## 第十二章 三相正弦稳态电路

- 1 三相电源
- 2 负载星形联接的三相电路分析
- 3 负载三角形联接的三相电路分析
- 4 三相电路的功率

## 1 三相电源

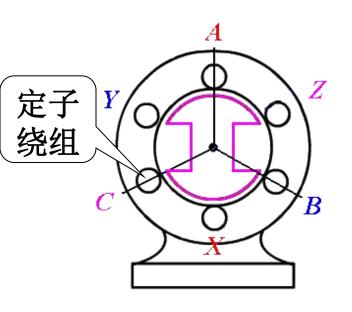
三相制电力系统:由三个频率相同、振幅相同、相位互差 120°的正弦交流电源供电的系统。又 称三相电路。

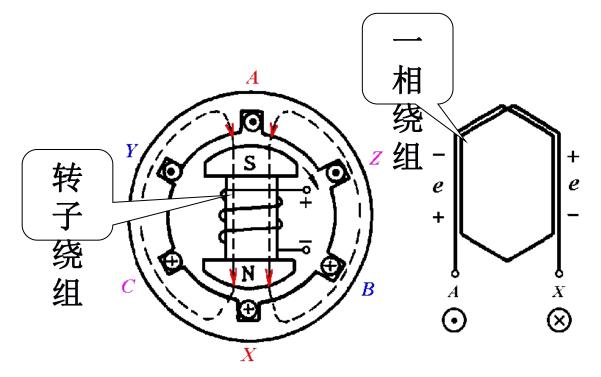
三相电力系统组成:由三相电源、三相负载和三相输电线路 三部分构成。

研究三相电路要注意其特殊性:

- (1) 特殊的电源; (2) 特殊的负载;
- (3) 特殊的连接; (4) 特殊的求解方式。

## 一、对称三相电源





## 1. 瞬时值表达式

$$u_{\rm A} = U_{\rm m} \sin(\omega t + 0^{\circ})$$

$$u_{\rm B} = U_{\rm m} \sin{(\omega t - 120^{\circ})}$$

$$u_{\rm C} = U_{\rm m} \sin(\omega t + 120^{\circ})$$

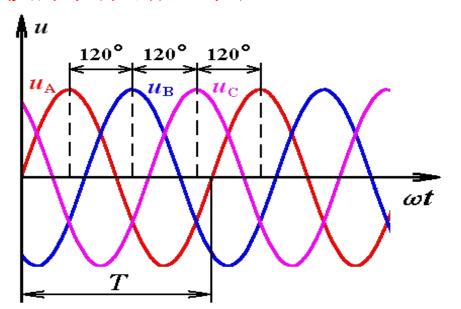
#### 2. 相量表示式

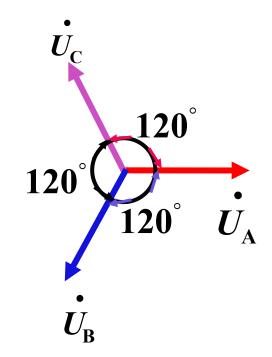
$$\dot{U}_{A} = U \angle 0^{\circ} \quad \mathbf{V}$$
 $\dot{U}_{B} = U \angle -120^{\circ} = U \angle 240^{\circ} \quad \mathbf{V}$ 

$$U_{\rm C} = U \angle -240^{\rm o} = U \angle 120^{\rm o} \ {
m V}$$

## 一、对称三相电源

## 3. 波形图及相量图





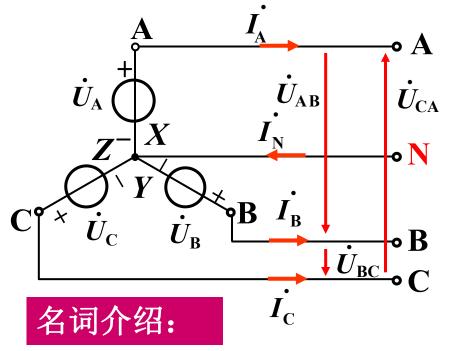
## 4. 三相对称交流电源的特征

- (1) 有效值相等,即:  $U_A = U_B = U_C = U$
- (2) 频率相等,即:  $f_A = f_B = f_C = f = 50$ Hz
- (3) 相位按相序依次互差120°,即:  $\varphi = 120^\circ$

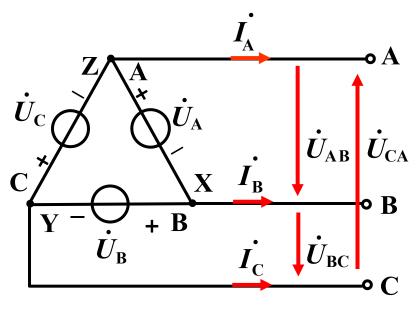
(4) 
$$u_A + u_B + u_C = 0$$
  $U_A + U_B + U_C = 0$ 

## 二、三相电源的联接

1. 星形(Y)联接:



2. 三角形(△)联接



- ① 端线(火线) ② 中线(零线) ③ 三相三线制、三相四线制
- ④ 线电压:端线与端线之间的电压。 $\dot{U}_{
  m AB}$ 、 $\dot{U}_{
  m BC}$ 、 $\dot{U}_{
  m CA}$
- ⑤ 相电压: 每相电源(负载)的电压。

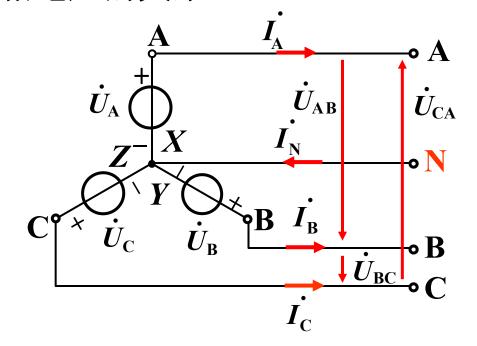
Y接:  $u_{AN}$ 、 $u_{BN}$ 、 $u_{CN}$ 

∆接: u<sub>AB</sub>、u<sub>BC</sub>、u<sub>CA</sub>

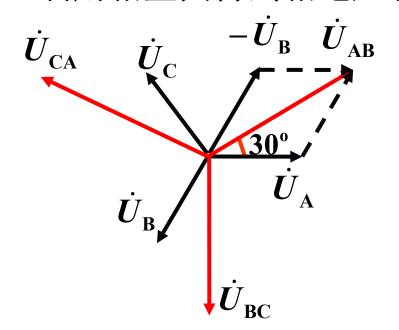
#### 三、三相对称电源线电压与相电压的关系

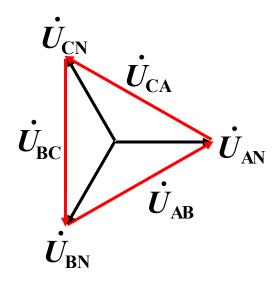
## 1. 星形(Y)联接:

