Dividimos y No Conquistamos (D&!C)

Contents

1	Ten	I a	2			
	1.1	C++ Template	2			
2	Dat		2			
	2.1	BIT	2			
	2.2	DSU	2			
	2.3	Sparse Table	3			
	2.4	Segment tree	3			
3	Dynamic Programming 4					
	3.1	Knapsack	4			
	3.2	LIS	4			
	3.3	Edit Distance	5			
	3.4	Kadane	5			
4	Stri	ngs	5			
	4.1	-	5			
	4.2	HASHING	6			
	4.3	KMP	7			
	4.4	LPS	7			
	4.5	RK	8			
	4.6		8			
5	Gra	mh	9			
•	5.1	±	9			
	5.2	Ü	9			
	5.3		9			
	5.4		9			
	5.5		1			
6	Mat	th 1	2			
•	6.1		2			
	6.2		3			
	6.3		.3			
	6.4		.3			
	6.5		4			
	6.6		4			
	0.0	JOSEI 1105	·±			

	7.3	POLYGON AREA	9
7	Geo 7.1 7.2	CONVEX HULL	. 8 .8
	6.11	fft	6
	6.9 6.10		16 16
	6.7 6.8	NTT	4 5

#include <bits/stdc++.h>

4

1 Template

1.1 C++ Template

```
using namespace std;
   #define TESTS
   #define LOCAL
   #define ll long long
   #define ii pair<11, 11>
   #define F first
   #define S second
   #define formi(i, o, n) for (int i = o; i < n; i ++)
   #define forn(i, n) forni(i, 0, n)
   #define pub push_back
   #define popf pop_front
13
   #ifdef LOCAL
   #define DBG(x) cout << "[" << x << "]";
   #else
   #define DBG(x) 42
   #endif
19
20
21
   void solve(){
22
23
^{24}
25
26
   int main(){
27
       ios::sync_with_stdio(0);cin.tie(0);
28
   #ifdef LOCAL
29
       freopen("in.txt","r", stdio);
30
       freopen("out.txt","w", stdout);
31
   #endif
32
       int tt = 1;
33
   #ifdef TESTS
34
       cin >> tt;
35
   #endif
36
       while(tt--)solve();
37
  |}
38
```

2 Data structures

2.1 BIT

```
#define LSOne(S) (S & -S)
   struct BIT {
       vector<int> B;
4
       int n;
5
       BIT(int n = 1): B(n + 1), n(n+1){}
6
       BIT(vector<int> &v): B(v.size()+1), n(v.size()+1) {
            for (int i = 1; i \le n; i \leftrightarrow ++){
8
                B[i] += v[i-1];
                if (i + LSOne(i) <= n){</pre>
10
                    B[i + LSOne(i)] += B[i];
11
12
            }
13
14
       void update(int i, int x){
15
            while (i \le n){
16
                B[i] += x;
17
                i += LSOne(i);
18
            }
19
       }
20
       int sum(int i){
21
            int res = 0;
22
            while (i > 0){
23
                res += B[i];
^{24}
                i -= LSOne(i);
25
            }
26
            return res;
27
       }
28
       int range_sum(int 1, int r){
29
            return sum(r) - sum(1 - 1);
30
31
32 };
                                        DSU
                                   2.2
struct DSU {
       vector<int> par, sz;
2
       int n;
3
```

DSU(int n = 1): par(n), sz(n, 1), n(n){

struct Node {

```
for (int i = 0; i < n; i ++) par[i] = i;
       }
6
       int find(int a){
7
           return a == par[a] ? a : par[a] = find(par[a]);
8
       }
9
       void join(int a, int b){
10
           a=find(a);
11
           b=find(b);
12
           if (a != b){
13
               if (sz[b] > sz[a]) swap(a,b);
14
               par[b] = a;
15
               sz[a] += sz[b];
16
           }
17
18
19 };
                                 Sparse Table
  int log2_floor(unsigned long long i) {
       return i ? __builtin_clzll(1) - __builtin_clzll(i) : -1;
2
3
   const int MAXN = 10;
   int K = log2_floor(MAXN);
   int st[K + 1][MAXN];
   // Load Array to st[0][i]
   std::copy(array.begin(), array.end(), st[0]);
11
   // Build
  for (int i = 1; (1 << i) <= n; i ++){
       for (int j = 0; j + (1 << (i - 1)) < n; <math>j ++){
           st[i][j] = min(st[i-1][j], st[i-1][j + (1 << (i - 1))]);
15
       }
16
17
18
   // Query
19
   int min_range(int 1, int r){
20
       int C = log2\_floor(r - l + 1);
21
       return min(st[C][1], st[C][r - (1 << C) + 1]);
^{22}
23 }
                            2.4 Segment tree
```

```
long long sum = 0;
2
       long long min_val = LLONG_MAX;
3
       long long max_val = LLONG_MIN;
4
       long long lazy = 0;
5
6
       // Merge function to combine two nodes
7
       void merge(const Node& left, const Node& right) {
8
           sum = left.sum + right.sum;
           min_val = min(left.min_val, right.min_val);
           max_val = max(left.max_val, right.max_val);
11
       }
12
13
       // Update function for lazy propagation
       void apply(int 1, int r, long long value) {
15
           sum += (r - 1 + 1) * value;
16
           min_val += value;
17
           max_val += value;
           lazy += value;
19
       }
20
   };
21
22
   struct SegTree {
23
       int n;
24
       vector<Node> tree;
25
26
       SegTree(int n) : n(n) {
27
           tree.resize(4 * n + 5);
28
       }
29
30
       SegTree(vector<int>& arr) : n(arr.size()) {
31
           tree.resize(4 * n + 5);
32
           build(arr, 0, 0, n-1);
33
       }
34
35
       // Push lazy value to children
36
       void push(int id, int 1, int r) {
37
           if (tree[id].lazy == 0) return;
38
39
           int mid = (1 + r) >> 1;
40
           tree[2*id + 1].apply(1, mid, tree[id].lazy);
41
           tree[2*id + 2].apply(mid+1, r, tree[id].lazy);
42
           tree[id].lazy = 0;
43
```

```
}
44
45
       void build(vector<int>& arr, int id, int 1, int r) {
46
           if (1 == r) {
47
               tree[id].sum = arr[1];
48
               tree[id].min_val = arr[1];
49
               tree[id].max_val = arr[1];
               return;
51
           }
52
53
           int mid = (1 + r) >> 1;
54
           build(arr, 2*id + 1, 1, mid);
55
           build(arr, 2*id + 2, mid+1, r);
56
           tree[id].merge(tree[2*id + 1], tree[2*id + 2]);
57
       }
58
59
       // Range update with lazy propagation
60
       void update(int id, int 1, int r, int q1, int qr, long long val) {
61
           if (ql > r || qr < l) return;
62
63
           if (ql <= l && r <= qr) {
64
               tree[id].apply(l, r, val);
65
               return;
66
           }
67
68
           push(id, 1, r);
69
           int mid = (1 + r) >> 1;
70
           update(2*id + 1, 1, mid, ql, qr, val);
71
           update(2*id + 2, mid+1, r, ql, qr, val);
72
           tree[id].merge(tree[2*id + 1], tree[2*id + 2]);
73
       }
74
75
       // Range query
76
       Node query(int id, int 1, int r, int ql, int qr) {
77
           if (ql > r || qr < l) return Node();</pre>
78
79
           if (ql <= l && r <= qr) {
80
               return tree[id]:
81
           }
82
83
           push(id, 1, r);
84
           int mid = (1 + r) >> 1;
85
           Node left = query(2*id + 1, 1, mid, ql, qr);
86
```

```
Node right = query(2*id + 2, mid+1, r, ql, qr);
88
89
           Node result:
           result.merge(left, right);
           return result;
91
       }
92
93
       // Public interface
       void update(int 1, int r, long long val) {
           update(0, 0, n-1, 1, r, val);
       }
97
98
       Node query(int 1, int r) {
99
           return query(0, 0, n-1, 1, r);
100
       }
101
102 };
```

