

## Newton's Law of Motion

- 1) A body at rest will remain at rest and a body in motion will remain in motion unless it is acted upon by an external force
- 2) The net force acting on an object is equal to the mass of that object times its acceleration
- 3) Newton's third law of motion: For every action, there is an equal and opposite reaction.

~~Flight~~ → scals.

Quantum Mechanics: The branch of mechanics that deals with the mathematical description of the motion and interaction of subatomic particles, incorporating the concepts of quantization of energy, wave-particle duality, the uncertainty principle, and the correspondence principle.

Classical Mechanics: describes the motion of macroscopic objects, from projectiles to parts of machinery, and astronomical objects, such as spacecraft, planets, stars and galaxies. If the present state of an object is known it is possible to predict by the laws of classical mechanics how it will move in the future and how it has moved in the past.

The elements most used in semiconducting devices are silicon and germanium.

### Semiconductor

- ① B MOS (Bipolar Metal oxide semiconductor)
- ② P MOS (Positive - channel . )
- ③ N MOS
- ④ CMOS

### Semiconductor Devices

- ① Diodes
- ② Transistors.

### Course Outcomes

- 1) Understand the principle of semiconductor physics.  
models of semiconductor junction.  
Carrier transport in semiconductor  
Models of MOS transistors.

Atom  $\rightarrow$  It has a nucleus containing protons (+ve charge) and neutrons (no charge) and electrons revolve around it.

(2) Electrons are -ve charged particle

(3) charge of proton is  $1.602 \times 10^{-19}$

(4) charge of electron is  $-1.602 \times 10^{-19}$

(5) mass of electron is  $9.109 \times 10^{-31}$

Rutherford theory doesn't explain that if the electron is revolving fast around the nucleus, then it will gain some acceleration and radiate energy, due to which it will collapse into the nucleus, but it doesn't happen;

Then Bohr model gives the theory that electron does not take all energy level, it takes discrete energy and remains stationary i.e. it does not radiate energy.



Light also show dual nature

Newton  $\rightarrow$  is not able to explain the interface  
Huygens ~~theory~~ was suggested ~~theory~~ wave motion  
Thomas. ~~in~~  
Youngs. ~~youngs.~~

Planks

Albert Einstein's suggested that light  
is composed of tiny particles called photons

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Last century physicist discovered the sound  
and light waves. Sound waves need  
medium like air, water and matter, generally  
for its propagation, But the light waves  
on the other hand need no medium.

Thus in vacuum one can see and cannot  
hear.

The matter waves are proposed by  
de-Broglie.

de-Broglie suggested that these waves are  
generated due to the motion of any body like  
a planet, a stone, a particle of dust or an  
electron.

human detectable range human eye ( $0.4$  to  $0.2$   
micron)  
and ear ( $20$ - $20$  kHz)

But we can't see or detect de Broglie waves. Hence  
nan  
c  
(~~matter~~ waves)

Therefore, matter waves should be detectable by an appropriate detector.

However to understand why they remain obscure, we should consider their wavelengths of the matter waves proposed by de-Broglie,

$$\lambda = \frac{h}{mv}$$

Let us consider three objects of different scale in mass and dimension.

(a) Planet (b) human body (c) electron.

to understand why matter waves are imperceptible (not certain)  $\frac{1}{10}$  to  $2 \times \frac{1}{10}$

(a) Planet  $m = 6 \times 10^{27}$   $v = 3 \times 10^6$  cm/sec

$$\lambda = \frac{h}{mv} = \frac{6.6 \times 10^{-27}}{6 \times 10^{27} \times 3 \times 10^6} = 36 \times 10^{-61} \text{ cm}$$

The value is extremely small ~~not~~

(b) human  $m = 50 \times 10^3$  gm, speed  $= 85$  cm/sec

$$\lambda = 1.38 \times 10^{-33} \text{ cm}$$

Even this is too small

(c) electron  $\cdot 10^{-27}$  gm acq.  $6.1 \times 10^7$  cm/sec.

This corresponds  $\lambda = 6 \times 10^{-7}$  cm. to wavelength of x-rays and is detectable with the principle of diffraction

Hence the presence of matter waves at the nano scale dimensioned particle is traceable and so the presence of ~~nan~~ nanoparticles could be analyzed in terms of de Broglie wavelength

- The detection of matter waves confirms the presence of moving particle say electrons which ultimately decodes the conductivity in nano devices.