$$\dot{U}_{\mathrm{AN}} = U \angle 0^{\mathrm{o}} \, \mathrm{V}$$
  $\dot{U}_{\mathrm{BN}} = U \angle -120^{\mathrm{o}} \, \mathrm{V}$   $\dot{U}_{\mathrm{CN}} = U \angle 120^{\mathrm{o}} \, \mathrm{V}$ 



# 三、三相对称电源线电压与相电压的关系 利用相量图得到相电压和线电压之间的关系:





#### 一般表示为:

$$\dot{U}_{\mathrm{AB}} = \dot{U}_{\mathrm{AN}} - \dot{U}_{\mathrm{BN}} = \sqrt{3}\dot{U}_{\mathrm{AN}} \angle 30^{\mathrm{o}}\,\mathrm{V}$$
 $\dot{U}_{\mathrm{BC}} = \dot{U}_{\mathrm{BN}} - \dot{U}_{\mathrm{CN}} = \sqrt{3}\dot{U}_{\mathrm{BN}} \angle 30^{\mathrm{o}}\,\mathrm{V}$ 
 $\dot{U}_{\mathrm{CA}} = \dot{U}_{\mathrm{CN}} - \dot{U}_{\mathrm{AN}} = \sqrt{3}\dot{U}_{\mathrm{CN}} \angle 30^{\mathrm{o}}\,\mathrm{V}$ 

## 结论

## 三、三相对称电源线电压与相电压的关系

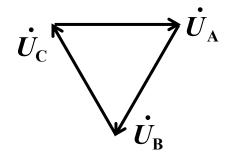
 三角形(△)联接 由接线方式可知:

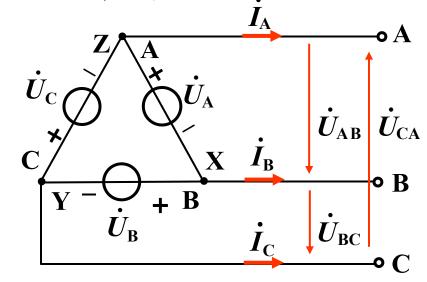
## 线电压等于对应的相电压

设:
$$\dot{U}_{A} = U \angle 0^{\circ} V$$

$$\dot{U}_{\rm B} = U \angle -120^{\rm o} \ {
m V}$$

$$\dot{U}_{\rm C} = U \angle 120^{\rm o} \ {\rm V}$$



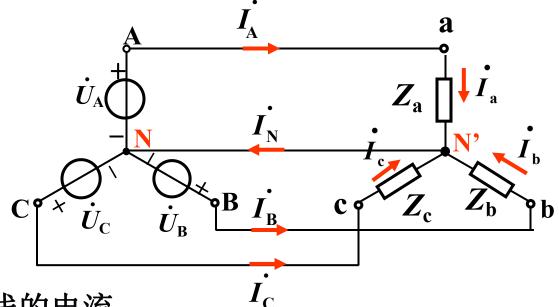


得: 
$$\dot{U}_{AB}$$
 =  $\dot{U}_{A}$  =  $U \angle 0^{\circ}$  V  $\dot{U}_{BC}$  =  $\dot{U}_{B}$  =  $U \angle -120^{\circ}$  V  $\dot{U}_{CA}$  =  $\dot{U}_{C}$  =  $U \angle +120^{\circ}$  V

## 2 负载星形联接的三相电路分析

一、三相四线制系统

#### 名词介绍:



线电流:流经端线的电流。

$$i_{A}$$
、 $i_{B}$ 、 $i_{C}$  或  $i_{A}$ 、 $i_{B}$ 、 $i_{C}$ 

相电流:流过每相负载的电流。

$$i_a$$
、 $i_b$ 、 $i_c$  或  $i_a$ 、 $i_b$ 、 $i_c$ 

中线电流:流过中线的电流  $i_N$ 

特点:

$$1) I_{\rm P} = I_{\rm L}$$

2) 
$$\dot{I}_{N} = \dot{I}_{a} + \dot{I}_{b} + \dot{I}_{c}$$

分析: 三相电路的解题关键, 找准相电压

$$\dot{I}_{a} = \frac{\dot{U}_{A}}{Z_{a}}$$
  $\dot{I}_{b} = \frac{\dot{U}_{B}}{Z_{b}}$   $\dot{I}_{c} = \frac{\dot{U}_{C}}{Z_{c}}$ 

1. 三相负载不对称,即:

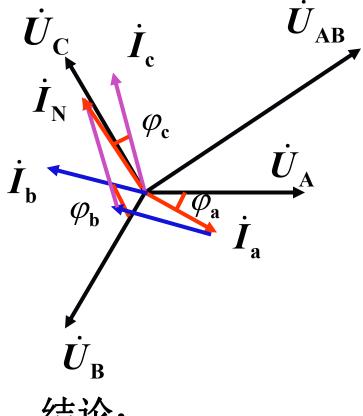
$$Z_{a} = |Z_{a}| \angle \varphi_{a}$$
  $Z_{b} = |Z_{b}| \angle \varphi_{b}$   $Z_{c} = |Z_{c}| \angle \varphi_{c}$ 

1) 
$$I_{a} = U_{A} / |Z_{a}| = I_{A}$$

$$I_{b} = U_{B} / |Z_{b}| = I_{B}$$

$$I_{c} = U_{C} / |Z_{c}| = I_{C}$$
2)  $\dot{I}_{N} = \dot{I}_{a} + \dot{I}_{b} + \dot{I}_{c} \neq 0$ 