3 Dynamic Programming

3.1 Knapsack

```
int knapsack(vector<int>& values, vector<int>& weights, int W) {
       int n = values.size();
       vector<vector<int>> dp(n + 1, vector<int>(W + 1, 0));
4
       for(int i = 1; i <= n; i++) {
5
           for(int w = 0: w \le W: w++) {
6
               if(weights[i-1] <= w) {</pre>
7
                   dp[i][w] = max(dp[i-1][w],
                                  dp[i-1][w-weights[i-1]] + values[i-1]);
               } else {
10
                   dp[i][w] = dp[i-1][w];
11
12
           }
13
       return dp[n][W];
15
16 }
```

3.2 LIS

```
vector<int> getLIS(vector<int>& arr) {
   int n = arr.size();
   vector<int> dp(n + 1, INT_MAX); // dp[i] = smallest value that ends
   an LIS of length i
```

 $dp[i][j] = 1 + min({dp[i-1][j]},$

16

// deletion

```
vector<int> len(n);
                                         // Length of LIS ending at each
                                                                                                                         dp[i][j-1],
                                                                                                                                          // insertion
4
                                                                                   17
           position
                                                                                                                         dp[i-1][j-1]}); // replacement
                                                                                   18
       dp[0] = INT_MIN;
                                                                                   19
5
                                                                                              }
6
                                                                                  20
       for(int i = 0; i < n; i++) {
                                                                                          }
                                                                                  21
                                                                                          return dp[n][m];
           int j = upper_bound(dp.begin(), dp.end(), arr[i]) - dp.begin();
8
                                                                                   22
                                                                                  23 }
           dp[j] = arr[i];
9
           len[i] = j;
10
                                                                                                                  3.4 Kadane
       }
11
12
                                                                                   pair<int, pair<int,int>> kadane(vector<int>& arr) {
       // Find maxLen and reconstruct sequence
13
                                                                                          int maxSoFar = arr[0], maxEndingHere = arr[0];
       int maxLen = 0;
14
                                                                                          int start = 0, end = 0, s = 0;
       for(int i = n-1; i \ge 0; i--) maxLen = max(maxLen, len[i]);
                                                                                   3
15
                                                                                   4
16
                                                                                          for(int i = 1; i < arr.size(); i++) {</pre>
       vector<int> lis;
                                                                                   5
17
       for(int i = n-1, currLen = maxLen; i \ge 0; i--) {
                                                                                              if(maxEndingHere + arr[i] < arr[i]) {</pre>
                                                                                   6
18
                                                                                                  maxEndingHere = arr[i];
           if(len[i] == currLen) {
                                                                                   7
19
                                                                                                  s = i;
               lis.push_back(arr[i]);
                                                                                   8
20
                                                                                              } else {
               currLen--;
                                                                                   9
21
                                                                                                  maxEndingHere += arr[i];
           }
                                                                                   10
22
       }
                                                                                              }
                                                                                  11
23
       reverse(lis.begin(), lis.end());
                                                                                  12
24
                                                                                              if(maxEndingHere > maxSoFar) {
       return lis;
                                                                                  13
25
                                                                                                  maxSoFar = maxEndingHere;
26 }
                                                                                  14
                                                                                                  start = s;
                                                                                  15
                                 Edit Distance
                                                                                                  end = i;
                                                                                  16
                                                                                              }
                                                                                  17
                                                                                   18
1
                                                                                          return {maxSoFar, {start, end}}; // max, 1, r
    //3. Edit Distance - O(n*m)
                                                                                   19
                                                                                  20 }
   int editDistance(string& s1, string& s2) {
3
       int n = s1.length(), m = s2.length();
4
                                                                                                                       Strings
       vector<vector<int>> dp(n + 1, vector<int>(m + 1));
5
6
                                                                                                                4.1 Prefix Tree
       // Base cases
7
       for(int i = 0; i \le n; i++) dp[i][0] = i;
8
       for(int j = 0; j \le m; j++) dp[0][j] = j;
                                                                                     #include <bits/stdc++.h>
9
                                                                                   2
10
       for(int i = 1: i <= n: i++) {
                                                                                      using namespace std;
11
                                                                                   3
           for(int j = 1; j <= m; j++) {
                                                                                   4
12
               if(s1[i-1] == s2[j-1]) {
                                                                                      struct TrieNodeStruct {
13
                    dp[i][j] = dp[i-1][j-1];
                                                                                          TrieNodeStruct* children[26];
14
                                                                                   6
               } else {
                                                                                   7
                                                                                          bool isEndOfWord;
15
```

```
TrieNodeStruct() {
9
           isEndOfWord = false;
10
           for(int i = 0; i < 26; i++) {
11
                children[i] = nullptr;
12
           }
13
       }
14
15
16
   struct TrieStruct {
17
       TrieNodeStruct* root;
18
19
       TrieStruct() {
20
           root = new TrieNodeStruct();
21
       }
22
23
       void insert(string word) {
24
           TrieNodeStruct* current = root;
25
           for(char c : word) {
26
                int index = c - 'a';
27
               if(current->children[index] == nullptr) {
28
                    current->children[index] = new TrieNodeStruct();
29
30
                current = current->children[index];
31
32
           current->isEndOfWord = true;
33
       }
34
35
       bool search(string word) {
36
           TrieNodeStruct* current = root;
37
           for(char c : word) {
38
                int index = c - 'a';
39
                if(current->children[index] == nullptr) {
40
                    return false:
41
42
                current = current->children[index];
43
44
           return current->isEndOfWord;
45
       }
46
47
       bool startsWithDirect(string prefix) {
48
           TrieNodeStruct* current = root;
49
           for(char c : prefix) {
50
                int index = c - 'a';
51
```

```
if(current->children[index] == nullptr) {
    return false;
}
current = current->children[index];
}
return true;
}
return true;
}
```

