$$

where  $k = 1.38 \times 10^{-23}$  J/K is Boltzmann's constant.

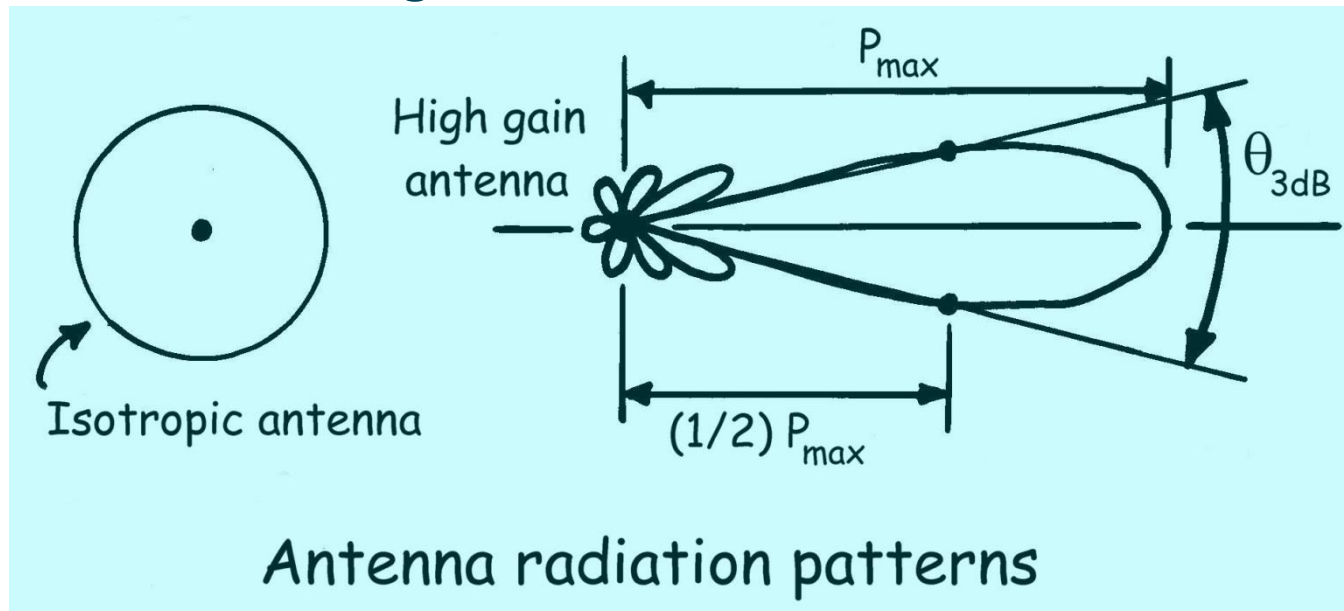
# Antenna Gain and Beamwidth

## Isotropic Radiator

- Radiates power with equal intensity in all directions
- Gain is defined to be unity (0 dB)

## High Gain Antenna

- Concentrates the radiated power in a particular direction (antenna boresight)



# Antenna Gain and Beamwidth

## Beamwidth

- **Beamwidth** is usually defined to be the half-power beamwidth. That is, 3 dB down from maximum boresight power. For a circular parabolic antenna, this is given (empirically) by

$$\theta_{3dB} \approx 72(\lambda/D) \quad (\text{degrees}) \quad (9.3)$$

where  $\lambda$  is the operating wavelength and  $D$  is the dish diameter.

# Antenna Gain and Beamwidth

## Antenna Gain

- **Antenna gain** is defined by

$$G = \frac{\text{maximum power flux}}{\text{power flux of an isotropic radiator}}$$

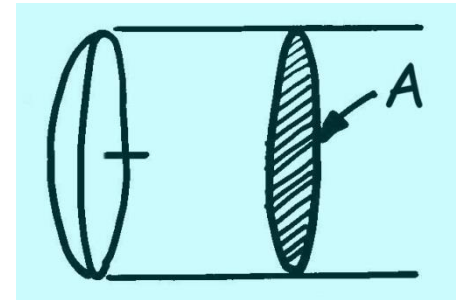
for the same transmitted power. In general, antenna gain is given (empirically) by

$$G = \frac{4\pi A_{eff}}{\lambda^2} = \frac{4\pi A}{\lambda^2} \eta \quad (9.4)$$

where  $A_{eff}$  is the effective aperture area,

$A$  is the projected aperture area, and

$\eta$  is the antenna efficiency ( $0.4 < \eta < 0.8$ )