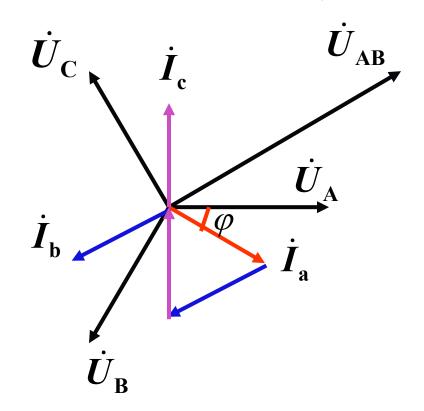
三相负载不对称 电压和电流的相量图



结论:

$$\dot{\boldsymbol{I}}_{\mathrm{N}} = \dot{\boldsymbol{I}}_{\mathrm{a}} + \dot{\boldsymbol{I}}_{\mathrm{b}} + \dot{\boldsymbol{I}}_{\mathrm{c}} \neq \boldsymbol{0}$$

## 三相负载对称 电压和电流的相量图



结论:

$$\dot{\boldsymbol{I}}_{\mathrm{N}} = \dot{\boldsymbol{I}}_{\mathrm{a}} + \dot{\boldsymbol{I}}_{\mathrm{b}} + \dot{\boldsymbol{I}}_{\mathrm{c}} = \boldsymbol{0}_{_{11}}$$

2. 当三相负载对称时,有:

$$Z_{a} = Z_{b} = Z_{c} = |Z| \angle \varphi$$

$$\therefore \dot{\boldsymbol{I}}_{a} = \frac{\dot{\boldsymbol{U}}_{A}}{\boldsymbol{Z}_{a}} = \frac{\boldsymbol{U}}{|\boldsymbol{Z}|} \angle - \varphi$$

$$\dot{\boldsymbol{I}}_{b} = \frac{\dot{\boldsymbol{U}}_{B}}{\boldsymbol{Z}_{b}} = \frac{\boldsymbol{U}}{|\boldsymbol{Z}|} \angle (-\varphi - 120^{\circ})$$

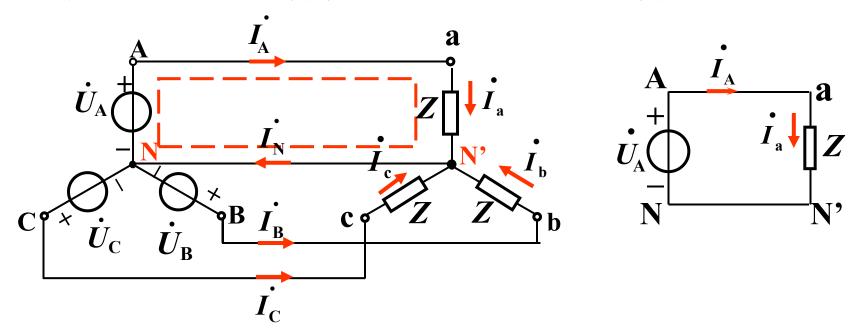
$$\dot{\boldsymbol{I}}_{c} = \frac{\dot{\boldsymbol{U}}_{C}}{\boldsymbol{Z}_{c}} = \frac{\boldsymbol{U}}{|\boldsymbol{Z}|} \angle (-\varphi + 120^{\circ})$$

1) i<sub>a</sub>、i<sub>b</sub>、i<sub>c</sub>为三相对称电流; 结论:

2) 
$$I_{\rm a} = I_{\rm b} = I_{\rm c} = U_{\rm P}/|Z| = U_{\rm L}/\sqrt{3}|Z|$$

3) 
$$\dot{I}_{N} = \dot{I}_{a} + \dot{I}_{b} + \dot{I}_{c} = 0$$

可将三相电路的计算简化为单相电路的计算



由一相计算电路可得:

同理 
$$\dot{I}_{\mathrm{B}} = \dot{I}_{\mathrm{b}} = \frac{\dot{U}_{\mathrm{b}\,\mathrm{N'}}}{Z} = \frac{\dot{U}_{\mathrm{B}}}{Z}$$

$$\dot{I}_{A} = \dot{I}_{a} = \frac{\dot{U}_{aN'}}{Z} = \frac{\dot{U}_{A}}{Z}$$

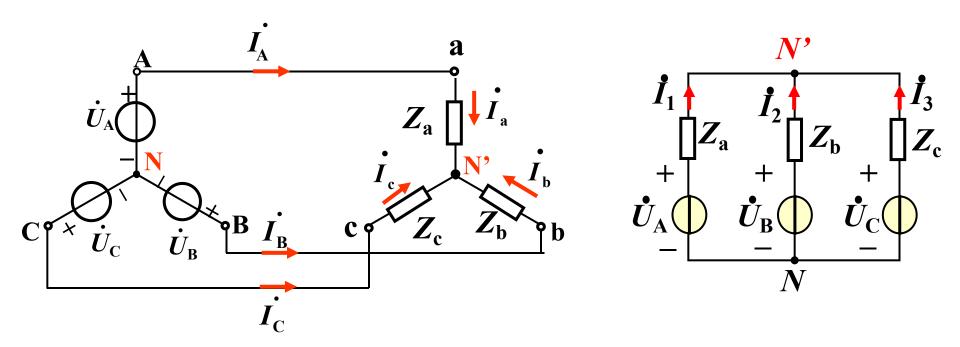
$$\dot{\boldsymbol{I}}_{\mathrm{C}} = \dot{\boldsymbol{I}}_{\mathrm{c}} = \frac{\dot{\boldsymbol{U}}_{\mathrm{c}\,\mathrm{N'}}}{\boldsymbol{Z}} = \frac{\dot{\boldsymbol{U}}_{\mathrm{C}}}{\boldsymbol{Z}}$$

## 结论

- 1.  $U_{N'N}=0$ ,电源中点与负载中点等电位。有无中线对电路情况没有影响。
- 2. 对称情况下,各相电压、电流都是对称的,只要 算出某一相的电压、电流,则其他两相的电压、 电流可直接写出。
- 3. Y形联接的对称三相负载,其相、线电压、电流的 关系为:

$$\dot{U}_{ab} = \sqrt{3}\dot{U}_{aN'} \angle 30^{\circ} \text{ V} \qquad \dot{I}_{A} = \dot{I}_{a}$$

## 二、三相三线制 (Y-Y)



以N点为参考点,对N'点列写节点方程:

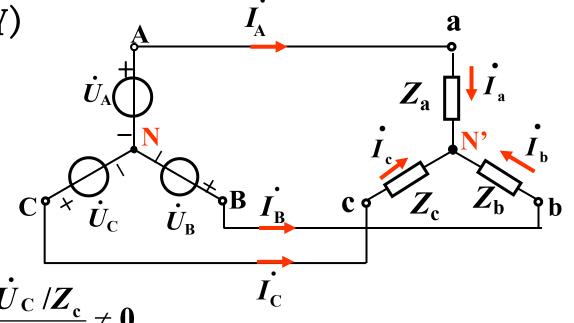
$$\dot{\boldsymbol{U}}_{\mathbf{N'N}} = \frac{\frac{\dot{\boldsymbol{U}}_{\mathbf{A}}}{\boldsymbol{Z}_{\mathbf{a}}} + \frac{\dot{\boldsymbol{U}}_{\mathbf{B}}}{\boldsymbol{Z}_{\mathbf{b}}} + \frac{\dot{\boldsymbol{U}}_{\mathbf{C}}}{\boldsymbol{Z}_{\mathbf{c}}}}{\frac{1}{\boldsymbol{Z}_{\mathbf{a}}} + \frac{1}{\boldsymbol{Z}_{\mathbf{b}}} + \frac{1}{\boldsymbol{Z}_{\mathbf{c}}}}$$

## 二、三相三线制 (Y-Y)

## 分析:

1. 三相负载不对称

$$Z_a \neq Z_b \neq Z_c \neq |Z| \angle \varphi$$



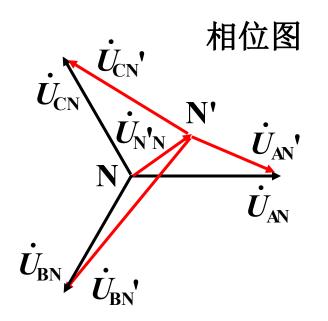
$$\dot{U}_{\mathrm{N'N}} = \frac{\dot{U}_{\mathrm{A}}/Z_{\mathrm{a}} + \dot{U}_{\mathrm{B}}/Z_{\mathrm{b}} + \dot{U}_{\mathrm{C}}/Z_{\mathrm{c}}}{1/Z_{\mathrm{a}} + 1/Z_{\mathrm{b}} + 1/Z_{\mathrm{c}}} \neq 0$$

负载各相电压:

$$\dot{\boldsymbol{U}}_{\mathrm{AN}}' = \dot{\boldsymbol{U}}_{\mathrm{AN}} - \dot{\boldsymbol{U}}_{\mathrm{N}}'_{\mathrm{N}}$$

$$\dot{\boldsymbol{U}}_{\mathrm{RN}}' = \dot{\boldsymbol{U}}_{\mathrm{RN}} - \dot{\boldsymbol{U}}_{\mathrm{N}'\mathrm{N}}$$

$$\dot{\boldsymbol{U}}_{\mathrm{CN}}$$
' =  $\dot{\boldsymbol{U}}_{\mathrm{CN}}$  -  $\dot{\boldsymbol{U}}_{\mathrm{N}}$ 'N



中性点位移

负载中点与电源中点不重合

## 二、三相三线制(Y-Y)

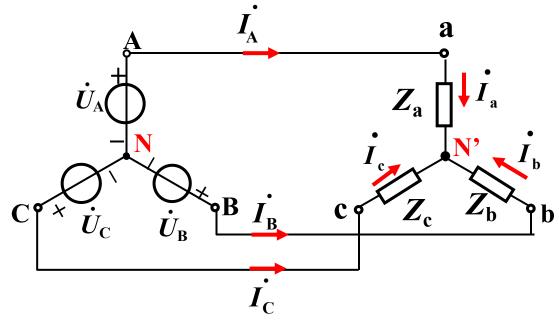
## 分析:

1. 三相负载不对称

各相电流为

$$\dot{\boldsymbol{I}}_{\mathrm{A}} = \dot{\boldsymbol{I}}_{\mathrm{a}} = \frac{\boldsymbol{U}_{\mathrm{A}} - \boldsymbol{U}_{\mathrm{N'N}}}{\boldsymbol{Z}_{\mathrm{a}}}$$

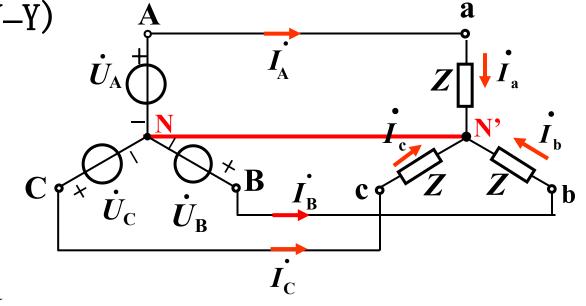
$$\dot{\boldsymbol{I}}_{\mathrm{B}} = \dot{\boldsymbol{I}}_{\mathrm{b}} = \frac{\dot{\boldsymbol{U}}_{\mathrm{B}} - \dot{\boldsymbol{U}}_{\mathrm{N'N}}}{\boldsymbol{Z}_{\mathrm{b}}}$$



$$\dot{\boldsymbol{I}}_{\mathrm{C}} = \dot{\boldsymbol{I}}_{\mathrm{c}} = \frac{\dot{\boldsymbol{U}}_{\mathrm{C}} - \dot{\boldsymbol{U}}_{\mathrm{N'N}}}{\boldsymbol{Z}_{\mathrm{c}}}$$

分析:

2. 三相负载对称



$$: \dot{U}_{N'N} = \frac{\frac{\dot{U}_{A}}{Z_{a}} + \frac{\dot{U}_{B}}{Z_{b}} + \frac{\dot{U}_{C}}{Z_{c}}}{\frac{1}{Z_{b}} + \frac{1}{Z_{c}}} = \frac{\frac{1}{Z}(\dot{U}_{A} + \dot{U}_{B} + \dot{U}_{C})}{\frac{3}{Z}} = 0$$

$$\therefore \dot{I}_{A} = \dot{I}_{a} = \frac{\dot{U}_{A}}{Z} \qquad \dot{I}_{B} = \dot{I}_{b} = \frac{\dot{U}_{B}}{Z}$$