## Rutherford's Theory of Atom

- The atom consists of a positively charged heavy nucleus surrounded by revolving negatively charged light particle called electrons.  
An ~~atom~~ Technically Atom is electrically neutral i.e. charge of all electron is equal to charge of protons.
- charge of protons is  $1.602 \times 10^{-19}$  coulombs.  
charge of electron is  $-1.602 \times 10^{-19}$  coulombs  
Mass of electron is  $9.109 \times 10^{-31}$  ~~coulombs~~ Kilogram

Bohr Model of Atom Bohr rejected the classical views on electron motion and introduced the concept of electron orbiting the nucleus the same way that the earth moves around the sun

- In 1913, Niels Bohr proposed a model for the hydrogen atom which retained the earlier nuclear model of Rutherford but made stipulation as to the behaviour of the electrons.

Following postulates are suggested

- ① Bohr postulated that in an atom, electron revolve in stable orbits without emitting radiant energy. Further, he stated that each atom can exist in certain stable states. Also each state has a definite total energy. These are stationary states of the atom.

[Planck's constant =  $6.626 \times 10^{-34}$  joule-seconds]

2. An The permissible orbits of an electron revolving round a nucleus are those for which the angular momentum of the electron is an integral multiple of  $h/2\pi$ , where  $h$  is the plank's constant.

$$m r_n v_n = n \left( \frac{h}{2\pi} \right)$$

$m$  and  $v_n$  are the mass and the velocity of the electron,  $r_n$  the radius of the orbit and  $n$  is the integer called the quantum number.

3. An atom radiates energy only when an electron jumps from stationary ~~orbit~~ orbit of energy  $E_i$  to a final orbit of energy  $E_f$  ( $E_i > E_f$ ). The frequency  $\nu$  of the radiation is given by

$$E_i - E_f = h\nu$$

$h$  is the plank's constant.

$$h = 6.626 \times 10^{-34}$$



## Important Equations

Radii of Bohr's stationary orbit

$$r_n = n^2 \left( \frac{h^2 \epsilon_0}{\pi m Z e^2} \right)$$

where  $n \rightarrow$  integer

$r_n \rightarrow$  radius of the  $n^{\text{th}}$  orbit

$h \rightarrow$  Planck's constant

$\epsilon_0 \rightarrow$  Electric constant

$m \rightarrow$  mass of electron.

hydrogen atom ( $Z=1$ )  $\rightarrow Z \rightarrow$  The Atomic no. of the atom.

$e \rightarrow$  Elementary charge.

• The velocity of Electron in Bohr's stationary orbit

$$v_n = \left( \frac{Z e^2}{2 h \epsilon_0} \right) \left( \frac{1}{n} \right)$$

• The Total Energy of Electron in Bohr's stationary orbit.

$$E_n = -\frac{m e^4}{8 \epsilon_0^2 h^2} \left( \frac{Z^2}{n^2} \right)$$

$$\text{or } E_n = -13.6 \left( \frac{Z^2}{n^2} \right) \text{ eV.}$$

-ve sign means the electron is bound to the nucleus.

Q1 Calculate the radii of the first, second and third permitted electron orbit in Bohr's hydrogen model.

$$r_n = \frac{60 h^2 n^2}{\pi m q^2} = \frac{(8.854 \times 10^{-12}) (6.62 \times 10^{-34})^2 n^2}{\pi (9.1 \times 10^{-31}) (1.6 \times 10^{-19})^2}$$

$$= 0.527 \times 10^{-10} n^2 \text{ m}$$

$$r_1 = 0.527 \times 10^{-10} \text{ m}$$

$$r_2 = 2.108 \times 10^{-10} \text{ m}$$

$$r_3 = 4.74 \times 10^{-10} \text{ m}$$

Q2 Let the charge ( $q$ ) of an electron is  $-1.6 \times 10^{-19} \text{ C}$  and mass  $= 9.1 \times 10^{-31} \text{ kg}$ .

$$v = 1 \times 10^5 \text{ m/s}$$

find momentum, K.E and wavelength

$$\lambda = \frac{h}{m v} = \frac{h}{p}$$

$$\boxed{K.E = \frac{1}{2} m v^2}$$

K.E

$$\boxed{p = m v} \rightarrow \text{momentum}$$

$$K.E = \frac{1}{2} m v^2 = \frac{1}{2} p^2$$

$$\boxed{K.E = \frac{1}{2} m v^2}$$

$$= \frac{1}{2} p^2$$

## Dual Nature of light and Matter

• It is well known that light exhibits the phenomenon of interference, diffraction, polarisation, photoelectric effect, Compton effect, and discrete emission and absorption.

