

SESA2024 Astronautics

Chapter 6: Attitude Control

Contents

Attitude Control Introduction

Rotational Dynamics

Momentum Management

Spacecraft Categories

Torques and Torquers

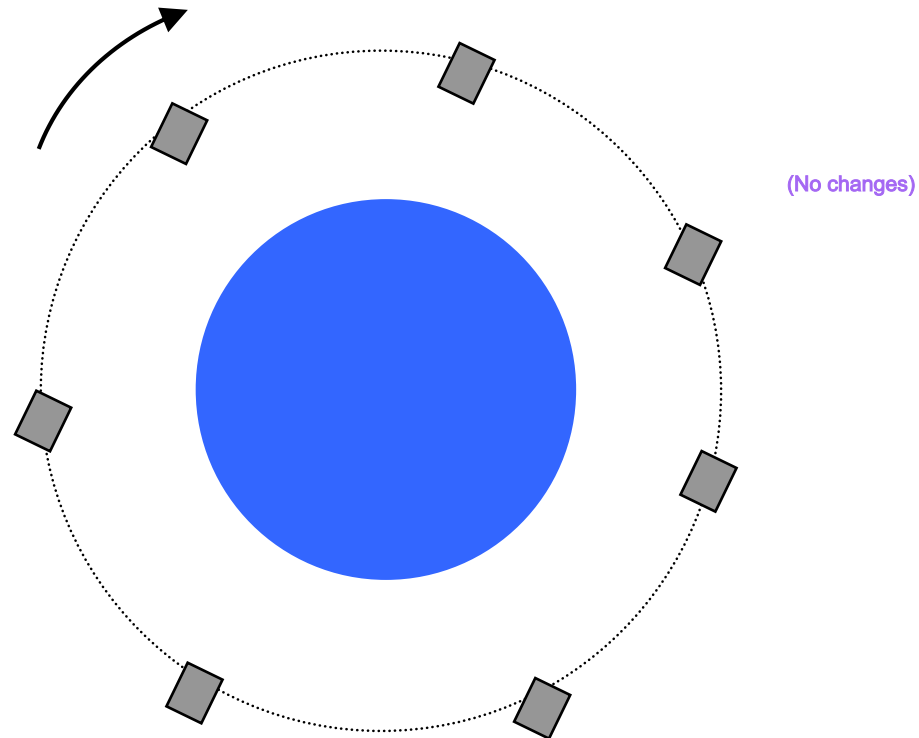
Attitude Sensors

On-board processing

Impact of the ACS on the Spacecraft System

Attitude Control Introduction

Basic motion: Consider a body in orbit (with no disturbances)...



Attitude Control Introduction

Primary Purposes of the Attitude Control System (ACS) are:

- To achieve the pointing requirements of the **payload**, in terms of directions, accuracy, stability, etc.

e.g. Earth pointing (comms payload, remote sensing payload, ...)

Diverse directions (astronomical observatory, ...)

- To achieve the pointing requirements for “**house-keeping**”, in all phases of the mission

e.g. Power raising  Sun pointing

Communications  Earth pointing

Thermal dissipation  Deep space

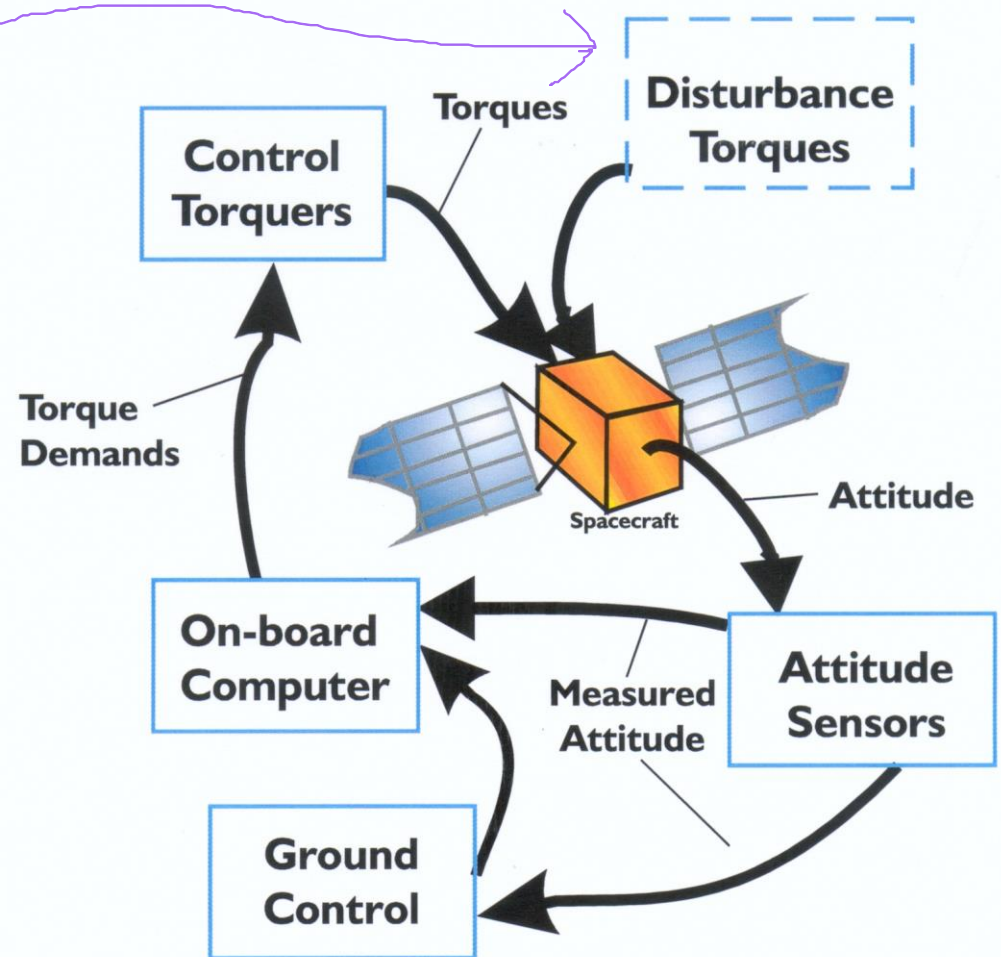
Thrust vector direction for rocket engine firing

- To ‘*manage the overall (angular) momentum*’ of the spacecraft to achieve its pointing mission.

Attitude Control Introduction

Typical ACS operation showing flow of information:

In situations where a satellite passes through thin parts of the atmosphere the large thin areas (such as solar panels) can have a non uniform tiny rotational force applied, which adds up over the course of many orbits.



So... we need to consider the rotational motion of spacecraft about its Centre of Mass (CM), and torques about the CM.

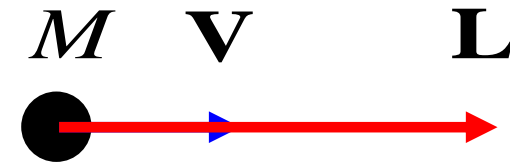
Rotational Dynamics

Linear Momentum

a 'stepping-stone' to translational/orbit dynamics

$$\mathbf{L} = M\mathbf{V}$$

\swarrow \downarrow \searrow
 vector scalar vector



Newton's second law:

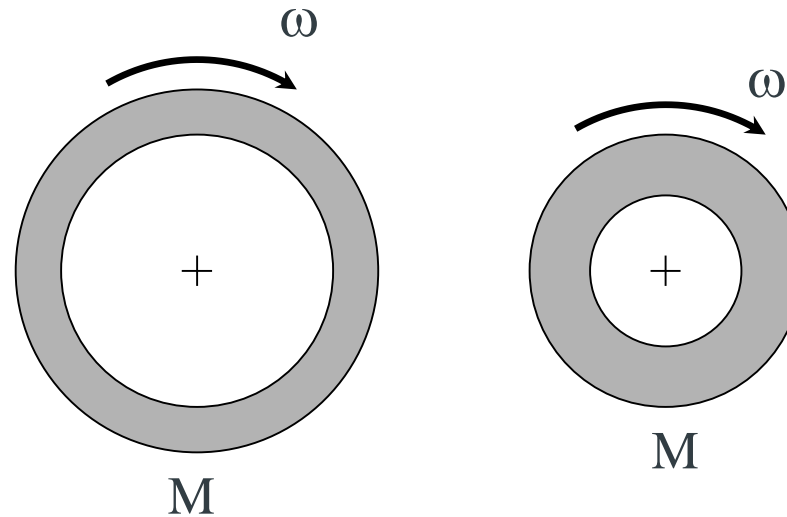
$$\frac{d}{dt}(\mathbf{L}) = \frac{d}{dt}(M\mathbf{V}) = \sum \mathbf{F}_{ext}$$

Free Motion:

- No Force, $\sum \mathbf{F}_{ext} = \mathbf{0} \Rightarrow$ Momentum \mathbf{L} is constant

Rotational Dynamics

Angular Momentum – *Inertia, one dimension*



Is the angular momentum the same?

Rotational Dynamics

Angular Momentum – *Inertia, rotational vectors*

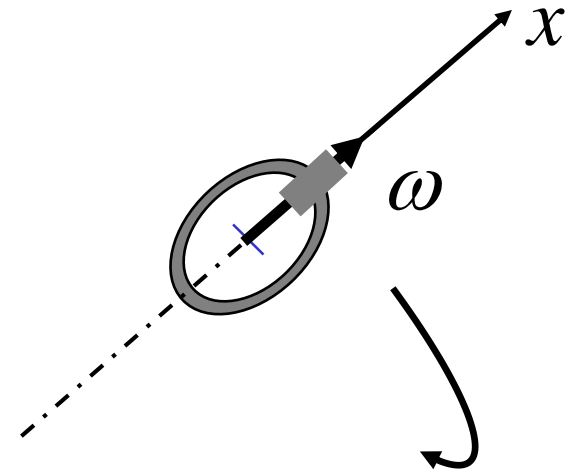
For this one dimensional motion:

$$\mathbf{H} = I_{xx} \boldsymbol{\omega}$$

vector
scalar
vector

Newton's second law:

$$\frac{d}{dt}(\mathbf{H}) = \frac{d}{dt}(I_{xx} \boldsymbol{\omega}) = \sum \mathbf{T}_{ext}$$



Free Motion:

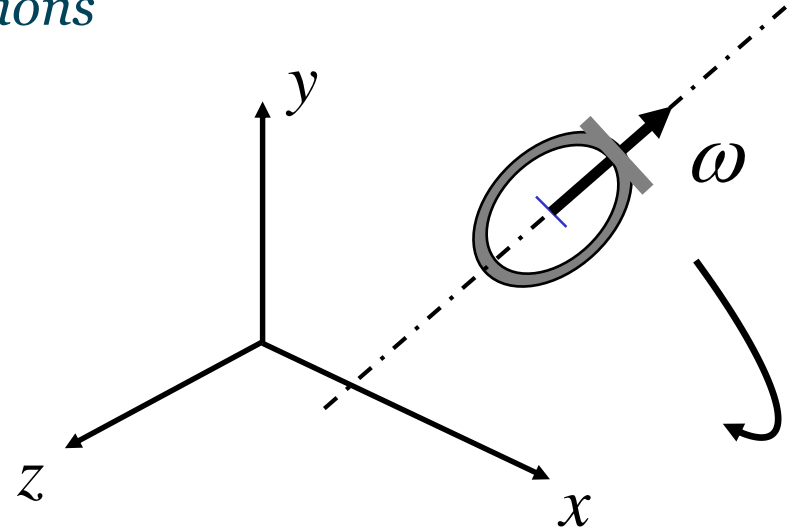
No torque, $\sum \mathbf{T}_{ext} = 0 \Rightarrow$ Momentum \mathbf{H} is constant

Rotational Dynamics

Angular Momentum – *In three dimensions*

In three dimensions:

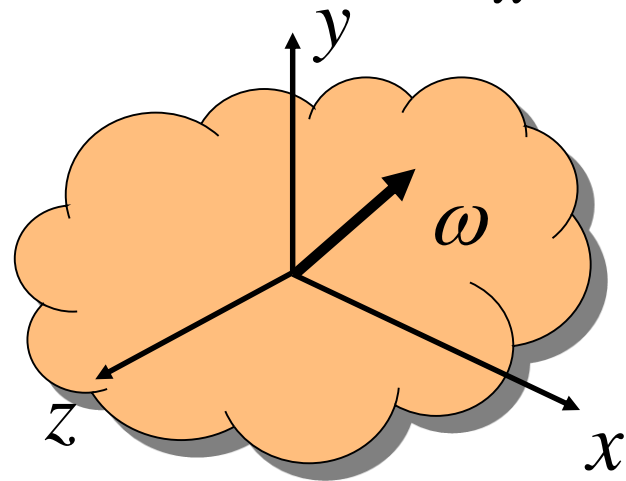
$$\boldsymbol{\omega} = \begin{pmatrix} \omega_x \\ \omega_y \\ \omega_z \end{pmatrix}$$



