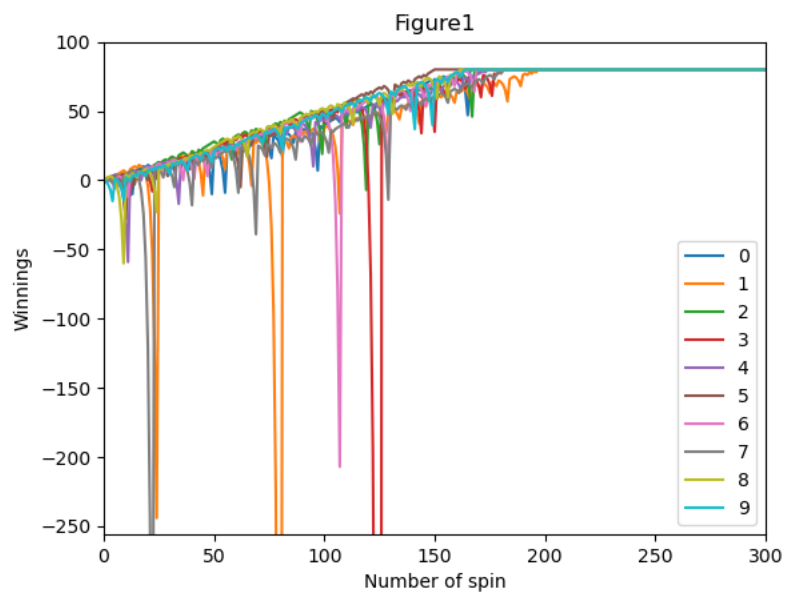
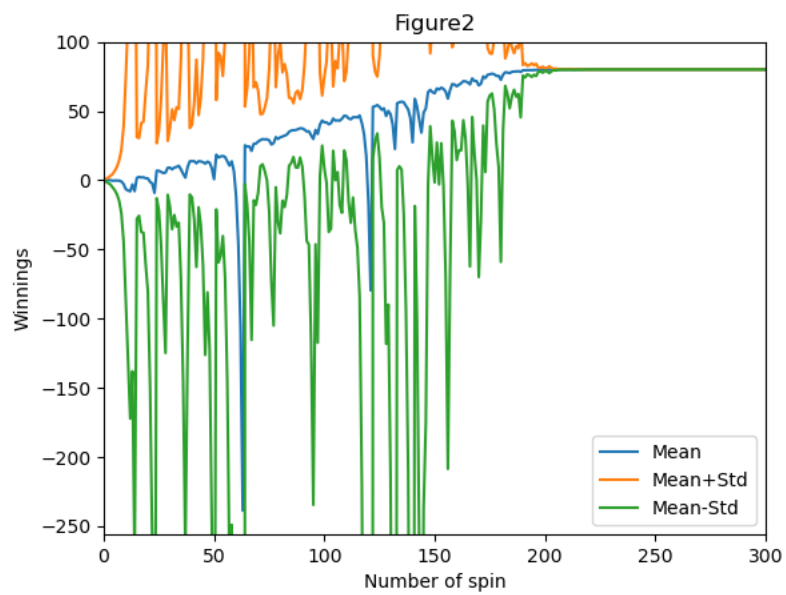
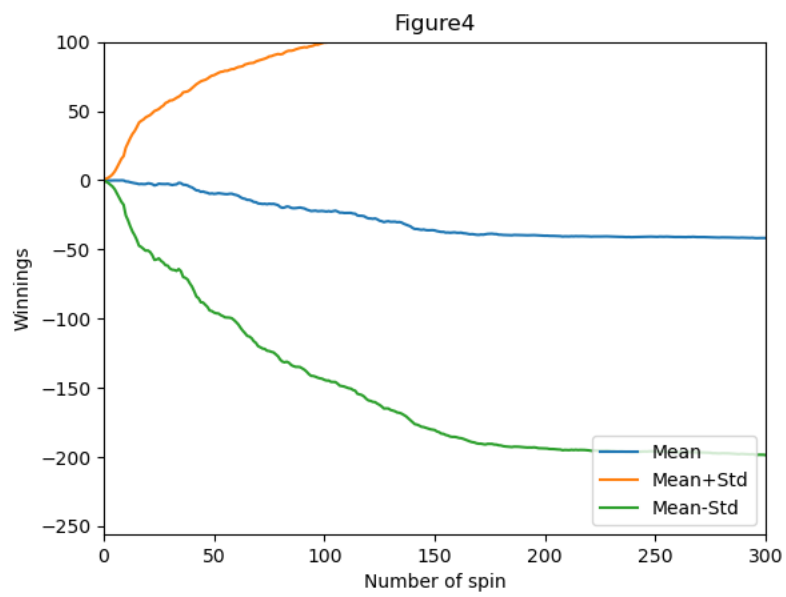
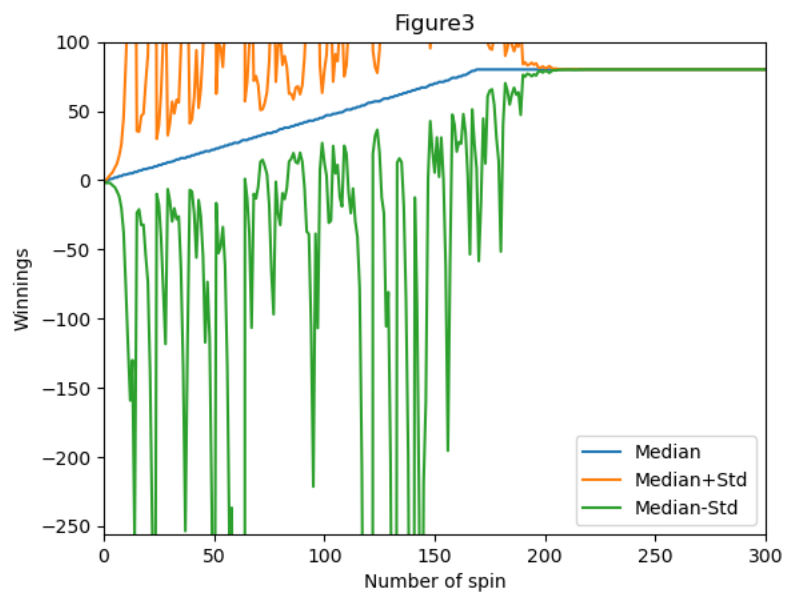