• The phenomena of interference, diffraction and polarisation can only be explained on the basis of wave theory of light. This shows that light possesses wave nature.

• The phenomena of photoelectric effect, Compton effect, discrete emission are explained on the basis of quantum theory of light, according to which light possesses corpuscular (or particle) nature.

• Thus we can say that light possesses dual nature. In some experiments it behaves as waves while in other experiments it behaves as particles.

• According to de-Broglie a moving particle, whatever its nature, has wave properties associated with it. Broglie proposed that the wavelength  $\lambda$  associated with any moving particle of momentum  $p$  (mass  $m$  and velocity  $v$ ) is given by

$$\lambda = h/p = \frac{h}{mv}$$

Where  $h$  is Planck's constant.

$$h = 6.6 \times 10^{-34} \text{ J s}$$



## Nave particle Duality

As we know that as the size of the object is very small and mass is also very small like electron, photon or any other entity.

- When we do experiment to analyze the behaviour of these separate entity or object, we see that, it behave like particle as well as wave.. [As seen in young's double slit method]
- So we need both i.e particle like nature and wave like nature for the analysis of the particle
- Let us take the example of electron or photon for the particle like nature we need  $K.E$  and momentum to define its nature, and ~~wavelength is used to define~~ for wave like nature we need wavelength.

So, This relation b/w wave like nature and particle like nature is defined by the

de-Broglie Equation

$$\lambda = \frac{h}{p}$$

↳ plank's Constant  
momentum.

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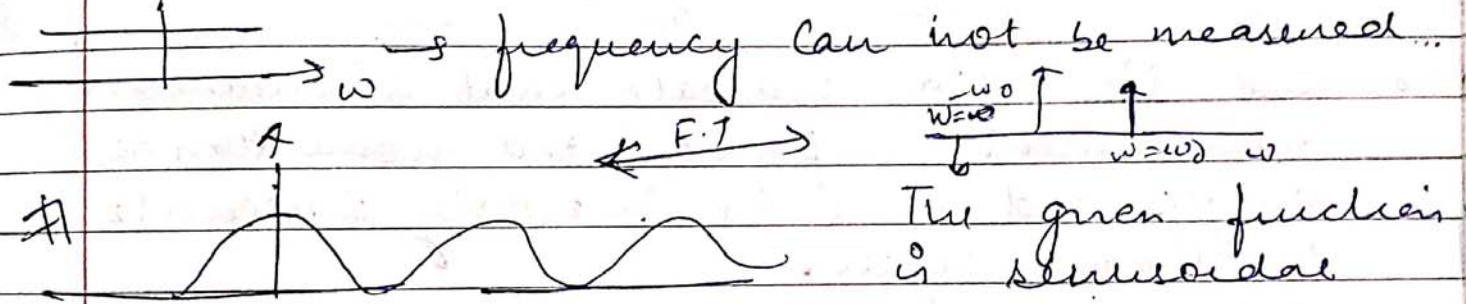
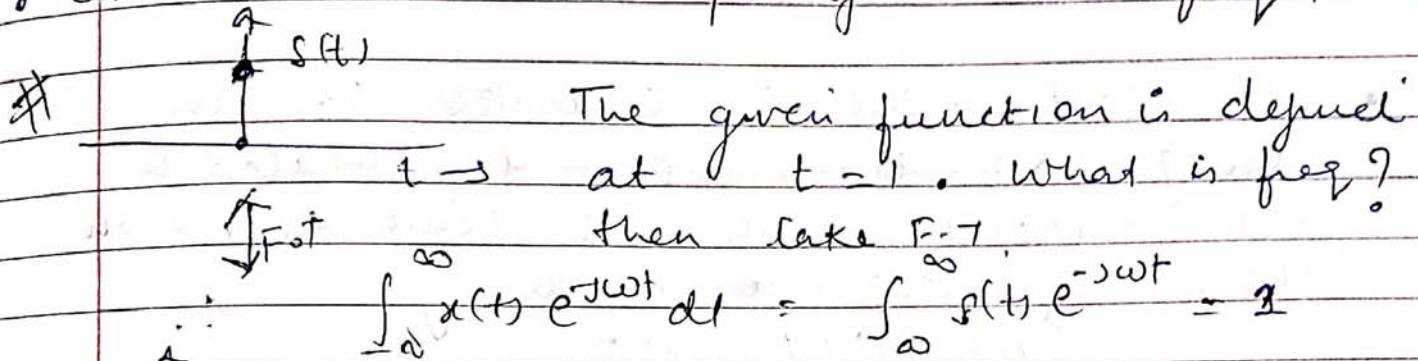


