

# STATE ESTIMATION OF AN UNMANNED GROUND VEHICLE USING INEXPENSIVE SENSORS

by

Noah Johnson

A Thesis

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# Acknowledgments

This is the acknowledgements section. You should replace this with your own acknowledgements.

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# State Estimation of an Unmanned Ground Vehicle Using Inexpensive Sensors

Noah Johnson

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## Abstract

In this thesis, I designed and constructed an unmanned ground vehicle for the purpose of autonomous navigation. Costs were minimized by reusing components already on-hand wherever possible. While the ultimate goal of autonomous navigation was not reached, I did succeed in both creating a drivable mobile base and fusing sensor data into an odometry estimate within the ROS framework, which is a good foundation for future extension to autonomous navigation.

The rover base consists of a Lynxmotion rover, an Arduino, and a Sabertooth motor driver. Sensors available include two quadrature rotary encoders, a mobile phone, and an ultrasonic distance sensor. The Arduino acts as a low-level robotic controller, publishing wheel encoder and range data, and accepting motor velocity commands. An Android app publishes IMU and GPS data from the mobile phone, and the laptop fuses these readings into a state estimation of pose and velocity using an extended Kalman filter.

Professor Gary Kalmanovich .....

May 18, 2017

# Chapter 1

## Introduction

### 1.1 Goal

Create a cheap outdoors autonomous robot. Given a 'map' of the New College campus, this robot should be able to navigate from one outdoors location to another using footpaths. In doing so, it should dynamically avoid obstacles such as people, and recalculate alternate routes when a route is unexpectedly blocked.

### 1.2 Navigation

intro to the concept of navigation

Since a map with GPS coordinates is provided, this is not Simultaneous Localization and Mapping (SLAM), but a simplified navigation problem.



## 1.3 Choice of Sensors

IR, Microsoft Kinect can't use because the rover will be outdoors during the day and the sun gives off ambient IR radiation.

LIDAR - state of the art

And LIDAR sensors would be too costly. constrained by cheap hardware, and the inability to use IR or LIDAR sensors.

# Chapter 2

## Theory

Robots estimate their environment stochastically, and so probability theory is vital to understanding their inner workings. First we will review the necessary theory, and then we will examine a class of algorithms for recursive state estimation.

### 2.1 Probability Background

Discrete random variables have a finite output space of possible values that may be observed. Let  $X$  be a random variable, then we define the probability that we observe value  $x$  from  $X$  as  $p(X = x) \equiv p(x)$ . Since  $x$  is arbitrary, this defines a probability distribution. For every random variable  $X$ , we have

$$\sum_{x \in X} p(x) = 1$$

Given two more random variables  $Y$  and  $Z$ , we'll define the joint distribution  $p(X = x \text{ and } Y = y \text{ and } Z = z) \equiv p(x, y, z)$ , and the conditional probability  $p(X = x \text{ given that } Y = y \text{ and } Z = z) \equiv p(x | y, z)$ . The conditional probability is defined to be

$$p(x | y, z) = \frac{p(x, y, z)}{p(y, z)} \quad (2.1)$$

The *Law of Total Probability* states that  $p(x) = \sum_{y \in Y} p(x, y)$ . Extending this law to use a third random variable  $Z$ , and incorporating the definition of conditional probability, we end up with the following equation:

$$p(x | z) = \sum_{y \in Y} p(x, y, z) = \sum_{y \in Y} p(y, z) p(x | y, z) \quad (2.2)$$

Lastly, we can use equation 2.1 to derive a version of Bayes' Theorem.

$$p(x | y, z) = \frac{p(x, y, z)}{p(y, z)} = \frac{p(y, x, z)}{p(x, z)} * \frac{p(x, z)}{p(y, z)} = \frac{p(y | x, z) p(x, z)}{p(y | z)} \quad (2.3)$$

In the future this will prove to be a useful tool to compute a posterior probability distribution  $p(x | y)$  from the inverse conditional probability  $p(y | x)$  and the prior probability distribution  $p(x)$ .

## 2.2 Bayes Filter

### 2.2.1 Scenario

Consider the general case of a robot which uses sensors to gather information about its environment. These sensors provide readings at discrete time steps  $t = 0, 1, 2, \dots$ . Some amount of noise is associated with each of these readings. At each time step  $t$ , the robot may execute commands to affect its environment, and wishes to know its current state. [14]

Let's encode the robot's current state at time  $t$  in the vector  $x_t$ . Similarly,  $z_t$  will represent a sensor measurement at time  $t$ , and  $u_t$  will represent the commands issued by the robot at time  $t$ . For each of these vectors we will use the notation  $z_{1:t} = z_1, z_2, \dots, z_t$ . [14]

The robot only has access to data in the form of  $z_t$  and  $u_t$ . Thus it cannot ever have perfect knowledge of its state  $x_t$ . It will have to make do by storing a probability distribution assigning a probability to every possible realization of  $x_t$ . This posterior probability distribution will represent the robot's belief in its current state, and should be conditioned on all available data. Thus we'll define the robot's belief distribution to be [14]:

$$bel(x_t) = p(x_t \mid z_{1:t}, u_{1:t}) \tag{2.4}$$

### 2.2.2 Derivation

We can use equation 2.3 to rewrite  $bel(x_t)$ :

$$bel(x_t) = p(x_t \mid z_{1:t}, u_{1:t}) = \frac{p(z_t \mid x_t, z_{1:t-1}, u_{1:t})p(x_t \mid z_{1:t-1}, u_{1:t})}{p(z_t \mid z_{1:t-1}, u_{1:t})}$$

In order to simplify  $p(z_t \mid x_t, z_{1:t-1}, u_{1:t})$ , we'll have to make an important assumption. We'll assume that the state  $x_t$  satisfies the Markov property, that is,  $x_t$  perfectly encapsulates all prior information. Thus if  $x_t$  is known, then  $z_{1:t}$  and  $u_{1:t}$  are redundant. This assumption lets us remove consideration of past sensor measurements and commands, and to rewrite the belief distribution as:

$$bel(x_t) = \frac{p(z_t \mid x_t)p(x_t \mid z_{1:t-1}, u_{1:t})}{p(z_t \mid z_{1:t-1}, u_{1:t})}$$

Notice that  $p(z_t \mid z_{1:t-1}, u_{1:t})$  is a constant with respect to  $x_t$ . Thus it makes sense to let  $\eta = (p(z_t \mid z_{1:t-1}, u_{1:t}))^{-1}$  and rewrite the belief distribution as:

$$bel(x_t) = \eta p(z_t \mid x_t)p(x_t \mid z_{1:t-1}, u_{1:t})$$

Now we are left with two distributions of interest. Looking closely one may notice that  $p(x_t \mid z_{1:t-1}, u_{1:t})$  is simply our original belief distribution, equation 2.4, but not conditioned on the most recent sensor measurement,  $z_t$ . Let us refer to this distribution as  $\overline{bel}(x_t)$ , and break it down further using equation 2.2 and our Markov

assumption [14]:

$$\begin{aligned}
\overline{bel}(x_t) &= p(x_t \mid z_{1:t-1}, u_{1:t}) \\
&= \sum_{x_{t-1}} p(x_t \mid x_{t-1}, z_{1:t-1}, u_{1:t}) p(x_{t-1} \mid z_{1:t-1}, u_{1:t}) \\
&= \sum_{x_{t-1}} p(x_t \mid x_{t-1}, u_t) p(x_{t-1} \mid z_{1:t-1}, u_{1:t}) \\
&= \sum_{x_{t-1}} p(x_t \mid x_{t-1}, u_t) bel(x_{t-1})
\end{aligned}$$

We have arrived at a recursive definition of  $bel(x_t)$  with respect to  $bel(x_{t-1})$ ! As long as  $p(x_t \mid x_{t-1}, u_t)$  and  $p(z_t \mid x_t)$  are known, we can recursively calculate  $bel(x_t)$ .

