Dividimos y No Conquistamos (D&!C)

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1 Template

1.1 C++ Template

```
#include <bits/stdc++.h>
   using namespace std;
  #define L(i, j, n) for (int i = (j); i < (int)n; i ++)
   #define SZ(x) int((x).size())
   #define ALL(x) begin(x),end(x)
   #define vec vector
  #define pb push_back
   #define eb emplace_back
   using ll = long long;
   using ld = long double;
  void solve(){}
   int main(){
      ios::sync_with_stdio(0);cin.tie(0);
13
      int TT = 1:
14
      //cin >> TT:
15
      while (TT--) {solve();}
16
17
   // IF NEEDED FOR FILE READ
   // freopen("in.txt", "r", stdin);
  // freopen("out.txt", "w", stdout);
                        1.2 Python Template
  import os, sys, io
```

```
import os, sys, io
finput = io.BytesIO(os.read(0, os.fstat(0).st_size)).readline
fprint = sys.stdout.write
```

2 Search

2.1 Ternary

```
// Minimo de 'f' en '(l,r)'.
template<class Fun>ll ternary(Fun f, ll l, ll r) {
  for (ll d = r-l; d > 2; d = r-l) {
    ll a = l + d/3, b = r - d/3;
    if (f(a) > f(b)) l = a; else r = b;
}
return l + 1;
}
// para error < EPS, usar iters=log((r-l)/EPS)/log(1.618)</pre>
```

```
template<class Fun>double golden(Fun f, double l, double r, int iters){
     double const ratio = (3-sqrt(5))/2;
11
     double x1=1+(r-1)*ratio, x2=r-(r-1)*ratio, f1=f(x1), f2=f(x2);
12
     while (iters--) {
13
       if (f1 > f2) 1=x1, x1=x2, f1=f2, x2=r-(r-1)*ratio, f2=f(x2);
14
       else
                    r=x2, x2=x1, f2=f1, x1=1+(r-1)*ratio, f1=f(x1);
15
     }
16
     return (1+r)/2;
17
18 }
                             Simulated Annealing
using my_clock = chrono::steady_clock;
2 | struct Random {
     mt19937_64 engine;
     Random(): engine(my_clock::now().time_since_epoch().count()) {}
     template<class Int>Int integer(Int n) {return integer<Int>(0, n);} //
         "([0,n)"
     template<class Int>Int integer(Int 1, Int r)
       {return uniform_int_distribution{1, r-1}(engine);} // '[1,r)'
     double real() {return uniform_real_distribution{}(engine);} // '[0,1)'
   } rng;
   struct Timer {
     using time = my_clock::time_point;
11
     time start = my_clock::now();
12
     double elapsed() { // Segundos desde el inicio.
13
       time now = my_clock::now();
14
       return chrono::duration<double>(now - start).count();
15
     }
16
   } timer;
17
   template<class See,class Upd>struct Annealing {
     using energy = invoke_result_t<See>;
19
     energy curr, low;
20
     See see;
21
     Upd upd;
22
     Annealing(See _see, Upd _upd): see{_see}, upd{_upd}
23
       \{\text{curr} = \text{low} = \text{see}(), \text{upd}();\}
24
     void simulate(double s, double mult=1) { // Simula por 's' segundos.
25
       double t0 = timer.elapsed();
26
       for (double t = t0; t-t0 < s; t = timer.elapsed()) {
27
         energy near = see();
28
29
         auto delta = double(curr - near);
         if (delta >= 0) upd(), curr = near, low = min(low, curr);
30
```

```
else {
31
           double temp = mult * (1 - (t-t0)/s);
32
           if (exp(delta/temp) > rng.real()) upd(), curr = near;
33
34
35
36
37
   auto see = [&] -> double {
38
       1 = rng.integer(gsz);r = rng.integer(gsz);
39
       swap(groups[1], groups[r]);
40
       int ans = 0, rem =0;
41
       L(i,0,gsz){
42
           if (groups[i] > rem) {
43
               rem = x:
44
               ans ++;
45
46
           rem -= groups[i];
47
48
       swap(groups[1], groups[r]);
49
       return ans;
50
51
auto upd = [&] {swap(groups[1], groups[r]);};
```

3 Data structures

3.1 Fenwick

```
#define LSO(S) (S & -S) //LeastsignificantOne
   struct FT { // 1-Index
2
       vec<int> ft; int n;
3
       FT(vec<int> &v): ft(SZ(v)+1), n(SZ(v)+1) { // O(n)
4
           L(i, 1, n){
5
                ft[i] += v[i-1];
6
                if (i + LSO(i) <= n)ft[i + LSO(i)]+=ft[i];</pre>
8
       }
9
       void update(int pos, int x){
10
           for (int it=pos;it<=n;it+=LSO(it))ft[it]+=x;</pre>
11
       }
12
       int sum(int pos){
13
           int res = 0;
14
           for (int it=pos;it>0;it-=LSO(it))res+=ft[it];
15
           return res;
16
```

```
17
       int getSum(int 1, int r){return sum(r) - sum(1 - 1);}
18
19 };
                           3.2 Fenwick - 2D
   #define LSO(S) (S & -S)
   struct BIT { // 1-Index
       vec<vec<int>> B;
       int n; // BUILD: N * N * log(N) * log(N)
       BIT(int n_ = 1): B(n_+1, vec < int > (n_+1)), sz(n_) {}
5
       void add(int i, int j, int delta){ // log(N) * log(N)
           for (int x = i; x \le n; x += LSO(x))
7
           for (int y = j; y \le n; y += LSO(y))
               B[x][y] += delta;
10
       int sum(int i, int j){ // log(N) * log(N)
11
           int tot = 0:
12
           for (int x = i; x > 0; x -= LSO(x))
13
           for(int y = j; y > 0; y = LSO(y))
14
               tot += B[x][y];
           return tot;
16
       }
17
       int getSum(int x1, int y1, int x2, int y2) {
18
           return sum(x2, y2) - sum(x2, y1) - sum(x1, y2) + sum(x1-1,y1-1);
19
20
21 };
                                3.3 DSU
1 struct DSU {
       vec<int> par, sz; int n;
2
       DSU(int n = 1): par(n), sz(n, 1), n(n) { iota(ALL(par), 0); }
       int find(int a){return a == par[a] ? a : par[a] = find(par[a]);}
4
       void join(int a, int b){
           a=find(a);b=find(b);
6
           if (a == b) return;
7
           if (sz[b] > sz[a]) swap(a,b);
           par[b] = a;
           sz[a] += sz[b];
       }
11
12 };
                        3.4 Index Compession
```

11

return {max(a.mx, b.mx), a.mx > b.mx ? a.cant : b.cant};

```
1 template<class T>
                                                                                 12
  struct Index{ // If only 1 use Don't need to copy T type
                                                                                        void build(int v, int L, int R){
                                                                                 13
                                                                                            if (L == R) \{ st[v] = \{0, 1\}; return ; \}
       vec<T> d; int sz;
                                                                                 14
       Index(const vec<T> &a): d(ALL(a)){
                                                                                            int m = MD(L, R);
                                                                                 15
4
                                                                                            build(LC(v), L, m); build(RC(v), m + 1, R);
           sort(ALL(d)); // Sort
                                                                                 16
           d.erase(unique(ALL(d)), end(d)); // Erase continuous duplicates
                                                                                            st[v] = merge(st[LC(v)], st[RC(v)]);
                                                                                 17
           sz = SZ(d); }
                                                                                 18
       inline int of(T e) const{return lower_bound(ALL(d), e) - begin(d);}
                                                                                        void push(int v, int L, int R){
                                                                                 19
           // get index
                                                                                            if (lz[v]){
                                                                                 20
       inline T at(int i) const{return d[i];} // get value of index
                                                                                                 if (L != R){
                                                                                 21
                                                                                                     st[LC(v)].mx += lz[v]; // Apply to left
10 | };
                                                                                 22
                                                                                                     st[RC(v)].mx += lz[v]; // And right
                                                                                 23
                            3.5 Sparse Table
                                                                                                     lz[LC(v)] += lz[v];
                                                                                 24
                                                                                                    lz[RC(v)] += lz[v];
                                                                                 25
1 | struct SPT {
                                                                                                }
                                                                                 26
       vec<vec<int>> st:
2
                                                                                                 lz[v] = 0;
                                                                                 27
       SPT(vec<int> &a) {
3
                                                                                            }
                                                                                 28
           int n = SZ(a), K = 0; while((1<<K)<=n) K ++;
                                                                                        }
                                                                                 29
           st = vec<vec<int>>(K, vec<int>(n));
5
                                                                                        void update(int v, int L, int R, int ql, int qr, ll w){
                                                                                 30
           L(i,0,n) st[0][i] = a[i];
                                                                                            if (ql > R || qr < L) return;
                                                                                 31
           L(i,1,K) for (int j = 0; j + (1 << i) <= n; j ++)
                                                                                            push(v, L, R);
                                                                                 32
               st[i][j] = min(st[i-1][j], st[i-1][j+(1 << (i-1))]);
8
                                                                                            if (ql == L \&\& qr == R){
                   // change op
                                                                                                 st[v].mx += w; // Update acutal node
                                                                                 34
       }
9
                                                                                                 lz[v] += w; // Add lazv
                                                                                 35
       int get(int 1, int r) {
10
                                                                                                 push(v, L, R); // Initial spread
                                                                                 36
           int bit = log2(r - 1 + 1);
11
                                                                                                 return;
                                                                                 37
           return min(st[bit][1], st[bit][r - (1<<bit) + 1]); // change op
12
                                                                                            }
                                                                                 38
       }
13
                                                                                            int m = MD(L, R);
                                                                                 39
14 };
                                                                                            update(LC(v), L, m, ql, min(qr, m), w);
                                                                                 40
                           3.6 Segment tree
                                                                                            update(RC(v), m + 1, R, max(m + 1, ql), qr, w);
                                                                                 41
                                                                                            st[v] = merge(st[LC(v)], st[RC(v)]);
                                                                                 42
                                                                                 43
  #define LC(v) (v<<1)
                                                                                        node query(int v, int L, int R, int ql, int qr){
   #define RC(v) ((v<<1)|1)
                                                                                 44
                                                                                            if (q1 > R || qr < L) return {oo, oo};
  #define MD(L, R) (L+((R-L)>>1))
                                                                                 45
                                                                                            push(v, L, R);
   struct node { ll mx;ll cant; };
                                                                                 46
                                                                                            if (ql == L && qr == R) return st[v];
                                                                                 47
  struct ST {
5
                                                                                            int m = MD(L, R);
       vec<node> st; vec<ll> lz; int n;
                                                                                 48
6
                                                                                            return merge(query(LC(v), L, m, ql, min(m, qr)), query(RC(v), m
       ST(int n = 1): st(4 * n + 10, {oo, oo}), lz(4 * n + 10, 0), n(n) {
                                                                                 49
7
                                                                                                 + 1, R, max(m + 1, ql), qr));
           build(1, 0, n - 1);}
       node merge(node a, node b){
                                                                                 50
8
                                                                                        node query(int 1, int r){return query(1, 0, n - 1, 1, r);}
           if (a.mx == oo) return b; if (b.mx == oo) return a;
                                                                                 51
9
                                                                                        void update(int l, int r, ll w){update(1, 0, n - 1, l, r, w);}
           if (a.mx == b.mx) return {a.mx, a.cant + b.cant};
                                                                                 52
```

