

## Homework #8 Solutions

1.

$V_1 - V_2 = I_2 R_2$   
 $= (0.5\text{mA}) 1\text{k}$   
 $= 0.5\text{V}$

$V_1 = V_G \quad V_1 - V_2$   
 $V_2 = V_D \quad V_G - V_D = 0.5$

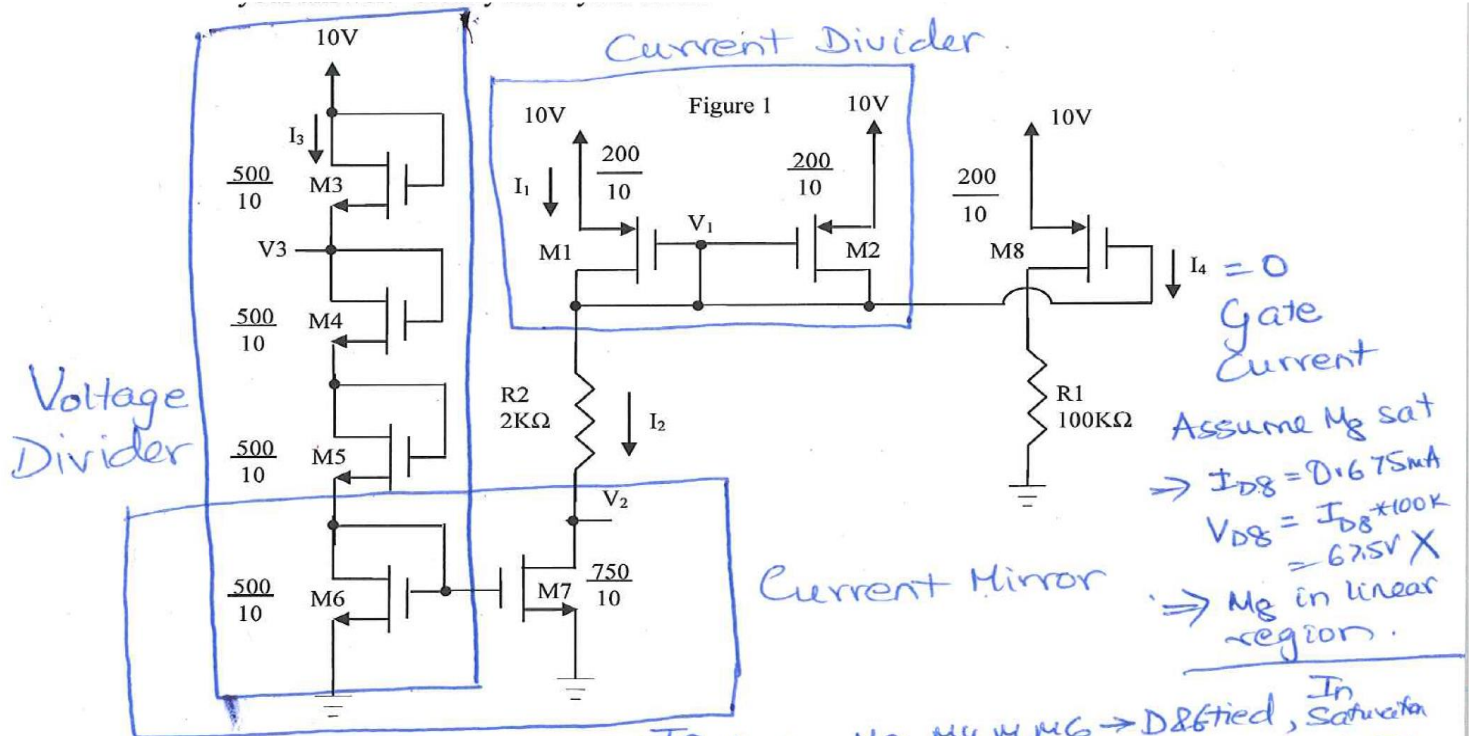
$0.5\text{mA} = \frac{1}{2} \frac{40\mu\text{A}}{V^2} \frac{250}{10} (V_1 - V_D)^2$

$(V_1 - 2)^2 = 1$   
 $V_1 - 2 = \pm\sqrt{1}$   
 $V_2 = \pm 1 + 2$   
 $V_2 = +3 > 2 \quad \checkmark$   
 $V_2 = +1 > 2 \quad \times$

$\Rightarrow V_2 = 3\text{V} \Rightarrow V_2 = 2.5\text{V}$

$R_2 = \frac{1}{2}\text{k} \Rightarrow I_2 R_2 \text{ smaller} \Rightarrow \text{stays sat.}$   
 $R_2 = 2\text{k} \Rightarrow I_2 R_2 = 1\text{V still saturated.}$   
 $-1 > -2 \quad \checkmark$

2.



Gate Current  
Assume  $M_8$  sat  
 $\Rightarrow I_{D8} = 0.675 \text{ mA}$   
 $V_{D8} = I_{D8} \times 100 \text{ K}$   
 $= 67.5 \text{ V} \times$   
 $\Rightarrow M_8$  in linear region.

PMOS  
 $M_1, M_2 \rightarrow D \& G$  tied  $\rightarrow$  Saturation  
Current Divider  $I_1 = I_2/2 = 675 \mu\text{A} = I_1$   
 $M_6/M_7 \rightarrow$  Current Mirror [To prove  $M_7$  saturated]  
 $\frac{I_{D6}}{I_{D7}} = \frac{(W/L)_6}{(W/L)_7} \Rightarrow I_{D7} = 900 \mu\text{A} \times \frac{750/10}{500/10} = 1.35 \text{ mA}$   
 $I_{D1} = 675 \mu\text{A} = \frac{1}{2} \times 15 \mu\text{A} \times \frac{200}{10} \left[ \frac{V_{GS1} - (-1.5)}{V_2 - 10} \right]^2$   
 $(V_{GS1} + 1.5)^2 = 4.5$   
 $V_{GS1} + 1.5 = \pm \sqrt{4.5}$   
 $= \pm 2.12$   
 $\Rightarrow V_{GS1} = -3.62 \text{ V} < -1.5 \checkmark$   
 $\Rightarrow V_{GS1} = -3.62 \text{ V} = V_1 - 10$   
 $\Rightarrow V_1 = 6.378 \text{ V} //$   
 $M_3, M_4, M_5, M_6 \rightarrow D \& G$  tied, Saturation  
Voltage Divider  $\Rightarrow 10/4 = 2.5 \text{ V}$   
across each NMOSFET.  $V_{GS} = 7.5$   
 $V_{GS3} = +2.5 \text{ V}$   
 $V_3 = 7.5 \text{ V}$   
 $I_3 = \frac{1}{2} \times 25 \mu\text{A} \times \frac{500}{10} \left( \frac{2.5}{2.5 - 1.5} \right)^2$   
 $I_3 = 900 \mu\text{A}$   
 $V_2 = V_1 - I_2 R_2$   
 $= 6.378 - 1.35 \times 2$   
 $= 3.678 \text{ V}$   
 $V_{D2} = V_2 = 3.678 \text{ V}$   
 $V_{GS2} - V_T = 2.5 - 1.3 \checkmark$   
 $M_7$  sat  $\checkmark$