$p(x_t \mid x_{t-1}, u_t)$  defines a stochastic model for the robot's state, defining how the robot's state will evolve over time based upon what commands it issues. This probability distribution is known as the *state transition probability*. [14]

$p(z_t \mid x_t)$  also defines a stochastic model, modeling the sensor measurements  $z_t$  as noisy projections of the robot's environment. This distribution will be referred to as the *measurement probability*. [14]

Once we have models for both the *state transition probability* and *measurement probability*, we can finally construct the algorithm known as Bayes' Filter [14]:

---

**Algorithm 1** Bayes Filter

---

```
1: function BAYESFILTERITERATE(  $bel(x_{t-1}), u_t, z_t$  )
2:   for each possible state  $x_t^* \in x_t$  do
3:      $\overline{bel}(x_t^*) = \sum_{x_{t-1}^* \in x_{t-1}} p(x_t^* | x_{t-1}^*, u_t) bel(x_{t-1}^*)$ 
4:      $bel(x_t^*) = \eta p(z_t | x_t^*) \overline{bel}(x_t^*)$ 
5:   end for
6:   Set  $\sum_{x_t^* \in x_t} bel(x_t^*) = 1$ , and solve for  $\eta$ 
7:   Use  $\eta$  to compute  $bel(x_t)$ 
8:   return  $bel(x_t)$ 
9: end function
```

---

### 2.2.3 Example

## 2.3 Kalman Filter

### 2.3.1 Extended Kalman Filter

# Chapter 3

## Hardware

### 3.1 Specific Hardware Used

The specific hardware used in this project was chosen to minimize cost while still producing a vehicle capable of navigating rough, uneven outdoors terrain. Parts that were already on hand, and that most college students would reasonably have access to, such as a personal laptop and an Android smartphone, were used over superior alternatives. In total these parts were purchased for less than \$500.

The mobile base used is the Lynxmotion A4WD1 Rover, see Figure 3-1. This kit comes with four 200 RPM DC gear motors, 100 PPR motor encoders, and 4.75" diameter wheels. The chassis consists of four aluminum side brackets, and two polycarbonate panels on the top and bottom. The rover is rated to carry up to 5 pounds.

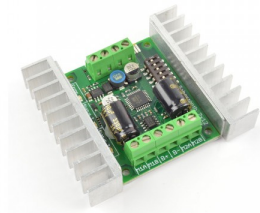
Figure 3-1: Lynxmotion 4WD Rover [11]





The motors are controlled by a Sabertooth dual-channel 12A 6V-24V regenerative motor driver, see Figure 3-2. This motor driver is powered by two LG 18650 HE2 rechargeable lithium ion cells, which sit in an 18650 battery case which has been soldered to act as a battery pack with two 18650 cells in series. The battery cells are individually charged before use with a NiteCore-i2-V2014 li-ion charger.

Figure 3-2: Sabertooth 2x12 [5]



On top of the rover is the PING))) ultrasonic distance sensor (see Figure 3-3), which is attached to a standard Parallax servo which pans back and forth 180 degrees. This range sensor emits an ultrasonic chirp, and times how long it takes for that chirp to echo back. Based on that time, the distance from the sensor to an obstacle can be calculated. The PING))) sensor can be used to detect objects from 2cm to 3 meters away. [9]

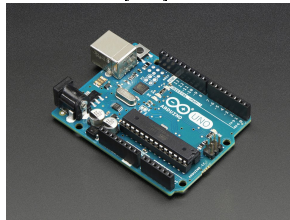
Figure 3-3: PING))) Ultrasonic Sensor [13]



At the center of the rover is an Arduino Uno R3, see Figure 3-4. This microcontroller board handles several important tasks. It tells the motor

driver what speed to set its two output channels to, and directly controls the panning motion of the standard Parallax servo. It also acts as a go-between for the digital output of the sensors on the rover and a laptop. It's connected to this laptop via a USB cable, which powers the board and allows communication over a serial port. Motor encoder values and ultrasonic range data are transmitted to the laptop, and motor power commands are received. An Arduino prototyping shield is stacked on top to allow re-usability of the board.

The specific laptop used in this project is the Dell Inspiron 3531, which has a quad core 2.16 GHz processor, and 4 GB of RAM. Any personal laptop running Ubuntu or Debian could be used here, and additional computational resources would be beneficial. However, this laptop was a personal work machine and already available to use at no additional cost. The laptop is used as the main processing unit for the navigation logic.



The last component is a Nexus 4 smartphone placed on the top panel of the rover, which is also connected to the laptop by USB. Inside this phone is an MPU-6050 chip which contains a gyroscope and accelerometer. Elsewhere on the phone's logic board are a magnetometer, otherwise known as a digital compass, and a GPS receiver. This was also a personal device already available, and acts as a cheap Inertial Measurement Unit (IMU) and GPS receiver for the robot.

## 3.2 Construction

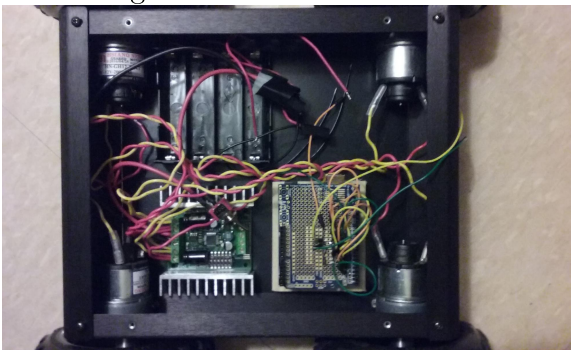
Figure 3-5 shows the base just after assembly. The aluminum side brackets' mounting holes did not line up properly with the motors, so a Dremel drill was used to widen them.

The Arduino Uno was screwed to a 2.5" x 3" x 0.5" wooden poplar block, with non-conductive nylon washers placed between the screw head and the Uno, and between the Uno and the wooden block. The wooden Arduino mounting board and the Sabertooth were both attached via double-sided foam mounting tape to the bottom panel of the rover. The battery holder was attached with glue dots to make removal easier.