₅₃ };

3.7 Segment Tree Iterativo

```
1 struct STI {
       vec<ll> st; int n, K;
2
       STI(vec<11> &a): n(SZ(a)), K(1) {
3
           while(K<=n) K<<=1;
           st.assign(2*K, 0); // 0 default
5
           L(i,0,n) st[K+i] = a[i];
           for (int i = K - 1; i > 0; i - - ) st[i] = st[i*2] + st[i*2+1];}
7
       void upd(int pos, ll w) {
8
           pos += K; st[pos] += w;
9
           while((pos>>=1) > 0) st[pos] = st[pos * 2] + st[pos * 2 + 1];}
10
       11 query(int 1, int r) { // [1, r]
11
           11 \text{ res} = 0:
12
           for (1 += K, r += K + 1; 1 < r; 1>>=1; r>>=1){
13
               if (1 & 1) res += st[l++]:
14
               if (r & 1) res += st[--r];
15
           }
16
           return res;
17
       }
18
19 };
```

3.8 Segment Tree Persistente

```
struct Vertex{Vertex * 1, *r;int sum;};
  const int MVertex = 6000000; // = N * logN * 2
  Vertex pool[MVertex]; // the idea is to keep versions on vec<Vertex*>
       roots; roots.pb(build(ST_L, ST_R));
  int p_num = 0;
                      //
   Vertex * init_leaf(int x) {
       pool[p_num].sum = x;
6
       pool[p_num].l = pool[p_num].r = NULL;
7
       return &pool[p_num++];
8
9
   Vertex * init_node(Vertex * 1, Vertex * r) {
       int sum = 0;
11
       if (1) sum += 1->sum;
12
       if (r) sum += r->sum:
13
       pool[p_num].sum = sum; pool[p_num].l = 1; pool[p_num].r = r;
14
       return &pool[p_num++];}
15
   Vertex * build(int L, int R){
16
       if (L == R){return init_leaf(0);}
17
       int m = MD(L, R); return init_node(build(L, m), build(m + 1, R));}
18
```

```
Vertex * update(Vertex * v, int L, int R, int pos, int w){
       if (L == R)return init_leaf(v->sum + w);
       int m = MD(L, R);
21
       if (pos <= m) return init_node(update(v->1, L, m, pos, w), v->r);
       return init_node(v->1, update(v->r, m + 1, R, pos, w));}
   int query(Vertex * v1, Vertex * vr, int L, int R, int q1, int qr) {
       if (!vl || !vr) return 0;
25
       if (ql > R \mid | qr < L) return 0;
26
       if (ql == L && qr == R) {return vr->sum - vl->sum;}
27
       int m = MD(L, R);
28
       return query(vl->1, vr->1, L, m, ql, min(m, qr)) +
29
           query(vl->r, vr->r, m + 1, R, max(m + 1, ql), qr);
30
                           3.9 Policy Based
#include <ext/pb_ds/assoc_container.hpp>
  using namespace __gnu_pbds;
   template<typename Key, typename Val=null_type>
   using indexed_set = tree<Key, Val, less<Key>, rb_tree_tag,
                            tree_order_statistics_node_update>;
6 // indexed set<char> s:
```

4 Graph

template<class Key,class Val=null_type>using htable=gp_hash_table<Key,

10 // como unordered_map (o unordered_set si Val es vacio), pero sin metodo

4.1 Bellman Ford

```
struct Edge {int a, b, cost;};
vector<Edge> edges;
  int solve(int s) // Source
  {
4
       vector<int> d(n, INF);
5
       d[s] = 0:
6
      for (int i = 0; i < n - 1; ++i)
7
          for (Edge e : edges)
8
              if (d[e.a] < INF)
9
                   d[e.b] = min(d[e.b], d[e.a] + e.cost);
10
```

7 // char val = *s.find_by_order(0); // acceso por indice

Val>:

count

// int idx = s.order_of_key('a'); // busca indice del valor

4.2 SCC

```
vec<int> dfs_num(N, -1), dfs_low(N, -1), in_stack(N);
   int dfs_count = 0;
   int numSCC = 0;
   stack<int> st;
   void dfs(int u){
     dfs_low[u]=dfs_num[u]=dfs_count++;
     st.push(u);
     in_stack[u] = 1;
     for(int v: G[u]) {
       if (dfs_num[v] == -1) dfs(v);
       if (in_stack[v]) dfs_low[u] = min(dfs_low[u], dfs_low[v]);
11
12
     if (dfs_num[u] == dfs_low[u]){
13
       numSCC ++:
14
       while(1){
15
         int v = st.top(); st.pop();
16
         in_stack[v] = 0;
17
         if (u == v) break;
18
19
     }
20
  |}
21
```