4.2 HASHING

```
#include <bits/stdc++.h>
   #define ll long long
   using namespace std;
   // este struct permite crear unordered_set de pares
   struct pair_hash {
     inline std::size_t operator()(const std::pair<11,11> & v) const {
       return v.first*31+v.second:
    }
10
   };
11
   const int p = 31; //representa la potencia, inicializalo en base a la
       cantidad de letras que use el alfabeto
   const int m = 1e9 + 9; //mod
15
   vector<ll> precompute_pow(ll size){ //el size debe ser el largo del
       string evaluado
     vector<ll> res(size);
17
     res[0] = 1;
18
19
     for(int i = 1; i < size; i++)</pre>
20
       res[i] = (res[i - 1] * p) % m;
21
22
     return res;
23
24
25
   vector<ll> precompute_hash(string s, vector<ll> pow){
     ll size = s.size():
27
     vector<ll> hs(size + 1, 0);
28
29
     for(int i = 0; i < size; i++)</pre>
```

```
hs[i+1] = (hs[i] * ((s[i] - 'a' + 1) * pow[i]) % m) % m;
31
32
     return hs;
33
34 }
                                 4.3 KMP
   #include <bits/stdc++.h>
   using namespace std;
   vector<int> kmp(string pat, string sec){ //geeks4geeks implementation
       with some changes
     int m = pat.length();
     int n = sec.length();
     cout << m << "" << n << endl;
7
8
     vector<int> lps = getLps(pat);
9
     vector<int> res;
10
     int i = 0;
12
     int j = 0;
13
14
     while((n - i) >= (m - j)){
15
       if(pat[j] == sec[i]){
16
         i++;
17
         j++;
18
19
       if(j == m){
20
         res.push_back(i - j);
^{21}
         j = lps[j - 1];
22
23
       else{
^{24}
         if(i < n && pat[j] != sec[i]){</pre>
25
           if(j != 0) j = lps[ j - 1 ];
26
            else i = i + 1;
27
         }
28
       }
29
     }
30
31
     return res;
32
   }
33
34
```

vector<int> getLps(string pat){ //geek4geeks implementatio with some

```
changes
     vector<int> lps(pat.length(), 0);
36
     int len = 0;
37
     int i = 1;
38
     lps[0] = 0;
39
     while(i < pat.length()){</pre>
40
       if(pat[i] == pat[len]){
41
         len++;
42
         lps[i] = len;
43
         i++;
44
45
       else //pat[i] != pat[len]
46
47
         lps[i] = 0;
48
         i++;
49
     }
51
52
     return lps;
53
54 }
                                  4.4 LPS
#include <bits/stdc++.h>
   using namespace std;
   vector<int> getLps(string pat){ //geek4geeks implementatio with some
       changes
     vector<int> lps(pat.length(), 0);
5
     int len = 0;
6
     int i = 1;
```

lps[0] = 0;

len++;

i++;

i++;

}

9

10

11

12

13

14

15

16

17

18

19

while(i < pat.length()){</pre>

lps[i] = len;

lps[i] = 0;

if(pat[i] == pat[len]){

else //pat[i] != pat[len]

```
}
20
                                                                                    4
                                                                                      vector<int> z_function(string s) {
^{21}
                                                                                           int n = s.length();
     return lps;
^{22}
23 }
                                                                                           vector<int> z(n, 0);
                                  4.5 RK
                                                                                           z[0] = n;
   #include <bits/stdc++.h>
                                                                                           int 1 = 0, r = 0;
   #define ll long long
                                                                                    12
                                                                                           for(int i = 1; i < n; i++) {
    using namespace std;
                                                                                               if(i <= r) {
                                                                                    14
                                                                                                    z[i] = min(r - i + 1, z[i - 1]);
                                                                                    15
    vector<int> rabin_karp(string s, string t) { //implementacion de cp-
                                                                                               }
                                                                                    16
       algorithms
                                                                                    17
     const int p = 31;
                                                                                               while(i + z[i] < n && s[z[i]] == s[i + z[i]]) {
                                                                                    18
     const int m = 1e9 + 9:
                                                                                                    z[i]++;
     int S = s.size(), T = t.size();
                                                                                               }
                                                                                    20
10
                                                                                    21
     vector<long long> p_pow(max(S, T));
11
                                                                                               if(i + z[i] - 1 > r) {
     p_pow[0] = 1;
12
                                                                                                   l = i;
     for (int i = 1; i < (int)p_pow.size(); i++)</pre>
13
                                                                                                   r = i + z[i] - 1;
                                                                                   24
       p_pow[i] = (p_pow[i-1] * p) % m;
14
                                                                                    25
15
                                                                                           }
                                                                                    26
     vector<long long> h(T + 1, 0);
16
                                                                                    27
     for (int i = 0; i < T; i++)
17
                                                                                   28
                                                                                           return z;
       h[i+1] = (h[i] + (t[i] - 'a' + 1) * p_pow[i]) % m;
18
                                                                                    29
     long long h_s = 0;
19
                                                                                    30
     for (int i = 0; i < S; i++)
20
                                                                                   31
       h_s = (h_s + (s[i] - 'a' + 1) * p_pow[i]) \% m;
21
                                                                                       vector<int> find_pattern(string text, string pattern) {
                                                                                    32
^{22}
                                                                                    33
     vector<int> occurrences;
23
                                                                                           string s = pattern + "$" + text;
                                                                                   34
     for (int i = 0; i + S - 1 < T; i++) {
^{24}
                                                                                           vector<int> z = z_function(s);
                                                                                    35
       long long cur_h = (h[i+S] + m - h[i]) \% m;
25
                                                                                           vector<int> result:
                                                                                    36
       if (cur_h == h_s * p_pow[i] % m)
26
                                                                                    37
         occurrences.push_back(i);
27
                                                                                   38
     }
28
                                                                                           for(int i = pattern.length() + 1; i < s.length(); i++) {</pre>
                                                                                    39
     return occurrences;
                                                                                               if(z[i] == pattern.length()) {
                                                                                    40
30 }
                                                                                                    result.push_back(i - pattern.length() - 1);
                                                                                    41
                                 Z FUNCTION
                                                                                    42
                                                                                           }
                                                                                    43
   #include <bits/stdc++.h>
                                                                                    44
                                                                                           return result;
2
                                                                                    45
                                                                                   46 }
3 using namespace std;
```

5 Graph

5.1 Tarjan

```
const int N = 10;
2
   vector<int> G[N];
   vector<int> dfs_low(N, -1), dfs_num(N, -1), ap(N, 0); // ap for
       Articulation Points
  int dfs_count = 0;
   int root = -1; // For AP
   void dfs(int u, int p = -1){
       dfs_low[u]=dfs_num[u]=dfs_count++;
9
       int child = 0;
10
       for (int v: G[u]){
11
           if (v == p) continue;
12
           if (dfs_num[v] == -1){
13
               child ++;
14
               dfs(v, u);
15
               dfs_low[u] = min(dfs_low[u], dfs_low[v]);
16
               if (dfs_low[v] > dfs_num[u]){
17
                  // Bridge from u -> v
18
                  cout << "Bridge," << u << ",,->,," << v << "\n";
19
20
               if (dfs_low[v] >= dfs_num[u]) {
21
                    // u is AP
^{22}
                    ap[u] = 1;
23
^{24}
           } else dfs_low[u] = min(dfs_low[u], dfs_num[v]);
25
       }
26
       if (u == root){
27
           ap[u] = child > 1;
28
29
30
```

