## Matrix Multiplication

- 1. Inner Product (Row by column)
  - a) Given two matrices A and B, the (i, j) entry of AB is the inner product of row i of A and column j of B
- 2. Linear combination of columns
- 3. Linear combination of rows
- 4. Summation of matrices (Column by row)

a) 
$$AB = a_1b_1^T + a_2b_2^T + \dots + a_nb_n^T$$

- 5. Block Multiplication
  - a) Multiply as the small matrices are scalars
  - b) Matrix multiplication is the composition of two linear functions
- 6. Symmetric Matrix
  - a)  $A^T = A$
  - b)  $AA^T$  and  $A^TA$  are square and symmetric