4.3 Bipartite Matching Hopcroft-Karp - With Konig

```
nt19937 rng((int) chrono::steady_clock::now().time_since_epoch().count()
       );
  struct hopcroft_karp {
     int n, m; // n is Left Partition Size, m is Right Partition Size
     vec<vec<int>> g;
     vec<int> dist, nxt, ma, mb;
     hopcroft_karp(int n_, int m_) : n(n_), m(m_), g(n),
       dist(n), nxt(n), ma(n, -1), mb(m, -1) {}
     void add(int a, int b) { g[a].pb(b); }
8
     bool dfs(int i) {
9
       for (int &id = nxt[i]; id < g[i].size(); id++) {</pre>
10
         int j = g[i][id];
11
         if (mb[i] == -1 \text{ or } (dist[mb[i]] == dist[i]+1 \text{ and } dfs(mb[i])))  {
12
           ma[i] = j, mb[j] = i;
13
           return true;
14
         }
15
       }
16
```

```
return false;
17
     }
18
     bool bfs() {
19
       for (int i = 0; i < n; i++) dist[i] = n;
20
       queue<int> q;
21
       for (int i = 0; i < n; i++) if (ma[i] == -1) {
         dist[i] = 0;
         q.push(i);
       }
       bool rep = 0;
       while (q.size()) {
27
         int i = q.front(); q.pop();
         for (int j : g[i]) {
29
           if (mb[j] == -1) rep = 1;
           else if (dist[mb[j]] > dist[i] + 1) {
              dist[mb[j]] = dist[i] + 1;
             q.push(mb[j]);
         }
35
       }
       return rep;
37
38
     int matching() {
39
       int ret = 0;
40
       for (auto& i : g) shuffle(ALL(i), rng);
41
       while (bfs()) {
42
         for (int i = 0; i < n; i++) nxt[i] = 0;
43
         for (int i = 0; i < n; i++)
44
           if (ma[i] == -1 \text{ and } dfs(i)) \text{ ret++};
45
46
       return ret;
47
48
     vec<int> cover[2]; // if cover[i][j] = 1 -> node i, j is part of cover
49
     int konig() {
50
       cover[0].assign(n,1); // n left size
51
       cover[1].assign(m,0); // m right size
52
       auto go = [&](auto&& me, int u) -> void {
53
         cover[0][u] = false:
         for (auto v : g[u]) if (!cover[1][v]) {
           cover[1][v] = true;
           me(me,mb[v]);
57
58
       };
59
```

```
L(u,0,n) if (ma[u] < 0) go(go,u);
                                                                                                }
60
                                                                                     36
       return size;
                                                                                              }
61
                                                                                    37
    }
                                                                                              L(k, 0, n) if (k!=j \text{ and } sn[k])
62
                                                                                    38
63 };
                                                                                                auto w = ds[k]-ds[j]; v[k] += w, u[vR[k]] -= w;
                                                                                     39
                                                                                              }
                                                                                     40
                              4.4 Hungarian
                                                                                              u[s] += ds[i];
                                                                                    41
                                                                                              while (dad[j] \ge 0) { int d = dad[j]; vR[j] = vR[d]; vL[vR[j]] = j;
                                                                                     42
                                                                                                  i = d; }
using vi = vec<int>;
                                                                                              vR[j] = s; vL[s] = j;
using vd = vec<ld>;
   const ld INF = 1e100;
                            // Para max asignacion, INF = 0, y negar costos
                                                                                            ld value = 0; L(i, 0, n) value += cs[i][vL[i]], ans.pb({i, vL[i]});
   bool zero(ld x) {return fabs(x) < 1e-9;} // Para int/ll: return x==0;
                                                                                    45
                                                                                            return value;
   vec<pii> ans; // Guarda las aristas usadas en el matching: [0..n)x[0..m)
                                                                                         }
   struct Hungarian{
                                                                                     47
                                                                                    48 };
     int n; vec<vd> cs; vi vL, vR;
7
     \label{eq:hungarian} \mbox{Hungarian(int N, int M) : $n(\max(N,M))$, $cs(n,vd(n))$, $vL(n)$, $vR(n)${\{}}
                                                                                                                 4.5 Flow - Dinics
       L(x, 0, N) L(y, 0, M) cs[x][y] = INF;
9
10
     void set(int x, int y, ld c) { cs[x][y] = c; }
                                                                                     1 | struct Dinic {
11
     ld assign(){
                                                                                          bool scaling = false; // com scaling -> O(nm log(MAXCAP)),
       int mat = 0; vd ds(n), u(n), v(n); vi dad(n), sn(n);
                                                                                                                       // com constante alta
                                                                                          int lim:
13
       L(i, 0, n) u[i] = *min_element(ALL(cs[i]));
                                                                                          struct edge {
14
       L(j, 0, n){
                                                                                            int to, cap, rev, flow;
15
         v[i] = cs[0][i]-u[0];
                                                                                            bool res;
16
                                                                                     6
         L(i, 1, n) v[j] = min(v[j], cs[i][j] - u[i]);
                                                                                            edge(int to_, int cap_, int rev_, bool res_)
17
                                                                                     7
                                                                                              : to(to_), cap(cap_), rev(rev_), flow(0), res(res_) {}
       }
18
                                                                                     8
       vL = vR = vi(n, -1):
                                                                                          };
                                                                                     9
19
       L(i,0, n) L(i,0,n) if (vR[i] == -1 \text{ and } zero(cs[i][i] - u[i] - v[i])
                                                                                          vec<vec<edge>> g;
20
                                                                                          vec<int> lev, beg;
                                                                                    11
         vL[i] = j; vR[j] = i; mat++; break;
                                                                                          11 F;
                                                                                    12
^{21}
                                                                                          Dinic(int n) : g(n), F(0) {}
22
                                                                                    13
       for(; mat < n; mat ++){</pre>
                                                                                          void add(int a, int b, int c) {
                                                                                    14
23
         int s = 0, j = 0, i;
                                                                                            g[a].emplace_back(b, c, g[b].size(), false);
                                                                                    15
24
         while(vL[s] != -1) s++;
                                                                                            g[b].emplace_back(a, 0, g[a].size()-1, true);
                                                                                    16
25
         fill(ALL(dad), -1); fill(ALL(sn), 0);
                                                                                    17
26
         L(k, 0, n) ds[k] = cs[s][k]-u[s]-v[k];
                                                                                          bool bfs(int s, int t) {
27
                                                                                    18
         while(true){
                                                                                            lev = vector\langle int \rangle(g.size(), -1); lev[s] = 0;
                                                                                    19
28
           i = -1;
                                                                                            beg = vector<int>(g.size(), 0);
                                                                                    20
29
           L(k, 0, n) if(!sn[k] and (j == -1 \text{ or } ds[k] < ds[j])) <math>j = k;
                                                                                            queue<int> q; q.push(s);
                                                                                    21
30
           sn[j] = 1; i = vR[j];
                                                                                            while (q.size()) {
                                                                                    22
31
           if(i == -1) break;
                                                                                              int u = q.front(); q.pop();
                                                                                    23
32
           L(k, 0, n) if(!sn[k]){
                                                                                              for (auto& i : g[u]) {
33
                                                                                    24
              auto new_ds = ds[j] + cs[i][k] - u[i]-v[k];
                                                                                                if (lev[i.to] != -1 or (i.flow == i.cap)) continue;
                                                                                    25
34
             if(ds[k] > new_ds) ds[k] = new_ds, dad[k] = j;
                                                                                                if (scaling and i.cap - i.flow < lim) continue;
35
                                                                                    26
```

```
lev[i.to] = lev[u] + 1;
                                                                                   3 template<typename T> struct mcmf {
27
           q.push(i.to);
                                                                                        struct edge {
28
         }
                                                                                         int to, rev, flow, cap; // para, id da reversa, fluxo, capacidade
29
       }
                                                                                         bool res; // se eh reversa
30
       return lev[t] != -1;
                                                                                         T cost; // custo da unidade de fluxo
31
                                                                                         edge(): to(0), rev(0), flow(0), cap(0), cost(0), res(false) {}
32
                                                                                         edge(int to_, int rev_, int flow_, int cap_, T cost_, bool res_)
     int dfs(int v, int s, int f = oo) {
33
                                                                                           : to(to_), rev(rev_), flow(flow_), cap(cap_), res(res_), cost(
       if (!f or v == s) return f;
34
                                                                                  10
       for (int& i = beg[v]; i < g[v].size(); i++) {</pre>
                                                                                                cost_) {}
35
         auto& e = g[v][i];
                                                                                       };
                                                                                  11
36
         if (lev[e.to] != lev[v] + 1) continue;
                                                                                       vec<vec<edge>> g;
37
                                                                                  12
         int foi = dfs(e.to, s, min(f, e.cap - e.flow));
                                                                                       vec<int> par_idx, par;
38
                                                                                  13
         if (!foi) continue:
                                                                                       T inf:
39
                                                                                  14
         e.flow += foi, g[e.to][e.rev].flow -= foi;
                                                                                       vec<T> dist:
                                                                                  15
         return foi:
                                                                                       mcmf(int n) : g(n), par_idx(n), par(n), inf(numeric_limits<T>::max()
                                                                                  16
41
       }
42
                                                                                       void add(int u, int v, int w, T cost) { // de u pra v com cap w e
       return 0;
43
                                                                                           custo cost
44
     ll max flow(int s. int t) {
                                                                                         edge a = edge(v, g[v].size(), 0, w, cost, false);
                                                                                  18
45