5.2 Bellman Ford

```
struct Edge {
int a, b, cost;
};
int n, m, v;
```

```
6 vector<Edge> edges;
   const int INF = 1000000000;
   void solve()
   {
10
       vector<int> d(n, INF);
       d[v] = 0;
       for (int i = 0; i < n - 1; ++i)
13
           for (Edge e : edges)
14
               if (d[e.a] < INF)
15
                   d[e.b] = min(d[e.b], d[e.a] + e.cost);
16
17 }
                                5.3 SCC
vector<int> dfs_num(N, -1), dfs_low(N, -1), visited(N);
  int dfs_count = 0;
  int numSCC = 0;
   stack<int> st;
   void dfs(int u){
     dfs_low[u]=dfs_num[u]=dfs_count++;
     st.push(u);
     visited[u] = 1;
     for(int v: G[u]) {
       if (dfs_num[v] == -1) dfs(v);
10
       if (visited[v]) dfs_low[u] = min(dfs_low[u], dfs_low[v]);
11
12
     if (dfs_num[u] == dfs_low[u]){
13
       numSCC ++;
14
       while(1){
15
         int v = st.top(); st.pop();
         visited[v] = 0;
17
         if (u == v) break;
19
    }
20
21 | }
                                 5.4 Flow
1 // Complexity (V * V * E);
2 struct Dinic {
       struct Edge {
           int to, rev;
4
```

long long cap, flow;

5

Page 9 of 22

49

50

51

52

53

54

55

56

57

58

59

60

61

62

63

64

66

67

69

70

71

72

73

74

75

76

77

78

79

80

81

82

83

84

85

86

87

88

89

90

```
Edge(int to, int rev, long long cap) :
               to(to), rev(rev), cap(cap), flow(0) {}
7
       };
8
9
       vector<vector<Edge>> g;
10
       vector<int> level, ptr;
11
       queue<int> q;
12
       int n, source, sink;
13
       const long long INF = 1e18;
14
15
       Dinic(int n, int s, int t) : n(n), source(s), sink(t) {
16
           g.resize(n);
17
           level.resize(n):
18
           ptr.resize(n);
19
       }
20
21
       void add_edge(int from, int to, long long cap) {
22
           g[from].emplace_back(to, g[to].size(), cap);
23
           g[to].emplace_back(from, g[from].size()-1, 0); // Reverse edge
24
       }
25
26
       bool bfs() {
27
           while(!q.empty()) {
28
               q.pop();
29
           }
30
           fill(level.begin(), level.end(), -1);
31
32
           q.push(source);
33
           level[source] = 0;
34
35
           while(!q.empty() && level[sink] == -1) {
36
               int v = q.front();
37
               q.pop();
38
39
               for(const Edge& e : g[v]) {
40
                    if(level[e.to] == -1 \&\& e.flow < e.cap) {
41
                        level[e.to] = level[v] + 1;
42
                        q.push(e.to);
43
                   }
44
               }
45
           }
46
           return level[sink] != -1;
47
       }
48
```

```
long long dfs(int v, long long pushed) {
   if(v == sink || pushed == 0) return pushed;
   for(int& i = ptr[v]; i < (int)g[v].size(); i++) {</pre>
        Edge& e = g[v][i];
        if(level[e.to] != level[v] + 1 || e.flow >= e.cap) continue;
        long long flow = dfs(e.to, min(pushed, e.cap - e.flow));
        if(flow == 0) continue;
        e.flow += flow:
        g[e.to][e.rev].flow -= flow;
        return flow;
    }
    return 0;
}
long long max_flow() {
    long long flow = 0;
    while(bfs()) {
        fill(ptr.begin(), ptr.end(), 0);
        while(long long pushed = dfs(source, INF)) {
            flow += pushed;
        }
    }
    return flow;
}
// Get the actual flow passing through each edge
vector<vector<long long>> get_flow() {
    vector<vector<long long>> flow(n, vector<long long>(n, 0));
    for(int v = 0; v < n; v++) {
        for(const Edge& e : g[v]) {
            if(e.cap > 0) { // Only original edges, not residual
                flow[v][e.to] = e.flow:
            }
    }
    return flow;
```

```
long long max_flow = flow.max_flow();
92
                                                                                      135
                                                                                              cout << "Maximum flow: " << max_flow << "\n";</pre>
        // Find minimum cut
                                                                                      136
93
        vector<bool> min_cut() {
                                                                                      137
94
            vector<bool> reachable(n, false);
                                                                                              // Get minimum cut
95
                                                                                      138
            queue<int> q;
                                                                                              vector<bool> cut = flow.min_cut();
                                                                                      139
96
                                                                                              cout << "Vertices on source side of min cut: ";</pre>
            q.push(source);
97
                                                                                      140
                                                                                              for(int i = 0; i < n; i++) {
            reachable[source] = true;
                                                                                      141
98
                                                                                                   if(cut[i]) cout << i << " ";
                                                                                      142
99
                                                                                              }
            while(!q.empty()) {
100
                                                                                      143
                                                                                              cout << "\n";
                 int v = q.front();
101
                                                                                      144
                 q.pop();
102
                                                                                      145
                                                                                              // Get flow through each edge
103
                                                                                      146
                 for(const Edge& e : g[v]) {
                                                                                              auto flow_matrix = flow.get_flow();
                                                                                      147
104
                     if(!reachable[e.to] && e.flow < e.cap) {</pre>
                                                                                              cout << "Flow matrix:\n":</pre>
                                                                                      148
105
                         reachable[e.to] = true;
                                                                                              for(int i = 0; i < n; i++) {
                                                                                      149
106
                         q.push(e.to);
                                                                                                   for(int j = 0; j < n; j++) {
107
                                                                                      150
                     }
                                                                                                       if(flow_matrix[i][j] > 0) {
108
                                                                                      151
                 }
                                                                                                            cout << i << " -> " << j << ": " << flow_matrix[i][j] <<
109
                                                                                      152
            }
                                                                                                                 "\n":
110
            return reachable;
111
        }
                                                                                      154
112
113
                                                                                      156
114
    // Example usage:
                                                                                              return 0;
                                                                                      157
115
                                                                                      158
116
    int main() {
                                                                                      159 */
117
        // Example: 6 vertices, source = 0, sink = 5
118
                                                                                                                        Ford Fulkerson
        int n = 6:
119
        Dinic flow(n, 0, 5);
120
                                                                                       1 #define ll long long
121
        // Add edges: (from, to, capacity)
                                                                                          const 11 INF = (11)4e18;
122
        flow.add_edge(0, 1, 16);
123
                                                                                          struct Edge {
        flow.add_edge(0, 2, 13);
                                                                                              int from, to;
124
        flow.add_edge(1, 2, 10);
                                                                                              ll cap, flow;
125
                                                                                       5
        flow.add_edge(1, 3, 12);
                                                                                              Edge(int from, int to, 11 cap) : from(from), to(to), cap(cap), flow
126
                                                                                       6
        flow.add_edge(2, 1, 4);
127
                                                                                                   (0) {}
        flow.add_edge(2, 4, 14);
128
                                                                                       7 };
        flow.add_edge(3, 2, 9);
129
        flow.add_edge(3, 5, 20);
                                                                                          struct MaxFlow {
130
        flow.add_edge(4, 3, 7);
                                                                                              vector<Edge> edges;
131
                                                                                       10
        flow.add_edge(4, 5, 4);
                                                                                              vector<vector<int>> adj;
132
                                                                                      11
133
                                                                                      12
                                                                                              vector<int> level, ptr;
        // Calculate maximum flow
134
                                                                                              int n;
                                                                                      13
```

```
queue<int> q;
14
15
       MaxFlow(int n) : n(n) {
16
           adj.resize(n);
17
           level.resize(n);
18
           ptr.resize(n);
19
       }
20
^{21}
       void add_edge(int from, int to, ll cap) {
^{22}
            edges.emplace_back(from, to, cap);
23
           edges.emplace_back(to, from, 0);
24
           adj[from].push_back(edges.size() - 2);
25
           adj[to].push_back(edges.size() - 1);
26
       }
27
28
       bool bfs(int s, int t) {
29
           while(!q.empty()) q.pop();
30
           fill(level.begin(), level.end(), -1);
31
32
           q.push(s);
33
           level[s] = 0;
34
35
           while(!q.empty() && level[t] == -1) {
36
                int v = q.front();
37
                q.pop();
38
39
                for(int id : adj[v]) {
40
                    if(level[edges[id].to] == -1 && edges[id].cap - edges[id
41
                        ].flow > 0) {
                        level[edges[id].to] = level[v] + 1;
42
                        q.push(edges[id].to);
43
                    }
44
                }
45
46
           return level[t] != -1;
47
       }
48
49
       11 dfs(int v, int t, ll pushed) {
50
           if(v == t || pushed == 0)
51
                return pushed;
52
53
           for(; ptr[v] < (int)adj[v].size(); ptr[v]++) {</pre>
54
                int id = adj[v][ptr[v]];
55
```

```
int u = edges[id].to;
56
57
                if(level[u] != level[v] + 1) continue;
58
59
                11 tr = dfs(u, t, min(pushed, edges[id].cap - edges[id].flow
60
                     ));
                if(tr > 0) {
61
                    edges[id].flow += tr;
62
                     edges[id ^ 1].flow -= tr;
63
                     return tr;
                }
65
            }
66
            return 0;
67
       }
68
69
       11 max_flow(int s, int t) {
70
            11 \text{ flow} = 0;
71
            while(bfs(s, t)) {
72
                fill(ptr.begin(), ptr.end(), 0);
73
                while(ll pushed = dfs(s, t, LLONG_MAX)) {
                     flow += pushed;
75
                }
76
            }
77
            return flow;
78
       }
79
80
       vector<ll> get_flows() {
81
            vector<ll> flows;
82
            for(int i = 0; i < edges.size(); i += 2) {</pre>
83
                flows.push_back(edges[i].flow);
84
            }
85
            return flows;
86
       }
87
88 };
```