Angular momentum:

$$\mathbf{H} = \mathbf{I}\boldsymbol{\omega}$$

vector matrix vector

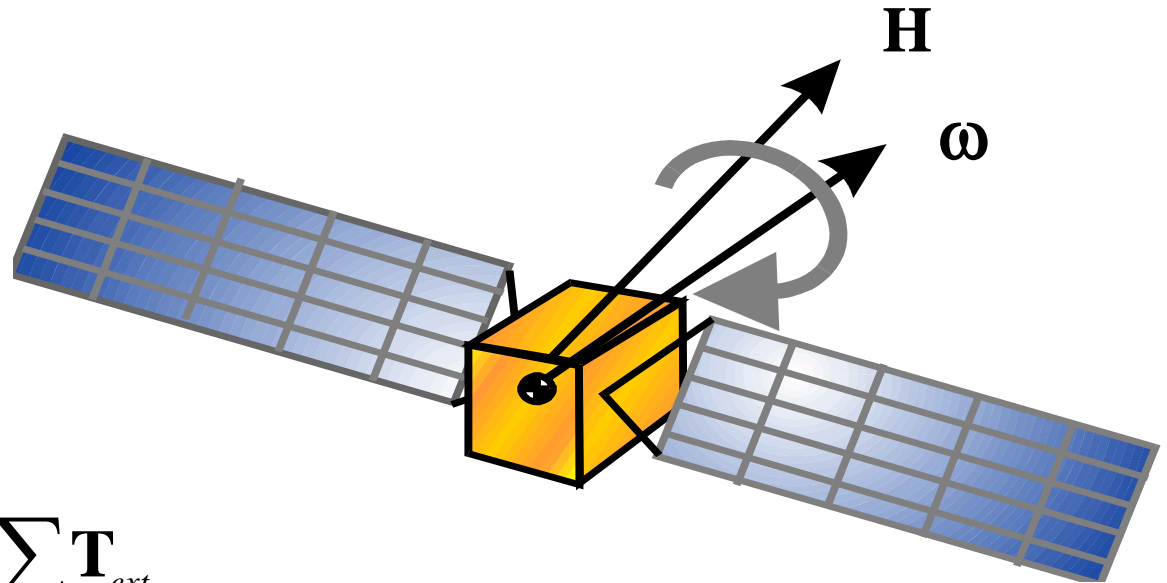


Rotational Dynamics

Angular Momentum – *in three dimensions*

$$\mathbf{H} = [\mathbf{I}] \boldsymbol{\omega}$$

\swarrow \downarrow \searrow
 vector matrix vector



Newton's second law:

$$\frac{d}{dt}(\mathbf{H}) = \frac{d}{dt}(\mathbf{I}\boldsymbol{\omega}) = \sum \mathbf{T}_{ext}$$

Free Motion:

- No torque, $\sum \mathbf{T}_{ext} = \mathbf{0} \Rightarrow$ Momentum \mathbf{H} is constant

Rotational Dynamics

Angular Momentum – *the inertia matrix*

Angular momentum of a rigid body such as the main structure of a Spacecraft is given by: $\mathbf{H} = [\mathbf{I}] \boldsymbol{\omega}$

Angular Velocity

Inertia Matrix referred
to Centre of Mass

$$[\mathbf{I}] = \begin{pmatrix} I_{xx} & -I_{xy} & -I_{xz} \\ -I_{xy} & I_{yy} & -I_{yz} \\ -I_{xz} & -I_{yz} & I_{zz} \end{pmatrix}$$

I_{xx}, I_{yy}, I_{zz} are Moments of Inertia

I_{xy}, I_{yz}, I_{zx} are Products of Inertia

Products of inertia are a measure of unbalance, and cause 'cross-coupling'

Rotational Dynamics

Angular Momentum

$$\mathbf{H} = [\mathbf{I}] \boldsymbol{\omega}$$

$$\mathbf{H} = \begin{pmatrix} I_{xx} & -I_{xy} & -I_{xz} \\ -I_{xy} & I_{yy} & -I_{yz} \\ -I_{xz} & -I_{yz} & I_{zz} \end{pmatrix} \begin{pmatrix} \omega_x \\ \omega_y \\ \omega_z \end{pmatrix}$$

So the components of the angular momentum vector are:

$$\mathbf{H} = \begin{pmatrix} (I_{xx} \omega_x - I_{xy} \omega_y - I_{xz} \omega_z) \\ (I_{yy} \omega_y - I_{yz} \omega_z - I_{xy} \omega_x) \\ (I_{zz} \omega_z - I_{xz} \omega_x - I_{yz} \omega_y) \end{pmatrix}$$

Rotational Dynamics

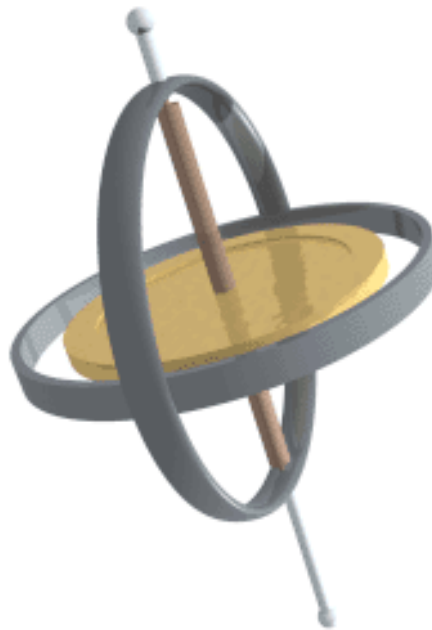
The Inertia Matrix



$[I]$ is an important quantity when sizing up the control system inputs for any vehicle.

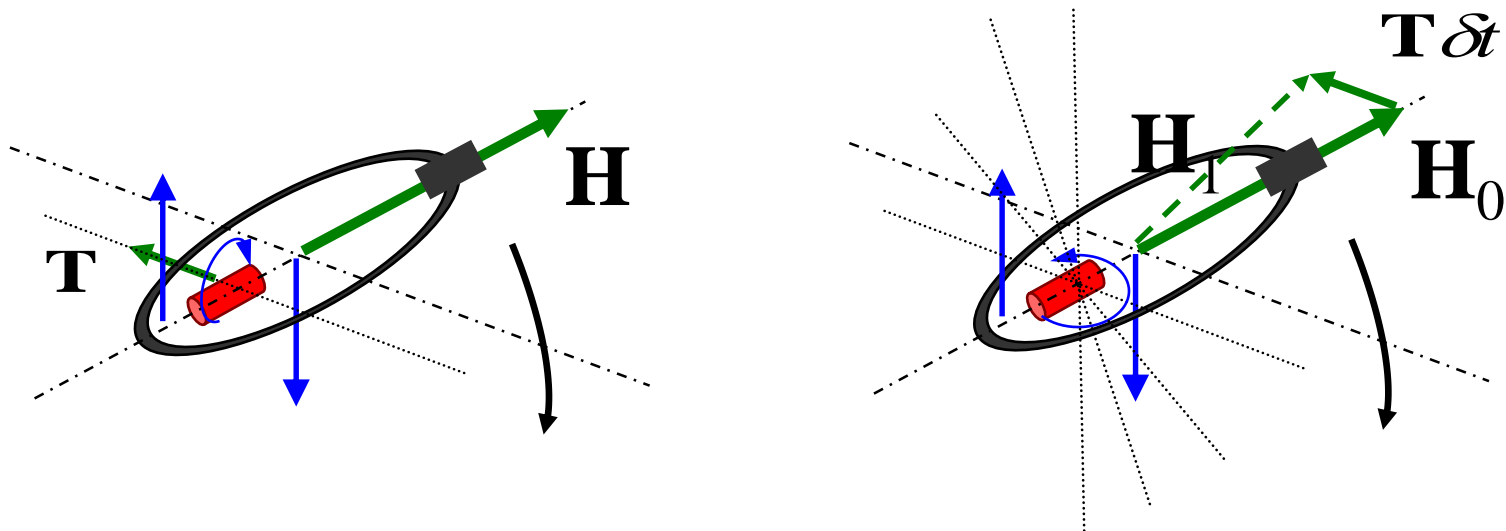
Rotational Dynamics

Rotational Motion – Gyroscopic precession



Rotational Dynamics

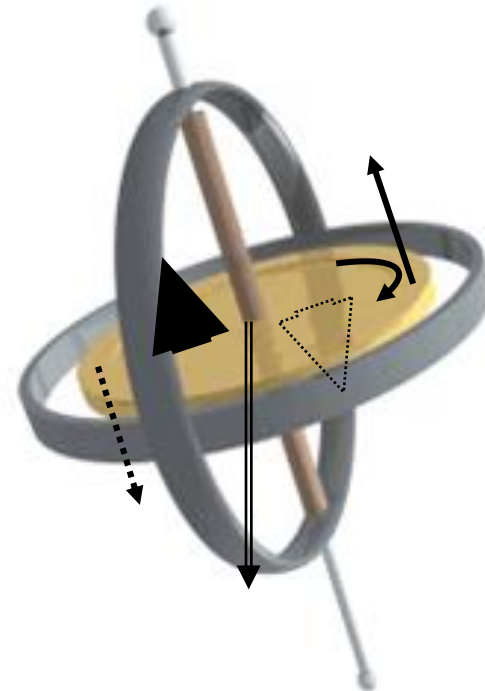
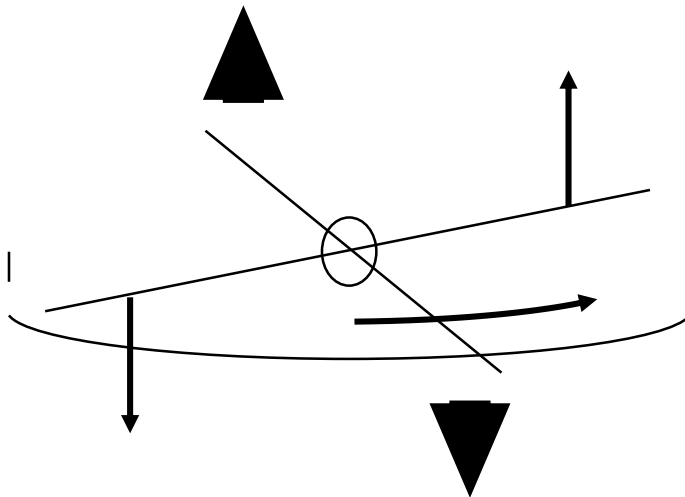
Rotational Motion – Gyroscopic precession



The rotational displacement occurs 90 degrees later in the direction of rotation.

Rotational Dynamics

Rotational Motion

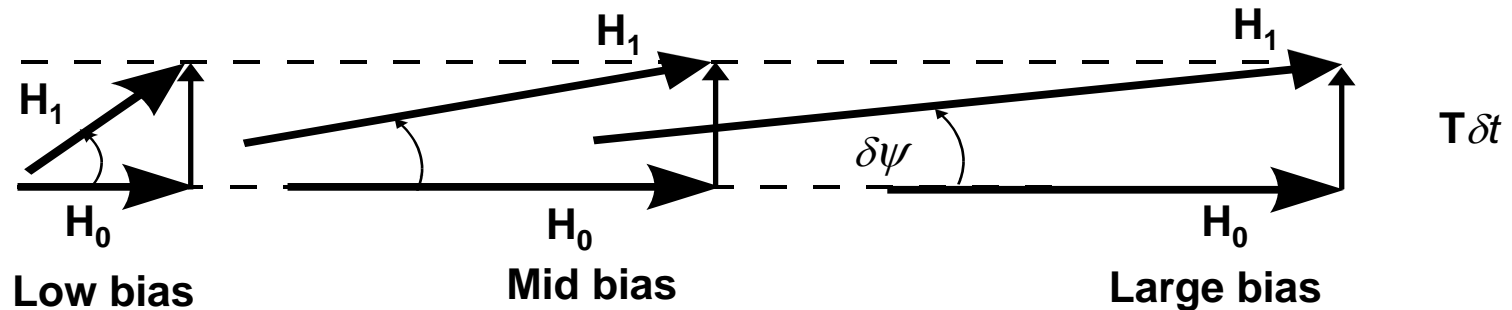


Rotational Dynamics

Rotational Motion – momentum bias

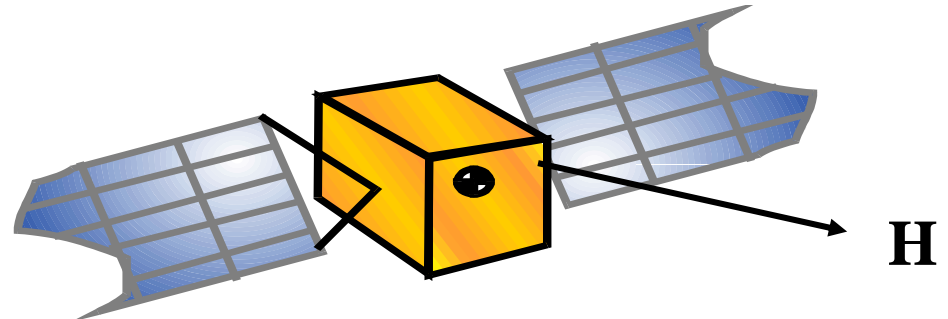
Momentum reduces sensitivity to torque – **gyroscopic rigidity**

During δt , the momentum changes direction $\delta\psi$ from \mathbf{H}_0 to \mathbf{H}_1



Momentum 'Management'

- The ACS must 'manage' the momentum **H** of the spacecraft, using control torquers to do so.



- This can be achieved using the principles of:

Conservation of momentum - using internal torquers to store/transfer momentum, Gimballing

$$(\sum \mathbf{T}_{\text{ext}} = \mathbf{0} \Rightarrow \text{Momentum } \mathbf{H} \text{ is constant})$$

Newton's second law - using external torquers to apply a torque to the satellite

$$(\sum \mathbf{T}_{\text{ext}} \neq \mathbf{0} \Rightarrow \text{Momentum } \mathbf{H} \text{ changes in magnitude/direction})$$

Momentum 'Management'

Notes:

1) Momentum build-up

External disturbance torques (e.g. aerodynamic disturbances, etc) will cause a progressive build-up of angular momentum

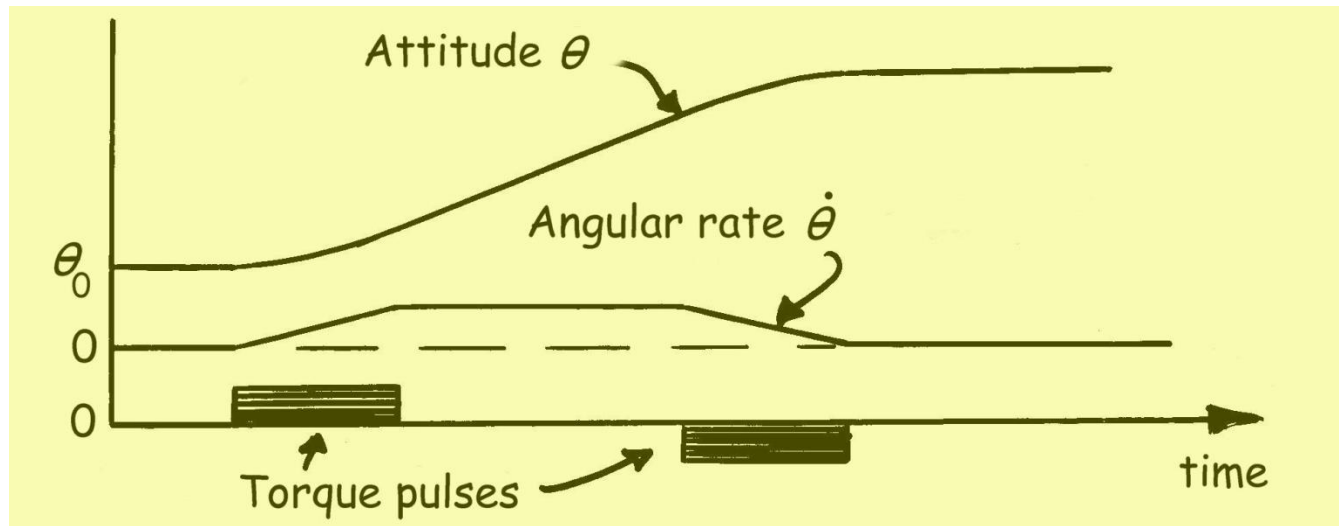
2) Only external torques affect the total angular momentum of the system... ... therefore spacecraft must carry external torquers (e.g. thrusters, magnetorquers, etc) if angular momentum is to be controlled.