# Antenna Gain and Beamwidth

## Antenna Gain

For a circular, parabolic antenna of diameter  $D$  equation (9.4) becomes

$$G = \eta \left( \frac{\pi D}{\lambda} \right)^2, \quad \eta \approx 0.65 \quad (9.5)$$

Examples of a parabolic dish antenna, operating at C-Band (4 GHz)

– Wavelength  $c = f\lambda \Rightarrow \lambda = \frac{c}{f} = \frac{3 \times 10^8 \text{ m/s}}{4 \times 10^9 \text{ Hz}} = 0.075 \text{ m}$

- 1 m dish

$$\theta_{3dB} \sim 5.4^\circ, \quad G = 30.6 \text{ dB}$$



# Antenna Gain and Beamwidth

- 6 m dish       $\theta_{3dB} \sim 0.9^\circ$ ,  $G = 46.1$  dB
- 25.9 m dish (Goonhilly A)

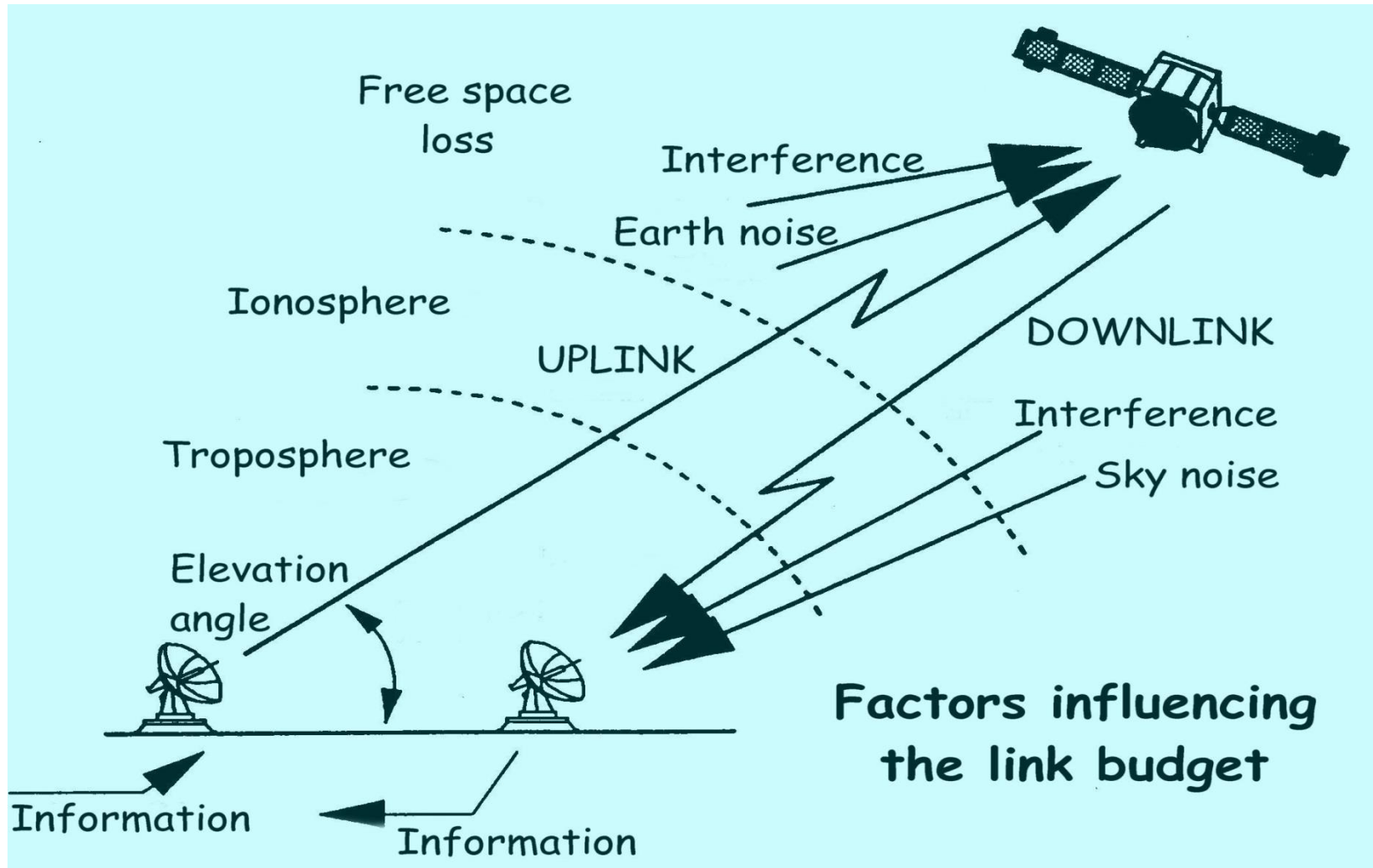


$$\theta_{3dB} \sim 0.2^\circ, \quad G = 58.5 \text{ dB}$$

Goonhilly Down, Cornwall

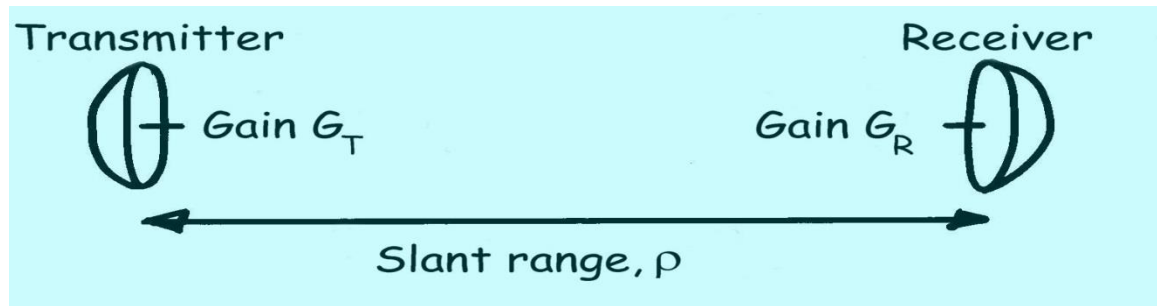


# The Communications Link Analysis



# The Communications Link Analysis

## Link Budget Equation



- If the transmitter were isotropic, power flux at the receiver would be

$$\phi = P_T / (4\pi\rho^2) \quad (\text{W/m}^2)$$

- Taking account of the transmitter gain  $G_T$

$$\phi = P_T G_T / (4\pi\rho^2)$$

- Received power is therefore

