1. Age

Young
$$\rightarrow$$
 Entropy(4, 2, 2) = $-4/8 \log(4/8 - 2/8 \log(2/8) - 2/8 \log(2/8) = 0.4515$
Pre-presbyopic \rightarrow Entropy(5, 2, 1) = $-5/8 \log(5/8) - 2/8 \log(2/8) - 1/8 \log(1/8) = 0.3909$
Presbyopic \rightarrow Entropy(6, 1, 1) = $-6/8 \log(6/8) - 1/8 \log(1//8) - 1/8 \log(1//8) = 0.3194$
Average Entropy = $0.4515(8/24) + 0.3909(8/24) + 0.3194(8/24) = 0.3870$

Spectacle-Prescrip

Myope
$$\rightarrow$$
 Entropy(7, 2, 3) = $-7/12 \log(7/12) - 2/12 \log(2/12) - 3/12 \log(3/12) = 0.4168$
Hypermetrope \rightarrow Entropy(8, 3, 1) = $-8/12 \log(8/12) - 3/12 \log(3/12) - 1/12 \log(1/12) = 0.3578$
Average Entropy = $0.4168(12/24) + 0.3578(12/24) = 0.3873$

Astigmatism

No
$$\rightarrow$$
 Entropy(7, 5, 0) = $-7/12 \log(7/12) - 5/12 \log(5/12) - 0/12 \log(0/12) = 0.2950$
Yes \rightarrow Entropy(8, 0, 4) = $-8/12 \log(8/12) - 0/12 \log(0/12) - 4/12 \log(4/12) = 0.2764$
Average Entropy = $0.2950(12/24) + 0.2764(12/24) = 0.2857$

Tear-prod-rate

Normal
$$\rightarrow$$
 Entropy(3, 5, 4) = $-3/12 \log(3/12) - 5/12 \log(5/12) - 4/12 \log(4/12) = 0.4680$
Reduced \rightarrow Entropy(12, 0, 0) = $-12/12 \log(12/12) - 0/12 \log(0/12) - 0/12 \log(0/12) = 0$
Average Entropy = $0.4680(12/24) + 0(12/24) = 0.2340$

Root: We select Tear-prod-rate for the root as the average entropy is the lowest.

Age

Young
$$\rightarrow$$
 Entropy(0, 2, 2) = $-0/4 \log(0/4) - 2/4 \log(2/4) - 2/4 \log(2/4) = 0.3010$
Pre-presbyopic \rightarrow Entropy(1, 2, 1) = $-1/4 \log(1/4) - 2/4 \log(2/4) - 1/4 \log(1/4) = 0.4515$
Presbyopic \rightarrow Entropy(2, 1, 1) = $-2/4 \log(2/4) - 1/4 \log(1/4) - 1/4 \log(1/4) = 0.4515$
Average Entropy = $0.3010(4/12) + 0.4515(4/12) + 0.4515(4/12) = 0.4013$

Spectacle-Prescrip

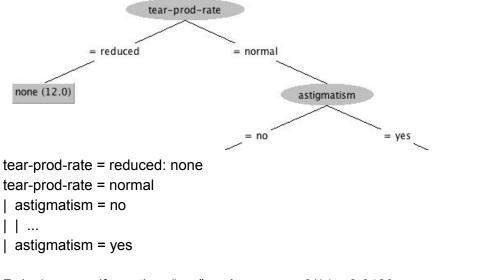
Myope
$$\rightarrow$$
 Entropy(2, 3, 1) = $-2/6 \log(2/6) - 3/6 \log(3/6) - 1/6 \log(1/6) = 0.4392$
Hypermetrope \rightarrow Entropy(1, 2, 3) = $-1/6 \log(1/6) - 2/6 \log(2/6) - 3/6 \log(3/6) = 0.4392$
Average Entropy = $0.4392(6/12) + 0.4392(6/12) = 0.4392$

Astigmatism

No
$$\rightarrow$$
 Entropy(1, 5, 0) = $-1/6 \log(1/6) - 5/6 \log(5/6) - 0/6 \log(0/6) = 0.1957$
Yes \rightarrow Entropy(2, 0, 4) = $-2/6 \log(2/6) - 0/6 \log(0/6) - 4/6 \log(4/6) = 0.2764$
Average Entropy = $0.1957(6/12) + 0.2764(6/12) = 0.2361$

Second Level: We select Astigmatism for the second level as the average entropy is the lowest.

Tree:



```
2. Rule 1: if ____ then "yes" → Accuracy = 9/14 = 0.6429

If outlook = overcast then "yes" → Accuracy = 4/4 = 1.0

Rule 2: if ____ then "yes" → Accuracy = 9/14 = 0.6429

If outlook = rainy then "yes" → Accuracy = % = 0.6

If outlook = rainy and windy = false then "yes" → Accuracy = 3/3 = 1.0
```

3.