Momentum Bias is a method commonly used to provide inherent stability.

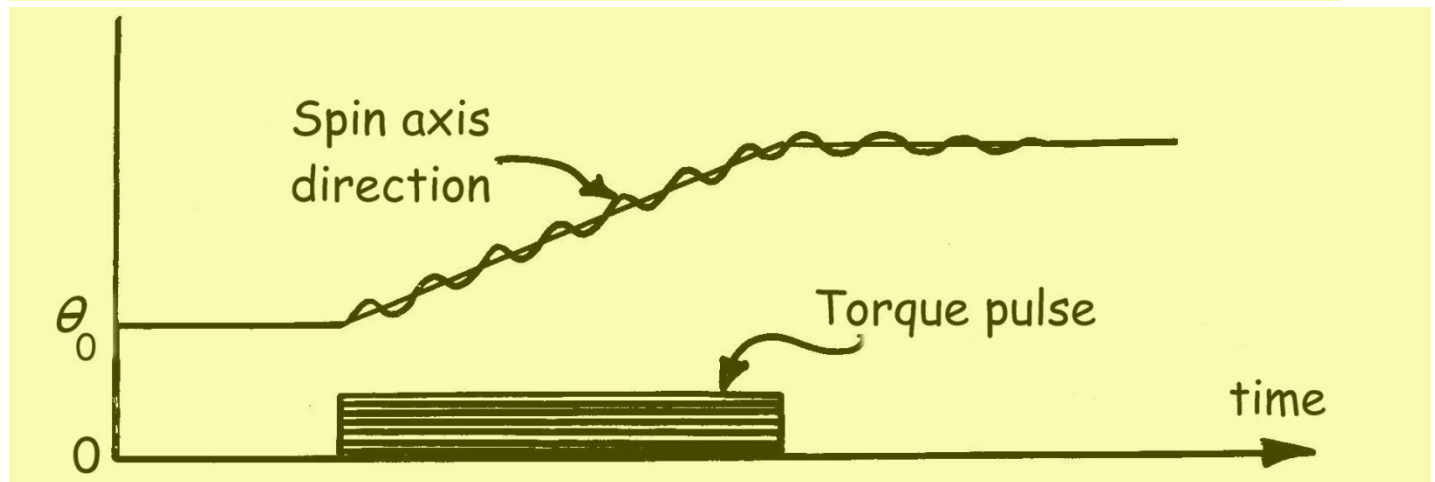
- But
- to use momentum bias, it is desirable that one body axis of the spacecraft remains invariantly pointing (usually perpendicular to the orbit plane)
 - bias also introduces an oscillatory **nutation mode**
 - a system with bias will have different torque responses

Momentum 'Management'

Torque response
without bias

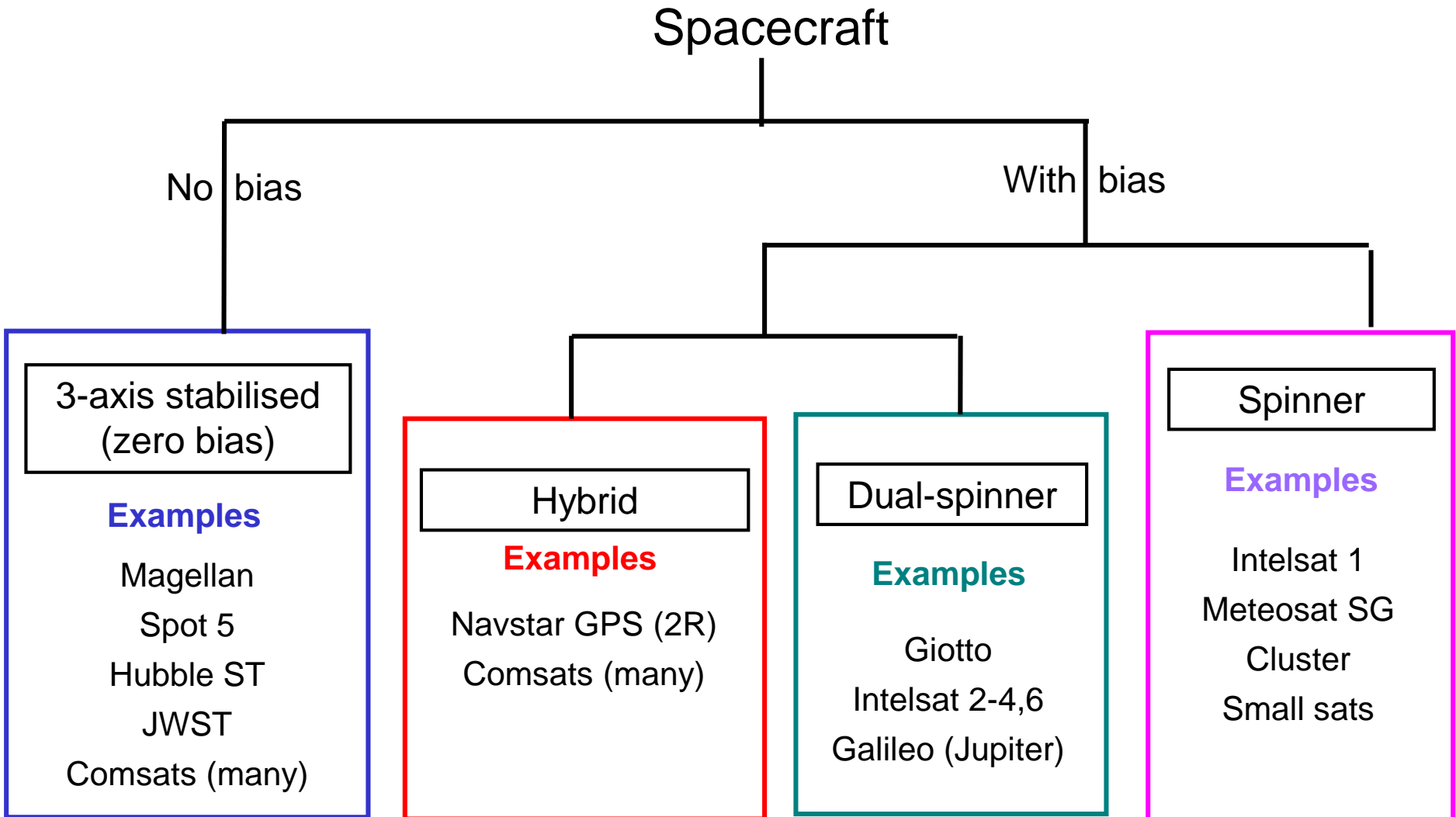


Torque response
with bias

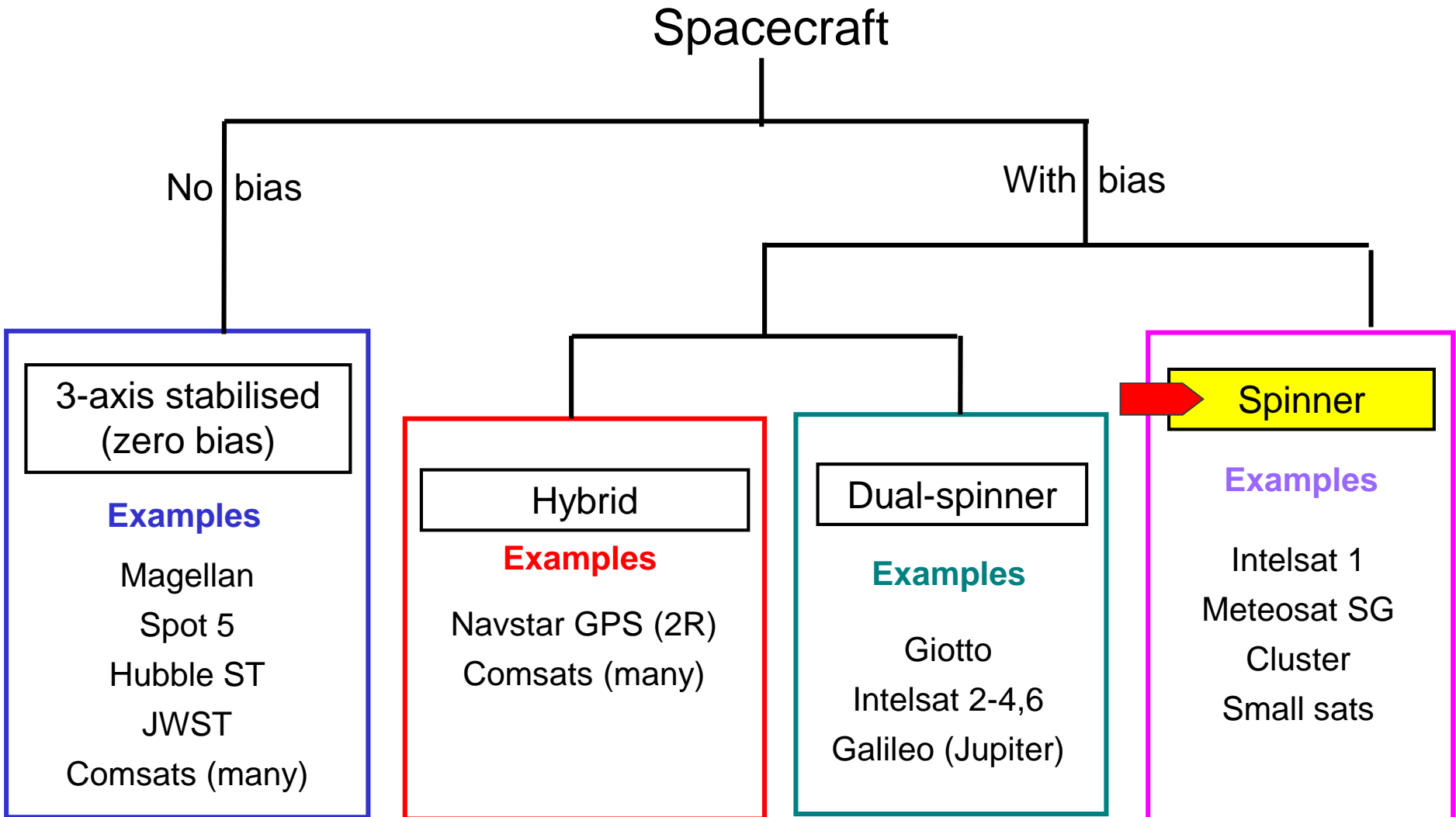


A constant torque can precess the bias direction at rate: $\dot{\theta} = T/H_0$, $H_0 = H_{bias}$

Spacecraft Categories



Spacecraft Categories



Spacecraft Categories – Spinner

Equation makers use of inertia matrix

Pure Spin Stabilisation

$$\mathbf{H} = [\mathbf{I}]\boldsymbol{\omega}$$

- whole spacecraft body spins at a rate of typically 10 to 60 rpm.

Major System Consequences

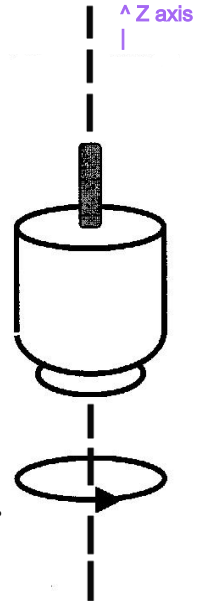
Becomes hard to balance these VVVV

- power
- thermal
- communications
- limited mounting space for non-scanning payloads!

Ideal inertia matrix:

$$\begin{bmatrix} I_{xx} & 0 & 0 \\ 0 & I_{xx} & 0 \\ 0 & 0 & I_{zz} \end{bmatrix}$$

I_z to be large,
0's to ensure long term stability.
 $I_{zz} > I_{xx}$
These conditions lead to
increased stability.



Choice of Spin Axis

The spin axis can only have a constant direction if it is a principal Axis.

For long-term stability it must be the axis of **maximum** inertia.

It may be the axis of **least** inertia for spin motion of limited duration.