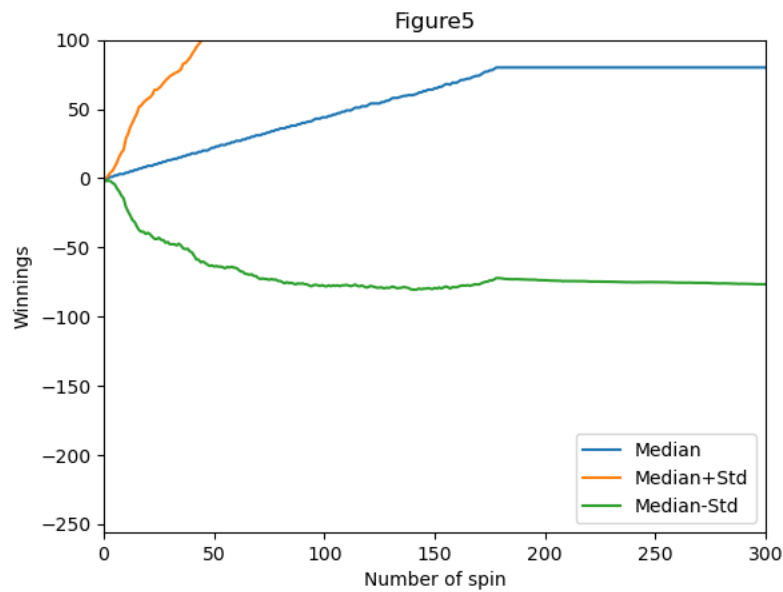
1. The probability of winning \$80 within 1000 sequential bets. So, if we reach 80 won spins in the first 1000 rolls, then we are done (since we will have won \$80). Then the problem reduces to using the binomial distribution (or in this case you could also approximate it with the normal distribution) with $p=0.474$, $n=1000$ and solving for $P(X \geq 80)$. This will be an incredibly high probability essentially 1. So the chance of not getting to \$80 is essentially 0 as you already realized. The betting strategy in experiment 1 generates \$1 for every win and effectively does not create a loss for an incorrect bet. That means we have to lose 921 times to win less than \$80. The odds for that are $(20/38)^{921}$, or one could also say non-existent.
2. Based on the previous answer's reasoning, we have an expected value of \$1 times $18/38$ or \$0.47 per bet. That means the expected value is \$470 for 1000 consecutive bets. Since the limit is \$80, all graphs end at that value. If we increase the limit to \$1000 and change the graph's dimensions, we can see that \$470 is the area where the winnings graphs end.
3. The more sequential bets reach their final value of \$80, the more the standard deviation stabilizes and eventually goes to zero. The more bets are ongoing, the higher the chances that one of them goes on a losing streak, which results in a significant standard deviation. Therefore, the maximum standard deviation is likely to occur between the first couple of bets (so that a losing streak can build up), but before many bets reach \$80.
4. We start at \$256. After losing eight times (nine times if we have already built some bankroll), we go bankrupt. Consequently, we are at 0.59% $((20 / 38) ** 8)$ risk to lose everything for each dollar we want to earn. Therefore, the probability of winning \$80 is 0.9941^{80} or 62.34%.
5. According to the previous question's answer, we have a 62.34% chance to win \$80, which leaves us with 27.66% to lose \$256. Accordingly, the expected value is $0.6234 * \$80 - 0.3766 * \$256 = -\$46.53$. This result seems to match our experiment. After 300 bets, we are on average at -\$40, and when we extend the timescale to 1000 bets, the graph converges towards \$45.
6. The standard deviation reaches a maximum value and stabilizes once all runs have either bankrupted or reached the \$80 goal.



7.







8. I learned a lot about coding in python, statistical analysis, as well as betting odds. I have not done anything like this before, and this was a really cool project to work on. I have always been interested in financial analysis and its intersection with coding, so this project and class in general are very interesting to me. I am surprised at the odds of certain things, such as the answers provided above.