可知
$$I_a$$
、 $I_b$ 、 $I_c$ 为三相对称电流

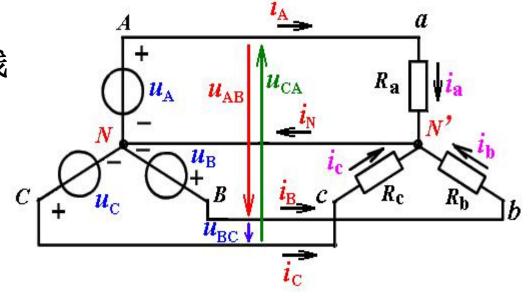
 $\dot{I}_{\rm C} = \dot{I}_{\rm c} = \frac{U_{\rm C}}{Z}$ 

例1. 已知对称三相四线制电源线电压为380V,相电压为 220V;负载为电灯组,在额定电压下其电阻分别为 $R_a$ =5  $\Omega$  , $R_b$ =10  $\Omega$  , $R_c$ =20  $\Omega$  。试求负载相电压、负载电流及中性线电流。电灯的额定电压为220 V。

• 解: : 负载接成Y<sub>0</sub> 有中性线

∴负载相电压为:

$$\dot{U}_{a} = \dot{U}_{A} = 220 \angle 0^{\circ} V$$
 $\dot{U}_{b} = \dot{U}_{B} = 220 \angle -120^{\circ} V$ 
 $\dot{U}_{c} = \dot{U}_{C} = 220 \angle 120^{\circ} V$ 



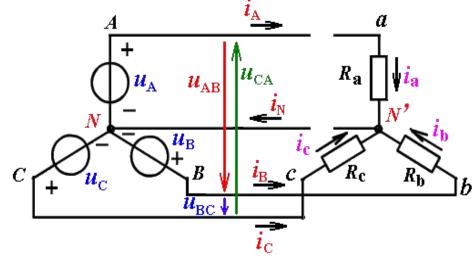
$$\dot{I}_{\rm b} = \frac{U_{\rm B}}{R_{\rm b}} = 22 \angle (-120^{\circ}) {\rm A}$$

则: 
$$\dot{I}_{N} = \dot{I}_{a} + \dot{I}_{b} + \dot{I}_{c} = 29.1 \angle (-19^{\circ})A$$

• 例2. 在例1中,当*A* 相和中性线断开时,试求负载的端电压。

解: 1.1 相和中性线断开

$$L_{\rm bc} = U_{\rm BC} = 380 {
m V}$$

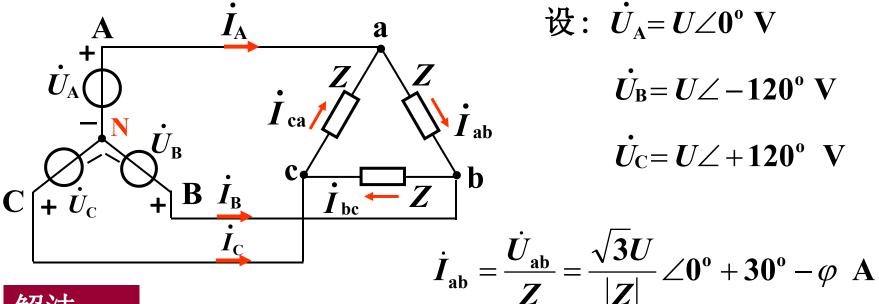


$$\therefore U_{bN'} = \frac{R_b}{R_b + R_c} U_{bc} = \frac{10}{10 + 20} \times 380 = 126.67 \text{ V}$$

$$U_{\rm cN'} = \frac{R_{\rm c}}{R_{\rm b} + R_{\rm c}} U_{\rm bc} = \frac{20}{10 + 20} \times 380 = 253.33 \text{ V}$$

## 3 负载三角形联接的三相电路分析

• Y-△对称三相电路的计算



#### 解法一

$$\dot{U}_{
m ab} = \dot{U}_{
m AB} = \sqrt{3}U \angle + 30^{
m o} \ 
m V$$
 $\dot{U}_{
m bc} = \dot{U}_{
m BC} = \sqrt{3}U \angle - 90^{
m o} \ 
m V$ 
 $\dot{U}_{
m ca} = \dot{U}_{
m CA} = \sqrt{3}U \angle + 150^{
m o} \ 
m V$ 

$$\dot{I}_{bc} = \frac{\dot{U}_{bc}}{Z} = \frac{\sqrt{3}U}{|Z|} \angle -90^{\circ} - \varphi A$$

$$\dot{I}_{ca} = \frac{\dot{U}_{ca}}{Z} = \frac{\sqrt{3}U}{|Z|} \angle + 150^{\circ} - \varphi A$$

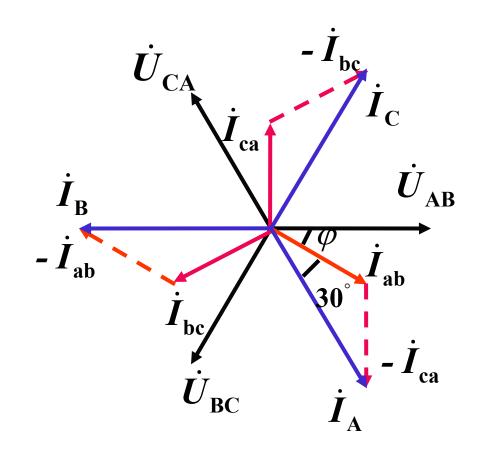
## Y-△对称三相电路的计算

#### 线电流:

$$\dot{I}_{\rm A} = \dot{I}_{\rm ab} - \dot{I}_{\rm ca} = \sqrt{3}\dot{I}_{\rm ab}\angle - 30^{\rm o}$$

$$\dot{I}_{\rm B} = \dot{I}_{\rm bc} - \dot{I}_{\rm ab} = \sqrt{3}\dot{I}_{\rm bc} \angle - 30^{\rm o}$$

$$\dot{I}_{\rm C} = \dot{I}_{\rm ca} - \dot{I}_{\rm bc} = \sqrt{3}\dot{I}_{\rm ca} \angle - 30^{\rm o}$$