Figure 3-5: Constructed Chassis



Figure 3-6: Pieces Mounted



The servo fits conveniently into a pre-cut opening in the top chassis panel, and is held in place with four 3mm x 6mm screws and corresponding washers.

Figure 3-7: Construction Finished



A mounting bracket is attached to the servo, and the PING))) sensor is screwed to that mounting bracket, using non-conductive washers and screws to separate the circuit board and the metal mounting bracket.

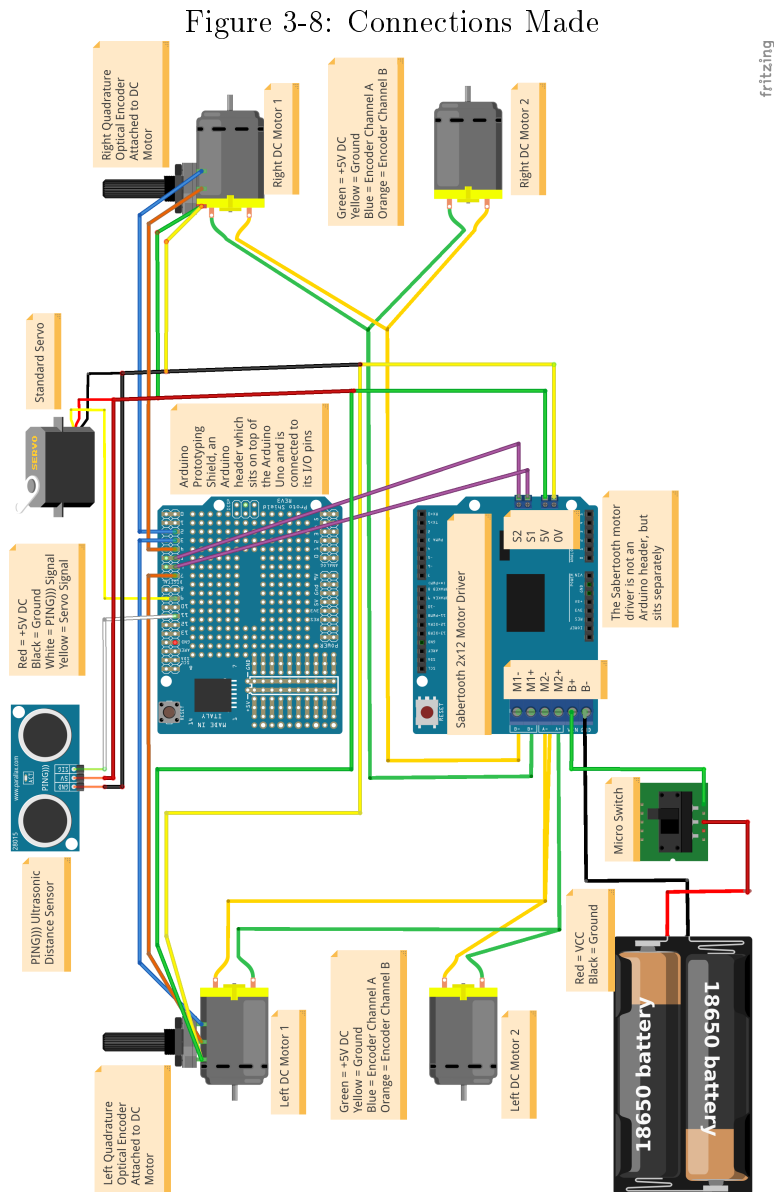
Another opening in the top panel allows the PING))) sensor to connect to the Arduino inside the body of the rover. This opening also allows the type A/B USB cable connected to the Arduino to extend out and reach the laptop. The smartphone sits on the top panel just to the left of this opening, secured in place by removable glue adhesive dots. It is also connected to the laptop via a micro-USB to USB cable.

Both USB cables are long, stretching to just under 10 feet. The USB 2.0 specification limits the length of cable between two 2.0 USB devices to less than five meters, or about 16 feet [15]. Thus there should be no problem with the current length, but extensions in the future could not go much further.

Connecting electronics on the rover to the laptop via USB means the processing laptop must manually be kept within 10 feet of the rover as it navigates. This design could easily be extended to include wireless or radio communication with a server, and a larger chassis would simply be able to carry the laptop on it. However, USB cables are cheap and still function as a proof of concept for an autonomous design.

Figure 3-8 is a schematic specifying the overall design for the rover.

Connections were made with flexible stranded core, 22 AWG breadboard wires. Connections to the Arduino's digital pins were made indirectly. A prototyping shield was stacked on top of the Arduino, and connected to its digital pins via pin headers.



This image was created with Fritzing

Signal pins were then soldered to the prototyping shield. Breadboard wires needing direct connection ideally should use terminal block connectors. However, these were difficult to find at a reasonable price, and so wires were soldered together tip to tip, and then wrapped in electrical tape.

The Sabertooth motor driver controls two motor channels. It drives DC motors from these channels in a relatively simple way. The speed of DC motors is proportional to the voltage supplied to them, and the direction of rotation can be flipped simply by flipping the polarity of the supplied voltage. The motor driver manages the voltage supplied to each channel by using pulse-width modulation, which involves switching the power on and off at a high frequency. This approximates a smooth waveform of the average voltage and current. An on-board H-bridge is used to flip the polarity. [8]

### **3.2.1 Power**

Besides the Arduino Uno, which is powered separately by a USB connection to the laptop, most of the rover's components are powered by the battery pack. This pack contains two individual 18650 lithium-ion cells placed into a battery holder and connected in series. The battery pack is then connected to the motor driver's battery terminals B+ and B-. The positive B+ output goes through a microswitch, which is attached to a side bracket in the rover, and is accessible from the outside. This acts as a kill switch for the battery pack.

Each 18650 cell holds 4.2V at full charge, and discharges down to a minimum

of 2.7V. The motor driver has a lithium cutoff mode which shuts the driver down when the average voltage of cells in the battery pack reaches 3.0V. Thus the voltage supplied to the four motors through the motor driver's output channels will range from 8.4V to 6.0V, which is within their acceptable operating range.

The specific li-ion cells being used can supply up to 20A continuously, and the motor driver can handle up to 12A per channel. The motors each draw a maximum current of 1.5A, and two are used per channel, putting the total possible current draw of 3A per channel well below the limits of the motor driver and battery pack.

The motor driver has an onboard battery eliminator circuit (BEC) which is an efficient 5V voltage regulator capable of supplying up to 1 amp of continuous current, with 1.5 Amps at peak. The ultrasonic sensor, its servo, and the two rotary encoders combined use less than 500 mA, and are all powered through this BEC. The Arduino is also connected to this BEC's ground, as the Uno and Sabertooth must share a common ground plane in order for the control signals to be interpreted correctly [4]. It's important to note that a BEC of some kind is essential in this project, as the Arduino's on-board 5V regulator can not handle the peak amperage draw of the servo, and if used risks overheating.