Equal inertias about axes at right angles to the spin axis are needed for constant precession in response to a torque

Nutation

This is the weird shakey motion

Spinning introduces an oscillatory 'nutation' mode which must be damped out –

- passive dampers
- active damping via control torquers

Location of masses in structure becomes really important to maintain balanced inertial matrix, limiting what can be done structurally

Spacecraft Categories - Spinner

Examples

Cluster



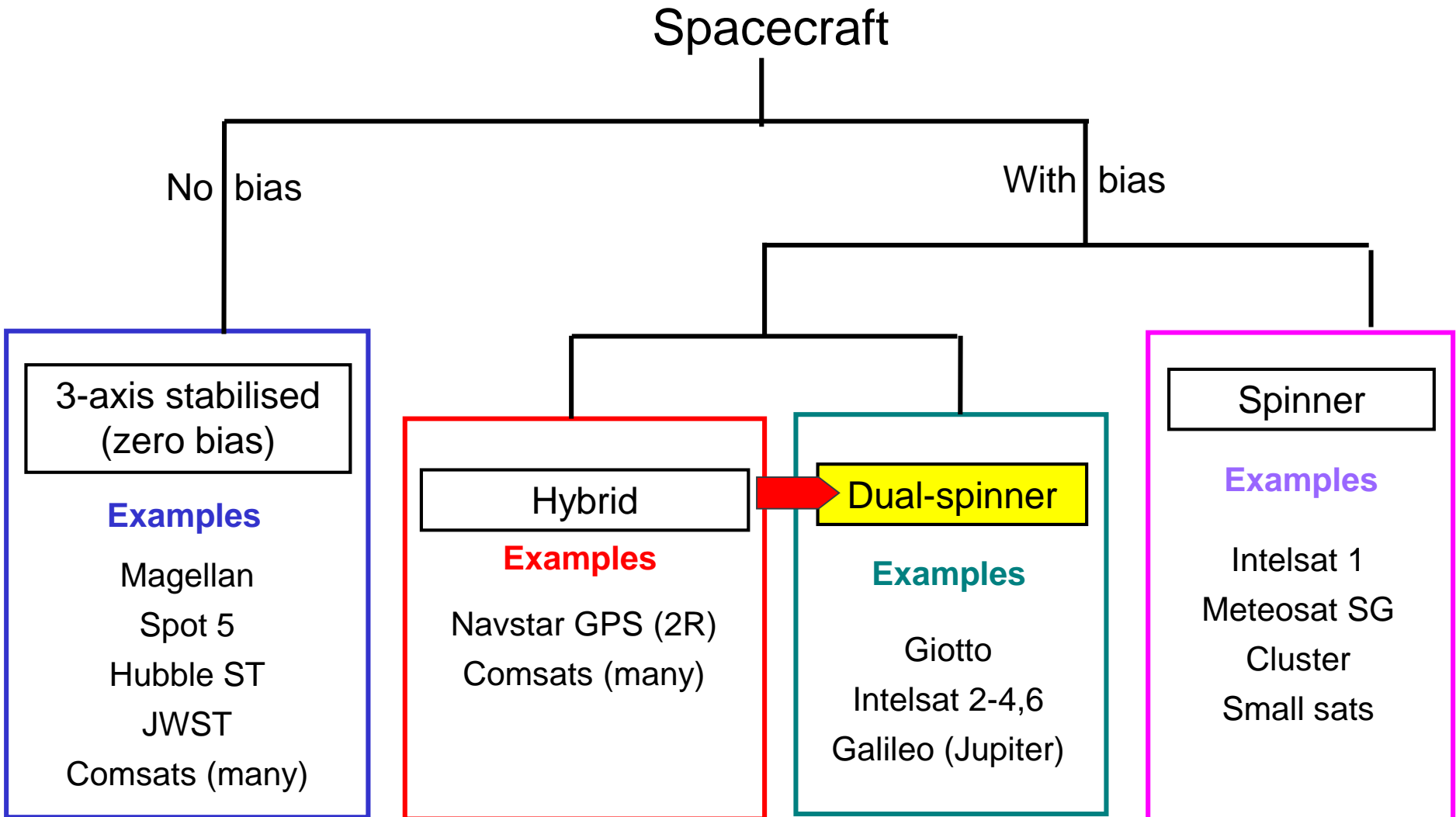
Astronautics - Chapter 6 - Attitude Control

Meteosat SG



Dr. H. M. Sykulski-Lawrence

Spacecraft Categories



Spacecraft Categories – Dual Spin

Part of the Structure Spinning

$$\mathbf{H} = [\mathbf{I}]\boldsymbol{\omega}$$

- Upper section is despun (for example Earth pointing). Lower section (contains subsystems) spins at a rate typically 10 to 60 rpm

Major System Consequences

Requires mechanical interface between different sections of the vehicle, which is annoying enough just for power and information, makes transfer of fluids very difficult too.

- power
- thermal
- communications
- limited mounting space
- transmission across bearing
- greater freedom of configuration

There are still constraints on the inertia matrix, which still apply to the non rotating part

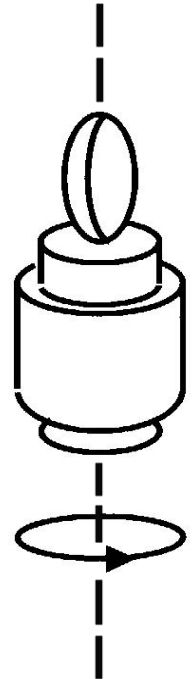
Can have directional stuff on non spinning part (still restricted in size to be small though)

Balance

The spinning part needs to have equal inertias about axes orthogonal to the spin axis

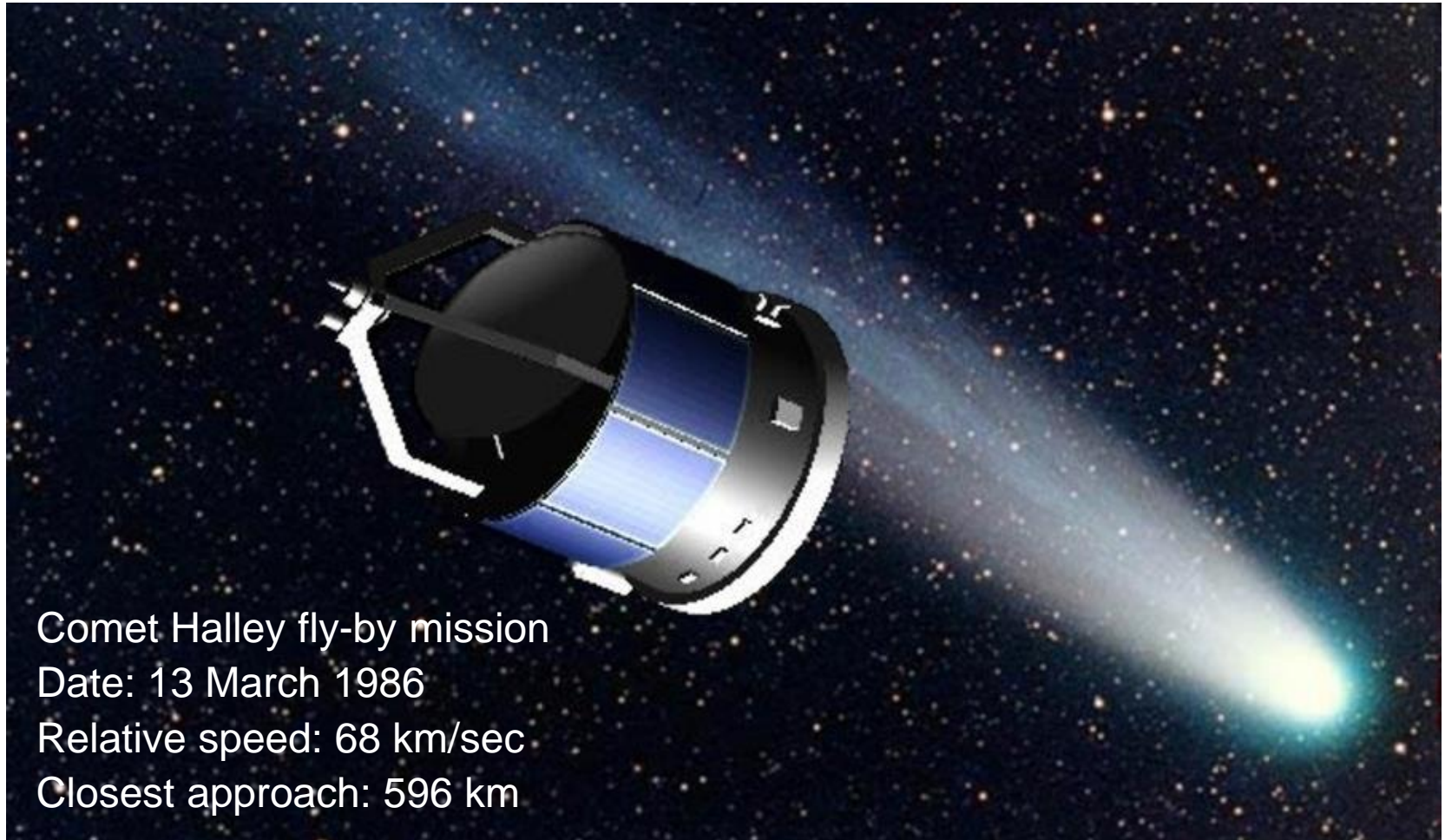
Nutation still occurs and must be damped by the ACS

Note that methods 1 and 2 have “large” I and “small” ω in the product $I \omega$



Spacecraft Categories – Dual Spin

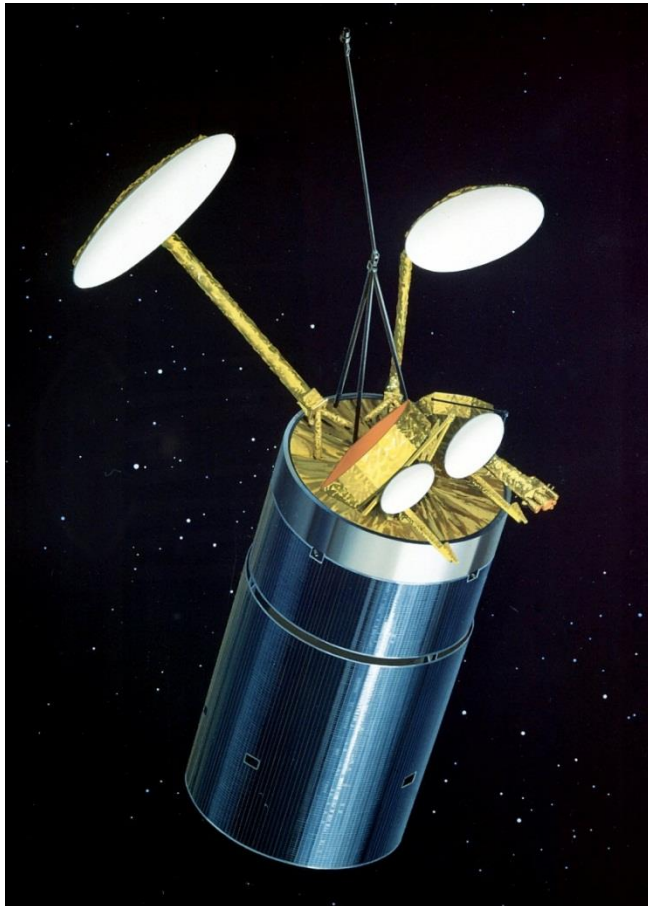
Examples: Giotto



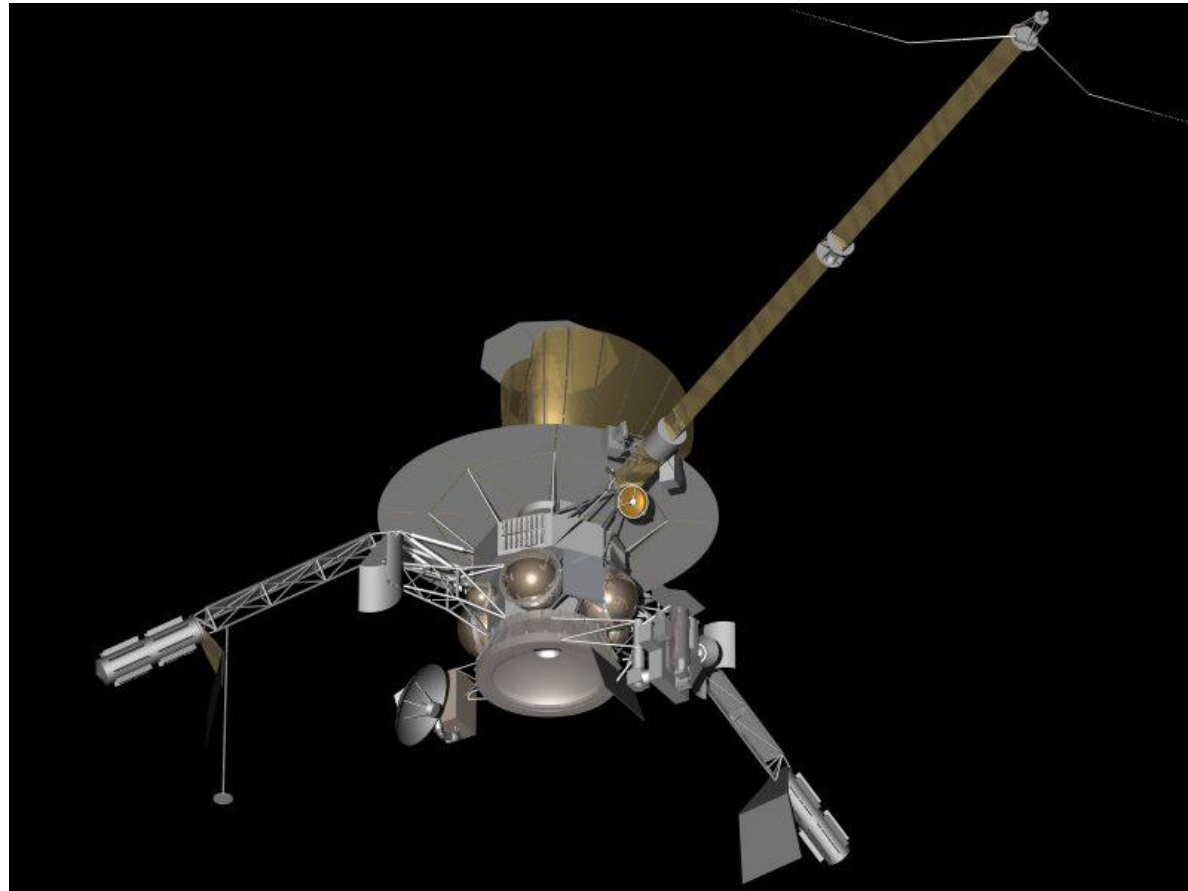
Spacecraft Categories – Dual Spin

Examples:

