

Equipment: 741 op-amp

Purposes:

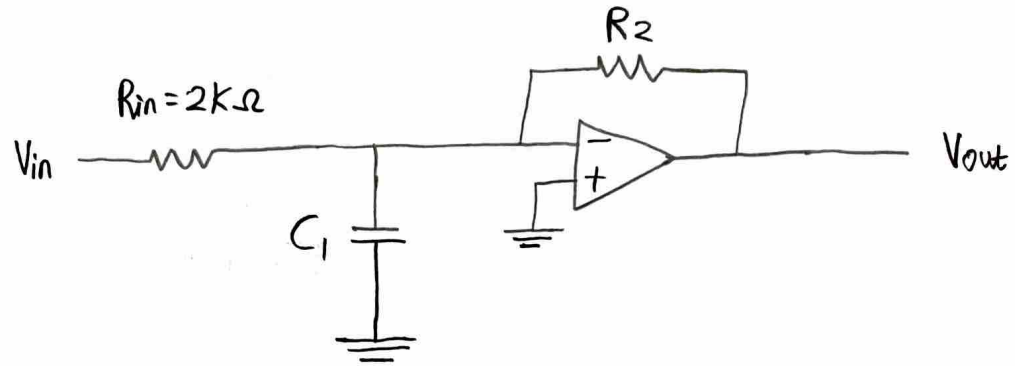
Active Low pass filter circuit
With① Gain at DC ($\omega=0$):

$$\frac{V_{out}}{V_{in}} = -15 \text{ V/V} \rightarrow \text{inverting amplifier}$$

② $R_{in} = 2 \text{ k}\Omega$

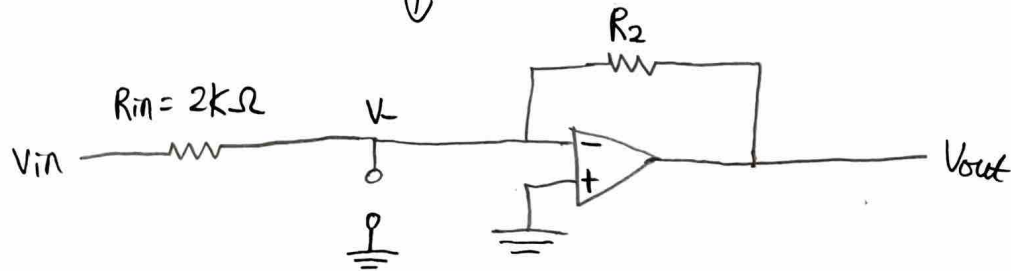
③ When 3 dB:

$$f = 5000 \text{ Hz}$$

 Z_C at DC ($\omega=0$):

$$Z_C = \frac{1}{j\omega C_1} = \frac{1}{j(0)C_1} = \infty \rightarrow \text{open circuit}$$

↓

KCL (to find R_2):

$$\frac{V_- - V_{in}}{R_{in}} + \frac{V_- - V_{out}}{R_2} = 0$$

$$R_2(V_- - V_{in}) + R_{in}(V_- - V_{out}) = 0$$

$$\downarrow V_+ = 0 \rightarrow V_- = V_+ \rightarrow V_+ = V_- = 0$$

$$-R_2 V_{in} - R_{in} V_{out} = 0$$

Assume
ideal
op-amp

$$\rightarrow A = \infty$$

$$V_o = A(V_+ - V_-)$$

$$\rightarrow \frac{V_o}{A} = V_+ - V_-$$

$$\downarrow \frac{V_o}{\infty} = 0$$

$$0 = V_+ - V_- \rightarrow V_- = V_+$$

KCL (continued):