The standard servo has the potential to draw peak currents of up to 1A, if it hits a snag and is stopped from moving. Therefore the input wires to the 5V and 0V BEC terminal connectors should be capable of handling those peaks. Since we are using 22 AWG wires, we are close to the limit, but a 22 AWG wire with 43 or more internal cores is rated to handle 1A. And the expected consistent draw is much lower, less than 500mA.

Note that the sensors attached to the microcontroller should be powered off before the Arduino, else the Arduino may try to power the whole Mega chip via its input pins. The sensors are powered from the BEC on the motor driver, so they may be turned off by using the microswitch between the battery holder and the motor driver.



# Chapter 4

## Arduino

The Arduino Uno in this project acts as a bridge between hardware and software, allowing the the laptop to read sensor data from the rover, and control the speed of its wheels.

### 4.1 Background

Arduino development boards are printed circuit boards capable of running small embedded programs. They contain an on-board microcontroller, timing crystal, USB port, I/O pins and more. The specific board used in this project, an Arduino Uno, uses the ATmega328P microcontroller with a 16 MHz quartz timing crystal and 14 digital I/O pins. It also has 6 analog-to-digital converter I/O pins, but we won't make use of them in this project.

Digital I/O pins can be configured to either read signals as input or generate them as output. Digital pins read input signals at specific times as binary values, i.e. the

connected signal's voltage is read as either on or off compared to a certain threshold voltage. Following the standard Arduino literature, we will refer to these signals as either HIGH or LOW. When digital pins are configured to generate HIGH or LOW signals, they produce a relative output voltage above or below the threshold voltage.

### **4.1.1 Servo Control Pulses**

An important use-case which pops up often when using the Arduino is that of interfacing with RC electronics. In this project's design, both the Sabertooth motor driver and the standard servo require their signal inputs to use the standard R/C transmission protocol.

This protocol involves sending brief HIGH pulses of variable width, between one and two milliseconds. There is a fixed delay between pulses, commonly about 20 ms of LOW signal. The width of the HIGH pulse communicates to a servo the desired position. Its internal components then drive its DC motors until the servo is rotated to the commanded position. In the case of the Sabertooth motor driver, the position is interpreted as a speed to drive the motors at.

## **4.2 Arduino Uno Connections**

Refer back to Figure 3-8 for a visual representation of how the Arduino Uno is connected to the other rover components.

### 4.2.1 Hardware Interrupt Pins

As one can see in Figure 3-8, only two optical quadrature encoders are used, placed on the front motors on the left and right side of the rover. This is due to a hardware limitation of the Arduino Uno. The ATmega328P microcontroller has only two interrupt pins, which are mapped to digital pins 2 and 3 on the Uno. These pins can trigger unique Interrupt Service Routines (ISRs) whenever the input signals change from LOW to HIGH voltage, or vice versa.

While it is possible to react to a change in any digital pin's voltage, it would be significantly slower than a hardware interrupt. An ISR is necessary to keep up with the fast rate of pin voltage changes that occur in the output of quadrature encoders.

If a different Arduino board such as the Mega were used, there would be sufficient hardware interrupt pins for all four encoders. Using a board with plentiful interrupts, one could even attach both channel outputs of the encoders to interrupt pins, rather than only one. This would double the encoders' resolution. See section 4.4.3 for more detail.

### 4.2.2 Digital Pin Connections

Each motor encoder has two output channels, A and B. Both encoders attach one of their output channels, channel A, to a hardware interrupt pin. In section 4.4.3 we will see why this configuration was chosen. The right motor's encoder connects channel A to pin 2, and channel B to pin 4. The left motor's encoder connects its channel A output to pin 3, and its channel B output to pin 7.

The S1 and S2 signal input terminals on the Sabertooth motor driver are connected to digital pins 5 and 6. The control signal for the hobby servo is connected to digital pin 9. The signal pin on the ultrasonic sensor is connected to digital pin 11. The Arduino's ground pin is connected to the ground of the motor driver's BEC, to ensure a common ground plane.

Most digital pin numbers used are arbitrary, and connections may be permuted without issue. The exceptions are pins 0-3, which must not be modified. Pins 0 and 1 must be left unattached for serial data transfer to work properly over USB. And pins 2 and 3 are hardware interrupt pins which must be used to handle the quadrature encoders' output.

## 4.3 Motor Driver's Configuration

The Sabertooth motor driver has two signal input terminals, S1 and S2, which allow the Arduino to issue instructions specifying how to drive the motors. The protocols used to communicate with the motor driver over these signal inputs are specified by six DIP switches on-board the driver. These DIP switches are manually flipped either up or down.

Setting switch 1 down and switch 2 up places the driver into R/C input mode, which configures S1 and S2 to expect servo control pulses, Å la R/C controllers. This protocol was briefly explained in section 4.1.1. [4]

Turning switch 3 down selects the lithium cutoff mode, which detects the number of lithium cells in series powering the driver, and shuts off when the battery pack's

voltage drops below 3.0V per cell, or 6.0V for the two cell battery pack this project uses. This prevents accidental damage to the 18650 cells which may be caused by over-discharge.

Flipping switch 4 down selects independent (differential) drive, which allows S1 and S2 to each independently control the speed of one motor channel. Using this mode, turning of the vehicle is achieved by lowering the relative speed of the motors on one side of the vehicle compared to the other.

Switch 5 is flipped up to ensure a linear rather than exponential response of the motors to the Arduino's input signal. Switch 6 is flipped down to select "microcontroller mode", which turns off auto-calibration of the zero-velocity input signal, and turns off an automatic timeout. Thus if the signal connection is somehow lost the motor driver will continue driving the motors according to the last signal received. This is necessary for smooth performance of the motors since the Arduino may slightly delay control pulses. Though this introduces a risk of loss of control should wires come disconnected, it is a small one that should only occur during a catastrophic crash.

## 4.4 Arduino Sketch

A sketch is Arduino-speak for an embedded program written for an Arduino board. There is an Arduino IDE which supports development of sketches in C or C++, and allows one to take advantage of a software library for common I/O interactions. After the code is written in this IDE, it is uploaded to the board over a USB serial

connection. The board will then continuously execute the code found in the sketch's main loop as long as the board is powered. This embedded software interacts with the various sensors and other electronics on a low level, through reading from and writing to the Arduino's digital I/O pins.

One of the standard Arduino libraries is the Servo library. This library allows one to configure a digital pin to output RC control pulses, as explained in section 4.1.1. The sketch used in this project uses this library to specify the speed of each set of wheels driven by the Sabertooth motor driver, and to control the position of the standard servo aiming the ultrasonic range sensor. The motor driver is sent pulses every 20 ms, with HIGH pulses from 1 ms to 2 ms. The standard servo is also sent pulses every 20 ms, with HIGH pulses from 0.75 ms to 2.25 ms as its datasheet specifies.