6 Math

6.1 BINARY POW

```
#include <iostream>
using namespace std;

typedef long long ll;
```

```
18 }
_{5} | 11 mod = 1e9+7;
6
                                                                                                   6.4 EUCLIDEAN EXTENDED
   ll binary_pow(ll base, ll exp) {
       ll result = 1;
       base %= mod;
                                                                                 1 | 11 extendedGCD(11 a, 11 b, 11 &x, 11 &y) {
9
       while (exp > 0) {
                                                                                       if (b == 0) {
10
           if (\exp \% 2 == 1) {
11
                                                                                           x = 1;
               result = (result * base) % mod;
12
                                                                                           y = 0;
13
                                                                                           return a;
           base = (base * base) % mod;
14
                                                                                 6
           exp /= 2;
15
                                                                                       ll x1, v1;
       }
16
                                                                                       11 gcd = extendedGCD(b, a % b, x1, y1);
17
                                                                                       x = v1;
       return result:
                                                                                       y = x1 - (a / b) * y1;
18
19 }
                                                                                       return gcd;
                                                                                11
                                                                                12
                                                                                   }
                            6.2 CATALAN
                                                                                14 bool findSolutionWithConstraints(ll a, ll b, ll c, ll x_min, ll y_min,
1 | 11 catalan(11 n) {
                                                                                       11 &x, 11 &y) {
       if (n == 0) return 1:
2
                                                                                       11 g = extendedGCD(a, b, x, y);
       11 catalan_num = (fact[2 * n] * inv_fact[n] % MOD) * inv_fact[n + 1]
            % MOD:
                                                                                17
                                                                                       if (c % g != 0) return false;
       return catalan num:
4
5 }
                                                                                       x *= c / g:
                            COMBINATORICS
                                                                                       y *= c / g;
                                                                                21
  vector<ll> fact, inv_fact;
                                                                                       // Ajustamos las variables a/g y b/g para mover las soluciones
  void precompute_factorials(ll n, ll mod) {
                                                                                       a /= g;
       fact.resize(n + 1);
                                                                                       b /= g;
3
       inv_fact.resize(n + 1);
4
      fact[0] = inv_fact[0] = 1;
                                                                                       if (x < x_min) {
5
       for (ll i = 1; i <= n; i++) {
                                                                                           ll k = (x_min - x + b - 1) / b; // Redondeo hacia arriba
                                                                                27
           fact[i] = (fact[i - 1] * i) \% mod;
                                                                                           x += k * b;
7
                                                                                28
                                                                                           v -= k * a;
                                                                                29
8
       inv_fact[n] = mod_inverse(fact[n], mod);
                                                                                       } else if (x > x_min) {
9
       for (ll i = n - 1; i \ge 1; i - -) {
                                                                                           11 k = (x - x_min) / b;
                                                                                31
10
           inv_fact[i] = (inv_fact[i + 1] * (i + 1)) % mod;
                                                                                           x -= k * b;
                                                                                32
11
       }
                                                                                           v += k * a:
                                                                                33
12
                                                                                       }
13
                                                                                34
14
   ll binomial_coefficient(ll n, ll k, ll mod) {
                                                                                       if (y < y_min) {
                                                                                36
15
       if (k > n) return 0;
                                                                                           ll k = (y_min - y + a - 1) / a; // Redondeo hacia arriba
                                                                                37
16
       return (fact[n] * inv_fact[k] % mod) * inv_fact[n - k] % mod;
                                                                                           x += k * b:
                                                                                38
17
```

