

	zx	nx	zy	ny	f	no	out=
1	0	1	1	1	1	1	x+1
2	1	1	0	1	1	1	y+1
3	0	0	1	1	1	0	x-1
4	1	1	0	0	1	0	y-1
5	0	0	0	0	1	0	x+y
6	0	1	0	0	1	1	x-y
7	0	0	0	1	1	1	y-x
8	0	0	0	0	0	0	x&y
9	0	1	0	1	0	1	x y

2X Setz $x = 0$, nx negiert x.
 2Y Setz $y = 0$, ny negiert y.
 $f=1 \Rightarrow x+y$, no negiert out.
 $f=0 \Rightarrow x&y$

1. Zeile: $\sim [\sim X + \underbrace{(1, \dots, 1)}_{16\text{-Stellen}}]$
 (Ein Komplement von X) 1111 1111 1111 1111₂

$$\begin{aligned}
 X_2 &= 0010 \quad 0101 \quad 0001 \quad 0110_2 = 9494_{10} \\
 X_{1k} &= 1101 \quad 1010 \quad 1110 \quad 1001_{1k} = -X \\
 &\quad \underline{11111111 \quad 11111111 \quad 11111111 \quad 11111111} \\
 &\quad 1101 \quad 1010 \quad 1110 \quad 1000_{1k} = -X - 1
 \end{aligned}$$

$(-X-1)_{1k} \Rightarrow (-X-1)_2 = 0010 \quad 0101 \quad 0001 \quad 0111 = 9495_{10} = (X+1)_2$ ✓

2. Zeile: $\sim [\underbrace{(1, \dots, 1)}_{16\text{-Stellen}} + \sim Y] = \sim [\sim Y + \underbrace{(1, \dots, 1)}_{16\text{-Stellen}}]$

\Rightarrow Analog zu (Z.1) ✓

3. Zeile: $no=0$ $2X=0, nx=0$ $f=1$ $2Y=1, ny=1$

$$\begin{aligned}
 X &+ \underbrace{(1, \dots, 1)}_{16\text{-Stellen}} &= X + (\sim 0) \\
 & &= X + ((-0) - 1) \\
 & &= X + (-1) \\
 & &= X - 1 \quad \checkmark
 \end{aligned}$$

4. Zeile: $\underbrace{(1, \dots, 1)}_{16\text{-Stellen}} + Y = Y + \underbrace{(1, \dots, 1)}_{16\text{-Stellen}} \Rightarrow$ Analog zu (Z.3) ✓

Zeile 5: $n_0 = 0$ $\begin{matrix} 2x=0 \\ nx=0 \end{matrix}$ $f=1$ $\begin{matrix} 2y=0 \\ ny=0 \end{matrix}$ \checkmark

Zeile 6: $n_0 = 1$ $\begin{matrix} 2x=0 \\ nx=1 \end{matrix}$ $f=1$ $\begin{matrix} 2y=0 \\ ny=0 \end{matrix}$

$$\begin{aligned} & \sim [\sim x + y] \quad \text{mit } \sim(\) = (\) - 1 \\ &= - [\sim x + y] - 1 \\ &= - [\sim x + y + 1] \quad \text{mit } \sim x = -x - 1 \\ &= - [-x - 1 + y + 1] \\ &= - [-x + y] \\ &= \underline{x - y} \quad \checkmark \end{aligned}$$

Zeile 7: $\sim [x + \sim y]$
 $= \sim [\sim y + x] \Rightarrow \text{Analog zu (2.6)} \quad \checkmark$

Zeile 8: $n_0 = 0$ $\begin{matrix} 2x=0 \\ nx=0 \end{matrix}$ $f=0$ $\begin{matrix} 2y=0 \\ ny=0 \end{matrix}$

$x \ \& \ y \quad \checkmark$

Zeile 9: $n_0 = 1$ $\begin{matrix} 2x=0 \\ nx=1 \end{matrix}$ $f=0$ $\begin{matrix} 2y=0 \\ ny=1 \end{matrix}$

$$\sim [\sim x \ \& \ \sim y]$$

, da wir nicht rechnen sondern bitweise vgl.:

$$(\overline{x} \wedge \overline{y}) = \overline{x} \vee \overline{y} = x \vee y = x | y$$

↑
nicht NAND
sondern bitweises OR!

Aufgabe 2:

zx	nx	zy	ny	f	no	out=
1	0	1	0	1	0	0
1	1	1	1	1	1	1
1	1	1	0	1	0	-1

Zeile 3: $(\underbrace{1, \dots, 1}_{16\text{-Stellen}}) + 0 = 1111 \dots 1111 \dots 1111 \dots 1111_{2k} = -1_{10}$

Bsp1: $no = 0 \quad \begin{matrix} zx=1 \\ nx=0 \end{matrix}, \quad f=1 \quad \begin{matrix} zy=1 \\ ny=1 \end{matrix}$

$$0 + (\underbrace{1, \dots, 1}_{16\text{-Stellen}}) = (\underbrace{1, \dots, 1}_{2k})_{2k} = -1_{10}$$

Bsp2: $no = 1 \quad \begin{matrix} zx=1 \\ nx=0 \end{matrix}, \quad f=1 \quad \begin{matrix} zy=1 \\ ny=0 \end{matrix}$

$$\sim \{0 + 0\} = \sim 0 = (\underbrace{1, \dots, 1}_{2k})_{2k} = -1_{10}$$

Bsp3: $no = 1 \quad \begin{matrix} zx=1 \\ nx=0 \end{matrix}, \quad f=0 \quad \begin{matrix} zy=1 \\ ny=0 \end{matrix}$

$$\sim \{0 \& 0\} = \sim \{0\} = (\underbrace{1, \dots, 1}_{2k})_{2k} = -1_{10}$$

Bsp4: $no = 1 \quad \begin{matrix} zx=1 \\ nx=1 \end{matrix}, \quad f=0 \quad \begin{matrix} zy=1 \\ ny=0 \end{matrix}$

$$\sim ((\underbrace{1, \dots, 1}_2 \& 0_{10})) = \sim(0) = (\underbrace{1, \dots, 1}_{2k})_{2k} = -1_{10}$$

Bsp5: $no = 1 \quad \begin{matrix} zx=1 \\ nx=0 \end{matrix}, \quad f=0 \quad \begin{matrix} zy=1 \\ ny=1 \end{matrix}$

$$\sim (0_{10} \& (\underbrace{1, \dots, 1}_2)) = \sim(0) = (\underbrace{1, \dots, 1}_{2k})_{2k} = -1_{10}$$

Tabelle:

	zx	nx	zy	ny	f	no	out
1.	1	0	1	1	1	0	-1
2.	1	0	1	0	1	1	-1
3.	1	0	1	0	0	1	-1
4.	1	1	1	0	0	1	-1
5.	1	0	1	1	0	1	-1