#### **4.4.1 Ultrasonic Sensor**

The PING))) ultrasonic distance sensor works by emitting a short burst of 40 kHz sound waves and timing the delay before an echo response. The Arduino triggers a ping by generating a brief 5  $\mu$ s (microsecond) pulse on the sensor's bi-directional signal pin. The sensor then generates a HIGH output pulse, which continues until either the echo is received or the maximum amount of time, 18.5 ms, has passed. This time may then be multiplied by the speed of sound in air to calculate an estimated distance of the first object in front of the sensor. [9]

The sketch uses the NewPing library to handle this protocol [3]. This library

provides a convenient method, `ping()` which returns the echo time in  $\mu s$ . The sketch avoids costly floating point computations by sending this echo time over serial rather than a distance.

#### 4.4.2 Servo

The ultrasonic sensor can only detect objects which are roughly straight in front of it. Thus for the rover to have a better approximation of its surroundings, the sensor needs to be panned back and forth. This is what the standard servo it is attached to allows. The sketch makes use of the Servo library to control the servo with R/C pulses. An angular degree from 0 to 180 is written to a Servo object, and the Servo library handles generating the output signal corresponding to that position on the appropriate digital pin.

The sketch sweeps the servo back and forth one degree at a time, and at each step an ultrasonic ping is emitted. The echo time for that ping is measured, and the current values of all sensors are published. This means that the delay between servo steps defines the publishing frequency of sensor data on the Arduino. This delay is currently set to 100 ms, which corresponds to a 10 Hz publishing frequency. The frequency could be increased for future work, but a bare minimum delay of 30 ms is necessary to give the servo time to finish moving, and the PING))) sensor time to recover and prepare for the next ping.

The basic idea is shown in the following code for an arbitrary servo step size:

```

while (servoPos < SERVO_LEFT) {

    sonicServo.write(servoPos); // Set servo position

    timer = millis(); // current time in ms

    while (millis() - timer < SERVO_STEP_DELAY) {

        nh.spinOnce(); // handle callbacks

    }

    ping_time_uS = sonar.ping(); // Get echo time

    publishSensorMessages(servoPos, ping_time_uS);

    servoPos += SERVO_STEP_SZ;

}

```

This code fragment is run inside the sketch's main loop, with a similar while-loop running right after, decrementing the servo position back to SERVO\_RIGHT.

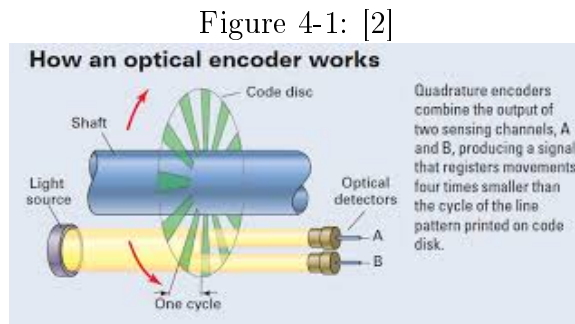
millis() is an Arduino built-in function which uses a hardware timer to count how many milliseconds have passed since the board was turned on. The callback handling that occurs while waiting reads the incoming serial buffer for any data, and if motor commands are found, an appropriate callback function is executed. publishSensorMessages() sends over serial the ping echo time, the servo's current angle, and the tick counts of both encoders. Section 5.2 will further describe how this data is passed between laptop and Arduino.



### 4.4.3 Quadrature Encoders

An important function of the Arduino sketch is to track the movement of the motors. Our system may command the motor driver to move the rover's wheels with a certain fraction of the maximum available power, but it is difficult to predict with precision the resulting angular velocity. For one thing, the RPM of DC motors is proportional to the supplied voltage. But the voltage supplied to the motors through the motor driver is coming from an external li-po battery pack, which generates variable voltage. It starts at 8.4V and drops to a minimum of 6.0V before the motor driver shuts off. Thus even if the same servo control pulse is continuously sent to the motor driver, the motors' angular velocity will decrease over time.

In order to determine the true angular velocity of the motors, rotary encoders are attached to them. These feedback devices are incremental position encoders, meaning they monitor the change in the motor shaft's position compared to some starting position.



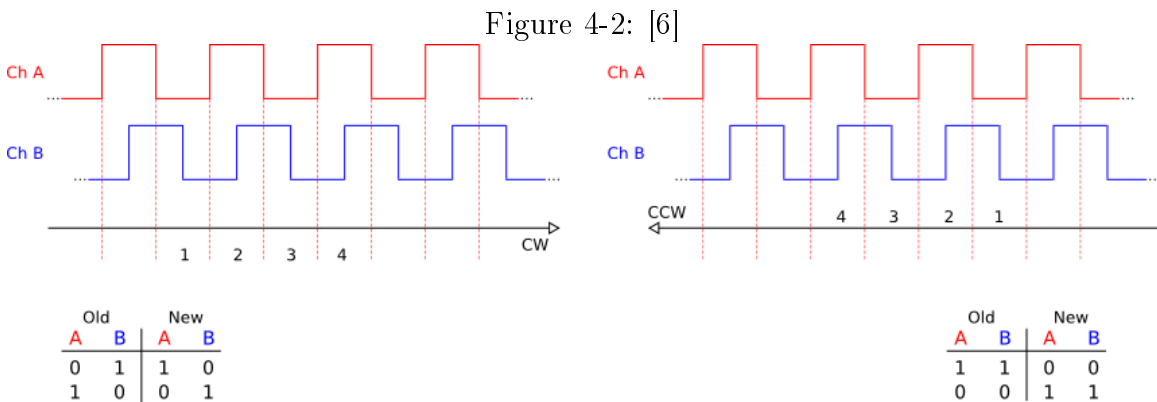
The motor encoders which came with the Lynxmotion rover kit are optical quadrature encoders. This type of encoder attaches a flat disk with thin slits known as the code disk to the motor's gear shaft. Two photodiodes, components which transform light into electric

current, are placed above the disk side by side. A light source shines light through

the disk from the other side. See Figure 4-1 for a visual illustration.

As the motor spins the gear shaft, the code disk turns with it. This produces an on-off pattern of light on the photodiodes, which produce two square waves as signal outputs. These two channels of output pulses are referred to as channels A and B. Depending on the direction of rotation, channel A's square wave will either lag behind or be ahead of channel B. This can be seen in Figure 4-2 which shows example output pulses as a motor turns clockwise (CW) or counter-clockwise (CCW). [6]

The number of slits in the code disk corresponds directly to how many pulses each channel will produce in one revolution of the DC motor. This is known as the pulses per revolution (PPR), and is given by the manufacturer. By counting how many pulses occur in one second, and using the PPR, one can calculate the angular speed of the motor. If one wishes for greater resolution, they can watch each square wave for a change in voltage from LOW to HIGH or HIGH to LOW. This gives a maximum resolution of  $4 * PPR$  detectable position increments per revolution.