## 结论

- (1) 负载上相电压与线电压相等,且对称。
- (2)线电流与相电流均为对称的。线电流大小是相电流的√3倍,相位落后相应相电流30°。

## Y-△对称三相电路的计算

利用计算相电流的 一相等效电路。

$$\therefore \dot{U}_{ab} = \dot{U}_{AB}$$
$$= \sqrt{3}U \angle + 30^{\circ} \text{ V}$$

$$= \sqrt{3}U \angle + 30^{\circ} \text{ V}$$

$$\therefore \dot{I}_{ab} = \frac{\dot{U}_{ab}}{Z} = \frac{\dot{U}_{AB}}{Z} = \frac{\sqrt{3}U}{|Z|} \angle + 30^{\circ} - \varphi \text{ A}$$

$$\dot{I}_{bc} = \frac{\sqrt{3U}}{|Z|} \angle -90^{\circ} - \varphi A$$

$$\dot{I}_{A} = \sqrt{3}\dot{I}_{ab}\angle -30^{\circ} = \frac{3U}{|Z|}\angle -\varphi A$$

$$\dot{I}_{\rm B} = \sqrt{3}\dot{I}_{\rm bc} \angle -30^{\rm o} \ {\rm A}$$

$$\dot{I}_{ca} = \frac{\sqrt{3}U}{|Z|} \angle + 150^{\circ} - \varphi A$$

$$\dot{I}_{\rm R} = \sqrt{3}\dot{I}_{\rm bc} \angle -30^{\rm o} \text{ A}$$
  $\dot{I}_{\rm C} = \sqrt{3}\dot{I}_{\rm ca} \angle -30^{\rm o} \text{ A}$ 

• 例2. 如图对称三相电路,电源线电压为380V, $|Z_1|$ =10 $\Omega$ , $\cos \varphi_1$  =0.6(滞后), $Z_2$ =  $-{
m j}50\Omega$ , $Z_N$ =1+  ${
m j}2\Omega$ 。

求:线电流、相电流,并定性画出相量图(以A相为例)。

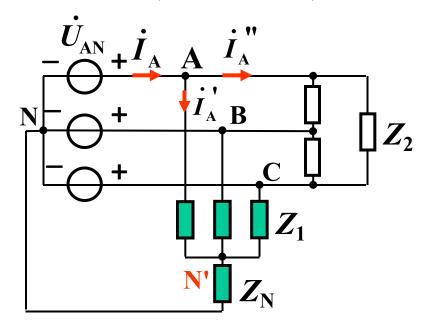
•解: 画出一相计算图如下图所示。

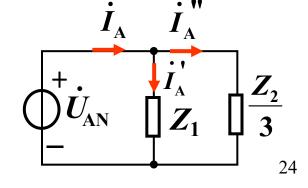
设
$$\dot{U}_{\mathrm{AN}}=220\angle0^{\mathrm{o}}~\mathrm{V}$$

则  $\dot{U}_{AB} = 380 \angle 30^{\circ} V$ 

: 
$$Z_1 = 10 \angle 53.13^\circ = 6 + j8 \Omega$$

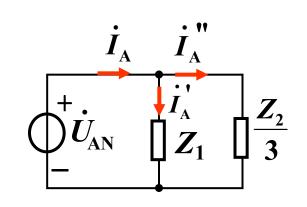
$$Z_2' = \frac{1}{3}Z_2 = -j\frac{50}{3}\Omega$$





$$\dot{I}_{A}^{"} = \frac{\dot{U}_{AN}}{Z_{2}^{'}} = \frac{220 \angle 0^{\circ}}{-j50/3} = 13.2 \angle 90^{\circ} A$$

$$\dot{I}_{A} = \dot{I}_{A}^{'} + \dot{I}_{A}^{"} = 13.9 \angle -18.4^{\circ} A$$



根据对称性,得B、C相的线电流、相电流:

$$I_{\rm R} = 13.9 \angle -138.4^{\circ} \,\text{A}$$
  $I_{\rm C} = 13.9 \angle 101.6^{\circ} \,\text{A}$ 

$$I_C = 13.9 \angle 101.6^{\circ} A$$

第一组负载的相电流

第二组负载的相电流

$$\begin{cases} \dot{I}_{A}' = 22 \angle -53.1^{\circ} A \\ \dot{I}_{B}' = 22 \angle -173.1^{\circ} A \\ \dot{I}_{C}' = 22 \angle 66.9^{\circ} A \end{cases}$$

$$\begin{cases} \dot{I}_{AB2} = \frac{1}{\sqrt{3}} \dot{I}_{A}^{"} \angle 30^{\circ} = 7.6 \angle 120^{\circ} A \\ \dot{I}_{BC2} = 7.6 \angle 0^{\circ} A \\ \dot{I}_{CA2} = 7.6 \angle -120^{\circ} A \end{cases}$$

依此作出相量图(略):

## 4 三相电路的功率

- 一、三相电路的功率
  - 1. 对称三相电路的瞬时功率 p

设对称三相电路中A相的电压、电流为

$$u_{\rm A} = \sqrt{2}U\sin\omega t$$
  $i_{\rm A} = \sqrt{2}I\sin(\omega t - \varphi)$ 

則 
$$p_{A} = u_{A}i_{A} = 2UI\sin\omega t \sin(\omega t - \varphi)$$
  
=  $UI[\cos\varphi - \cos(2\omega t - \varphi)]$ 

$$p_{\rm B} = u_{\rm B}i_{\rm B} = UI\cos\varphi - UI\cos[(2\omega t - 120^{\circ}) - \varphi]$$

$$p_{\rm C} = u_{\rm C}i_{\rm C} = UI\cos\varphi - UI\cos[(2\omega t + 120^{\circ}) - \varphi]$$

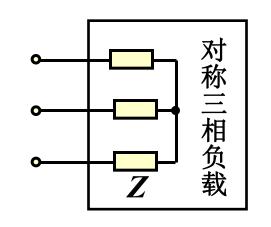
$$p = p_A + p_B + p_C$$

## 对称三相电路的有功功率P

一相负载的功率:  $U_{\rm n}I_{\rm n}\cos\varphi_{\rm nh}$ 

且: 
$$P_a = P_b = P_c = P_p = U_p I_p \cos \varphi_{ph}$$

有: 三相总有功功率  $P = 3P_p = 3U_p I_p \cos \varphi_{ph}$ 



对称三相负载 $Z=|Z|\angle \varphi$ 

"Y"形负载: 
$$U_{\rm L} = \sqrt{3}U_{\rm ph}$$
,  $I_{\rm L} = I_{\rm ph}$  
$$P = 3 \cdot \frac{1}{\sqrt{3}} U_{\rm L} I_{\rm L} \cos \varphi = \sqrt{3} U_{\rm L} I_{\rm L} \cos \varphi_{\rm ph}$$