for (ll i = 2; i <= n; ++i) {

```
y -= k * a;
                                                                                             result = (result + k) % i;
39
                                                                                  9
       } else if (y > y_min) {
                                                                                 10
40
           11 k = (y - y_min) / a;
                                                                                         return result;
                                                                                 11
41
           x -= k * b;
                                                                                 12
^{42}
           y += k * a;
                                                                                 13
43
44
                                                                                 14
                                                                                     ll josephus_recursive(ll n, ll k) {
45
       return x >= x_min && y >= y_min;
46
47 }
                                                                                        if (n == 1)
                                                                                 17
                                                                                            return 0;
                             EULER TOTIENT
                                                                                 19
                                                                                         return (josephus_recursive(n - 1, k) + k) % n;
                                                                                 20
   #include <bits/stdc++.h>
                                                                                 21
   using namespace std;
                                                                                 22
   typedef long long 11;
                                                                                     11 josephus_power_of_2(11 n) {
                                                                                 25
   vector<ll> compute_totients(ll n) {
6
                                                                                         11 power = 1;
       vector<ll> phi(n + 1);
                                                                                         while (power <= n) {</pre>
                                                                                 27
       for (ll i = 0; i <= n; i++) {
8
                                                                                             power <<= 1;
           phi[i] = i;
9
                                                                                        }
                                                                                 29
       }
10
                                                                                        power >>= 1;
11
                                                                                 31
       for (ll i = 2; i <= n; i++) {
12
                                                                                 32
           if (phi[i] == i) { // i es primo
13
                                                                                        return 2 * (n - power);
                                                                                 33
               for (ll j = i; j <= n; j += i) {
14
                                                                                 34 }
                   phi[j] = phi[j] * (i - 1) / i;
15
               }
                                                                                                                    MOBIUS
16
                                                                                                               6.7
17
       }
18
                                                                                  #include <bits/stdc++.h>
19
                                                                                    using namespace std;
       return phi;
20
                                                                                    typedef long long 11;
21 | }
                            6.6 JOSEPHUS
                                                                                    vector<ll> compute_mobius(ll n) {
                                                                                         vector<ll> mu(n + 1, 1);
   #include <iostream>
   using namespace std;
                                                                                         vector<bool> is_prime(n + 1, true);
                                                                                  8
                                                                                  9
                                                                                        for (ll i = 2; i <= n; i++) {
   typedef long long 11;
                                                                                 10
                                                                                            if (is_prime[i]) { // i es un primo
                                                                                 11
                                                                                                 for (ll j = i; j <= n; j += i) {
   ll josephus_iterative(ll n, ll k) {
6
                                                                                 12
                                                                                                     mu[j] *= -1; // Multiplicamos por -1 para cada primo
       11 result = 0;
                                                                                 13
```

14

is_prime[j] = false;

```
}
                                                                                                a = (1LL * a * a) % m:
15
                                                                                    14
                for (ll j = i * i; j <= n; j += i * i) {
                                                                                                exp /= 2;
                                                                                    15
16
                    mu[j] = 0; // Si tiene un cuadrado de un primo, se pone
                                                                                            }
                                                                                     16
17
                                                                                            return res;
                                                                                     17
                }
                                                                                        }
                                                                                     18
18
           }
19
                                                                                    19
       }
                                                                                        void ntt(vector<ll> & a, bool invert) {
20
                                                                                            int n = a.size();
^{21}
       return mu;
^{22}
                                                                                    22
                                                                                            for (int i = 1, j = 0; i < n; i++) {
23
                                                                                    23
                                                                                                int bit = n >> 1;
24
                                                                                    24
                                                                                                for (; j & bit; bit >>= 1)
25
                                                                                    25
   ll mobius(ll x) {
                                                                                                     j ^= bit;
                                                                                    26
       11 count = 0;
                                                                                                j ^= bit;
27
                                                                                    27
       for (ll i = 2; i * i <= x; i++) {
                                                                                    28
28
           if (x \% (i * i) == 0)
                                                                                                if (i < j)
29
                                                                                    29
                                                                                                     swap(a[i], a[j]);
               return 0;
30
                                                                                    30
           if (x \% i == 0) {
                                                                                            }
31
                                                                                    31
                count++:
                                                                                    32
32
                x /= i;
                                                                                            for (int len = 2; len <= n; len <<= 1) {
33
           }
                                                                                                int wlen = invert ? root_1 : root;
                                                                                    34
34
       }
                                                                                                for (int i = len; i < root_pw; i <<= 1)</pre>
35
                                                                                                     wlen = (int)(1LL * wlen * wlen % mod);
36
                                                                                    36
       if (x > 1) count++;
37
                                                                                    37
                                                                                                for (int i = 0; i < n; i += len) {
                                                                                    38
38
       return (count % 2 == 0) ? 1 : -1;
                                                                                                     int w = 1;
39
                                                                                    39
40 }
                                                                                                     for (int j = 0; j < len / 2; j++) {
                                                                                    40
                                                                                                         int u = a[i+j], v = (int)(1LL * a[i+j+len/2] * w % mod);
                                                                                    41
                                  6.8 NTT
                                                                                                         a[i+j] = u + v < mod ? u + v : u + v - mod;
                                                                                    42
                                                                                                         a[i+j+len/2] = u - v >= 0 ? u - v : u - v + mod;
                                                                                    43
                                                                                                         w = (int)(1LL * w * wlen % mod);
  #include <bits/stdc++.h>
                                                                                    44
   using namespace std;
                                                                                     45
                                                                                                }
   using cd = complex<double>;
                                                                                    46
                                                                                            }
                                                                                    47
   typedef long long 11;
   const 11 mod = 998244353;
                                                                                            if (invert) {
   const ll root = 31;
                                                                                                int n_1 = inverse(n, mod);
   const ll root_1 = inverse(root, mod);
                                                                                                for (auto & x : a)
   const ll root_pw = 1 << 23;</pre>
                                                                                    51
                                                                                                     x = (int)(1LL * x * n_1 \% mod);
                                                                                    52
                                                                                            }
   ll inverse(ll a. ll m) {
                                                                                     53
                                                                                        }
       11 \text{ res} = 1, \exp = m - 2;
                                                                                    54
11
       while (exp) {
                                                                                    55
12
                                                                                    56 | vector<ll> multiply(vector<ll> const &a, vector<ll> const &b) {
```