Handling rapid changes in voltage is exactly what hardware interrupts are designed for. Unfortunately, for maximum resolution each encoder needs two hardware

interrupt pins, one for each channel. The Arduino Uno only has two hardware interrupt pins, and our rover has two sides. It would be nice if we could at least use two encoders, one for each side.

We achieve this by reacting to changes in voltage in only one channel per encoder. In the two tables in Figure 4-2, LOW voltage values are encoded as 0, and HIGH voltage values as 1. The first plot in the figure shows the output of the two channels when the motor is moving in the CW direction. When channel A transitions from the section labeled 1 to section 2, it is rising from 0 to 1, and channel B has value 0. That information alone tells us that the motor's gear shaft is turning, but not in what direction. However, at the next transition between sections 2 and 3, channel A falls from 1 to 0, and channel B has value 1. Now we are confident that channel B began its pulse after channel A. This means that the photodiode generating channel B detected light after channel A's photodiode, i.e. the code disk is turning in the direction of photodiode A to B. Datasheet specifications will tell us that this translates to the CW direction. It turns out that for each channel A transition event, the previous and new channel values are sufficient to uniquely determine the direction of rotation of the motor. Thus, while only monitoring one of the channels lowers our resolution to  $2 * PPR$  counts per revolution, it allows us to use hardware interrupts for two quadrature encoders rather than only one. [6]

The sketch uses an implementation described in [6], which creates a lookup table using the four binary digits representing the previous and current channel states. These digits form a four-bit binary number, which indexes into a sixteen element array. Each element of this array stores either 1, -1, or 0, where 1 represents a

movement in the CW direction, -1 represents a movement in the CCW direction, and 0 represents an indeterminate transition. This lookup table is then used by the sketch when it reacts to a hardware interrupt caused by the channel A output of one of the encoders. When this interrupt occurs, the code reads the values of channels A and B from the corresponding digital pins, and combines them with the previous values to find the appropriate index in the lookup table. The value at that index is then added to a global counter variable, which keeps track of the net number of incremental movements from the motor's starting position. A net negative number indicates how far the motor has rotated in the CCW direction since it started, and a net positive number indicates how far the motor has rotated in the CW direction. [6]

The implementation described above is shown in the following C code of the ISR for the left encoder. [6]

```
volatile long encLeftCount = 0L;

const int8_t encoder_lookup_table[] =
{0,0,0,-1,0,0,1,0,0,1,0,0,-1,0,0,0};

void encoderLeft_isr() {

static uint8_t encLeft_val = 0;

encLeft_val = encLeft_val << 2;

encLeft_val = encLeft_val |

( ((PIND & 0b100) >> 1) |

((PIND & 0b10000) >> 4) );
```

```
encLeftCount = encLeftCount +  
    encoder_lookup_table[encLeft_val & 0b1111];  
}
```

When the digital pin connected to the left encoder's Channel A output changes, the main loop of the sketch is interrupted, and this ISR is executed. Until this ISR finishes, no other code is run, including other ISRs, though they may be flagged for future execution. Therefore ISRs must be as fast as possible, to not cause any interrupt events to be dropped, and to ensure that the main loop continues running smoothly.

To this end, this ISR makes use of constants and low-level C and avr microcontroller commands to ensure a speedy execution, at the price of readability. `PIND` is an avr command which returns input readings from digital pins 0-7 encoded into a byte. Bit shifting and masking are then used to extract and store the values of pins 2 (channel A) and 4 (channel B) into the two least significant bits of the `encLeft_val` variable. This variable is static, and so retains its value between ISR executions. The count is then incremented according to the lookup table.

When the sketch's main loop publishes sensor readings, it needs to publish the current encoder tick count for the right and left encoders. However, reading from multi-byte variables which are accessed within and without an ISR risks data corruption in the event that the ISR interrupts the main thread in-between readings of bytes. Since the encoder tick count variables are four bytes long, interrupt guards must be used around a read to make it atomic. These guards temporarily stop the custom ISR

from executing while the global variables are copied over to local ones. This is shown for the left encoder count in the following snippet from the sketch:

```
detachInterrupt(digitalPinToInterrupt(encLeftAPin));  
encMsg.leftTicks = encLeftCount;  
attachInterrupt(digitalPinToInterrupt(encLeftAPin),  
    encoderLeft_isr, CHANGE);  
t = 0;
```

Similar guards are used for the right encoder count variable.

Because we are turning interrupts off briefly, there is the risk that we could miss an interrupt event on one of the channel A pins. Missing an edge pulse from one of the encoders would not only lose that tick, but would also throw off the next value we index into the lookup table. Luckily, the Arduino has a single-bit interrupt event flag for every interrupt event. Therefore in the worst case scenario, an encoder interrupt event occurs just after the ISR handler is detached, and that event is flagged. As long as the ISR is reattached and handles that flag before a second interrupt event occurs, there won't be a problem. After reattaching the ISR, the next program instruction is guaranteed to be executed before handling any flagged events. To ensure speedy handling of a flagged event, a meaningless assignment of zero is made to the local variable `t`.

Let's calculate how often each interrupt event occurs. Each encoder generates 100 pulses per revolution. We will only be watching one of the square waves (output

channel A), so that's 200 edge transitions per revolution. The motors are rated for 200 rpm, so at maximum speed the two encoders would revolve less than 3.4 times per second. So there will be at most

$$3.4 \text{ rev/sec} * 200 \text{ events/rev} = 680 \text{ events/sec}$$

Meaning we are guaranteed to have at least  $1/680 \approx 1.4 \text{ ms}$  between encoder interrupt events.

So the interrupt guards need to take significantly less than  $1.4 \text{ ms}$  in order to allow a flagged interrupt event to be handled before the next event occurs. Each global encoder count variable is four bytes, so assignment compiles to four machine instructions. The assignment of zero to the one-byte variable `t` takes one machine instruction. The helper macro `digitalPinToInterrupt()` is a preprocessor `#define`, and so takes zero machine instructions. Therefore there are five total machine instructions executed before the ISR is executed. The Arduino Uno uses a 16 MHz quartz timing crystal, so executing one instruction takes

$$1/(16000000 \text{ Hz}) = 0.000000625 \text{ seconds} = 62.5 \text{ nanoseconds}$$

Thus to run the five instructions takes  $5 * 62.5 \text{ ns} = 0.3125 \text{ }\mu\text{s}$ . Then the flagged event must be handled. External interrupt calling has an overhead of  $5.125 \text{ }\mu\text{s}$ , to enter and leave the function [7]. Thus as long as the ISR executes in less than  $1.4 \text{ ms} - 0.0003125 \text{ ms} - 0.005125 \text{ ms} = 1.3945625 \text{ ms}$ , the sketch will never miss an

encoder event. Testing of the ISR indicates that this is an order of magnitude more time than needed.