$$P_R = \phi A_{R,eff} \quad (\text{W}) \quad \rightarrow \quad P_R = \frac{P_T G_T}{(4\pi\rho^2)} A_{R,eff}$$

# The Communications Link Analysis

## Link Budget Equation

- But from equation (9.4) we have

$$G_R = (4\pi A_{R,eff}) / \lambda^2 \quad \rightarrow \quad A_{R,eff} = G_R \lambda^2 / 4\pi$$

so that

$$P_R = \frac{P_T G_T}{(4\pi\rho^2)} A_{R,eff} = \frac{P_T G_T}{4\pi\rho^2} \left( \frac{G_R \lambda^2}{4\pi} \right) \equiv \frac{P_T G_T G_R}{L_{FS}}$$

where the free space loss  $L_{FS}$  is defined by

$$L_{FS} = \left( \frac{4\pi\rho}{\lambda} \right)^2$$

# The Communications Link Analysis

## Link Budget Equation

- Introduce additional losses  $L_A$ , due to atmospheric absorption, precipitation, depointing, internal (circuit) losses, etc.,

$$P_R = \frac{P_T G_T G_R}{(L_{FS} L_A)} \quad (\text{W})$$

- Now let  $P_R \equiv C$  (carrier power), and introduce noise density  $N_0$  at the receiver, given by

$$N_0 = k T_R \quad (\text{W/Hz})$$

- Then

$$\frac{C}{N_0} = \frac{P_T G_T G_R}{(L_{FS} L_A)} \left( \frac{1}{k T_R} \right) = (P_T G_T) \left( \frac{G_R}{T_R} \right) \left( \frac{1}{L_{FS} L_A} \right) \left( \frac{1}{k} \right)$$