                                                                                         edge b = edge(u, g[u].size(), 0, 0, -cost, true);
       for (lim = scaling ? (1<<30) : 1; lim; lim /= 2)
46
         while (bfs(s, t)) while (int ff = dfs(s, t)) F += ff;
                                                                                         g[u].push_back(a);
                                                                                  20
47
       return F;
                                                                                         g[v].push_back(b);
48
                                                                                  21
     }
                                                                                  22
49
                                                                                       vec<T> spfa(int s) { // nao precisa se nao tiver custo negativo
                                                                                  23
50
   vec<pair<int, int>> get_cut(Dinic& g, int s, int t) {
                                                                                         deque<int> q;
                                                                                  24
51
                                                                                         vec<bool> is_inside(g.size(), 0);
     g.max_flow(s, t);
                                                                                  25
52
     vec<pair<int, int>> cut;
                                                                                         dist = vec<T>(g.size(), inf);
                                                                                  26
53
     vec<int> vis(g.g.size(), 0), st = {s};
                                                                                         dist[s] = 0;
                                                                                  27
54
     vis[s] = 1;
                                                                                         q.push_back(s);
                                                                                  28
55
     while (st.size()) {
                                                                                         is_inside[s] = true;
56
       int u = st.back(); st.pop_back();
                                                                                         while (!q.empty()) {
57
                                                                                  30
       for (auto e : g.g[u]) if (!vis[e.to] and e.flow < e.cap)</pre>
                                                                                           int v = q.front();
                                                                                  31
58
         vis[e.to] = 1, st.push_back(e.to);
                                                                                           q.pop_front();
                                                                                  32
59
                                                                                           is_inside[v] = false;
     }
                                                                                  33
60
     for (int i = 0; i < g.g.size(); i++) for (auto e : g.g[i])
                                                                                           for (int i = 0; i < g[v].size(); i++) {
                                                                                  34
61
       if (vis[i] and !vis[e.to] and !e.res) cut.emplace_back(i, e.to);
                                                                                              auto [to, rev, flow, cap, res, cost] = g[v][i];
                                                                                  35
                                                                                             if (flow < cap and dist[v] + cost < dist[to]) {</pre>
     return cut:
63
                                                                                  36
                                                                                                dist[to] = dist[v] + cost:
64 | }
                                                                                  37
                    4.6 Flow - MinCostMaxFlow
                                                                                                if (is_inside[to]) continue;
                                                                                  39
                                                                                                if (!q.empty() and dist[to] > dist[q.front()]) q.push_back(to)
                                                                                  40
_1 // 0(nm + f * m log n)
                                                                                                else q.push_front(to);
2 // const ll oo = (ll)1e18;
                                                                                  41
```

```
is_inside[to] = true;
                                                                                              while (u != s) {
42
                                                                                     85
                                                                                                 g[par[u]][par_idx[u]].flow += mn_flow;
                                                                                     86
43
         }
                                                                                                g[u][g[par[u]][par_idx[u]].rev].flow -= mn_flow;
                                                                                     87
44
       }
                                                                                                 u = par[u];
45
       return dist;
                                                                                              }
                                                                                     89
46
                                                                                              f += mn_flow;
47
                                                                                     90
     bool dijkstra(int s, int t, vec<T>& pot) {
48
                                                                                     91
       priority_queue<pair<T, int>, vec<pair<T, int>>, greater<>> q;
                                                                                            return make_pair(f, ret);
49
                                                                                     92
       dist = vec<T>(g.size(), inf);
50
                                                                                     93
       dist[s] = 0;
                                                                                          // Opcional: retorna as arestas originais por onde passa flow = cap
51
                                                                                     94
       q.emplace(0, s);
                                                                                          vec<pair<int,int>> recover() {
52
                                                                                     95
                                                                                            vec<pair<int,int>> used;
       while (q.size()) {
53
                                                                                     96
                                                                                            for (int i = 0; i < g.size(); i++) for (edge e : g[i])
         auto [d, v] = q.top();
                                                                                     97
                                                                                              if(e.flow == e.cap && !e.res) used.push_back({i, e.to});
         q.pop();
55
         if (dist[v] < d) continue;</pre>
                                                                                            return used:
                                                                                     99
56
         for (int i = 0; i < g[v].size(); i++) {
                                                                                         }
57
                                                                                     100
                                                                                    <sub>101</sub> |};
           auto [to, rev, flow, cap, res, cost] = g[v][i];
58
           cost += pot[v] - pot[to];
59
                                                                                                                       4.7 2 Sat
           if (flow < cap and dist[v] + cost < dist[to]) {</pre>
60
              dist[to] = dist[v] + cost;
61
              q.emplace(dist[to], to);
                                                                                     1 struct TwoSat {
62
              par_idx[to] = i, par[to] = v;
63
                                                                                            int n, v_n;
64
                                                                                            vec<bool> vis, assign;
65
                                                                                            vec<int> order, comp;
                                                                                     4
       }
                                                                                            vec<vec<int>> g, g_t;
66
                                                                                     5
       return dist[t] < inf;</pre>
                                                                                            TwoSat(int n_{-}): n(n_{-}), v_{-}n(2 * n_{-}), vis(v_{-}n), assign(n_{-}), comp(v_{-}n_{-})
67
                                                                                     6
                                                                                                 , - 1), g(v_n), g_t(v_n) {
68
     pair<int, T> min_cost_flow(int s, int t, int flow = (int)1e9) {
                                                                                                 order.reserve(v_n);
69
                                                                                     7
       vec<T> pot(g.size(), 0);
                                                                                            }
70
                                                                                     8
       pot = spfa(s); // mudar algoritmo de caminho minimo aqui
                                                                                            void add_disj(int a, bool na, int b, bool nb) { // negated_a,
71
                                                                                     9
       int f = 0;
72
                                                                                                 negated_b
       T ret = 0:
                                                                                                 a = 2 * a ^na;
73
                                                                                     10
       while (f < flow and dijkstra(s, t, pot)) {
                                                                                                 b = 2 * b ^nb;
74
                                                                                     11
         for (int i = 0; i < g.size(); i++)
                                                                                                 int neg_a = a ^1;
75
                                                                                     12
           if (dist[i] < inf) pot[i] += dist[i];</pre>
                                                                                                 int neg_b = b^1;
76
                                                                                     13
         int mn_flow = flow - f, u = t;
77
                                                                                                 g[neg_a].pb(b);
                                                                                     14
         while (u != s){
78
                                                                                                 g[neg_b].pb(a);
                                                                                     15
           mn_flow = min(mn_flow,
                                                                                                 g_t[a].pb(neg_b);
79
                                                                                     16
             g[par[u]][par_idx[u]].cap - g[par[u]][par_idx[u]].flow);
                                                                                                 g_t[b].pb(neg_a);
80
                                                                                     17
           u = par[u];
81
                                                                                     18
                                                                                            void dfs1(int u){
82
                                                                                     19
         ret += pot[t] * mn_flow;
                                                                                                 vis[u] = 1:
83
                                                                                     20
         u = t;
84
                                                                                                 for (int v: g[u]) if (!vis[v]) dfs1(v);
                                                                                     21
```

```
order.pb(u);
22
       }
23
       void dfs2(int u, int cc) {
^{24}
            comp[u] = cc;
25
           for (int v: g_t[u]) if (comp[v] == -1) dfs2(v, cc);
26
       }
27
       bool solve() {
28
           order.clear();
29
           vis.assign(v_n, 0);
30
           L(i,0, v_n) if (!vis[i]) dfs1(i);
31
           comp.assign(v_n, - 1);
32
           int cc = 0;
33
           L(i, 0, v_n) \{
34
                int v = order[v_n - 1 - i];
35
                if (comp[v] == -1) dfs2(v, cc ++);
36
37
           assign.assign(n, false);
38
           for (int i = 0;i < v_n; i += 2) {
39
                if (comp[i] == comp[i+1]) return false;
40
                assign[i / 2] = comp[i] > comp[i + 1];
41
           }
42
           return true;
43
       }
44
45 };
```