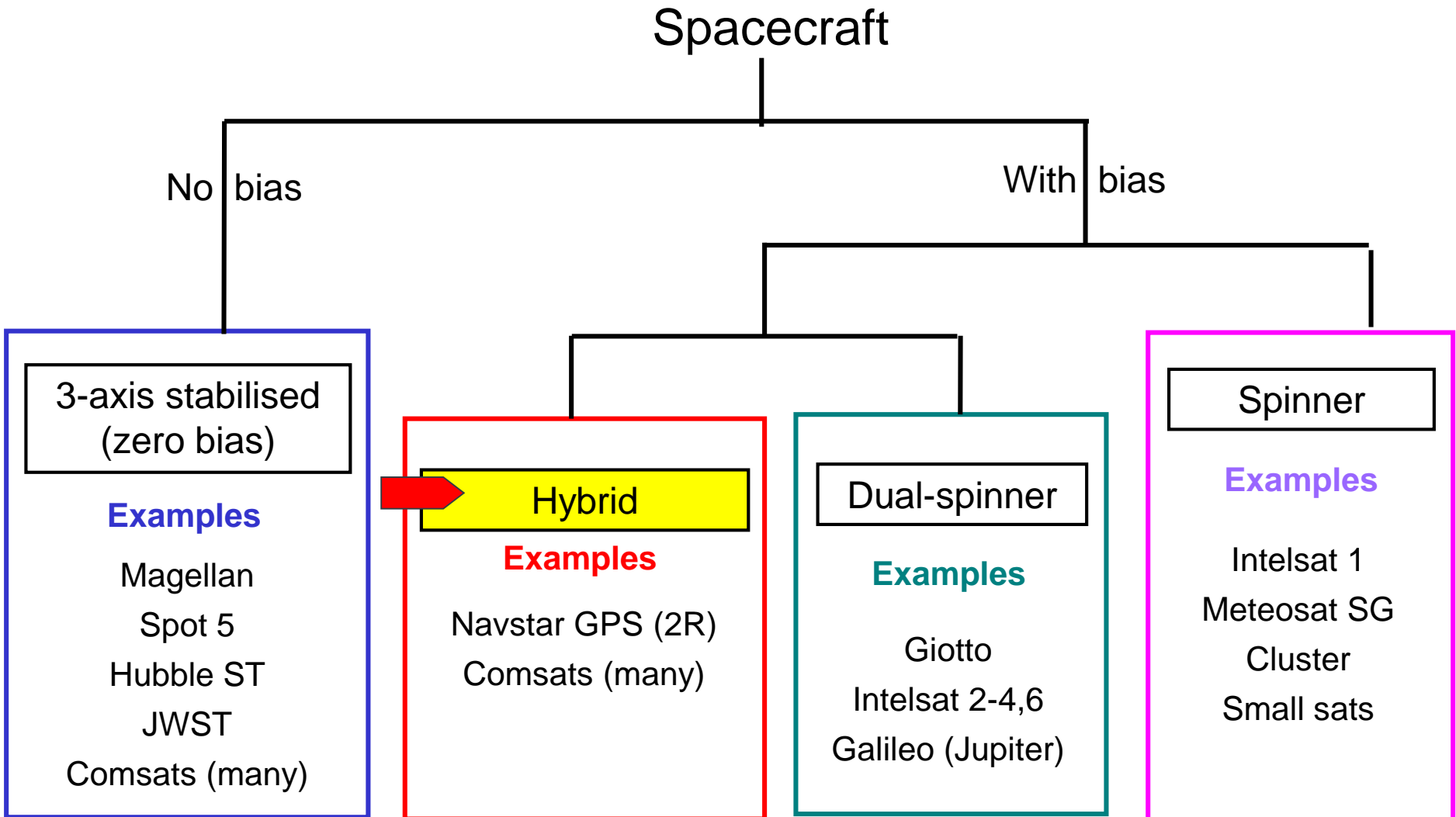
Intelsat 6



Galileo (Jupiter)



Spacecraft Categories



Spacecraft Categories - Hybrid

Bias using a momentum wheel

- A rapidly rotating wheel (a momentum wheel with a rotation rate of typically 6500 rpm) is installed within the spacecraft

Negative: Kinda waste of mass

Configuration

The freedom of the 3-axis stabilised spacecraft, but with the interior installation of a momentum wheel (or array of momentum wheels)

Nutation

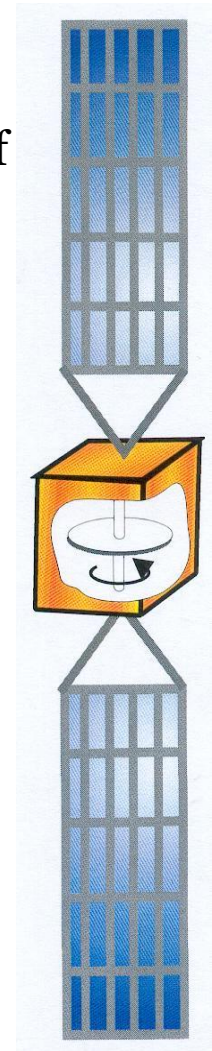
... still occurs and must be stabilised by the ACS

Hence still require dampeners

Momentum Storage

The wheel provides momentum storage for one component of momentum, accommodating fluctuations of about $\pm 10\%$ of the bias

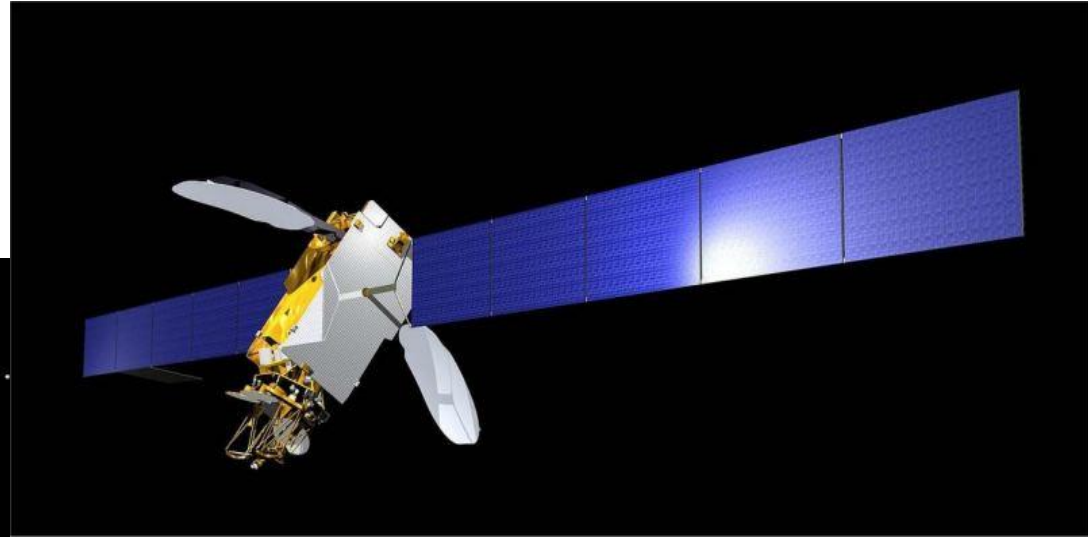
Gives cheap control capabilities (cheap as in they only require energy not fuel, atleast till they are saturated)



Spacecraft Categories - Hybrid

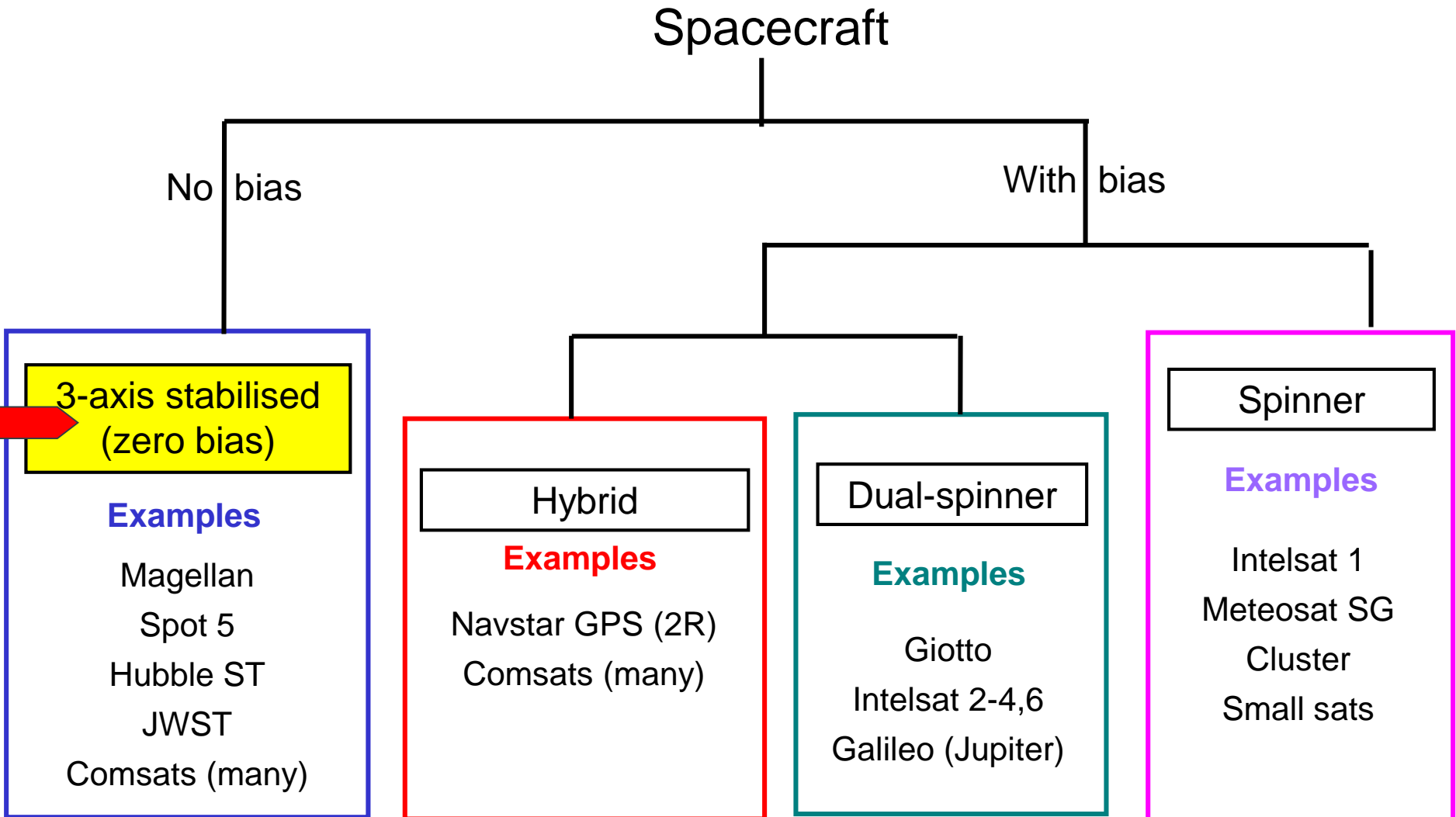
Examples:

Navstar GPS



Eurostar 3000

Spacecraft Categories



Spacecraft Categories – 3 axis

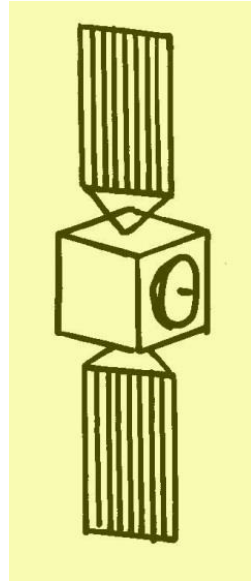
No momentum bias

- The spacecraft has no significant rotating components (and therefore has effectively zero angular momentum)

Used when full motion around all axes is required for the mission

Example:

Hubble Space Telescope

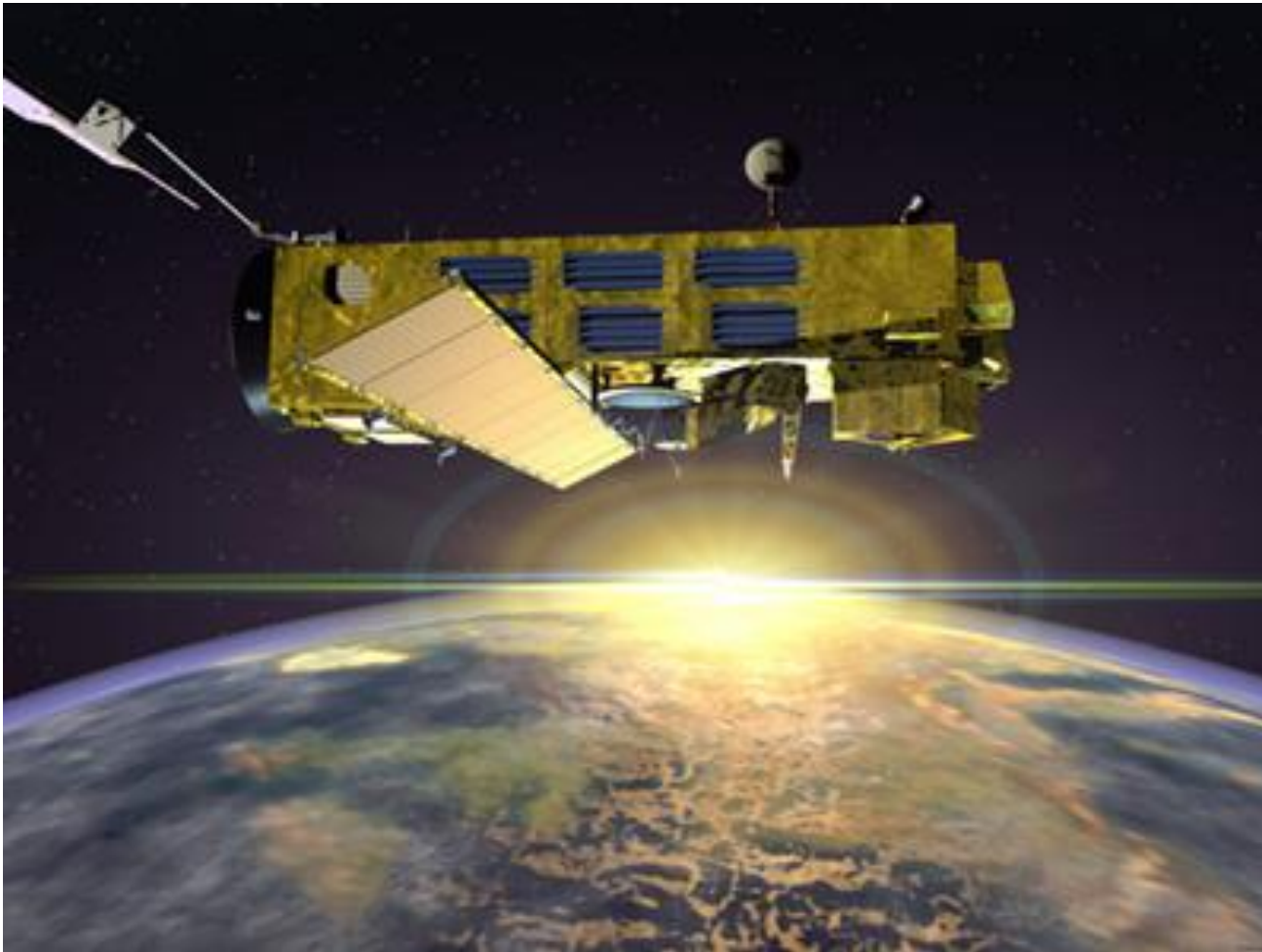


Much more freedom to change direction, because rotation just introduces stiffness in some axis.