if (exp % 2 == 1) res = (1LL * res * a) % m;

```
vector<ll> fa(a.begin(), a.end()), fb(b.begin(), b.end());
57
                                                                                   23
       11 n = 1;
                                                                                   24
58
       while (n < a.size() + b.size())</pre>
59
           n <<= 1;
60
                                                                                   25
       fa.resize(n);
61
                                                                                   26
       fb.resize(n);
62
                                                                                   27
63
                                                                                   28
       ntt(fa, false);
64
                                                                                   29
       ntt(fb, false);
65
       for (ll i = 0; i < n; i++)
66
           fa[i] = (fa[i] * fb[i]) % mod;
                                                                                   31 }
67
       ntt(fa, true);
68
69
       vector<ll> result(n):
70
       for (ll i = 0; i < n; i++)
71
           result[i] = fa[i];
72
       return result;
73
74 | }
                        PRIME FACTORIZATION
```

```
1
   vector<pair<11, 11>> prime_factors(11 n) {
       vector<pair<11, 11>> factors;
3
       for (ll i = 2; i * i <= n; i++) {
4
           if (n \% i == 0) {
5
               11 count = 0;
6
               while (n \% i == 0) {
                   n /= i;
                    count++;
9
10
               factors.push_back({i, count});
11
12
       }
13
       if (n > 1) factors.push_back(\{n, 1\});
14
       return factors;
15
16
17
18
   vector<ll> divisors(ll n) {
19
       vector<ll> divs;
20
       for (ll i = 1; i * i <= n; i++) {
21
           if (n % i == 0) {
22
```

```
divs.push_back(i);
               if (i != n / i) { // Evita duplicar si n es un cuadrado
                    perfecto
                   divs.push_back(n / i);
           }
       }
       sort(divs.begin(), divs.end()); // Ordena los divisores en orden
           ascendente
       return divs;
                               6.10 SIEVE
 1 | #include <iostream>
   #include <vector>
   using namespace std;
   typedef long long 11;
   vector<ll> sieve_of_eratosthenes(ll n) {
8
       vector<ll> primes;
9
       vector<ll> primoRel(n,0);
10
       for(int i = 2; i < n; i++){
11
           if(!primoRel[i]){
12
               primes.push_back(i);
13
               for(int j = i*i; j < n; j+=i){
14
                   primoRel[j] = i;
15
16
           }
17
       }
18
19
       return primes;
20
21 }
                                  6.11 fft
 1 | #include <bits/stdc++.h>
   using namespace std;
   using cd = complex<double>;
   typedef long long 11;
   const double PI = acos(-1);
5
6
```

```
void fft(vector<cd> &a, bool invert) {
                                                                               50
       ll n = a.size();
8
                                                                               51
       if (n == 1)
                                                                                   //Exponensiacion binommial-----
9
                                                                               52
          return;
10
      vector<cd> a0(n / 2), a1(n / 2);
                                                                                  vector<ll> binomial_exponentiation(const vector<ll> &a, int exp) {
11
      for (ll i = 0; 2 * i < n; i++) {
                                                                                      vector<ll> result = {1};
12
          a0[i] = a[2 * i];
                                                                                      vector<ll> base = a;
13
                                                                               56
          a1[i] = a[2 * i + 1];
14
       }
                                                                                      while (exp > 0) {
15
       fft(a0, invert);
                                                                                          if (\exp \% 2 == 1) {
16
       fft(a1, invert);
                                                                                              result = multiply(result, base);
17
                                                                               60
       double ang = 2 * PI / n * (invert ? -1 : 1);
18
                                                                               61
       cd w(1), wn(cos(ang), sin(ang));
                                                                                          base = multiply(base, base);
                                                                               62
       for (ll i = 0: 2 * i < n: i++) {
                                                                                          exp /= 2;
                                                                               63
20
          a[i] = a0[i] + w * a1[i];
                                                                                      }
21
                                                                               64
          a[i + n / 2] = a0[i] - w * a1[i];
                                                                                      while (result.size() > 1 && result.back() == 0) {
          if (invert) {
23
              a[i] /= 2;
                                                                                          result.pop_back();
              a[i + n / 2] /= 2:
                                                                                      }
                                                                               68
25
26
                                                                                      return result;
          w *= wn;
                                                                               70
27
28
                                                                               71
29
                                                                               72
                                                                                   //FFT PRECISO -----
30
   vector<ll> multiply(vector<ll> const &a, vector<ll> const &b) {
                                                                               74
31
       vector<cd> fa(a.begin(), a.end()), fb(b.begin(), b.end());
                                                                                  #define ll long long
32
       11 n = 1:
                                                                                  using namespace std;
33
       while (n < a.size() + b.size())</pre>
                                                                                  const double pi = acos(-1);
34
          n <<= 1:
35
       fa.resize(n);
                                                                                  typedef long double ld;
36
       fb.resize(n);
                                                                                  typedef complex<ld> cd;
37
                                                                                  const ld PI = acos(-1);
38
       fft(fa, false);
39
       fft(fb. false):
                                                                                  void fft(vector<cd>& a. bool invert) {
40
       for (ll i = 0; i < n; i++)
                                                                                      int n = a.size();
                                                                               84
41
          fa[i] *= fb[i]:
                                                                               85
42
       fft(fa, true);
43
                                                                                      for (int i = 1, j = 0; i < n; ++i) {
44
       vector<ll> result(n);
                                                                                          int bit = n \gg 1;
45
       for (ll i = 0; i < n; i++)
                                                                                          for (; j & bit; bit >>=1)
46
          result[i] = round(fa[i].real());
                                                                                              j ^= bit;
47
       return result;
                                                                                          j ^= bit;
48
                                                                               91
49 }
                                                                                          if (i < j)
                                                                               92
```

```
swap(a[i], a[j]);
93
        }
94
95
        // Cooley-Tukey FFT
96
        for (int len = 2; len <= n; len <<=1) {
97
            ld ang = 2 * PI / len * (invert ? -1 : 1);
98
             cd wlen(cosl(ang), sinl(ang));
99
            for (int i = 0; i < n; i += len) {
100
                 cd w(1);
101
                 int len2 = len \gg 1;
102
                 for (int j = 0; j < len2; ++j) {
103
                     cd u = a[i + j];
104
                     cd v = a[i + j + len2] * w;
105
                     a[i + j] = u + v;
106
                     a[i + j + len2] = u - v;
107
                     w *= wlen;
108
                 }
109
            }
110
        }
111
112
113
        if (invert) {
114
            for (cd & x : a)
115
                 x /= n;
116
        }
117
118
119
    vector<ll> multiply(const vector<ll>& a, const vector<ll>& b) {
120
        const 11 BASE = 1e6;
121
122
        int n = 1;
123
        while(n < (int)(a.size() + b.size()))</pre>
124
            n <<= 1:
125
126
        vector<cd> al(n), ah(n), bl(n), bh(n);
127
        for (size_t i = 0; i < a.size(); ++i) {</pre>
128
            al[i] = a[i] \% BASE;
129
            ah[i] = a[i] / BASE;
130
        }
131
        for (size_t i = 0; i < b.size(); ++i) {</pre>
132
            bl[i] = b[i] \% BASE;
133
            bh[i] = b[i] / BASE;
134
        }
135
```

```
136
        fft(al, false);
137
        fft(ah, false);
138
        fft(bl, false);
139
        fft(bh, false);
140
141
        vector<cd> lx(n), lh(n), hl(n), hh(n);
142
        for (int i = 0; i < n; ++i) {
143
            lx[i] = al[i] * bl[i];
144
            lh[i] = al[i] * bh[i];
145
            hl[i] = ah[i] * bl[i];
146
            hh[i] = ah[i] * bh[i];
147
        }
148
149
        fft(lx, true);
150
        fft(lh, true);
151
        fft(hl, true);
152
        fft(hh, true);
153
154
        vector<ll> result(n);
155
        for (int i = 0; i < n; ++i) {
156
            11 temp_ll = llround(lx[i].real());
157
            11 temp_lh = llround(lh[i].real());
158
            ll temp_hl = llround(hl[i].real());
159
            11 temp_hh = llround(hh[i].real());
160
161
            result[i] = temp_ll +
162
                         ((temp_lh + temp_hl) * BASE) +
163
                         (temp_hh * BASE * BASE);
164
        }
165
166
        return result;
167
168 }
```