# The Communications Link Analysis

## Link Budget Equation

- In dBs, this gives

$$10\log_{10}\left(\frac{C}{N_0}\right) = 10\log_{10}\left((P_T G_T)\left(\frac{G_R}{T_R}\right)\left(\frac{1}{L_{FS} L_A}\right)\left(\frac{1}{k}\right)\right)$$

Therefore the budget equation for the satellite communications link ...

$$\underbrace{10\log_{10}\left(\frac{C}{N_0}\right)}_{\text{Carrier Power to Noise density ratio}} = \underbrace{10\log_{10}(P_T G_T)}_{\text{EIRP}} + \underbrace{10\log_{10}\left(\frac{G_R}{T_R}\right)}_{\text{Ground Station Figure of Merit}} - \underbrace{20\log_{10}\left(\frac{4\pi\rho}{\lambda}\right)}_{\text{Free space loss}} - \underbrace{10\log_{10} L_A}_{\text{Atmospheric losses}} - \underbrace{10\log_{10} k}_{\text{Constant}} \quad (9.6)$$



# The Communications Link Analysis

## Figures of Merit

### Equivalent Isotropic Radiated Power (EIRP)

- This is given by

$$EIRP = P_T G_T \quad (W) \quad (9.7)$$

- If the transmitter were replaced by an isotropic radiator, the EIRP would be the power required by the isotropic radiator to achieve the same power flux at the receiver as the original transmitter.

### Receiver G/T ratio

- This is a measure of the sensitivity of the receiver – it can be shown to be directly proportional to the  $C/N_0$  ratio

# Link Quality

For a digital link, the link quality is given in terms of the Bit Error Rate (BER), which is the probability that a bit is received incorrectly.

- If  $R_b$  is the link data rate (bps), the time to receive one bit of information is

$$t_b = 1/R_b \quad (\text{seconds})$$

- Also the energy per bit is given by

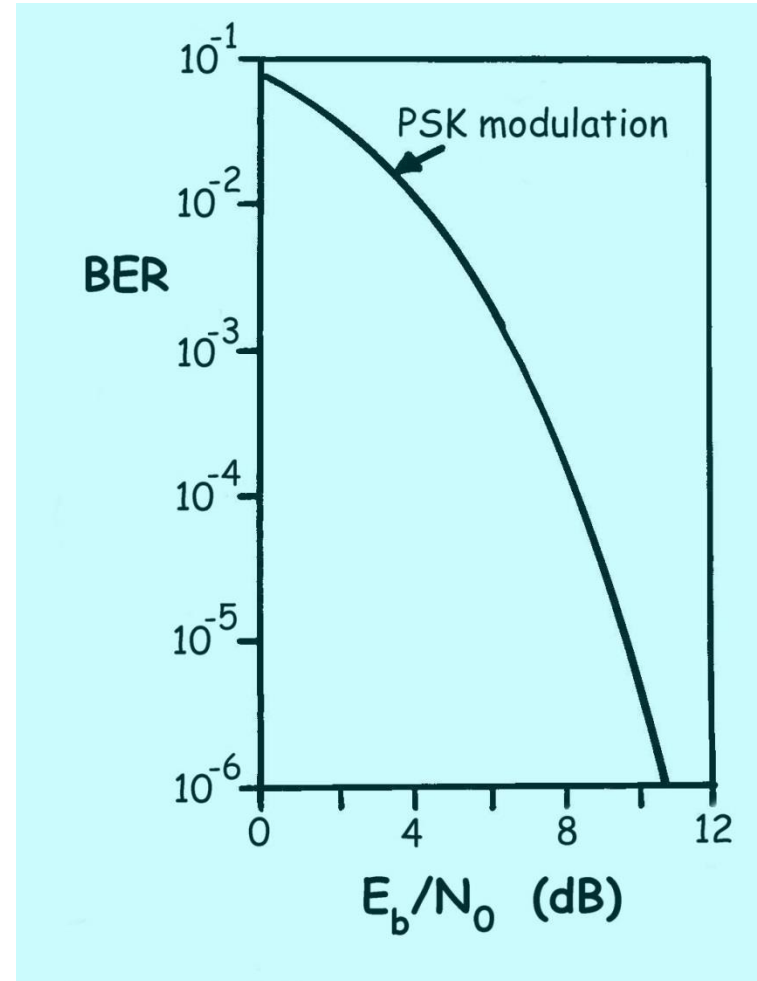
$$E_b = C t_b \rightarrow C = \frac{E_b}{t_b}$$

