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# Identification of Human Genetic Locus from Unknown Meat Sample by Restriction Fragment Length Polymorphism

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## 1 Introduction

This project models the effect of two subgroups within a population. These subgroups are colloquially termed either "normally" susceptible ( $S_n$ , default average person) or "highly" susceptible ( $S_h$ , a subgroup that differs from the average by some parameters).  $S_h$  are modelled as a linear-transform of  $S_n$  and may differ in any combination of infection rate, recovery rate, death rate, and/or relapsation rate (loss of immunity) from  $S_n$  by a scalar increase or decrease relative to  $S_n$ 's respective transition rate.

## 2 The SIR Model

### Susceptible Population $S$

This project assumes the total population  $S$  consists of two groups as per:

$$S = S_n + S_h = \alpha_n \cdot S + \alpha_h \cdot S$$

where  $\alpha_i$  are the percentages of each sub-group within the population,  $\alpha_n + \alpha_h = 1$ .

### Infectious Population $I$

As both  $S_n$  and  $S_h$  are assumed to have different susceptibilities, they are assigned two different rates of infection:  $\beta_n$  and  $\beta_h$ , where we assume for simplicity sake (see Introduction) that  $\beta_h = k \cdot \beta_n$  for some  $k \in \mathbb{R}$ . Given the scalar relation between  $\beta_n$  and  $\beta_h$  we abbreviate  $\beta_n \equiv \beta$ , as we will do for any transition rate henceforth.

### Removed Population $R$

The removed population  $R$  consists of two sub-populations, namely the recovered population  $R'$  and the deceased population  $D$ . Infectious individuals may transition into either  $R'$  or  $D$ , given two separate transition rates.

We define the recovery rate  $\gamma$  and death rate  $\theta$  whose scaled rates for the "highly" susceptibles are  $\gamma_h = j \cdot \gamma$  and  $\theta_h = q \cdot \theta$  for some  $j, q \in \mathbb{R}$ , respectively. We further define a relapsation rate  $\delta$  that mimics how immunity is lost over time (perhaps due to newly emerging mutant pathogens) and allows individuals from  $R'$  to relapse into  $S$ . Here as well "highly" susceptibles are linearly scaled as  $\delta_h = h \cdot \delta$  for some  $h \in \mathbb{R}$ .

## System of Equations

The outlined model allows transitions between Susceptible  $S$  to Infectious  $I$ , from  $I$  to either Removed population  $R'$  or  $D$ , and from  $R'$  back to  $S$ . This allows the following set of first order differential equations to be formulated:

$$\begin{aligned}\frac{dS(t)}{dt} &= -\beta\Phi_k \cdot S(t) \cdot I(t) + \delta\Phi_h \cdot R'(t) \\ \frac{dI(t)}{dt} &= \beta\Phi_k \cdot S(t) \cdot I(t) - \gamma\Phi_j \cdot I(t) - \theta\Phi_q \cdot I(t) \\ \frac{dR'(t)}{dt} &= \gamma\Phi_j \cdot I(t) - \delta\Phi_h \cdot R'(t) \\ \frac{dD(t)}{dt} &= \theta\Phi_q \cdot I(t)\end{aligned}$$

Where  $\Phi_x = \alpha_n + x \cdot \alpha_h$  describes the impact of "highly" susceptibles within the total population for some scalar factor  $x$  of a given transition.

This set of differential equations now has four separate rates of transition: (1)  $\beta$ , the rate of infection, where "highly" susceptibles are distinguished by a  $k$ -fold increase/decrease. (2)  $\gamma$ , the rate of recovery, where "highly" susceptibles are distinguished by a  $j$ -fold increase/decrease. (3)  $\delta$ , the relapsation rate, where "highly" susceptibles are distinguished by an  $h$ -fold increase/decrease. And (4)  $\theta$ , the death rate, where "highly" susceptibles are distinguished by a  $q$ -fold increase/decrease compared to "normally" susceptibles. All of these are editable to explore different scenarios of heterogeneous populations.

## 3 Modelling

To apply the formulated model, a python module was developed to numerically solve the outlined system of equation using `scipy` and `numpy`. An interactive web-app was developed using `streamlit` to ease model exploration. THE APP IS AVAILABLE WHERE??...

## 4 Discussion

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**Table 1** HEPES 0.5M, pH7.4 | 500ml

Component	Instruction
HEPES	59.58g
MilliQ	fill-up to 450ml
NaOH 5M	to pH7.4 (~17.5ml)
MilliQ	fill-up to 500ml
Sterile Filter	

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This is a <sup>1</sup> Text of note.

## 5 Supplementary Data

<sup>1</sup>Something of a footnote here...