$$-R_2 V_{in} - R_{in} V_{out} = 0$$

$$R_2 V_{in} + R_{in} V_{out} = 0$$

$$R_{in} V_{out} = -R_2 V_{in}$$

$$\frac{V_{out}}{V_{in}} = -\frac{R_2}{R_{in}}$$

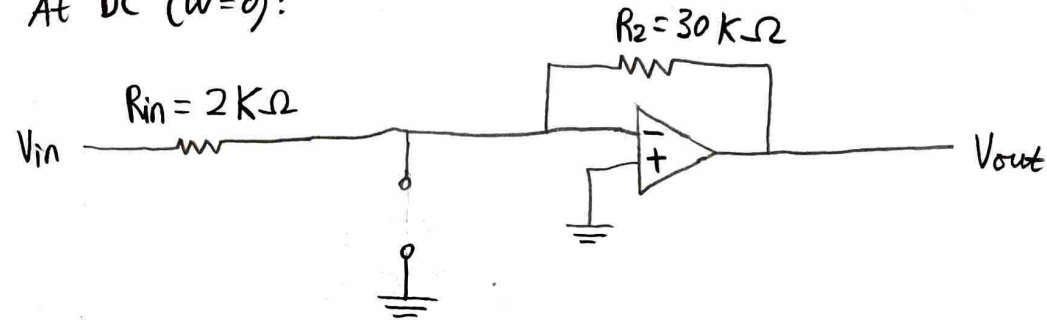
$$\frac{V_{out}}{V_{in}} = -15$$

$$R_{in} = 2000 \Omega$$

$$-15 = -\frac{R_2}{2000}$$

$$R_2 = 30 \text{ k}\Omega$$

At DC ($\omega = 0$):



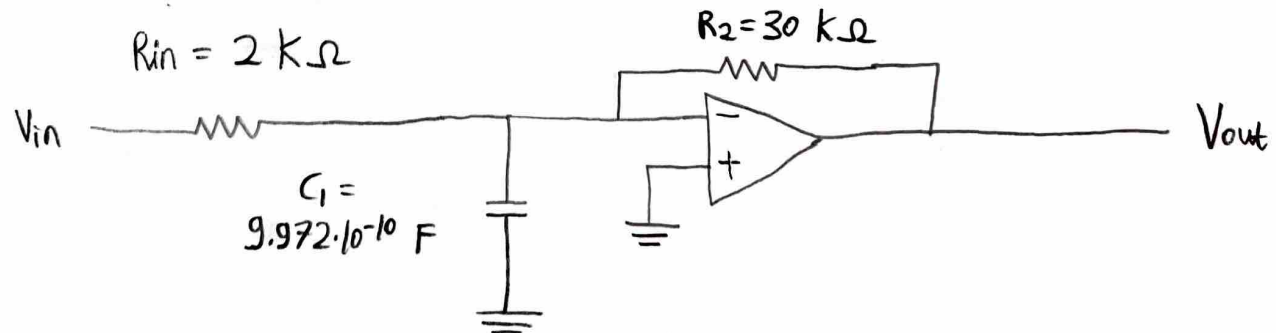
To find C_1 :