- Hence we have

$$\frac{C}{N_0} = \frac{E_b}{t_b} \frac{1}{N_0} = \frac{E_b}{N_0} \frac{1}{t_b} \rightarrow \frac{C}{N_0} = \frac{E_b}{N_0} R_b \quad (9.8)$$

# Link Quality

- For a particular type of modulation (e.g. PSK),  $E_b/N_0$  and BER are related



## Example

- A geostationary Earth orbit spacecraft broadcasts TV channels at a data rate of 92 Mbps to a user community at a slant range of 38,400 km, with a C-Band downlink frequency of 4 GHz. The user's receiver has a parabolic dish antenna of 0.4 m diameter, and a receiver system noise temperature of 150 K. If a BER of  $10^{-6}$  is required at the receiver and there is an additional loss of 5 dB, estimate the satellite EIRP.
- If the spacecraft transmitting antenna is a 2 m diameter parabolic dish, and the spacecraft transponders are 50% efficient, estimate the transponder electrical power.

# Chapter 9 Summary

## The Communications Subsystem

## Atmospheric Windows

## Encoding, Modulation and Bandwidth

## Noise

## Antenna Gain and Beamwidth

## The Communications Link Analysis

## Link Quality

## Example

### Key points:

- Function of the subsystem and examples of missions for which the communications subsystem is the payload
- Introduce the decibel and the transmission medium

- Environmental constraints on the transmission
- Useful communication bands and standards

- Basic introduction to encoding, modulation and bandwidth
- Example to outline these principles

- Definition, sources and quantification of noise in the communications link

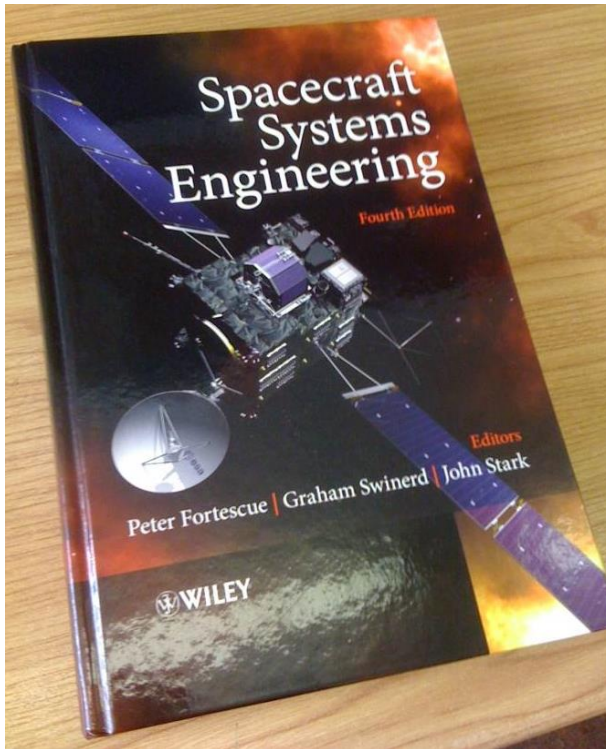
- Introduction to antenna gain and beamwidth
- How these values can be calculated using formula's based on empirical data (with examples)

- Derivation of the link budget equation
- Introduction to each term in the link budget equation and the importance of the EIRP

- How link 'quality' is accounted for in the link budget equation for digital communications

- Link budget equation example

## Chapter 9 Summary



Read Chapter 12  
of Fortescue, Stark  
& Swinerd