

## Parshvanath Charitable Trust's A P STATE INVESTMENT OF TEDERATION OF AMERICAN (Approved by AICTE New Delhi & Govt. of Maharashtra, Affiliated to University of Mumbai) (Religious Jain Minority)

# Bayesian Classification: Why?

- A statistical classifier: performs probabilistic prediction, i.e., predicts class membership probabilities
- Foundation: Based on Bayes' Theorem.
- <u>Performance:</u> A simple Bayesian classifier, <u>naïve</u> Bayesian classifier, has comparable performance with decision tree and selected neural network classifiers
- Incremental: Each training example can incrementally increase/decrease the probability that a hypothesis is correct — prior knowledge can be combined with observed data
- <u>Standard</u>: Even when Bayesian methods are computationally intractable, they can provide a standard of optimal decision making against which other methods can be measured

## **Bayesian Theorem: Basics**

- Let X be a data sample ("evidence"): class label is unknown
- Let H be a hypothesis that X belongs to class C
- Classification is to determine P(H|X), the probability that the hypothesis holds given the observed data sample X
- P(H) (prior probability), the initial probability
  - E.g., X will buy computer, regardless of age, income,
- P(X): probability that sample data is observed
- P(X|H) (posteriori probability), the probability of observing the sample X, given that the hypothesis holds
  - E.g., Given that X will buy computer, the prob. that X is 31..40, medium income.

(Religious Jain Minority)

## **Bayesian Theorem**

 Given training data X, posteriori probability of a hypothesis H, P(H|X), follows the Bayes theorem

$$P(H|\mathbf{X}) = \frac{P(\mathbf{X}|H)P(H)}{P(\mathbf{X})}$$

- Informally, this can be written as posteriori = likelihood x prior/evidence
- Predicts **X** belongs to  $C_2$  iff the probability  $P(C_i|\mathbf{X})$  is the highest among all the  $P(C_{\downarrow}|X)$  for all the k classes
- Practical difficulty: require initial knowledge of many probabilities, significant computational cost

## i owards <u>Naive</u> Bayesian Classifier

- Let D be a training set of tuples and their associated class labels, and each tuple is represented by an n-D attribute vector  $\mathbf{X} = (\mathbf{x}_1, \mathbf{x}_2, ..., \mathbf{x}_n)$
- Suppose there are m classes C<sub>1</sub>, C<sub>2</sub>, ..., C<sub>m</sub>.
- Classification is to derive the maximum posteriori, i.e., the maximal P(C<sub>i</sub>|X)
- This can be derived from Bayes' theorem

$$P(C_i|\mathbf{X}) = \frac{P(\mathbf{X}|C_i)P(C_i)}{P(\mathbf{X})}$$

Since P(X) is constant for all classes, only

$$P(C_i|\mathbf{X}) = P(\mathbf{X}|C_i)P(C_i)$$

needs to be maximized

#### Parshvanath Charitable Trust's

#### A. P. STINT INSTRUMED OF TECHNOLOGY

(Approved by AICTE New Delhi & Govt. of Maharashtra, Affiliated to University of Mumbai) (Religious Jain Minority)

## Naïve Bayesian Classifier: Training **Dataset**

Class:

C1:buys computer =

'yes'

C2:buys\_computer = 'no'

Data sample X = (age <= 30,Income = medium.Student = yesCredit rating = Fair)

age	income	student	redit_rating	_com
<=30	high	no	fair	no
<=30	high	no	excellent	no
3140	high	no	fair	yes
>40	medium	no	fair	yes
>40	low	yes	fair	yes
>40	low	yes	excellent	no
3140	low	yes	excellent	yes
<=30	medium	no	fair	no
<=30	low	yes	fair	yes
>40	medium	yes	fair	yes
<=30	medium	yes	excellent	yes
3140	medium	no	excellent	yes
3140	high	yes	fair	yes
>40	medium	no	excellent	no

## Naïve Bayesian Classifier: An **Example**

- P(C): P(buys\_computer = "yes") = 9/14 = 0.643 P(buys computer = "no") = 5/14 = 0.357
- Compute P(X|C) for each class

```
P(age = "<=30" | buys_computer = "yes") = 2/9 = 0.222
```

P(age = "<= 30" | buys\_computer = "no") = 3/5 = 0.6
P(income = "medium" | buys\_computer = "yes") = 4/9 = 0.444
P(income = "medium" | buys\_computer = "no") = 2/5 = 0.4

P(student = "yes" | buys\_computer = "yes) = 6/9 = 0.667P(student = "yes" | buys\_computer = "no") = 1/5 = 0.2

P(credit\_rating = "fair" | buys\_computer = "yes") = 6/9 = 0.667

P(credit\_rating = "fair" | buys\_computer = "no") = 2/5 = 0.4

X = (age <= 30, income = medium, student = yes, credit\_rating = fair)

 $P(X|C_i)$ : P(X|buys computer = "yes") = 0.222 x 0.444 x 0.667 x 0.667 = 0.044

 $P(X|buys computer = "no") = 0.6 \times 0.4 \times 0.2 \times 0.4 = 0.019$ 

P(X|C,)\*P(C,): P(X|buys\_computer = "yes") \* P(buys\_computer = "yes") = 0.028  $P(X|buys\_computer = "no") * P(buys\_computer = "no") = 0.007$ 

Therefore, X belongs to class ("buys computer = yes")



### Parshvanath Charitable Trust's A. P. SHAH INSIMMUMD OF MECHNOLOGY

(Approved by AICTE New Delhi & Govt. of Maharashtra, Affiliated to University of Mumbai) (Religious Jain Minority)

## Naive Bayesian Classifier: **Comments**

- Advantages
  - Easy to implement
  - Good results obtained in most of the cases
- Disadvantages
  - Assumption: class conditional independence, therefore loss of accuracy
  - Practically, dependencies exist among variables
    - E.g., hospitals: patients: Profile: age, family history, etc. Symptoms: fever, cough etc., Disease: lung cancer, diabetes, etc.
    - Dependencies among these cannot be modeled by Naïve Bayesian Classifier
- How to deal with these dependencies?

February Bayesian Belief Networks