# Chapter 5

## ROS

### 5.1 Overview

The Robot Operating System (ROS) is a meta operating system for open-source robotics.

- package management

- asynchronous messaging between components

#### 5.1.1 Messages

- publishing and subscribing messages

#### 5.1.2 Topics

All software components in this project communicate using the asynchronous, distributed framework supported by ROS.

- many to many

ROS Master, like a DNS server node to node, TCP/IP sockets

### **5.1.3 Packages**

contain nodes, message definitions, and service files There are also meta-packages which are, simply enough, collections of related packages.

### **5.1.4 Nodes**

processes

### **5.1.5 Launch Files**

XML launch files systems get complicated, with dozens of nodes nobody wants to go through and manually start all those up, so it makes sense to streamline and aggregate startup (launch) files for all of them in the same place allows bringing multiple nodes up at once, and also specifying their parameters in YAML files

### **5.1.6 Frames**

coordinate axes reference frames position and orientation quaternion vectors represent orientation messages have `frame_ids` detailing which frame they are in

### **5.1.7 Transforms**

conversions between frames handled by the ROS package `tf` broadcasting transforms

## 5.1.8 User defined packages

auto\_rover package

## 5.2 roserial

Communication between the Arduino and laptop is handled with the ROS meta-package roserial. Different client packages support different client machines, such as embedded linux devices, or different microcontroller boards. These client packages create local support libraries or header files on those machines, which use a serialization protocol to send and receive ROS messages over a serial port. On the other side of the serial connection, host packages run a bridging node which communicates with the ROS network on behalf of the client machine. Subscribed topics have their messages serialized and sent to the client machine, and outgoing messages from the client are de-serialized and published.

### 5.2.1 roserial\_arduino

roserial\_arduino is one client package of roserial, which creates an Arduino library to provide bare-bones ROS support to sketches. The sketch running on this project's Uno board uses this library to publish sensor data as messages, and subscribe to motor command topics.

Every time the sketch wishes to update the laptop with its newest sensor readings, it publishes three messages. First the servo angle in degrees is published to the `"/ping/angleDeg"` topic, as a standard Int8 message. This message just contains

a single data field: an 8-bit signed integer. Next the echo time in microseconds is published to the `"/ping/timeUS"` topic, as a standard `UInt16` message which contains a single 16 bit data field representing an unsigned integer. Lastly the two encoder tick counts are both placed into a single custom message called `EncCount`, and published to the `"/odom/encTicks"` topic. This custom message type has two 32 bit fields, one for each encoder. This message type will be further explained in section 5.6.1.

When the sketch is waiting between updates, it continually listens to the serial port for motor commands. These commands are `Int8` messages on the `"/cmd/left"` or `"/cmd/right"` topics, which the sketch subscribes to. When these messages are found in the serial input buffer, a short callback function is executed, which writes the R/C pulse command to the proper motor channel.

Arduino boards use different types of memory. Flash memory is used to store sketch code, and static random access memory (SRAM) is used to store dynamic variables at runtime. The Uno has 32kB of flash memory, but only 2kB of SRAM. The `roscpp` Arduino library is large, and takes up quite a lot of SRAM space. Its input and output serial buffers alone use 560 bytes. This makes running out of space for local variables quite easy, which can lead to instability and crashes when running the sketch. To save space, a modified version of `roscpp_arduino` which supports storing constant strings in flash memory rather than SRAM has been used. Since topic names and error messages use long descriptive strings, this saves several hundred kB of space in SRAM and ensures the sketch's stability.

The `roscpp` Arduino library abstracts away most of the serial communication protocol, but does allow the baud rate to be specified. In this use case, baud rate is

equivalent to bits per second. The more bits per second sent over serial, the more frequently the microcontroller needs to sample the incoming and outgoing line. So the baud rate cannot be set arbitrarily high, as the Uno has a limited clock speed. If it is set too low, however, then the stream of sensor data being published would overwhelm the connection. Significantly less data will be streaming in than transmitted out, so the amount of outgoing data is the deciding factor. Thus to calculate an appropriate baud rate, the amount of sensor data transmitted per second must be known.

rosserial uses a serial protocol with 8 bytes of overhead for every message. Each sensor update publishes three messages: an eight-byte EncCount message, a one-byte Int8 message, and a two-byte UInt16 message. This means that each update pushes 11 bytes of data in three messages, with 24 bytes of overhead. Thus a total of 35 bytes are sent over serial.

Since the PING))) sensor requires a minimum delay of 30 ms between pings, the sketch cannot publish its sensor values at a rate higher than 33 Hz. Therefore the sketch will not push more than:

$$33 \text{ Hz} * 35 \text{ Bytes} = 1155 \text{ Bytes per second (Bps)}$$

The Uno uses one start bit and one stop bit to surround each byte of information sent over serial. Thus it takes 10 bits to send one byte of information. Therefore the minimum baud rate required is:

$$1155 \text{ Bps} * 10 \text{ bits per byte} = 11550 \text{ bits per second}$$

We'll choose a standard baud rate of 28,800 to more than double that for some breathing room, and to account for the fact that the `rosserial` Arduino library occasionally transmits time-keeping and synchronization messages of its own.

### 5.2.2 `rosserial_python`

`rosserial_python` is one host package of `rosserial`, which acts as a bridge between the Arduino and the ROS network. It runs a node on the laptop which communicates with the Arduino using the `rosserial` protocol. It automatically handles setup, communication with the ROS master, subscription, and publishing on behalf of the Arduino. When launched, the serial node must be configured to use the same baud rate as the Arduino: 28,800. It must also be configured to connect to whichever serial port name the Arduino uses. For simplicity, a symbolic link was created using a `udev` rule on the laptop, to ensure that the port name will always be accessible as `"/dev/arduino"`.

## 5.3 `differential_drive`

The `differential_drive` package was created by Jon Stephan to create a simple interface for controlling a differential-drive robot [1]. Differential drive is . Because the rover has four wheels, turning in-place involves wheel slippage. This is referred to as a skid-steering design.

(high variance in odometry tick count readings)

forked from

modified to use EncCount messages

### **5.3.1 diff\_tf**

The diff\_tf node modified to not publish a transform We use a simple rolling average with the kinematics equations for a differential drive robot (an approximation of our skid-steering rover), where the two imaginary wheels on both side of the rover are assumed to 'exist' at an average position of the two actual wheels. This average then gives us an estimate of the position and velocity of our rover, which we publish in an Odometry message. This odometry message is essentially dead reckoning, and is one of the inputs fused into the state estimation node.

produce odometry messages from encoder ticks

encoder ticks per meter must be calibrated

covariance matrix

### **5.3.2 virtual\_joystick**

generate twist messages, like the ROS navigation stack would

### **5.3.3 twist\_to\_motors**

translate twist messages to motor velocities for each motor channel, publish those

### 5.3.4 pid\_velocity

translate motor velocities to actual motor commands, which roserial\_python will transmit over serial to the arduino

### 5.3.5 Encoder Calibration

### 5.3.6 PID Parameter Tuning

## 5.4 Ros Sensors App

Android app to publish IMU and GPS data from a smartphone.

phone frame

### 5.4.1 GPS

GPS receivers background

navsatfix message covariance matrix

### 5.4.2 IMU

IMU chips background: magnetometers, accelerometers, gyroscopes what a quaternion is

publishes IMU message

IMU messages are expected to be in ENU reference frame, instead of NED.