4.8 Euler Tour

```
// Directed version (uncomment commented code for undirected)
  struct edge {
2
       int v;
3
       list<edge>::iterator rev;
       edge(int y):y(y){}
5
   };
6
   list<edge> g[N];
   void add_edge(int a, int b){
       g[a].push_front(edge(b));//auto ia=g[a].begin();
9
         g[b].push_front(edge(a));auto ib=g[b].begin();
10
         ia->rev=ib;ib->rev=ia;
11
12
   vec<int> p;
13
   void go(int x){
14
       while(g[x].size()){
15
           int y=g[x].front().y;
16
```

```
//g[y].erase(g[x].front().rev);
17
           g[x].pop_front();
18
           go(y);
19
20
       p.push_back(x);
21
22
   vec<int> get_path(int x){ // get a path that begins in x
   // check that a path exists from x before calling to get_path!
       p.clear();go(x);reverse(p.begin(),p.end());
       return p;
26
27 }
```

5 Trees

5.1 Heavy Light Decomposition

```
int ans[N], par[N], depth[N], head[N], pos[N];
   vec<int> heavy(N, - 1);
   int t = 0;
   vec<int> g[N];
   int dfs(int u) {
       int size = 1;
       int max_size = 0;
       for (int v: g[u]) if (v != par[u]) {
8
           par[v] = u;
9
           depth[v] = depth[u] + 1;
10
           int cur_size = dfs(v);
11
           size += cur_size;
12
           if (cur_size > max_size) {
13
               max_size = cur_size;
14
               heavv[u] = v;
15
           }
16
       }
17
       return size;
18
19
   void decompose(int u, int h){
20
       head[u] = h;
21
       pos[u] = t ++;
22
       if (heavy[u] != -1){ decompose(heavy[u], h); }
23
       for (int v: G[u]) if (v != par[u] && v != heavy[u]) {
24
           decompose(v, v);
25
       }
26
27 }
```

```
28 int query(int a, int b) {
       int resp = -1;
29
       for (; head[a] != head[b]; b = par[head[b]]){ // Subi todo el heavy
30
           path y a su padre // Next
           if (depth[head[a]] > depth[head[b]]) swap(a, b);
31
           resp = max(resp, st.query(pos[head[b]], pos[b])); // pos[head[b]
32
               ]] < pos[b]
       }
33
       if (depth[a] > depth[b]) swap(a, b); // Una vez misma path(head)
34
           entonces es una query [a,b]
       resp = max(resp, st.query(pos[a], pos[b]));
35
       return resp;
36
37
   dfs(root):
  decompose(root, root);
                              5.2 Centroid
1 | int sz[N];
  bool removed[N];
   int getSize(int u, int p){
       sz[u] = 1:
4
       for(int v: G[u]) if (v != p && !removed[v]){
5
           sz[u] += getSize(v, u);
       }
7
       return sz[u];
8
9
   int centroid(int u, int p, int tz){
       for (int v: g[u])
11
           if (v != p && !removed[v] && sz[v] * 2 > tz) return centroid(v,
12
               u, tz);
       return u;
13
14
   int build(int u){
       int c = centroid(u, -1, getSize(u, -1));
16
       removed[c] = 1:
       for (int v: G[c]) if (!removed[v]) { build(v); }
       return c;
19
20 }
                 5.3 LCA - Binary exponentiation
vec<int> g[N];
2 | int K; // K should be (1<<K) > n
```

```
3 int jump[20][N];
   int depth[N];
   void dfs(int u, int p){
       for (int v: g[u]) if (v != p) {
            jump[0][v] = u;
8
           L(i, 1, K + 1) {
9
                jump[i][v] = -1;
10
                if (jump[i - 1][v] != -1) {
11
                    jump[i][v] = jump[i - 1][jump[i - 1][v]];
12
13
           }
14
           depth[v] = depth[u] + 1;
15
           dfs(v, u);
       }
17
18
   int LCA(int u, int v){
       if (depth[u] < depth[v]) swap(u, v); // Make u the deepest
21
       for (int i = K; i \ge 0; i \longrightarrow 0) // make them same depth
           if (jump[i][u] != -1 \&\& depth[jump[i][u]] >= depth[v]){
23
                u = jump[i][u];
24
           }
25
       }
26
       if (u == v) return u; // u is parent of v
27
       for (int i = K; i \ge 0; i --){
28
           if (jump[i][u] != jump[i][v] && jump[i][u] != -1 && jump[i][v]
29
                ! = -1){}
                u = jump[i][u];
                v = jump[i][v];
31
           }
32
33
       return jump[0][u];
34
35 }
                         5.4 LCA - Const Time
1 struct LCA {
       vec<int> depth, in, euler;
       vec<vec<int>> g, st;
3
4
       inline int Min(int i, int j) {return depth[i] <= depth[j] ? i : j;}</pre>
5
```

void dfs(int u, int p) {

6

```
in[u] = SZ(euler);
 7
            euler.pb(u);
 8
            for (int v: g[u]) if (v != p){
 9
                depth[v] = depth[u] + 1;
10
                dfs(v, u);
11
                euler.pb(u);
12
            }
13
       }
14
       LCA(int n_): depth(n_), g(vec < vec < int >> (n_)), K(0), n(n_), in(n_) {
15
            euler.reserve(2 * n); }
       void add_edge(int u, int v) {g[u].pb(v);}
16
        void build(int root){
17
            dfs(root, -1):
18
            int ln = SZ(euler);
19
            while((1<<K)<=ln)K++;
20
            st = vec<vec<int>> (K, vec<int>(ln));
21
            L(i,0,\ln) st[0][i] = euler[i];
22
            for (int i = 1; (1 << i) <= ln; i ++) {
23
                for (int j = 0; j + (1 << i) <= ln; <math>j ++) {
24
                     st[i][j] = Min(st[i-1][j], st[i-1][j + (1 << (i-1))]);
25
                }
26
            }
27
       }
28
        int get(int u, int v) {
29
            int su = in[u];
30
            int sv = in[v];
31
            if (sv < su) swap(sv, su);
32
            int bit = log2(sv - su + 1);
33
            return Min(st[bit][su], st[bit][sv - (1<<bit) + 1]);</pre>
34
       }
35
<sub>36</sub> };
```

6 Dynamic Programming

6.1 Knapsack

```
dp[i][w] = max(dp[i-1][w],
                                 dp[i-1][w-weights[i-1]] + values[i-1]);
9
               } else {
10
                   dp[i][w] = dp[i-1][w];
11
12
           }
13
       }
14
       return dp[n][W];
15
16 }
                                 6.2 LIS
vector<int> getLIS(vector<int>& arr) {
       int n = arr.size();
       vector<int> dp(n + 1, INT_MAX); // dp[i] = smallest value that ends
3
            an LIS of length i
       vector<int> len(n);
                                        // Length of LIS ending at each
4
           position
       dp[0] = INT_MIN;
5
       for(int i = 0; i < n; i++) {
6
           int j = upper_bound(dp.begin(), dp.end(), arr[i]) - dp.begin();
7
           dp[j] = arr[i];
           len[i] = j;
9
       }
10
       // Find maxLen and reconstruct sequence
       int maxLen = 0;
12
       for(int i = n-1; i \ge 0; i--) maxLen = max(maxLen, len[i]);
13
       vector<int> lis;
14
       for(int i = n-1, currLen = maxLen; i \ge 0; i--) {
           if(len[i] == currLen) {
16
               lis.push_back(arr[i]);
               currLen--;
18
           }
19
20
       reverse(lis.begin(), lis.end());
21
       return lis:
22
23 }
                                Edit Distance
                           6.3
int editDistance(string& s1, string& s2) {
       int n = s1.length(), m = s2.length();
       vector<vector<int>> dp(n + 1, vector<int>(m + 1));
3
```

for(int i = 0; $i \le n$; i++) dp[i][0] = i;

```
for(int j = 0; j \le m; j++) dp[0][j] = j;
5
       for(int i = 1; i <= n; i++) {
6
           for(int j = 1; j <= m; j++) {
               if(s1[i-1] == s2[j-1]) {
8
                   dp[i][j] = dp[i-1][j-1];
9
               } else {
10
                   dp[i][j] = 1 + min({dp[i-1][j]},
                                                      // deletion
11
                                      dp[i][j-1],
                                                       // insertion
12
                                      dp[i-1][j-1]}); // replacement
13
14
           }
15
       }
16
       return dp[n][m];
17
18 }
                               6.4 Kadane
   pair<int, pair<int,int>> kadane(vector<int>& arr) {
       int maxSoFar = arr[0], maxEndingHere = arr[0];
2
       int start = 0, end = 0, s = 0;
3
4
       for(int i = 1; i < arr.size(); i++) {</pre>
5
           if(maxEndingHere + arr[i] < arr[i]) {</pre>
6
               maxEndingHere = arr[i];
7
               s = i:
           } else {
9
               maxEndingHere += arr[i];
10
           }
11
12
           if(maxEndingHere > maxSoFar) {
13
               maxSoFar = maxEndingHere;
14
               start = s;
15
               end = i;
16
           }
17
18
       return {maxSoFar, {start, end}}; // max, 1, r
19
20 | }
                                    Strings
                               7.1 Hashing
```

static constexpr ll ms[] = {1'000'000'007, 1'000'000'403};

```
static constexpr 11 b = 500'000'000;
   struct StrHash { // Hash polinomial con exponentes decrecientes.
     vec<11> hs[2], bs[2];
     StrHash(string const& s) {
       int n = SZ(s);
       L(k, 0, 2) {
         hs[k].resize(n+1), bs[k].resize(n+1, 1);
         L(i, 0, n) {
           hs[k][i+1] = (hs[k][i] * b + s[i]) % ms[k];
           bs[k][i+1] = bs[k][i] * b
                                               % ms[k];
         }
12
       }
13
     }
14
     ll get(int idx, int len) const { // Hashes en 's[idx, idx+len)'.
       ll h[2];
16
       L(k, 0, 2) {
         h[k] = hs[k][idx+len] - hs[k][idx] * bs[k][len] % ms[k];
18
         if (h[k] < 0) h[k] += ms[k];
19
20
       return (h[0] << 32) | h[1];
21
22
   };
23
24
   pll union_hash(vec<pll> hs, vec<ll> lens){ //use arrays makes it slower
     11 len = 0;
26
     for(int i = hs.size()-1; i > 0; i--){
27
       len += lens[i];
28
       pll& [11, 12] = hs[i];
29
       pll& [r1, r2] = hs[i-1];
       11 = ((11 * binpow(b, len, ms[0])) \% ms[0] + r1) \% ms[0];
31
       12 = ((12 * binpow(b, len, ms[1])) \% ms[1] + r2) \% ms[1];
32
     }
33
34
     return hs[0]:
36 }
                             7.2 Prefix Trie
1 struct Trie {
       map<char, int> ch;
2
       bool eee:
3
       Trie(): eee(0) {}
4
<sub>5</sub> | };
```

```
6 | vec<Trie> t;
   void initTrie(){t.clear();t.pb(Trie());}
   void insert(string &word) {
       int v = 0;
9
       for(char c : word) {
10
           if(!t[v].ch[c]) {
11
               t[v].ch[c] = SZ(t);
12
               t.pb(Trie());
13
           }
14
           v = t[v].ch[c];
15
16
       t[v].eee = 1;
17
18 }
```