" $\Delta$ "形负载: $U_{\mathbf{I}} = U_{\mathbf{P}}$ ,  $I_{\mathbf{I}} = \sqrt{3}I_{\mathbf{P}}$ 

$$P = 3U_{\rm L} \frac{1}{\sqrt{3}} I_{\rm L} \cos \varphi = \sqrt{3} U_{\rm L} I_{\rm L} \cos \varphi_{\rm ph}$$

结论: 对称三相电路总有功功率  $P = \sqrt{3}U_1I_1\cos\varphi$ 

$$P = \sqrt{3}U_{\rm L}I_{\rm L}\cos\varphi$$

## 3. 对称三相电路的无功功率Q

$$Q = Q_a + Q_b + Q_c = 3Q_p$$

同理,三相总无功功率  $Q = 3Q_p = \sqrt{3}U_L I_L \sin \varphi$ 

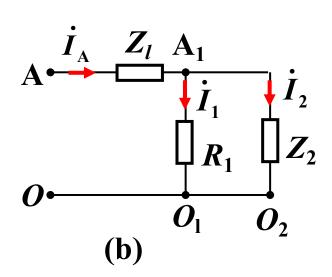
#### 4. 对称三相电路的视在功率S

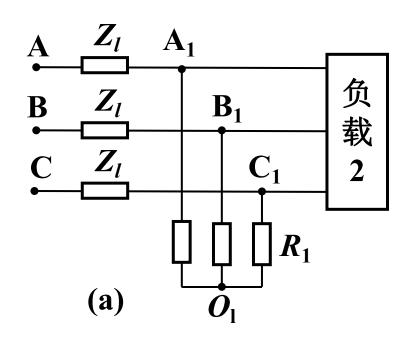
$$S = \sqrt{3}U_{\rm L}I_{\rm L} = \sqrt{P^2 + Q^2}$$

功率因数可定义为:  $\cos \varphi = P/S$ 

例1. 如图(a)对称三相电路,第一组负载 $R_1$ =110 $\Omega$ ,第二组负载平均功率 $P_2$ = 5280kw, $\cos \varphi_2$ =0.8(滞后),且两组负载的额定工作相电压有效值为220V,线路阻抗  $Z_i$ =1+j1 $\Omega$ 。试求负载在额定运行时对称三相电源的线电压 $U_L$ 、线电流 $I_L$ 及对称三相电路吸收的有功功率、无功功率、视在功率和功率因数。

解: 设第二组负载为Y接, 取A相计算电路,如图(b)





设 
$$\dot{U}_{A1}=220\angle0^{\circ}$$
 V

由已知条件得

$$I_2 = \frac{P_2}{\sqrt{3}U_{A_1B_1}\cos\varphi_2} = \frac{5280}{\sqrt{3}\times380\times0.8} = 10A$$

$$U_2 = \frac{V_2}{\sqrt{3}U_{A_1B_1}\cos\varphi_2} = \frac{3280}{\sqrt{3}\times380\times0.8} = 10A$$
 $\cos\varphi_2 = 0.8, \quad \varphi = 36.9^\circ$ 

$$\vec{I}_{2} = 10 \angle -36.9^{\circ} A \qquad \qquad \vec{I}_{1} = \frac{\vec{U}_{A1}}{R_{1}} = \frac{220 \angle 0^{\circ}}{110} = 2 \angle 0^{\circ} A$$

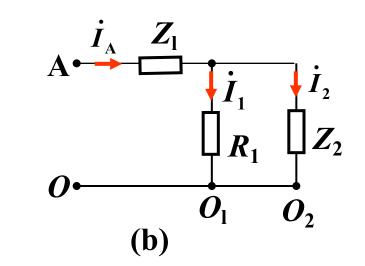
$$\dot{I}_{A} = \dot{I}_{1} + \dot{I}_{2} = 2 + 10 \angle -36.9^{\circ} = 10 - j6 = 11.66 \angle -30.96^{\circ} A$$

$$\dot{U}_{AO} = Z_l \dot{I}_A + \dot{U}_{A_1} = (1+j1) \times 11.66 \angle -30.96^{\circ} + 220 \angle 0^{\circ}$$
  
= 236\angle 0.97° V

$$\dot{U}_{AB} = \sqrt{3} \, \dot{U}_{A} \angle 30^{\circ} = \sqrt{3 \times 236} \angle (0.97^{\circ} + 30^{\circ})$$
  
= 408.8 \angle 30.97° V

$$\dot{U}_{AB} = 408.8 \angle 30.97^{\circ} \text{ V}$$
 $\dot{U}_{A} = 236 \angle 0.97^{\circ} \text{ V}$ 
 $\dot{I}_{A} = 11.66 \angle -30.96^{\circ} \text{ A}$ 

$$U_{L} = 408.8 \text{ V}, \qquad I_{L} = 11.66 \text{ A}$$



$$P = \sqrt{3}U_{L}I_{L}\cos\varphi$$

$$= \sqrt{3} \times 408.8 \times 11.66\cos \left[0.97^{\circ} - (-30.97^{\circ})\right] = 7.007\text{kW}$$

$$Q = \sqrt{3}U_{L}I_{L}\sin \varphi$$
  
=  $\sqrt{3} \times 408.8 \times 11.66\sin 31$  .93° = 4.367kvar

$$S = \sqrt{3}U_{\rm L}I_{\rm L} = \sqrt{3} \times 408.8 \times 11.66 = 8.256 {\rm kVA}$$
  
 $\cos \varphi = \cos \left[0.97 \, ^{\rm o} - (-30.96 \, ^{\rm o})\right] = \cos 31.93 \, ^{\rm o} = 0.85$ 