Android TYPE\_ROTATION\_VECTOR sensor fuses magnetometer and accelerometer data to produce an quaternion representation of an orientation in the ENU frame.



Android accelerometer readings tell us the linear acceleration of the rover, but are reported with respect to the local orientation of the phone, and so the node converts them to the ENU orientation before publishing them, in the phone frame (which just specifies a static translation)

Android gyroscope readings tell us the angular velocity of the rover, but are reported with respect to the local axes of the phone. However, our rover operates solely in 2D, and so we aren't interested in angular velocities of roll or pitch. And since the phone lays face-up on top of the rover, the phone's local z axis is the same as the ENU up axis, and so we don't need to transform the gyroscope reading for rad/sec rotation of yaw.

covariance matrices

### 5.4.3 How to use

usb tethering on linux

## 5.5 robot\_localization package

package for state estimation

[12]

### 5.5.1 Data Format Conventions

REP-103 and REP-105 for conventions true north, magnetic declination

## 5.6 auto\_rover

custom package this is where custom message type, EncCount is defined, and header files are created

### 5.6.1 EncCount

### 5.6.2 range\_converter

ping sensor at ultrasound frame

Adjust code for conversion of ultrasonic sensor ping times to distance, to take into account the ambient air temperature If an echo has been received, then the speed of sound in air in m/s,  $C_{air}$ , is calculated using the current air temperature in Celsius  $T_C$ :

$$C_{air} = 331.5 + (0.6 * T_C) *$$

Multiplying  $C_{air}$  by the duration of the timed output pulse gives the estimated distance of the first object in front of the sensor.

Subscribes to /ping/timeUS and /ping/angleDeg topics, reads servo angle and ping time from those topics. Those messages sent from arduino to minimize amount of data being sent over serial. Then this node converts that to a distance in meters and an ultrasound -> base\_link transform. transform uses static translation from center of rover to center of PING))) sensor, as well as instantaneously changing rotation at each ping snapshot.

### 5.6.3

First `ekf_localization` node takes in odometry estimate from wheel encoders via `diff_tf` node, and IMU message from phone node. Produces a fused estimate of odometry.

`navsat_transform_node` takes in odometry message from first `ekf` node, which is the robot's current position estimate in the frame specified by its start location. It also takes in the `navsatfix` and `imu` messages from the phone, and fuses all these to produce a different odometry estimate which is the gps data converted to the coordinates of the robot's world frame.

Second `ekf_localization` node fuses the gps and odometry outputs from the previous two nodes into a final odometry message which is the final estimation of the robot's current state.

[12]

# Chapter 6

## Future Steps

### 6.1 Field Test scenario

#### 6.1.1 Results

Used virtual\_joystick node with other differential\_drive control nodes to drive rover around a parking lot. Recorded data into a ROS bag file, which is ...

here is route fitted on top of satellite image of that parking lot:

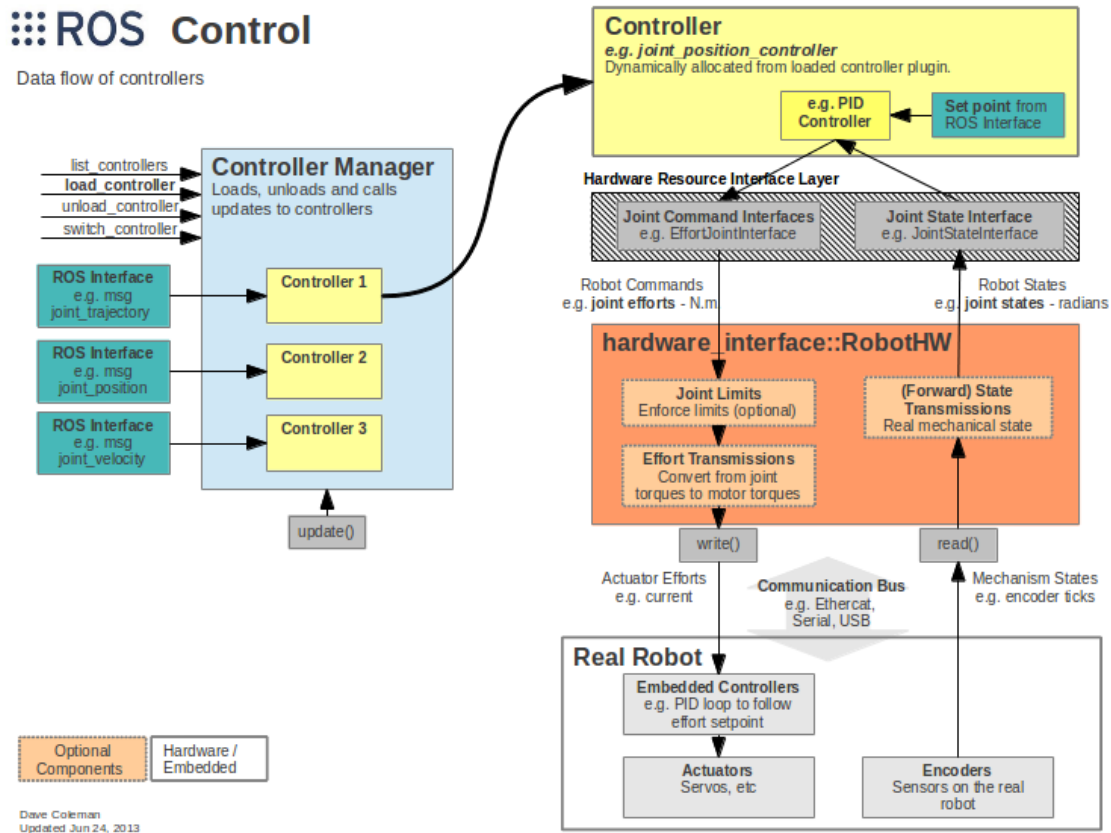
### 6.2 ROS Navigation Stack

#### 6.2.1 ros\_controller

#### 6.2.2 GPS Waypoints

GPS markers form a linearized path travel in a straight line from one GPS node to another

Figure 6-1: ROS control overview [1]



## 6.3 Project Limitations

how this project is limited

introduction of a camera, but attaching a webcam directly to the chassis of the robot would be troublesome to work with, sense there would be no shock absorption and the video frames would wobble.

Integration of GPS data into position estimate causes discrete jumps, may make it unsuitable for use in the navigation stack. Solution: ditch GPS, use range data from ultrasonic sensor with amcl

## 6.4 Conclusion

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