7.3 KMP

```
1 | vec<int> kmp(string pat, string sec){ //geeks4geeks implementation with
       some changes
     int m = pat.length();
     int n = sec.length();
     cout << m << "" << n << endl;
5
     vec<int> lps = getLps(pat);
6
     vec<int> res:
7
     int i = 0;
9
     int j = 0;
10
11
     while((n - i) >= (m - j)){
12
       if(pat[j] == sec[i]){
13
         i++;
14
         j++;
15
16
       if(j == m){
17
         res.push_back(i - j);
18
         j = lps[j - 1];
19
20
       else{
21
         if(i < n && pat[j] != sec[i]){</pre>
22
           if(j != 0) j = lps[ j - 1 ];
23
            else i = i + 1;
24
         }
25
       }
26
```

```
}
27
28
     return res;
29
30 }
                                 7.4 LPS
vec<int> getLps(string pat){ //geek4geeks implementatio with some
       changes
     vec<int> lps(pat.length(), 0);
     int len = 0;
     int i = 1;
     lps[0] = 0;
5
     while(i < pat.length()){</pre>
6
       if(pat[i] == pat[len]){
7
         len++;
8
         lps[i] = len;
         i++;
10
       }
11
       else //pat[i] != pat[len]
12
       {
13
         lps[i] = 0;
14
         i++:
15
       }
16
17
     return lps;
18
19 }
                           7.5 Z-FUNCTION
template<class Char=char>vec<int> zfun(const basic_string<Char>& w) {
     int n = SZ(w), l = 0, r = 0; vec<int> <math>z(n);
    z[0] = w.length();
    L(i, 1, n) {
       if (i \le r) \{z[i] = min(r - i + 1, z[i - 1]);\}
       while (i + z[i] < n \&\& w[z[i]] == w[i + z[i]]) \{++z[i]:\}
6
       if (i + z[i] - 1 > r) \{l = i, r = i + z[i] - 1;\}
7
    }
8
     return z;
9
10 }
                             7.6 Manacher
1 | struct Manacher {
```

r = t;

```
vec<int> p;
2
     Manacher(string const& s) {
3
       int n = SZ(s), m = 2*n+1, l = -1, r = 1;
4
       vec < char > t(m); L(i, 0, n) t[2*i+1] = s[i];
5
       p.resize(m); L(i, 1, m) {
         if (i < r) p[i] = min(r-i, p[l+r-i]);
         while (p[i] \le i \&\& i \le m-p[i] \&\& t[i-p[i]] == t[i+p[i]]) ++p[i];
         if (i+p[i] > r) l = i-p[i], r = i+p[i];
9
       }
10
     } // Retorna palindromos de la forma {comienzo, largo}.
     pii at(int i) const {int k = p[i]-1; return pair{i/2-k/2, k};}
12
    pii odd(int i) const {return at(2*i+1);} // Mayor centrado en s[i].
13
    pii even(int i) const {return at(2*i);} // Mayor centrado en s[i-1,i].
15 };
```

7.7 Aho-Corasick

```
bool vis[N], r[N];
   struct ACvertex {
     map<char,int> next,go;
     int p,link;
     char pch;
     vec<int> leaf;
     ACACvertex(int p=-1, char pch=-1):p(p),pch(pch),link(-1){}
7
8
   vec<ACvertex> t:
   void aho_init(){ //do not forget!!
     t.clear();t.pb(ACvertex());
11
12
   void add_string(string &s, int id){
13
     int v=0;
14
     for(char c:s){
15
       if(!t[v].next.count(c)){
16
         t[v].next[c]=t.size();
17
         t.pb(ACvertex(v,c));
18
19
       v=t[v].next[c];
20
21
     t[v].leaf.pb(id);
22
23
   int go(int v, char c);
   int get_link(int v){ // Failure link
     if(t[v].link<0)</pre>
```

```
if(!v||!t[v].p)t[v].link=0;
27
       else t[v].link=go(get_link(t[v].p),t[v].pch);
28
     return t[v].link;
29
30
   int go(int v, char c){ // state = go(state, ch) this state is ACvertex
31
       id
     if(!t[v].go.count(c))
32
       if(t[v].next.count(c))t[v].go[c]=t[v].next[c];
33
       else t[v].go[c]=v==0?0:go(get_link(v),c);
34
     return t[v].go[c];
36
   void proc(int x){
37
       if (x == -1|| vis[x]) return:
38
       vis[x] = 1;
39
       L(i,0,SZ(t[x].leaf)) r[t[x].leaf[i]] = 1;
40
       proc(get_link(x));
41
42 }
                            7.8 Suffix-Array
| #define RB(x) ((x) < n ? r[x] : 0)
   void csort(vec<int>& sa, vec<int>& r, int k) {
     int n = SZ(sa);
     vec<int> f(max(255, n)), t(n);
    L(i,0, n) ++f[RB(i+k)];
5
     int sum = 0:
    L(i,0, \max(255, n)) f[i] = (sum += f[i]) - f[i];
    L(i,0, n) t[f[RB(sa[i]+k)]++] = sa[i];
     sa = t;
9
10
   vec<int> compute_sa(string& s){ // O(n*log2(n))
     int n = SZ(s) + 1, rank;
12
     vec<int> sa(n), r(n), t(n);
13
     iota(all(sa), 0);
14
     L(i,0, n) r[i] = s[i];
15
     for (int k = 1; k < n; k *= 2) {
16
       csort(sa, r, k), csort(sa, r, 0);
17
       t[sa[0]] = rank = 0;
18
       L(i, 1, n) {
19
         if(r[sa[i]] != r[sa[i-1]] || RB(sa[i]+k) != RB(sa[i-1]+k)) ++rank;
20
         t[sa[i]] = rank;
21
       }
22
```

```
if (r[sa[n-1]] == n-1) break;
24
25
     return sa; // sa[i] = i-th suffix of s in lexicographical order
26
27
    vec<int> compute_lcp(string& s, vec<int>& sa){
28
      int n = SZ(s) + 1, K = 0;
29
     vec<int> lcp(n), plcp(n), phi(n);
     phi[sa[0]] = -1;
31
     L(i, 1, n) phi[sa[i]] = sa[i-1];
32
     L(i,0,n) {
33
       if (phi[i] < 0) { plcp[i] = 0; continue; }</pre>
34
       while(s[i+K] == s[phi[i]+K]) ++K;
35
       plcp[i] = K;
       K = \max(K - 1, 0);
37
38
     L(i,0, n) lcp[i] = plcp[sa[i]];
     return lcp; // lcp[i] = longest common prefix between sa[i-1] and sa[i
41 }
```

8 Math

8.1 Euclidean Extended

```
1 | 11 extendedGCD(11 a, 11 b, 11 &x, 11 &y) {
       if (b == 0) {
2
           x = 1:
3
           y = 0;
4
           return a;
5
       }
6
       ll x1, y1;
       ll gcd = extendedGCD(b, a % b, x1, y1);
8
       x = v1;
9
       y = x1 - (a / b) * y1;
10
       return gcd;
11
12
13
  |bool findSolutionWithConstraints(ll a, ll b, ll c, ll x_min, ll y_min,
       11 &x, 11 &y) {
       11 g = extendedGCD(a, b, x, y);
15
16
       if (c % g != 0) return false;
17
18
```

```
x *= c / g;
19
       y *= c / g;
20
21
       // Ajustamos las variables a/g y b/g para mover las soluciones
       a /= g;
23
       b /= g;
24
       if (x < x_min) {
           ll k = (x_min - x + b - 1) / b; // Redondeo hacia arriba
           x += k * b;
           y -= k * a;
29
       } else if (x > x_min) {
           11 k = (x - x min) / b:
31
           x -= k * b;
           y += k * a;
       }
35
       if (y < y_min) {
           ll k = (y_min - y + a - 1) / a; // Redondeo hacia arriba
37
           x += k * b;
           v -= k * a;
39
       } else if (y > y_min) {
           11 k = (y - y_min) / a;
41
           x -= k * b;
           v += k * a;
43
       }
44
45
46
       return x \ge x_min & y \ge y_min;
47 }
```

8.2 Euler Totient

```
#include <bits/stdc++.h>
using namespace std;
typedef long long ll;

vector<ll> compute_totients(ll n) {
    vector<ll> phi(n + 1);
    for (ll i = 0; i <= n; i++) {
        phi[i] = i;
    }
}</pre>
```

```
for (ll i = 2; i <= n; i++) {
12
           if (phi[i] == i) { // i es primo
13
               for (ll j = i; j <= n; j += i) {
14
                   phi[j] = phi[j] * (i - 1) / i;
15
               }
16
           }
17
       }
18
19
       return phi;
20
21 }
```