Ideal for things like the hubble telescope

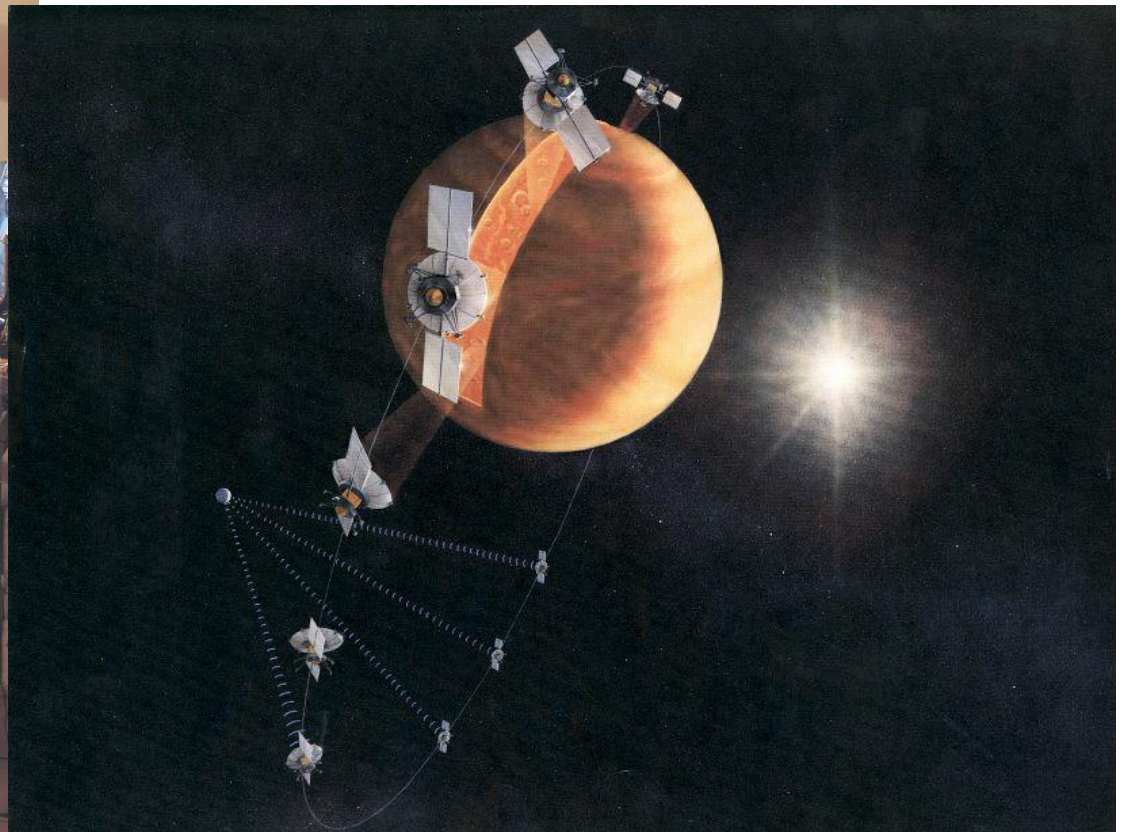
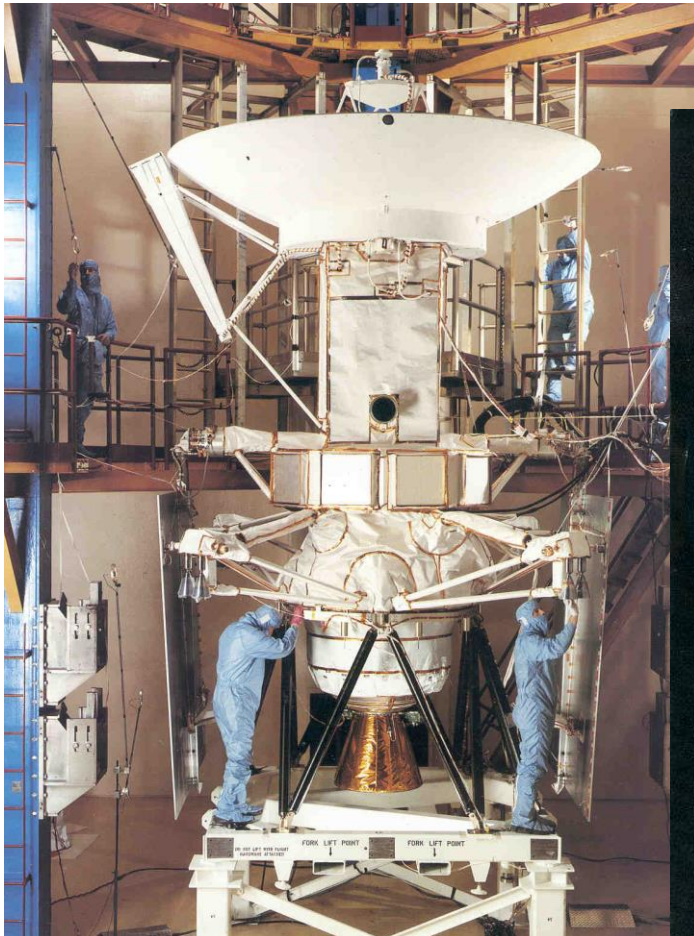
Spacecraft Categories – 3 axis

Example: Envisat 1



Spacecraft Categories – 3 axis

Example: Magellan VOIR mission (Venus Radar mapper)

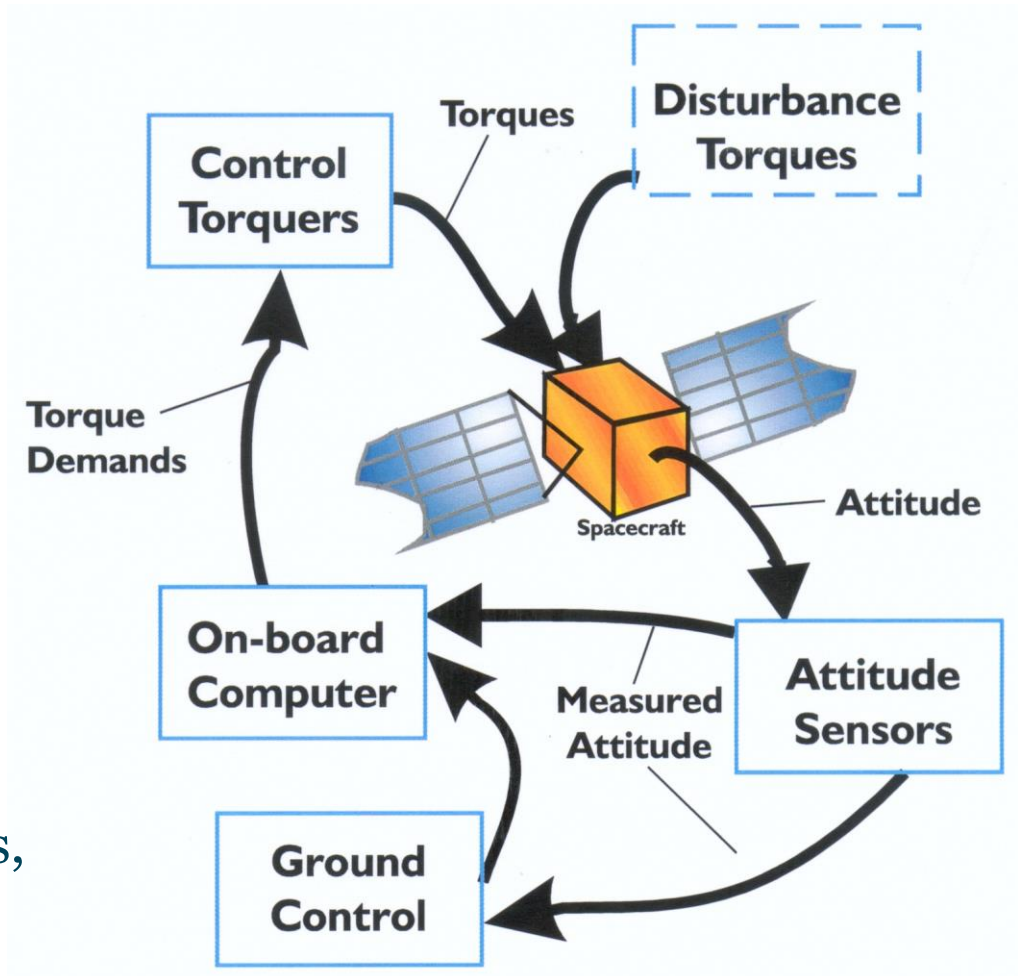


Attitude Control Introduction

Typical ACS operation showing flow of information:

Services required:

- power,
 - propulsion,
 - on-board data handling,
 - communications,
- etc.



Torques and Torquers

Categories of Torques:

External:

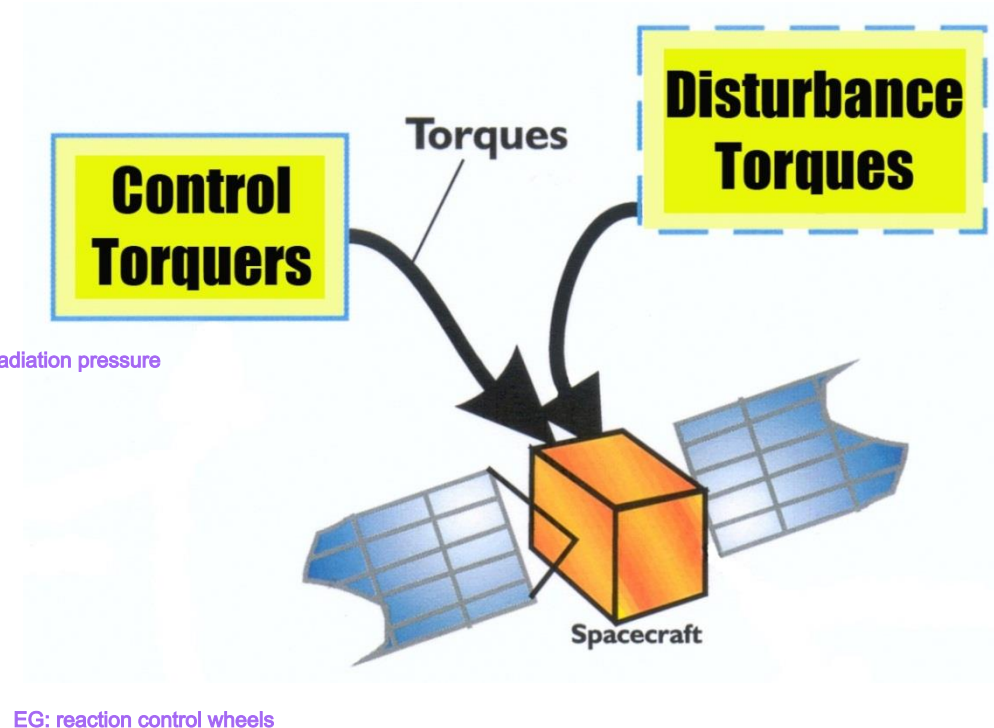
- Due to interactions with the environment

➔ **changes the overall angular momentum of the system**
EG: radiation pressure

Internal:

- Due to interactions between two parts of the spacecraft

➔ **overall angular momentum of the system is conserved**



Torques and Torquers

External torques and torquers

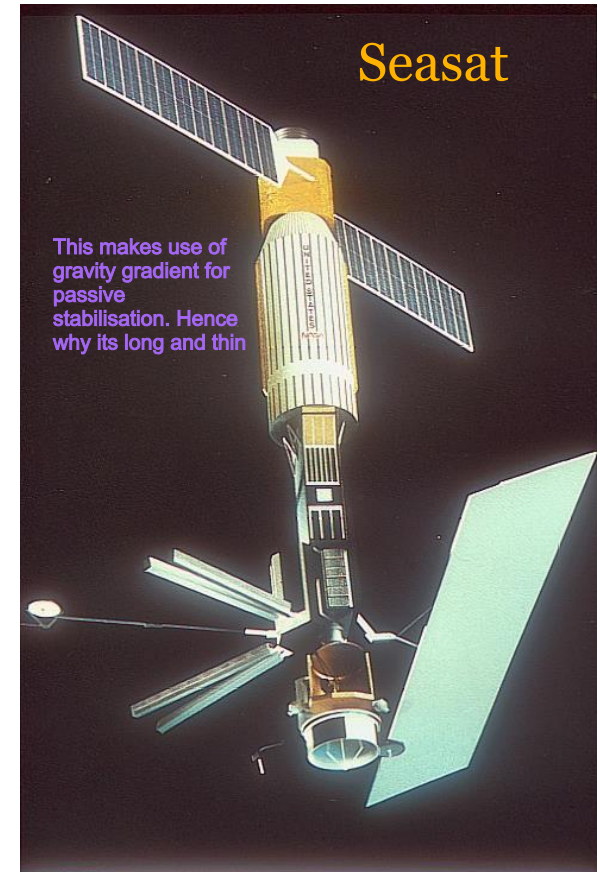
A. Naturally occurring (disturbance) torques

- Aerodynamic Effected by geometry, hence one reason why satellites in low orbits are symmetrical < 500 km
- Gravity gradient Effects are heavily dependent on inertia matrix
Think tidal lock but smaller scale Easy to see the shapes that can cause it with a simple diagram Can be used for passive stabilisation < 30,000 to 40,000 km
- Solar radiation Effect is really really small, but for long duration builds noticeably all heights
- Magnetic Interaction between planetary and local magnetic fields Can be used for stabilisation by purposefully using on board magnetic fields, often passive < 30,000 to 40,000 km
- Thrust misalignment all heights

This is just over/under burning as well as tiny misalignments. Due to the insane accuracy required to not have this it's basically inevitable.
EG: 1mm misalignment from 1kN burn, even that has a significant effect

Spin stabilisation is great for reducing thrust misalignment effects!