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# Heisenberg's Uncertainty Principle

- principle of quantum mechanics described by Heisenberg
- The position and momentum of a particle cannot be accurately measured at the same time.

• Let us consider an example of time and freq.



What is the position of this function in  $t$ , answer is available at all time, not exact position but it is defined in freq., one can identify its freq. or wavelength.

# From the above observation, we can say that any given function cannot be accurately measured at same time.

- So The magnitude of this inherent uncertainty is described by the Heisenberg uncertainty principle.

In general a signal in time/space  $\longleftrightarrow$  frequency with have this restriction



- Date / /
- In any measurement of the position and momentum of a particle, the uncertainties in the two measured quantities will be related by

$$(\Delta x)(\Delta p_x) \geq \frac{h}{4\pi}$$

- Similarly, the uncertainties in an energy measurement will be related to the uncertainty in the time at which the measurement was made by

$$(\Delta E)(\Delta t) \geq \frac{h}{4\pi}$$

- These limitations indicate that simultaneous measurement of position and momentum of energy and time are inherently inaccurate to some degree.
- One implication of the uncertainty principle is that we cannot properly define the position of an electron - i.e. we must define the "probability" of finding an electron at a certain position.
- Thus one of the important results of quantum mechanics is that a probability density function can be obtained for a particle in a certain environment, and this function can be used to find the expectation value of important quantities like position, momentum, and energy.



## Questions :

Q A ball of mass  $10\text{g}$  has velocity  $1.0\text{ m/s}$ . Calculate the wavelength associated with it. ~~very~~  
 given  $h = 6.62 \times 10^{-34}\text{ joule-sec}$

Soln

$$\lambda = \frac{h}{mv} = \frac{6.62 \times 10^{-34}\text{ joule-sec}}{(10 \times 10^{-3}\text{ kg})(1\text{ m/sec})}$$

$$= 6.62 \times 10^{-32}\text{ m}$$

Q Calculate the de-Broglie wavelength of neutron of energy  $28.8\text{ eV}$ , given

$$h = 6.62 \times 10^{-34}\text{ joule-sec}$$

$$m = 1.67 \times 10^{-27}\text{ kg}$$

$$\lambda = \frac{h}{mv} = \frac{h}{\sqrt{2mE}} = \frac{6.62 \times 10^{-34}}{\sqrt{2 \times 1.67 \times 10^{-27} \times 28.8 \times 1.6 \times 10^{-19}}}$$

$$28.8\text{ eV} = 28.8 \times 1.6 \times 10^{-19}\text{ joule}$$

$$= 4.2 \times 10^{-10}\text{ m} = 4.2\text{ \AA}$$

Q An electron has a speed  $1.05 \times 10^4\text{ m/s}$  with an accuracy of  $0.01\%$ . Calculate the uncertainty in the position of the electron.