$$f_0 = \frac{1}{2\pi(R_{in} + R_2)C_1}$$

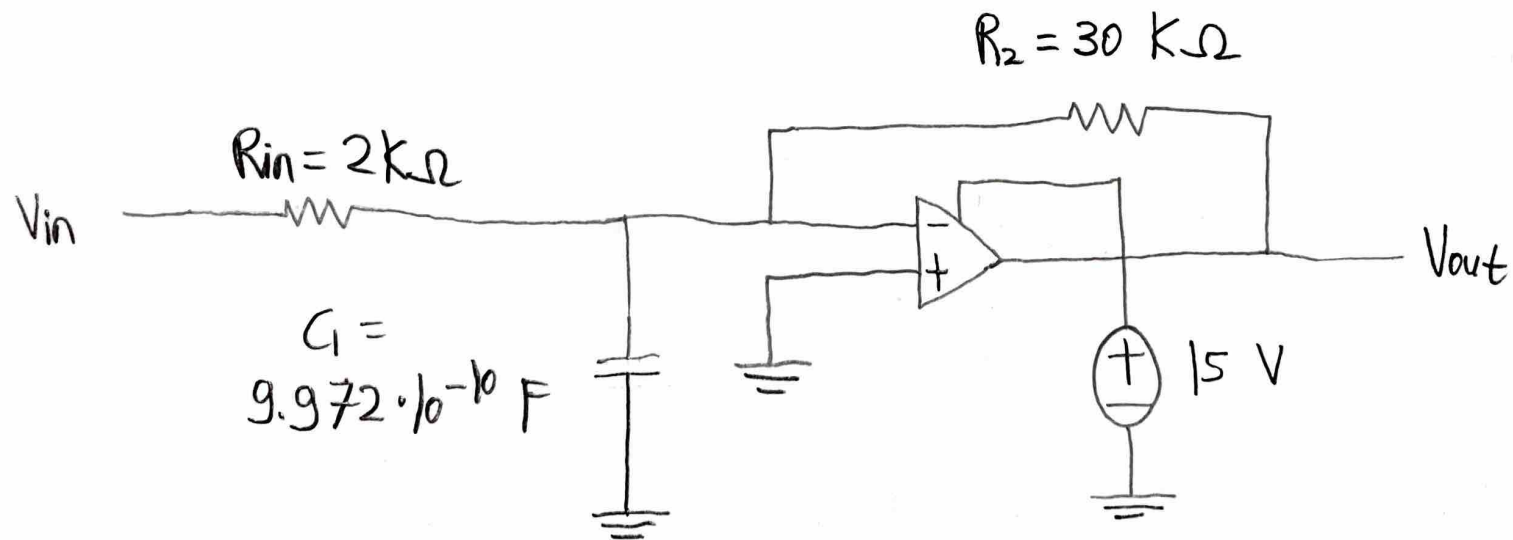
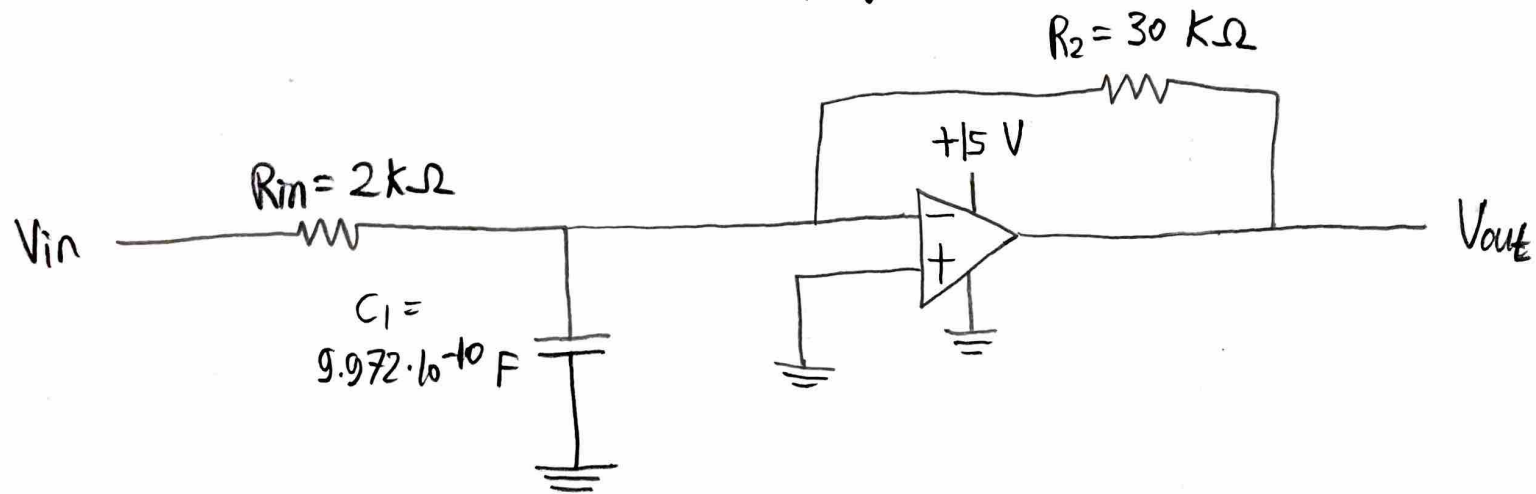
$$5000 = \frac{1}{2\pi(32000)C_1}$$

$$C_1 = 9.972 \cdot 10^{-10} \text{ F}$$

My final filter design (generalized for every value of ω):



⑥ Assign $\pm 15\text{ V}$ DC power supply:

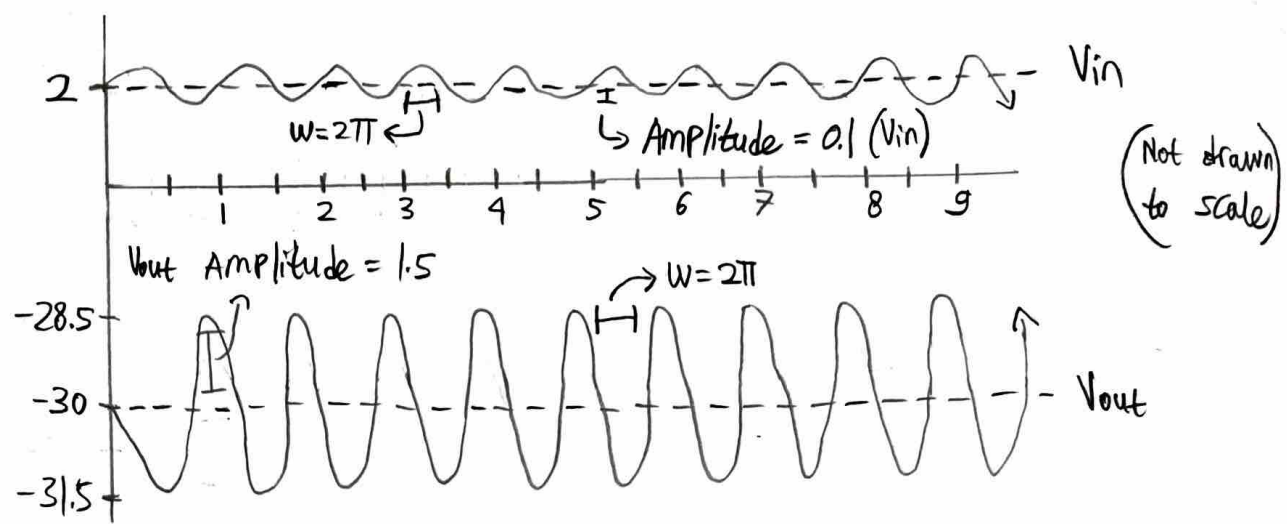


① i. $V_{in}(t) = 2 + 0.1 \sin 2\pi t$

$$V_{out}(t) = V_{in}(t) \cdot \frac{V_{out}}{V_{in}}$$

$$= [2 + 0.1 \sin(2\pi t)] \cdot (-15)$$

$$= -30 - 1.5 \sin(2\pi t)$$

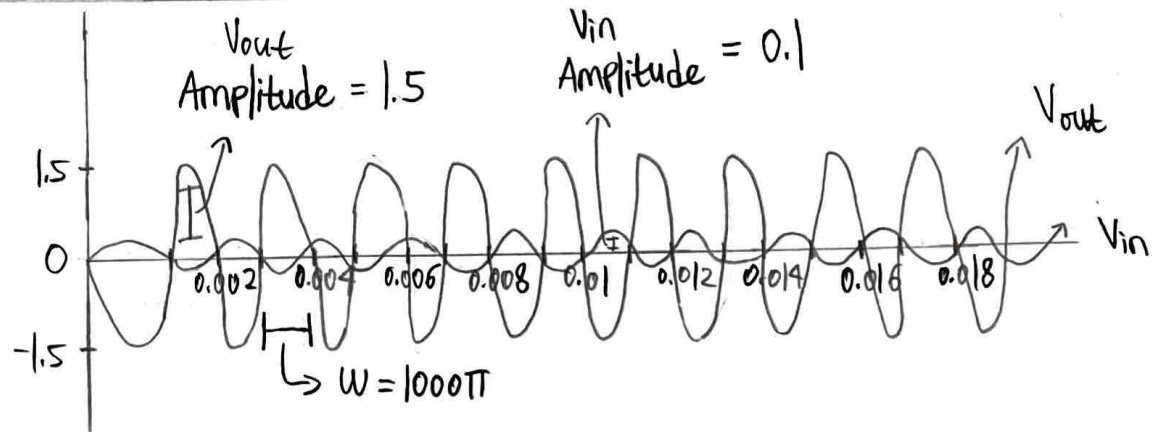


② ii. $V_{in}(t) = 0.1 \sin(1000\pi t)$

$$V_{out}(t) = V_{in}(t) \cdot \frac{V_{out}}{V_{in}}$$

$$= [0.1 \sin(1000\pi t)] (-15)$$

$$= -1.5 \sin(1000\pi t)$$



③ iii. $V_{in}(t) = 0.1 \sin(40000\pi t)$

$$V_{out}(t) = V_{in}(t) \cdot \frac{V_{out}}{V_{in}}$$

$$= [0.1 \sin(40000\pi t)] (-15)$$

$$= -1.5 \sin(40000\pi t)$$