8.3 Josephus

```
#include <iostream>
   using namespace std;
    typedef long long 11;
5
   ll josephus_iterative(ll n, ll k) {
       11 result = 0;
7
       for (ll i = 2; i <= n; ++i) {
8
            result = (result + k) % i;
9
10
       return result;
11
12
13
14
   ll josephus_recursive(ll n, ll k) {
15
16
       if (n == 1)
17
            return 0;
18
19
       return (josephus_recursive(n - 1, k) + k) % n;
20
^{21}
^{22}
23
   11 josephus_power_of_2(11 n) {
^{24}
25
       11 power = 1;
26
       while (power <= n) {</pre>
27
            power <<= 1;
28
       }
29
       power >>= 1;
30
```

```
31
32
33
       return 2 * (n - power);
34 }
                                8.4 Mobius
 #include <bits/stdc++.h>
   using namespace std;
   typedef long long 11;
   vector<ll> compute_mobius(ll n) {
       vector<ll> mu(n + 1, 1);
       vector<bool> is_prime(n + 1, true);
9
       for (ll i = 2; i <= n; i++) {
10
           if (is_prime[i]) { // i es un primo
11
               for (ll j = i; j <= n; j += i) {
12
                    mu[j] *= -1; // Multiplicamos por -1 para cada primo
13
                    is_prime[j] = false;
15
               for (ll j = i * i; j \le n; j += i * i) {
                    mu[j] = 0; // Si tiene un cuadrado de un primo, se pone
17
                        en 0
               }
18
           }
19
       }
20
21
       return mu;
22
23
24
25
   11 mobius(ll x) {
       11 count = 0;
27
       for (11 i = 2; i * i <= x; i++) {
28
           if (x \% (i * i) == 0)
29
               return 0:
30
           if (x \% i == 0) {
31
                count++;
32
                x /= i;
33
           }
34
```

```
36
                                                                                      36
       if (x > 1) count++;
37
                                                                                      37
38
                                                                                      38
       return (count % 2 == 0) ? 1 : -1;
39
                                                                                      39
40 }
                                                                                      40
                                                                                      41
                                   8.5 NTT
                                                                                      42
  #include <bits/stdc++.h>
   using namespace std;
                                                                                                  }
   using cd = complex<double>;
                                                                                      46
                                                                                              }
   typedef long long 11;
                                                                                      47
   const 11 mod = 998244353;
                                                                                      48
   const ll root = 31;
   const ll root_1 = inverse(root, mod);
   const ll root_pw = 1 << 23;</pre>
                                                                                              }
   ll inverse(ll a, ll m) {
10
                                                                                          }
       11 \text{ res} = 1, \exp = m - 2;
                                                                                      54
11
       while (exp) {
           if (exp % 2 == 1) res = (1LL * res * a) % m;
13
           a = (1LL * a * a) % m;
14
           exp /= 2;
                                                                                      58
15
16
                                                                                      60
17
       return res;
                                                                                      61
18
19
   void ntt(vector<ll> & a, bool invert) {
                                                                                      63
20
       int n = a.size();
^{21}
22
       for (int i = 1, j = 0; i < n; i++) {
                                                                                      66
23
           int bit = n \gg 1;
                                                                                      67
24
           for (; j & bit; bit >>= 1)
                                                                                      68
25
                j ^= bit;
26
           i ^= bit;
27
                                                                                      71
28
                                                                                      72
           if (i < j)
29
                swap(a[i], a[j]);
30
                                                                                      74 }
       }
31
32
       for (int len = 2; len <= n; len <<= 1) {
33
```

int wlen = invert ? root_1 : root;

for (int i = len; i < root_pw; i <<= 1)

34

35

```
wlen = (int)(1LL * wlen * wlen % mod);
        for (int i = 0; i < n; i += len) {
            int w = 1;
            for (int j = 0; j < len / 2; j++) {
                int u = a[i+j], v = (int)(1LL * a[i+j+len/2] * w % mod);
                a[i+j] = u + v < mod ? u + v : u + v - mod;
                a[i+j+len/2] = u - v >= 0 ? u - v : u - v + mod;
                w = (int)(1LL * w * wlen % mod);
           }
   if (invert) {
       int n_1 = inverse(n, mod);
        for (auto & x : a)
            x = (int)(1LL * x * n_1 \% mod);
vector<ll> multiply(vector<ll> const &a, vector<ll> const &b) {
    vector<ll> fa(a.begin(), a.end()), fb(b.begin(), b.end());
   11 n = 1;
    while (n < a.size() + b.size())</pre>
       n <<= 1;
   fa.resize(n);
   fb.resize(n);
    ntt(fa, false);
   ntt(fb, false);
   for (ll i = 0; i < n; i++)
       fa[i] = (fa[i] * fb[i]) % mod;
   ntt(fa, true);
   vector<ll> result(n);
   for (ll i = 0; i < n; i++)
       result[i] = fa[i];
   return result:
                             8.6 FFT
```

1 typedef long long 11;

```
typedef complex<double> C;
                                                                                         vll res(a.size() + b.size() - 1):
                                                                                 43
   typedef vector<double> vd;
                                                                                         for (int i = 0; i < res.size(); i++) {
                                                                                 44
   typedef vector<ll> vll;
                                                                                             res[i] = llround(imag(out[i]) / (4 * n));
                                                                                 45
   const double PI = acos(-1);
                                                                                  46
                                                                                         return res;
                                                                                  47
                                                                                 48 }
   void fft(vector<C>& a) {
       int n = a.size(), L = 31 - __builtin_clz(n);
8
                                                                                                                   8.7 Rho
       static vector<C> R(2, 1);
9
       static vector<C> rt(2, 1);
10
       for (static int k = 2; k < n; k *= 2) {
                                                                                  1 //RECOMENDADO USAR UNSIGNED LONG LONG
11
           R.resize(n); rt.resize(n);
                                                                                    static inline ll mulmod(ll a, ll b, ll m) {
12
           auto x = polar(1.0, PI / k);
13
                                                                                         return (11)((__int128)a * b % m);
           for (int i = k; i < 2 * k; i++)
                                                                                     }
14
                                                                                  4
               rt[i] = R[i] = i & 1 ? R[i / 2] * x : R[i / 2];
15
                                                                                  5
       }
                                                                                     static inline ll powmod(ll b, ll e, ll m) {
16
       vector<int> rev(n);
17
                                                                                         11 r = 1;
       for (int i = 0; i < n; i++) rev[i] = (rev[i / 2] | (i & 1) << L) /
18
                                                                                         while (e) {
           2;
                                                                                             if (e \& 1) r = mulmod(r, b, m);
                                                                                  9
       for (int i = 0; i < n; i++) if (i < rev[i]) swap(a[i], a[rev[i]]);
                                                                                             b = mulmod(b, b, m);
19
       for (int k = 1; k < n; k *= 2)
                                                                                             e >>= 1:
20
                                                                                 11
           for (int i = 0; i < n; i += 2 * k) for (int j = 0; j < k; j++) {
                                                                                         }
21
                                                                                 12
               auto x = (double*)&rt[j + k], y = (double*)&a[i + j + k];
22
                                                                                  13
                                                                                         return r;
               C z(x[0] * y[0] - x[1] * y[1], x[0] * y[1] + x[1] * y[0]);
                                                                                    }
23
                                                                                 14
               a[i + j + k] = a[i + j] - z;
24
                                                                                  15
               a[i + j] += z;
                                                                                    // RNG rapido
25
                                                                                 static inline ll splitmix64(ll x) {
26
                                                                                        x += 0x9e3779b97f4a7c15ULL;
27
                                                                                        x = (x ^ (x >> 30)) * 0xbf58476d1ce4e5b9ULL;
28
   vll multiply(const vll& a, const vll& b) {
                                                                                        x = (x ^ (x >> 27)) * 0x94d049bb133111ebULL;
29
       if (a.empty() || b.empty()) return {};
                                                                                         return x \hat{} (x >> 31);
30
                                                                                 21
       vd fa(a.begin(), a.end()), fb(b.begin(), b.end());
                                                                                    |}
31
                                                                                 22
       int L = 32 - \_builtin\_clz(fa.size() + fb.size() - 1), n = 1 << L;
32
                                                                                    static ll rng_state = 0x1234567890abcdefULL ^ chrono::
       vector<C> in(n), out(n);
                                                                                         high_resolution_clock::now().time_since_epoch().count();
33
                                                                                 static inline ll rnd() { return splitmix64(rng_state += 0
34
       for (int i = 0; i < a.size(); i++) in[i] = C(fa[i], 0);
                                                                                         x9e3779b97f4a7c15ULL); }
35
       for (int i = 0; i < b.size(); i++) in[i].imag(fb[i]);</pre>
36
                                                                                 25
37
                                                                                    // trial division pequena para acelerar
       fft(in):
                                                                                    static const int SMALL_P_MAX = 1000;
38
       for (C\& x : in) x *= x;
                                                                                     static vector<int> small_primes;
39
       for (int i = 0; i < n; i++) out[i] = in[-i & (n - 1)] - conj(in[i]);
40
                                                                                 29
             // Corregido aqui
                                                                                     static void sieve_small() {
       fft(out);
41
                                                                                 31
                                                                                         vector<bool> is(SMALL_P_MAX + 1, true);
42
                                                                                         is[0] = is[1] = false;
                                                                                 32
```

```
for (int i = 2; i * i \le SMALL_P_MAX; ++i) if (is[i])
33
                                                                                    73
           for (int j = i * i; j <= SMALL_P_MAX; j += i) is[j] = false;</pre>
                                                                                                11 y = x;
                                                                                    74
34
       for (int i = 2; i <= SMALL_P_MAX; ++i) if (is[i]) small_primes.</pre>
                                                                                                11 d = 1;
                                                                                    75
35
           push_back(i);
                                                                                    76
                                                                                    77
36
37
       bool isPrime(ll n) {
38
                                                                                    79
       if (n < 2) return false;
39
       // divide por primos pequenos
40
       for (int p : small_primes) {
41
           if ((11)p * (11)p > n) break;
42
                                                                                    83
           if (n \% p == (11)0) return n == (11)p;
43
       }
                                                                                                return d:
44
                                                                                    85
       if (n < 4) return true; // 2,3
                                                                                            }
                                                                                    86
45
       // Miller-Rabin deterministico para 64-bit
                                                                                       }
                                                                                    87
46
       11 d = n - 1, s = 0;
47
       while ((d \& 1) == 0) d >>= 1, ++s;
48
       auto witness = [&](ll a) -> bool {
                                                                                            if (n == 1) return;
49
           if (a % n == 0) return false:
50
           11 x = powmod(a \% n, d, n);
                                                                                            for (int p : small_primes) {
51
           if (x == 1 \mid | x == n - 1) return false;
52
           for (int i = 1; i < s; ++i) {
53
                x = mulmod(x, x, n);
                                                                                            }
                                                                                    95
54
                if (x == n - 1) return false;
                                                                                            if (n == 1) return;
55
           }
56
           return true; // es testigo: n compuesto
                                                                                            11 d = pollard_rho(n);
57
       };
                                                                                            fact(d, F);
58
       // Bases correctas para 64-bit
                                                                                            fact(n / d, F);
                                                                                    100
59
       for (11 a : {2ULL, 3ULL, 5ULL, 7ULL, 11ULL, 13ULL, 17ULL, 19ULL, 23
                                                                                    101 }
60
           ULL.
                     325ULL, 9375ULL, 28178ULL, 450775ULL, 9780504ULL,
61
                         1795265022ULL}) {
           if (a == 0) continue:
62
           if (a % n == 0) continue:
63
           if (witness(a)) return false;
                                                                                            if (n % 2 != 0) {
64
65
                                                                                                n++;
                                                                                     4
       return true;
66
                                                                                     5
                                                                                           1d h = (b - a) / n:
67
                                                                                     6
                                                                                            ld s = f(a) + f(b);
68
   ll pollard_rho(ll n) {
69
                                                                                     8
       if ((n & 1ULL) == OULL) return 2ULL;
70
                                                                                     9
       while (true) {
71
                                                                                    10
           ll c = (rnd() \% (n - 1)) + 1; // [1..n-1]
72
                                                                                                1d x = a + i * h;
                                                                                    11
```

```
11 x = (rnd() \% (n - 2)) + 2; // [2..n-1]
        // limite de iteraciones para evitar lazos raros
        for (int it = 0; it < 1'000'000 \&\& d == 1; ++it) {
            x = (mulmod(x, x, n) + c) \% n;
            y = (mulmod(y, y, n) + c) \% n;
            y = (mulmod(y, y, n) + c) \% n;
            11 diff = x > y ? x - y : y - x;
            d = std::gcd(diff, n);
        if (d == 1 || d == n) continue;
void fact(ll n, map<ll,int> &F) {
    if (isPrime(n)) { F[n]++; return; }
       if ((ll)p * (ll)p > n) break;
        while (n \% p == 0) \{ F[p] ++; n /= p; \}
   if (isPrime(n)) { F[n]++; return; }
```