Note that: the altitude ranges given are very approximate



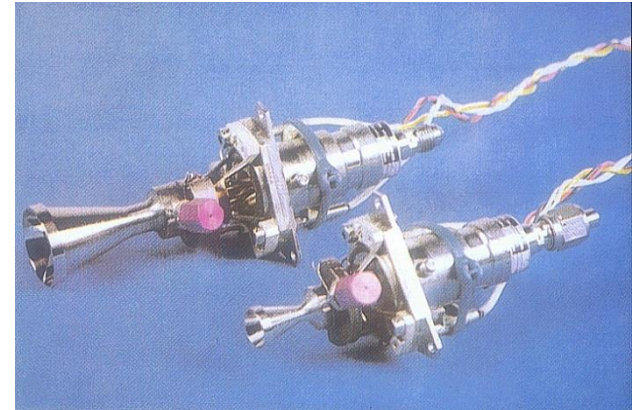
Torques and Torquers

External torques and torquers

B. Controllable external torquers

- Gas jets (thrusters)
 - Suitable for any torque size
 - ON-OFF control only
 - Require propellant

Finite so big L
Also tend to be quite complex plumbing wise so also L



– Magnetorquers

No rapid response, slow as. Better for long term attitude control.

- No torque about field line
- Require on-board magnetic field model
- require power (no propellant)

Also no moving parts

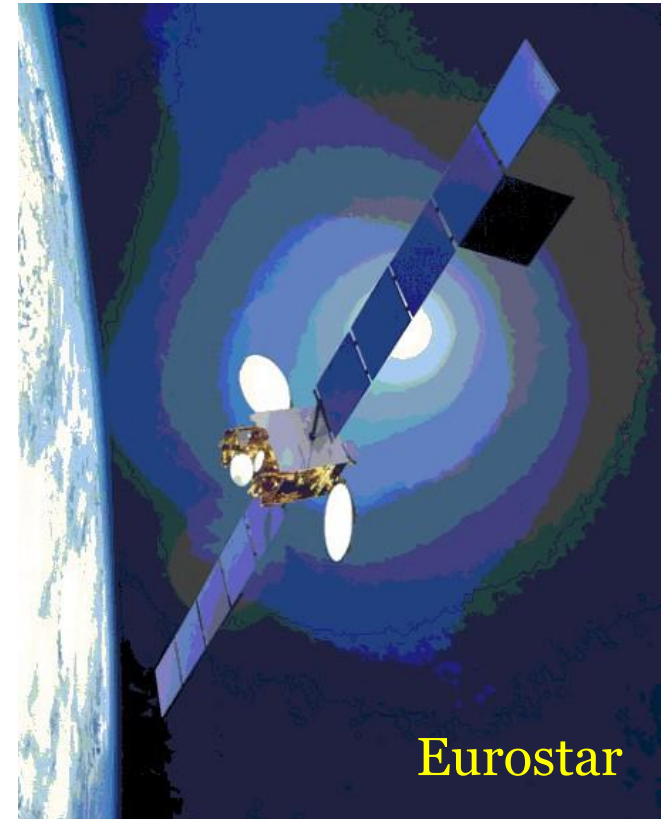


Torques and Torquers

External torques and torquers

- Adjustable spacecraft geometry (to utilise aerodynamic or solar radiation pressure torques)
 - Low torque capability (slow as)
 - No propellant required
Additional mechanical complexity

Note: A control torquer of type B is a necessity, to control the total spacecraft angular momentum



Torques and Torquers

Internal torques and torquers

- These do not affect the total angular momentum build-up of the spacecraft. They transfer momentum from one part of the spacecraft to another.

A. Internal disturbance torques

- Mechanisms (e.g. deployment of a solar array)
- Fuel movement (sometimes referred to as 'fuel slosh')
- Astronaut movement

Torques and Torquers

Internal torques and torquers

B. Controllable internal torquers

- Dual spin mechanisms
- Reaction wheels (commonly used for large ‘slew manoeuvres’)
- Momentum wheels (used to generate momentum bias)

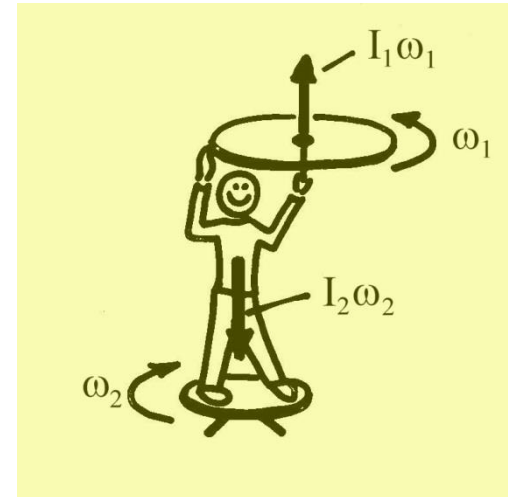


Torques and Torquers

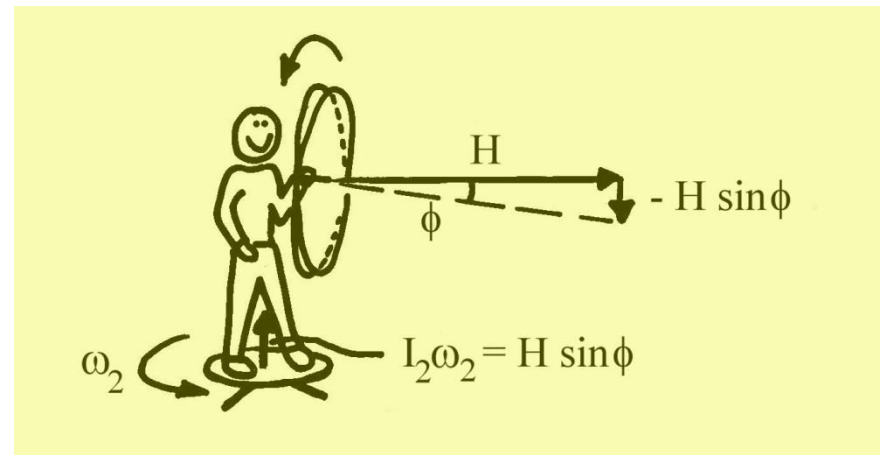
Demonstrations of internal torquers

- Reaction wheel demo

$$I_1 \omega_1 = I_2 \omega_2$$



- Gimballed momentum wheel demo (sometimes referred to as a 'control moment gyro')



Torques and Torquers

Use of momentum storage

These wheel devices store angular momentum, with their torque motor controlling the flow of momentum between the wheel and the spacecraft. Their function, if installed, is primary pointing control. The use of external torquers are required to prevent excessive build-up of angular momentum

Control of spacecraft pointing can be achieved avoiding the frequent use of external torquers (thrusters or magnetorquers) ...

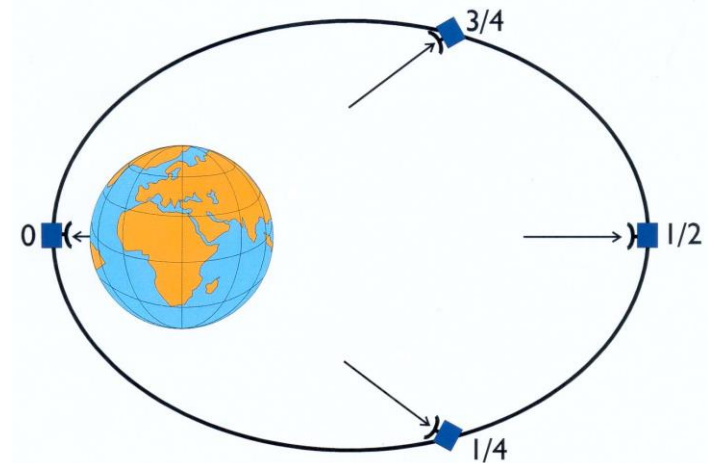
Torques and Torquers

Use of momentum storage

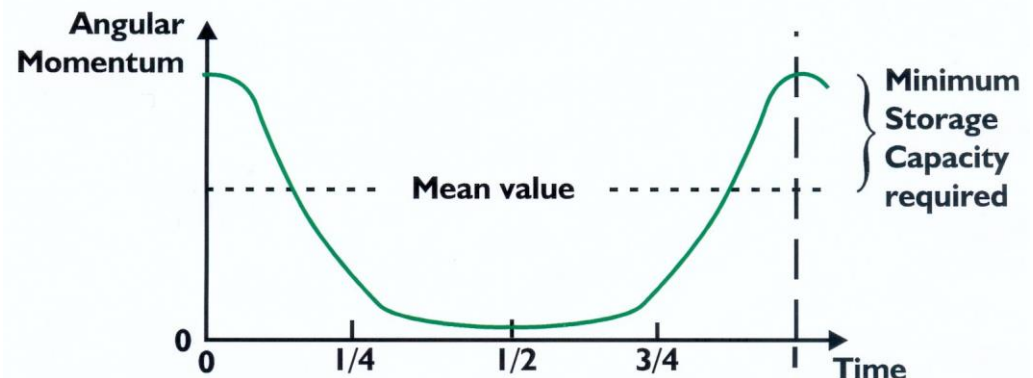
Momentum storage capacity can be chosen so as to avoid the use of external torquers (fuel) for controlling repointing and other events in which the 'before' and 'after' momenta are equal

(i.e. periodic variation in momentum)

Example: Earth-pointing from an elliptic orbit ...



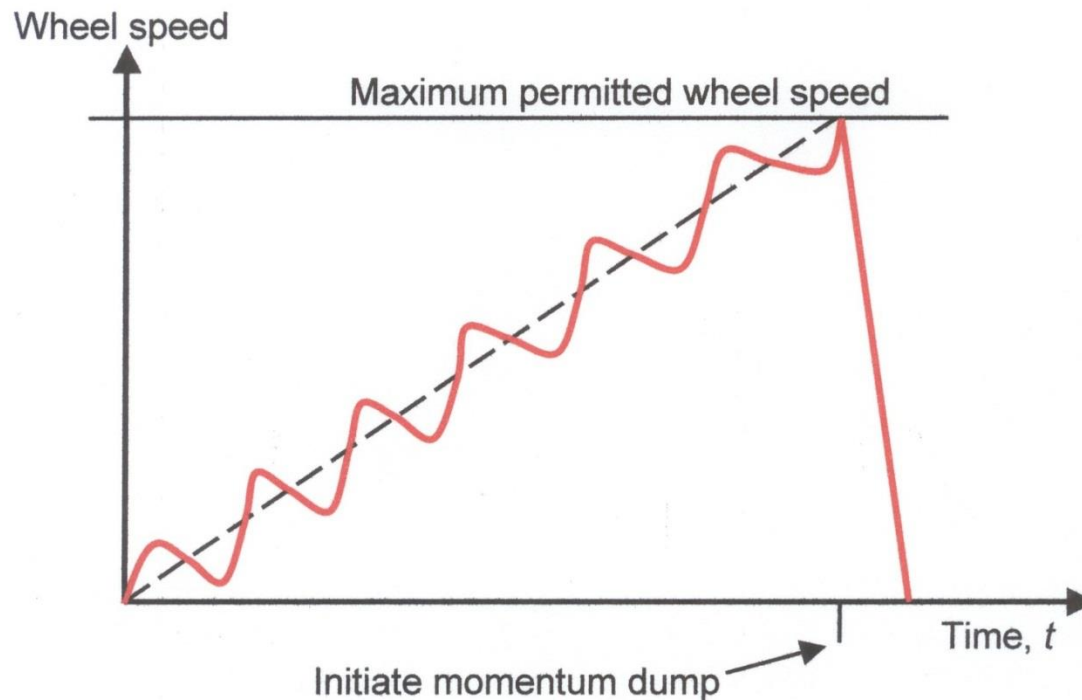
The local vertical's angular rate, and therefore the spacecraft's angular momentum, varies throughout one orbit



Torques and Torquers

Momentum dumping (or 'wheel desaturation')

Disturbance torques can cause the mean angular momentum of the system to increase. Pointing control then requires progressively higher wheel speeds



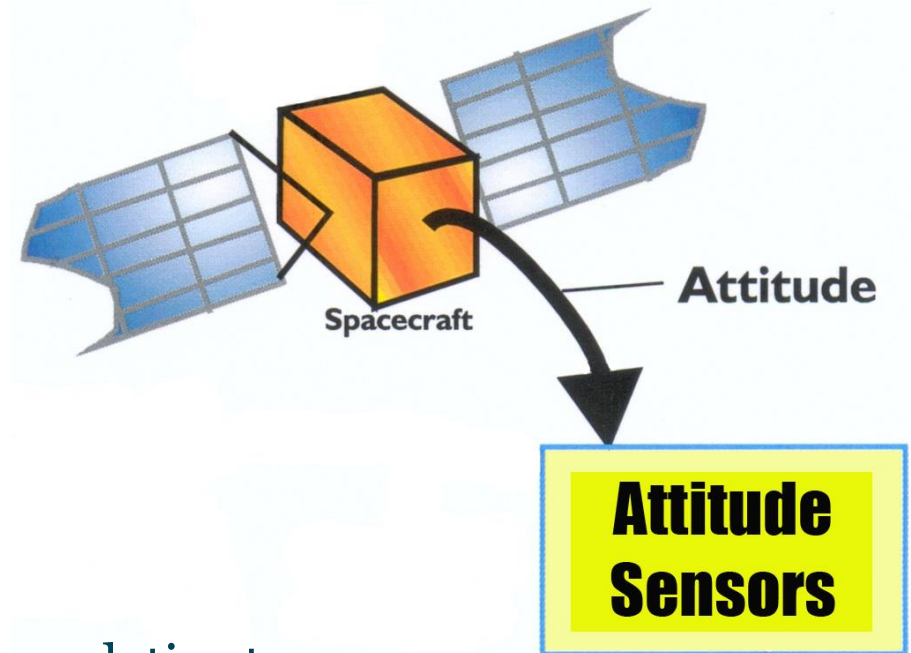
Initiate momentum dump once max wheel speed is attained:

- Torque wheel to slow it down
- While switching to external torquers for pointing control

Attitude sensors

Categories of sensors

Note that: Attitude control is less accurate than its measurement



Reference Sensors

... which give attitude information relative to a reference source (e.g. a star)

Inertial Sensors

... which measure changes in attitude

Attitude sensors

Categories of sensors

A. Reference sensors

- These give information about the vector direction from the spacecraft to a reference object, in the spacecraft body axes.
- Potential accuracy is limited by the characteristics of the reference object:

Potential Accuracies

Note that: the accuracies given are very approximate best performances

○ Stars	~ 1 arcsec
○ Sun	~ 1 arcmin
○ Earth (horizon)	~ 6 arcmin
○ Magnetometer	~ 30 arcmin
○ GPS	~ 6 arcmin*

*Depends on receiver baseline

Attitude sensors

Categories of sensors

B. Inertial sensors

- These are gyroscopic devices which give ‘change-of-attitude’ information only
- They need to be calibrated regularly using reference sensors (☆)
- They will continue to function whilst a reference object is eclipsed.