## • 二、三相电路功率的测量(对称,不对称)

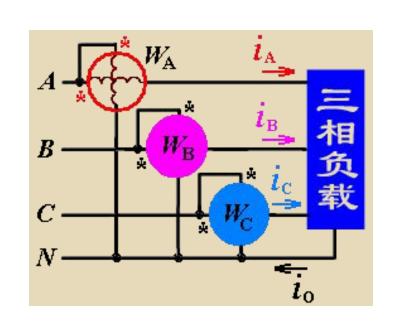
- 1. 三表法: 适用于三相四线制的电路测量
- (1)若负载不对称,则

$$p = u_{AN} i_A + u_{BN} i_B + u_{CN} i_C$$
$$P = P_A + P_B + P_C$$

(2) 若负载对称,则

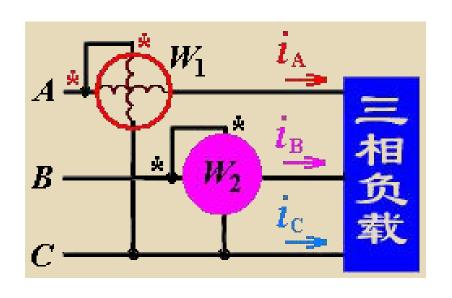
$$P = 3P_{\rm A} = 3P_{\rm B} = 3P_{\rm C} = 3U_{\rm ph}I_{\rm ph}\cos\varphi_{\rm ph}$$

需一块表,读数乘以3。即为一表法



## • 二、三相电路功率的测量(对称,不对称)

2. 二表法: 适用于三相三线制的电路测量



若:  $W_1$ 的读数为 $P_1$ ,  $W_2$ 的读数为 $P_2$ ,

则:  $P = P_1 + P_2$  即为三相总功率。

证明: (参见书本)

例:  $U_l$  =380V, $Z_1$ =30+j40Ω,电动机 P=1700W, $\cos \varphi$ =0.8(滞后)。

- 求: (1) 线电流和电源发出总功率;
  - (2) 用两表法测电动机负载的功率,画接线图,求两表读数。

解: (1) 
$$\dot{U}_{AN} = 220 \angle 0^{\circ} \text{ V}$$

$$\dot{I}_{A1} = \frac{\dot{U}_{AN}}{Z_1} = \frac{220 \angle 0^{\circ}}{30 + j40}$$

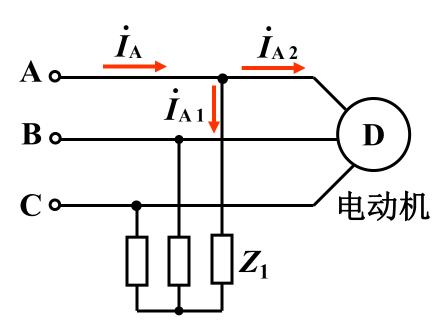
$$= 4.41 \angle -53.1^{\circ} \text{ A}$$

电动机负载:

$$P = \sqrt{3}U_1I_{\Delta},\cos\varphi = 1.7 \text{ kW}$$

$$I_{A2} = \frac{P}{\sqrt{3}U_1 \cos\varphi} = \frac{P}{\sqrt{3} \times 380 \times 0.8} = 3.23A$$

$$:. \dot{I}_{A2} = 3.23 \angle -36.9^{\circ} \text{ A}$$



总电流: 
$$\dot{I}_{A} = \dot{I}_{A1} + \dot{I}_{A2}$$
  
=  $4.41 \angle -53.1^{\circ} +3.23 \angle -36.9^{\circ}$   
=  $7.56 \angle -46.2^{\circ}$  A

$$P_{\mathbb{H}} = \sqrt{3}U_1I_A\cos\varphi_{\mathbb{H}}$$

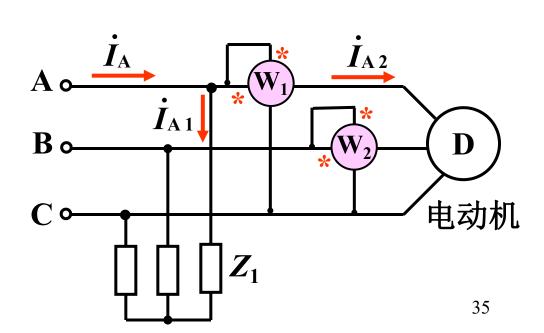
$$= \sqrt{3} \times 380 \times 7.56\cos 46. \ 2^{\circ} = 3.44 \text{ kW}$$

 $P_{Z_1} = 3 \times I_{A_1}^2 \times R_1 = 3 \times 4.41^2 \times 30 = 1.74 \text{ kW}$ 

## (2) 两表的读数如图

$$\dot{I}_{A2} = 3.23 \angle -36.9^{\circ} \text{ A}$$

$$\dot{I}_{B2} = 3.23 \angle -156.9^{\circ} \text{ A}$$



$$\therefore \dot{U}_{AB} = 380 \angle 30^{\circ} \text{ V}$$

$$\therefore \dot{U}_{\rm BC} = 380 \angle -90^{\circ} \text{ V}$$

$$\dot{U}_{AC} = -\dot{U}_{CA}$$

$$= -380 \angle 150^{\circ} \text{ V}$$

$$= 380 \angle -30^{\circ} \text{ V}$$

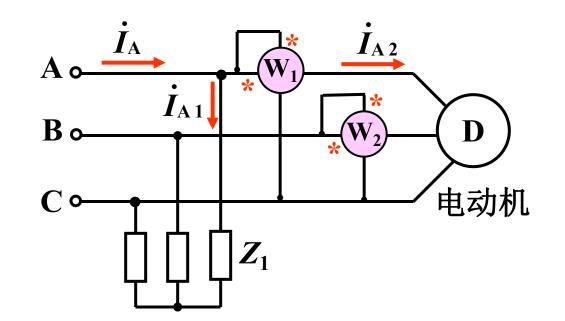


表
$$W_1$$
的读数 $P_1$ :  $P_1 = U_{AC}I_{A2}\cos\varphi_1$   
= 380×3.23 $\cos(-30^\circ + 36.9^\circ)$   
= 1218.5 $W$ 

表
$$W_2$$
的读数 $P_2$ :  $P_2 = U_{BC}I_{B2}\cos\varphi_2$  =  $380 \times 3.23\cos(-156.9^{\circ} + 90^{\circ})$  =  $481.6W$ 

## 第七章作业

12-6, 12-8, 12-29