8.8 Simpson

```
1 | ld simpsonRule(function<ld(ld)> f, ld a, ld b, int n) {
      // Asegurarse de que n sea par
      // Suma de terminos interiores con los factores apropiados
      for (int i = 1; i < n; i++) {
```

```
s += (i % 2 == 1 ? 4.0L : 2.0L) * f(x);

// Multiplica por h/3
return (h / 3.0L) * s;

// Ejemplo: integrar la funcion x^2 entre 0 y 3
auto f = [&](ld x){ return x * x; };

ld a = 0.0L, b = 3.0L;
int n = 1000; // numero de subintervalos
ld resultado = simpsonRule(f, a, b, n);
```

9 Geometry

9.1 Convex Hull

```
typedef pair<11, 11> Point;
   11 cross_product(Point 0, Point A, Point B) {
       return (A.first - O.first) * (B.second - O.second) - (A.second - O.
3
           second) * (B.first - O.first);
4
   vector<Point> convex_hull(vector<Point>& points) {
5
       sort(points.begin(), points.end());
6
       points.erase(unique(points.begin(), points.end());
7
       vector<Point> hull;
8
       // Parte inferior
9
       for (const auto& p : points) {
10
           while (hull.size() >= 2 && cross_product(hull[hull.size() - 2],
11
               hull[hull.size() - 1], p) < 0)
               hull.pop_back();
12
           if (hull.empty() || hull.back() != p) {
13
               hull.push_back(p);
14
           }
15
       }
16
       // Parte superior
17
       int t = hull.size() + 1;
18
       for (int i = points.size() - 1; i >= 0; --i) {
19
           while (hull.size() >= t && cross_product(hull[hull.size() - 2],
20
               hull[hull.size() - 1], points[i]) < 0)</pre>
               hull.pop_back();
21
           if (hull.empty() || hull.back() != points[i]) {
22
               hull.push_back(points[i]);
23
           }
24
       }
25
```

```
hull.pop_back();
       return hull;
27
28 }
                             9.2 Operations
1 | 11 cross_product(pair<11, 11> P1, pair<11, 11> P2, pair<11, 11> P3) {
       ll x1 = P2.first - P1.first:
       11 y1 = P2.second - P1.second;
3
       11 \times 2 = P3.first - P1.first;
4
       11 y2 = P3.second - P1.second;
5
       return x1 * y2 - y1 * x2;
6
   }
7
   double distancia(pair<11, 11> P1, pair<11, 11> P2) {
       return sqrt((P2.first - P1.first) * (P2.first - P1.first) +
                    (P2.second - P1.second) * (P2.second - P1.second));
10
11
   11 dot_product(pair<11, 11> P1, pair<11, 11> P2, pair<11, 11> P3) {
12
       11 x1 = P2.first - P1.first;
13
       11 y1 = P2.second - P1.second;
14
       11 \times 2 = P3.first - P1.first;
       11 \text{ y2} = P3.\text{second} - P1.\text{second};
16
       return x1 * x2 + y1 * y2;
17
18 }
                           9.3 Polygon Area
   typedef pair<11, 11> Point;
   double polygon_area(const vector<Point>& polygon) {
       ll area = 0:
       int n = polygon.size();
       for (int i = 0; i < n; ++i) {
           11 j = (i + 1) \% n;
           area += (polygon[i].first * polygon[j].second - polygon[i].
7
               second * polygon[j].first);
       }
8
       return abs(area) / 2.0:
9
10 }
                            9.4 Ray Casting
1 | typedef pair<ll, ll> Point;
bool is_point_in_polygon(const vector<Point>& polygon, Point p) {
```

bool inside = false;

```
26 }
       int n = polygon.size();
4
      for (int i = 0, j = n - 1; i < n; j = i++) {
5
           if ((polygon[i].second > p.second) != (polygon[j].second > p.
6
               second) &&
               p.first < (polygon[j].first - polygon[i].first) * (p.second</pre>
7
                   - polygon[i].second) /
                          (polygon[j].second - polygon[i].second) + polygon[
8
                              i].first) {
               inside = !inside;
9
10
       }
11
       return inside;
12
13 }
```

10 Other

10.1 Mo's algorithm

```
const int BLOCK_SIZE = 450; using U64 = uint64_t;
  struct query {int 1, r, id; U64 order; };
   U64 hilbertorder(U64 x, U64 y) {
       const U64 logn = _{-}lg(max(x, y) * 2 + 1) | 1;
       const U64 maxn = (1ull << logn) - 1;</pre>
5
       U64 \text{ res} = 0:
       for (U64 s = 1ull << (logn - 1); s; s >>= 1) {
7
           bool rx = x & s, ry = y & s;
           res = (res << 2) | (rx ? ry ? 2 : 1 : ry ? 3 : 0);
9
           if (!rx) {
10
               if (ry) x ^= maxn, y ^= maxn;
11
               swap(x, y);
12
13
14
       return res;
15
   } // sort by this order
16
   auto add = [&](int ix) { /* Add A[ix] to state*/};
   auto rem = [&](int ix) { /* Remove A[ix] from state*/}
   int c_1 = 0, c_r = -1; // Cursors [0,-1] so r add 0 on first q
  L(const auto &qr: queries){
20
       while(c_1 > qr.1) add(--c_1);
21
       while(c_r < qr.r) add(++c_r);</pre>
22
       while(c_1 < qr.1) rem(c_1++);
23
       while (c_r > qr.r) rem(c_r--);
24
       ans[qr.id] = /*State.Answer()*/;
25
```