$$\Delta p \Delta x = h$$

$$p = mv$$

$$\Delta v = 1.05 \times 10^4 \times \frac{0.01}{100}$$

$$= 1.05 \times 10^2 \times 0.01$$

$$= 1.05 \times 10^2 \times 10^{-5} = 1.05 \times 10^{-3}$$

$$\Delta p = m \Delta v = 9 \times 10^{-31} \times 1.05 \times 10^5$$

$$9.45 \times 10^{-31}$$

$$\Delta p \Delta x = \hbar \Rightarrow 13.5 \times 10^{-31} \Delta x = 1.05 \times 10^{-34}$$

$$\Delta x = \frac{1.05 \times 10^{-34}}{13.5}$$

$$9.45 \times 10^{-31}$$

$$= \frac{1.05}{13.5} \times 10^{-34}$$

$$= 0.77 \times 10^{-34}$$

$$0.111 \times 10^{-3}$$

~~Answer~~

$\Delta x$

=

$$1.05 \times 10^{-34} \times 100$$

$$9 \times 10^{-31} \times \frac{1.05 \times 10^4 \times 0.01}{100}$$

$$= \frac{1.05 \times 10^{-32}}{9 \times 10^{-31} \times 1.05 \times 10^4 \times 0.01}$$

$$= \frac{10^{-32}}{9 \times 10^{-27}} = 11.11 \times 10^{-5}$$

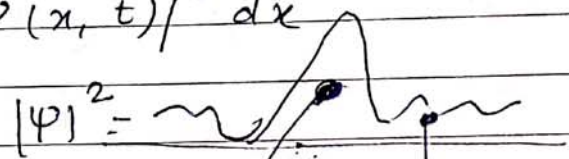
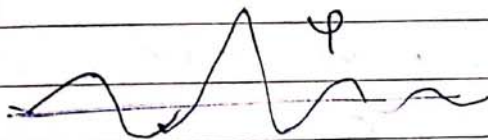
$$= 1.11 \times 10^{-4} \text{ m/s}$$



Wave function :- Mathematical function  $\left\{ \begin{array}{l} \text{space} \\ \text{time} \end{array} \right\}$    
  $\rightarrow$  it's a function of

- contains information on all measurable parameters of the particle
- If we consider 1 Dimensional (say x-direction), the wavefunction is  $\psi(x, t)$
- $\psi \psi^* =$  for complex  $\psi$   
 $\psi \psi^* =$  Probab. Probability density of finding the particle b/w  $x$  and  $x+dx$

- If  $\psi(x, t)$  is real  
Probability of finding the particle b/w  $x$  and  $x+dx = |\psi(x, t)|^2 dx$



- Probability of finding the particle b/w  $x=a$  and  $b$  is  $\int_a^b |\psi|^2 dx$ .

Operators  $\rightarrow$  contains information on all measurable parameters of the particle

- Momentum Operator :  $\hat{p}_x = \frac{\hbar}{i} \frac{\partial}{\partial x}$

$$\text{Thus } \frac{\hbar}{i} \frac{\partial \psi}{\partial x} = p_x \psi$$

- Energy operator :  $\hat{E} = \frac{\hbar}{i} \frac{\partial}{\partial t}$ , Thus  $\frac{\hbar}{i} \frac{\partial \psi}{\partial t} = E \psi$



• Kinetic Energy :  $\frac{p_x^2}{2m} = \frac{1}{2m} \frac{\hbar}{i} \frac{\partial}{\partial x} \left( \frac{\hbar}{i} \frac{\partial \psi}{\partial x} \right)$

$= -\frac{\hbar^2}{2m} \frac{\partial^2 \psi}{\partial x^2}$  — K.E operator

To understand

# To find momentum in x direction then we use momentum operator  $\hat{p}_x$

$\left( \frac{\hbar}{i} \frac{\partial}{\partial x} \right) \psi$  → means take this operator and applied on the  $\psi$  then I get the momentum in the x-direction next  $\psi$

#

Let  $\psi$  is a plane wave

$$\psi = e^{i(kx - \omega t)}$$

$$k = \frac{2\pi}{\lambda}, \quad \omega = 2\pi\nu$$

$$i = \sqrt{-1}$$

(1) Let use momentum operator

$$\frac{\hbar}{i} \frac{d\psi}{dx} = \frac{\hbar}{i} i k e^{i(kx - \omega t)}$$

$$\psi = e^{i(kx - \omega t)}$$

$$\frac{d\psi}{dx} = \frac{i k e^{i(kx - \omega t)}}{\psi}$$

$$= \hbar k \psi = \hbar \frac{2\pi}{\lambda} \psi$$

$$\frac{\hbar \cdot 2\pi}{\lambda} \psi = \left( \frac{h}{\lambda} \right) \psi$$

