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Regular Expression Examples

① $L = \{ w \in \{0,1\}^* : w \text{ starts with '10'} \}$

$$10 (0|1)^*$$

② $L = \{ w \in \{0,1\}^* : w \text{ ends with '10'} \}$

$$(0|1)^* 10$$

③ $L = \{ w \in \{0,1\}^* : w \text{ does not end with '10'} \}$

$$(0|1)^* (11|00|01) | (0|1)^* \epsilon$$

④ $L = \{ w \in \{0,1\}^* : \text{length of } w \text{ is even} \}$

$$((0|1)(0|1))^*$$

$$\text{or, } (00|10|01|11)^*$$

⑤ $L = \{ w \in \{0,1\}^* : \text{length of } w \text{ is odd} \}$

$$((0|1)(0|1))^* (0|1)$$

⑥ $L = \{ w \in \{0,1\}^* : w \text{ contains '101' as substring} \}$
 $(0|1)^* 101 (0|1)^*$

⑦ $L = \{ w \in \{0,1\}^* \text{ doesn't contain '11'} \}$
 $(0|10)^* (1| \epsilon)$

⑧ $L = \{ w \in \{0,1\}^* \text{ does not contain '00'} \}$
 $(1|01)^* (0| \epsilon)$

⑨ $L = \{ \text{does not contain '111'} \}$
 $(0|10|110)^* (1|11| \epsilon)$

⑩ $L = \{ \text{length expressed as } 3k+2 \}$
 $((0|1)(0|1)(0|1))^* (0|1)(0|1)$

⑪ $\{ \text{length expressed as } 2k+1 \}$
 $((0|1)(0|1))^* (0|1)$

⑫ $\{ w \text{ contains '00' or '11'} \}$
 $(0|1)^* 00 (0|1)^* \mid (0|1)^* 11 (0|1)^*$

⑬ $L = \{ w \text{ contains at least two '1's'} \}$
 $(0|1)^* 1 (0|1)^* 1 (0|1)^*$

⑭ $L = \{ w \text{ contains exactly two '1's'} \}$
 $0^* 1 0^* 1 0^*$

⑮ $L = \{ w \text{ contains at most two '1's'} \}$
 $0^* + 0^* 1 0^* + 0^* 1 0^* 1 0^*$

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- (16) $L = \{ \text{length of } w \text{ is not multiple of } 3 \}$

$$(011)(011)(011)^*(011)(011| \epsilon)$$

- (17) $L = \{ \text{Number of 1's in } w \text{ is multiple of } 3 \}$

$$0^* | (0^*10^*10^*10^*)^*$$

- (18) $L = \{ w \text{ starts & ends with same symbol} \}$

$$0(011)^*0 | 1(011)^*1 | 0 | 1$$

- (19) $L = \{ w \text{ starts and ends with different symbol} \}$

$$0(011)^*1 + 1(011)^*0$$

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- (20) $L = \{ w \text{ doesn't contain } 01 \}$

$$1^*0^*$$

- (21) $L = \{ w \text{ contains } 0 \text{ at every 3rd position} \}$

$$(011)(011)0^*(011)(011) | ((011)(011)0^*)^* (011) | ((011)(011)0^*)^*$$

- (22) $L = \{ w \text{ have 0's & 1's in alternate} \}$

$$(1| \epsilon)(01)^*(0| \epsilon) | (0| \epsilon)(10)^*(1| \epsilon)$$

- (23) $L_1 = w \text{ divisible by three}$
 $(\Sigma \Sigma \Sigma)^* \text{ or } ((011)(011)(011))^*$

$L_2 = \text{every second letter is } 0$

$$(011)0^*(011| \epsilon)^*$$

- (a) $L_1 \cap L_2$
 $(\Sigma 0 \Sigma 0 \Sigma 0)^*(\Sigma 0 \Sigma | \epsilon)$

(24) $L = \{ 0 \text{ followed by two } 1\text{'s} \}$

$$1^* (0111^*)^*$$

(25) $L = \{ w \text{ have } 1 \text{ at every odd position} \}$

$$(1(01)^*)^* (1\epsilon)$$