(☆) Note: Spacecraft must carry sensors of Type A

Attitude sensors

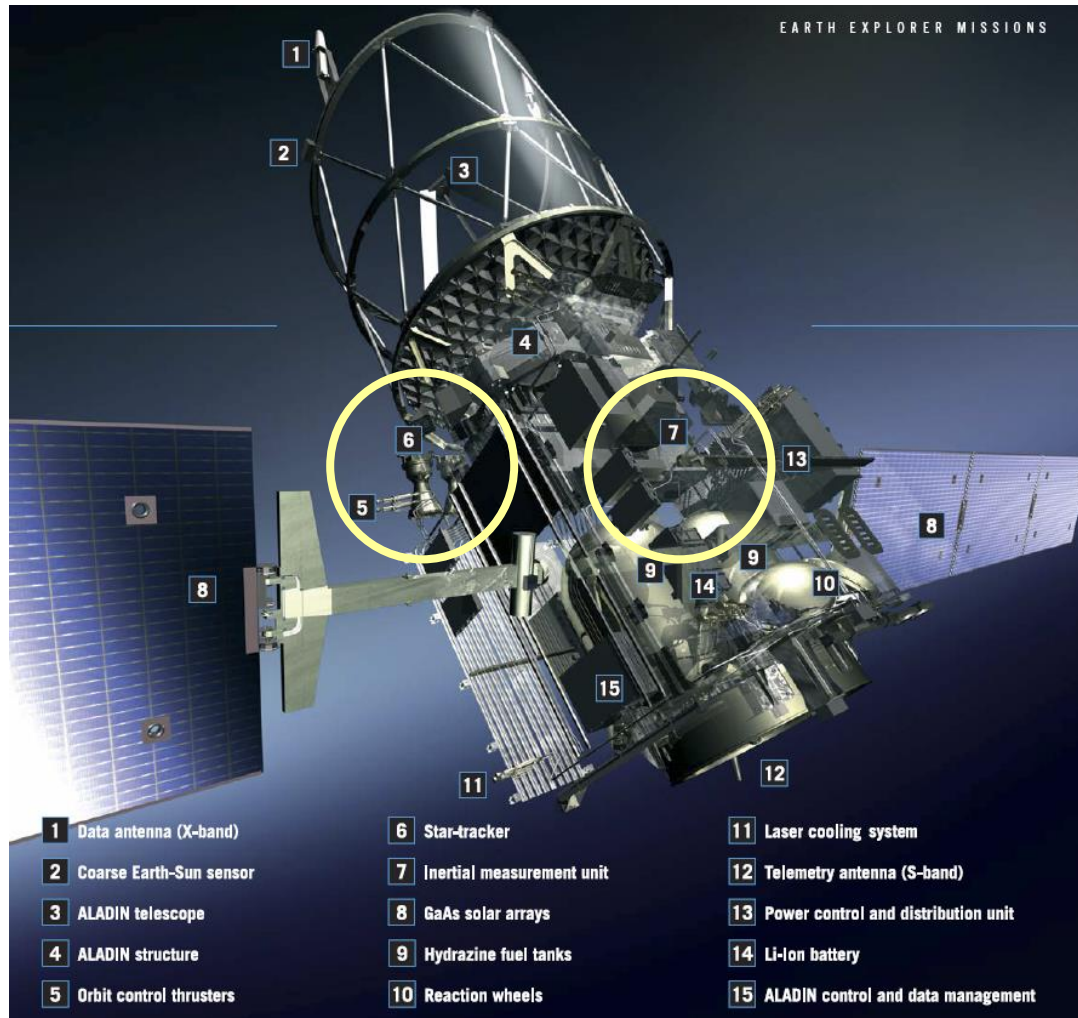
Example: Space shuttle attitude sensing system

- Gyros and star trackers.



Attitude sensors

Example: AEOLUS – Combination of star mapper and IMU



On-board Processing – closing the loop

On-board verses ground:

- The amount of autonomy given to the OBC varies considerably
- In general, modal control will be done by the OBC, with monitoring, resetting commands from Ground Control

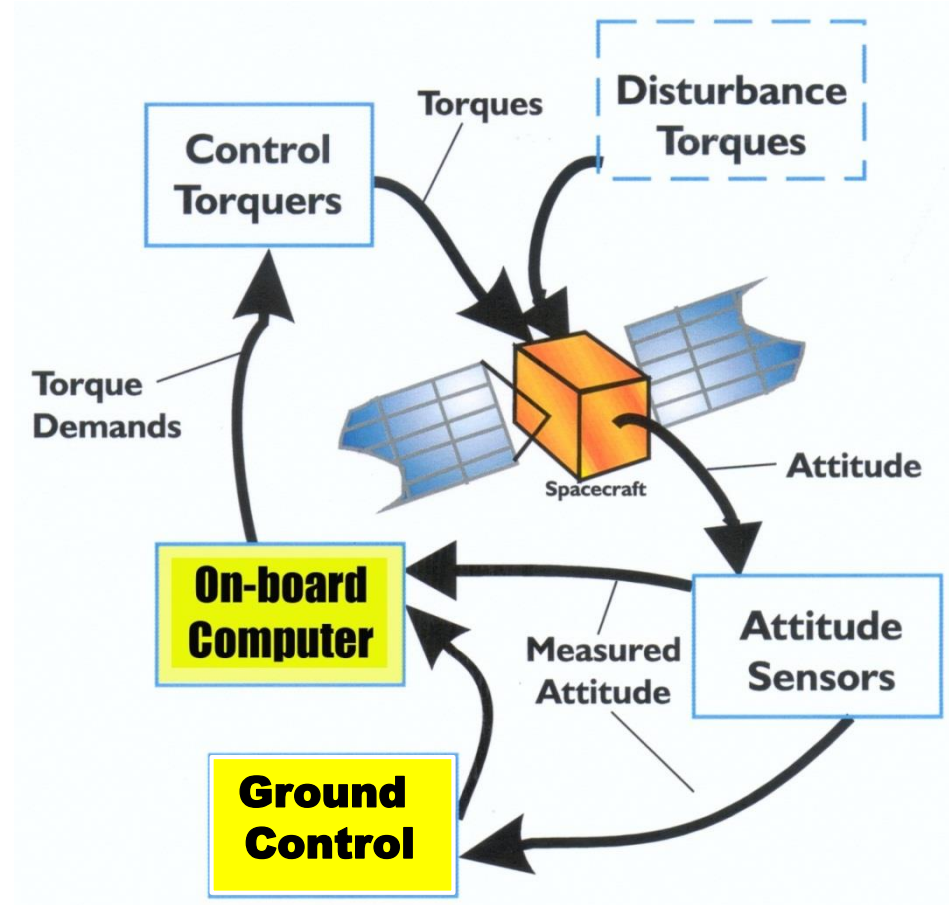
Operational modes:

Standby

Initial Acquisition Mode (IAM)/Safe Mode (SM)

Thruster Control Mode (TCM)

Normal Mode (NM)



Impact of ACS on the spacecraft system

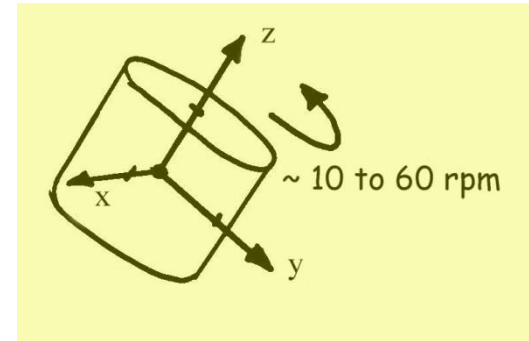
ACS has major interactions with other subsystems

- **Major system consequences for Type 1 (pure spinner) and Type 2 (dual-spinner)**
 - Power: Power limited.
 - Thermal: Spin distributes solar thermal input equitably. This decreases thermal design complexity, but placement of radiator surfaces can be problematic.
 - Communications: Antenna pointing problematic. This difficulty is eased in Type 2 configurations.
 - Payload accommodation: Limited physical space for non-scanning payloads
 - Transmission across electromechanical bearing: Type 2

Impact of ACS on the spacecraft system

- Mass distribution: The inertia matrix must take a particular form ...

$$[\mathbf{I}] = \begin{pmatrix} I_{xx} & 0 & 0 \\ 0 & I_{xx} & 0 \\ 0 & 0 & I_{zz} \end{pmatrix}, \quad (I_{xx} = I_{yy})$$




Further for long-term stability, we require $I_{zz} > I_{xx}$.

- Nutation: Spinning introduces this oscillatory mode. This must be damped out using
 - Passive dampers
 - Active damping via control torquers

Impact of ACS on the spacecraft system

- **Major system consequences for Type 3 (hybrid) and Type 4 (3-axis)**
 - Power: Deployed solar arrays may be used, providing greater power generation capability.
 - Thermal: Significant thermal gradients can occur, increasing complexity of thermal design.
 - Communications and payload accommodation: Greater flexibility than for Types 1 and 2.
 - Mass distribution and nutation: No major constraints, although Type 3 (hybrid) will exhibit nutation.

ACS Conclusions

- Attitude stabilisation type + diverse attitude pointing requirements
 Profound effect upon spacecraft configuration
- Mass distribution has an important effect on attitude motion
 - Stability
 - Response to control torques
- There are many workable alternative designs for an ACS

Chapter 6 Summary

Attitude Control Introduction



Rotational Dynamics



Momentum Management



Spacecraft Categories



Torques and Torquers

Attitude Sensors

On-board processing



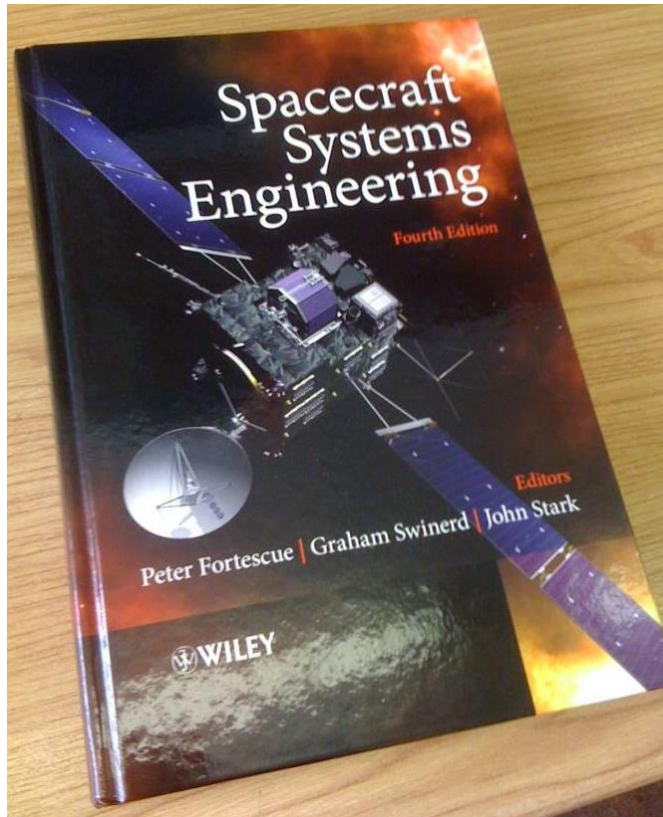
Impact of the ACS on the Spacecraft System



Key points:

- Purposes and requirements of the Attitude Control Subsystem
- ACS typical feedback control loop
- Basic principles of angular momentum
- The inertia matrix and its importance to vehicle response and design
- Gyroscopic precession and gyroscopic rigidity (momentum bias)
- How the overall momentum is managed for the spacecraft
- Key principles of momentum management, the use of momentum bias and how it affects the systems response to applied torques
- The four active types of spacecraft stabilisation
- The consequences of these types on the spacecraft design
- Categorisation of torques and torquers and examples of each
- The practical use of momentum storage leading to momentum dumping
- Categorisation of sensors used in the ACS subsystem
- Modes of operation
- Important impacts of the ACS subsystem on the design and operation of the spacecraft

Chapter 6 Summary



Read Chapter 9 of
Fortescue, Stark &
Swinerd