CSE 330 [Numerical Methods]

Assignment 01 [Spring 2025]

Instructions for submission: [Handwritten submission]

- Write your Name, Student ID, Section No. in the cover page of the assignment.
- Mark the answers properly for each corresponding question.
- There is no late submission.
- 1. In the classes, we discussed three forms of floating number representations, as shown below,

Standard/General Form: $F = \pm (0.d1d2d3 \cdots dm)\beta \beta^e$,

Normalized Form: $F = \pm (1.d1d2d3 \cdot \cdot \cdot dm)\beta \beta^e$,

Denormalized Form: $F = \pm (0.1d1d2d3 \cdot \cdot \cdot dm)\beta \beta^e$

Now, let's take, $\beta = 2$, m = 4 and $-2 \le e \le 6$. Based on these, answer the following:

- (a) (6 marks) What are the maximum/largest and minimum/smallest numbers that can be stored in the system by these three forms defined above (express your answer in decimal values)?
- (b) (3 marks) What are the **non-negative minimum/smallest** numbers that can be stored in the system by the three forms defined above (express your answer in decimal values)?
- (c) (3 marks) How many numbers in total/possible combinations can be represented by this system? Find this separately for each of the three forms above including the **negative numbers**.
- 2. Consider the real number $x = (5.625)_{10}$
- (a) (2 marks) First convert the decimal number x in binary format.
- (b) (3 marks) Find fl(x) if you store it in a system with m = 3 using the **denormalized** form of floating point representation.
- (c) (6 marks) Now convert back to decimal form the stored value you obtained in the previous part, and calculate the Rounding Error and Machine Epsilon.
- 3. Consider the quadratic equation, $x^2 60x + 1 = 0$ Below, calculate **up to 6 significant** figures.
- (a) (4 marks) Find out where the loss of significance occurs when you calculate the roots?
- (b) (3 marks) Evaluate the correct roots such that loss of significance does not occur.