$\hat{p} \rightarrow$  momentum

So therefore it is momentum operator

(2) use Energy operator

$$E = -\frac{\hbar}{i} \frac{d}{dt} \psi$$

$$= -\frac{\hbar}{i} [-i\omega e^{i(kx - \omega t)}]$$

$$= \hbar \omega e^{i(kx - \omega t)}$$

$$= \hbar \omega \psi$$

$$\frac{\hbar \cdot 2\pi \nu \psi}{2\pi}$$

$$\hbar \nu \psi$$

Energy

→ so

$-\frac{\hbar}{i} \frac{d}{dt}$  is Energy operator

$$\psi = e^{i(kx - \omega t)}$$

$$-i\omega e^{i(kx - \omega t)}$$

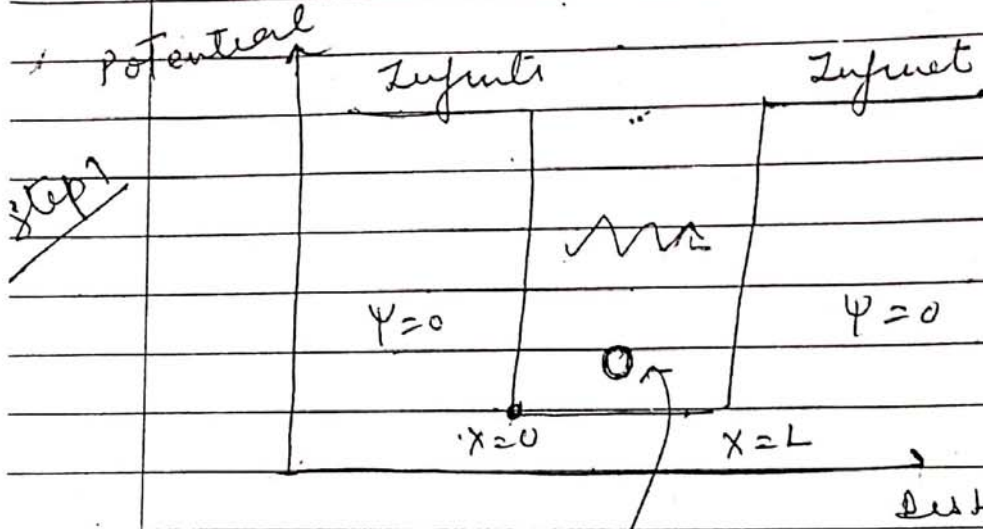
$\psi$

(3) Similarly for  $K \rightarrow E$



# Application of Schrodinger's Equation

## 1) Particle in a 1-Dimensional Box: Infinite Potential Barrier

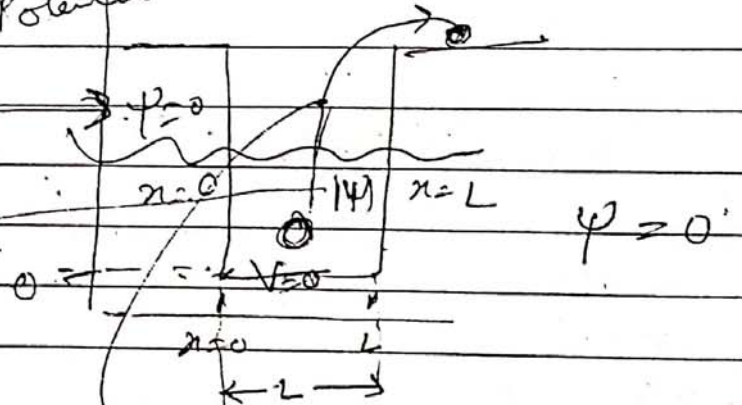


particle is located here and for

$$\frac{-\hbar^2}{2m} \frac{d^2 \psi}{dx^2} + V\psi = E\psi \quad (1)$$

$x > L$  } potential = 0  
 $x < 0$  }

Potential



it requires infinite amount of energy to be here

particle is confined only in the box

So magnitude of  $\psi$  (Amplitude) should be zero outside the box

Nature of wave function inside the box is to be determined