7 Geometry

7.1 CONVEX HULL

```
#include <iostream>
#include <vector>
#include <algorithm>
using namespace std;
```

```
typedef long long 11;
   typedef pair<11, 11> Point;
   11 cross_product(Point O, Point A, Point B) {
       return (A.first - O.first) * (B.second - O.second) - (A.second - O.
10
           second) * (B.first - O.first);
11
^{12}
   vector<Point> convex_hull(vector<Point>& points) {
13
       sort(points.begin(), points.end());
14
       points.erase(unique(points.begin(), points.end());
15
       vector<Point> hull;
16
17
       // Parte inferior
18
       for (const auto& p : points) {
19
           while (hull.size() >= 2 && cross_product(hull[hull.size() - 2],
20
               hull[hull.size() - 1], p) < 0)
               hull.pop_back();
21
           if (hull.empty() || hull.back() != p) {
22
               hull.push_back(p);
23
           }
24
       }
25
26
       // Parte superior
27
       int t = hull.size() + 1;
28
       for (int i = points.size() - 1; i \ge 0; --i) {
29
           while (hull.size() >= t && cross_product(hull[hull.size() - 2],
30
               hull[hull.size() - 1], points[i]) < 0)</pre>
               hull.pop_back();
31
           if (hull.empty() || hull.back() != points[i]) {
32
               hull.push_back(points[i]);
33
           }
34
       }
35
36
       hull.pop_back();
37
       return hull:
38
39 }
                                OPERATIONS
```

```
#include <bits/stdc++.h>
using namespace std;
```

```
typedef long long 11;
5
6
   11 cross_product(pair<11, 11> P1, pair<11, 11> P2, pair<11, 11> P3) {
       11 x1 = P2.first - P1.first;
8
       11 v1 = P2.second - P1.second;
9
       11 \times 2 = P3.first - P1.first;
10
       11 y2 = P3.second - P1.second;
       return x1 * y2 - y1 * x2;
12
13
14
15
   double distancia(pair<11, 11> P1, pair<11, 11> P2) {
       return sqrt((P2.first - P1.first) * (P2.first - P1.first) +
                    (P2.second - P1.second) * (P2.second - P1.second));
18
19
20
21
   11 dot_product(pair<11, 11> P1, pair<11, 11> P2, pair<11, 11> P3) {
       11 x1 = P2.first - P1.first;
       11 y1 = P2.second - P1.second;
       11 x2 = P3.first - P1.first;
       11 y2 = P3.second - P1.second;
       return x1 * x2 + y1 * y2;
27
28 }
```

7.3 POLYGON AREA

```
1 | #include <iostream>
   #include <vector>
   #include <cmath>
   using namespace std;
   typedef long long 11;
   typedef pair<11, 11> Point;
   double polygon_area(const vector<Point>& polygon) {
       ll area = 0:
11
       int n = polygon.size();
       for (int i = 0; i < n; ++i) {
13
           11 j = (i + 1) \% n;
14
           area += (polygon[i].first * polygon[j].second - polygon[i].
15
```

const int N = 1e5;

```
second * polygon[j].first);
16
       return abs(area) / 2.0;
17
18 }
                         7.4 RAY CASTING
   #include <iostream>
   #include <vector>
   using namespace std;
   typedef long long 11;
   typedef pair<11, 11> Point;
   bool is_point_in_polygon(const vector<Point>& polygon, Point p) {
9
       bool inside = false;
10
       int n = polygon.size();
11
       for (int i = 0, j = n - 1; i < n; j = i++) {
12
           if ((polygon[i].second > p.second) != (polygon[j].second > p.
13
               second) &&
               p.first < (polygon[j].first - polygon[i].first) * (p.second</pre>
14
                   - polygon[i].second) /
                         (polygon[j].second - polygon[i].second) + polygon[
15
                             il.first) {
               inside = !inside:
16
17
       }
18
       return inside;
19
20 }
                                     Trees
                              8.1 Centroid
   #include <bits/stdc++.h>
   using namespace std;
   #define L(i, j, n) for (int i = (j); i < int(n); i ++)
   #define ii pair<int, int>
   const int inf = 1e9;
```

```
9 | vector<int> G[N]:
  int ct[N];
   set<ii> dist[N];
  int up[N][18];
  int colors[N];
   int depth[N];
   int sz[N];
   bool removed[N];
   int n, root, L;
   int getSize(int u, int p){
       int szi = 1;
       for(int v: G[u]){
21
           if (p == v || removed[v]) continue;
           szi += getSize(v, u);
23
24
       return sz[u] = szi;
25
26
27
   int centroid(int u, int tree_size, int p){
       for (int v: G[u]){
29
           if (v == p || removed[v]) continue;
30
           if (sz[v] * 2 > tree_size) return centroid(v, tree_size, u);
31
       }
32
       return u;
33
34
35
   void build(int node, int tree_size, int p)
37
       getSize(node, - 1);
       int cen = centroid(node, tree_size, -1);
       removed[cen] = 1;
40
       ct[cen] = p;
       if (p == -1) root = cen;
       if (tree_size == 1) return;
       for (int v: G[cen]){
           if (removed[v]) continue;
47
           build(v, sz[v], cen);
49
50
51 | }
```

```
52
   void update(int v){
53
       int u = v;
54
       while(v != -1){
55
           dist[v].insert(distance(u, v), v);
56
           v = par[v];
57
       }
58
       return res;
59
60
61
   int query(int v){
62
       int u = v;
63
       int res = INT MAX:
64
       while(v != -1){
65
           res = min(res, distance(u, v), dist[v].begin()->first); //
66
                Minimun
           v = par[v];
67
       }
68
       return res;
69
70 }
```

8.2 LCA

```
#include <bits/stdc++.h>
   using namespace std;
   #define L(i, j, n) for (int i = (j); i < int(n); i ++)
   #define ii pair<int, int>
   const int inf = 1e9;
   const int N = 1e5;
   vector<int> G[N], ct[N];
   set<ii> dist[N];
   int up[N][18];
11
   int colors[N];
   int depth[N];
13
   int sz[N];
   bool removed[N];
   int n, root, L;
17
   int getSize(int u, int p){
18
       int szi = 1;
19
       for(int v: G[u]){
```

```
if (p == v || removed[v]) continue;
21
           szi += getSize(v, u);
22
23
       return sz[u] = szi;
^{24}
   }
25
26
   int centroid(int u, int tree_size, int p){
       for (int v: G[u]){
           if (v == p || removed[v]) continue;
           if (sz[v] * 2 > tree_size) return centroid(v, tree_size, u);
       }
31
       return u;
32
   }
33
   void build(int node, int tree_size, int p)
   {
36
       getSize(node, - 1);
37
       int cen = centroid(node, tree_size, -1);
       removed[cen] = 1:
39
       if (p != -1){
           ct[cen].push_back(p);
41
       } else root = cen;
43
       if (tree_size == 1) return;
44
45
       for (int v: G[cen]){
46
           if (removed[v]) continue;
47
           build(v, sz[v], cen);
48
       }
49
50
51
   void dfs(int u, int p){
       up[u][0] = p;
       for (int i = 1; i \le L; i ++){
           if (up[u][i-1] != -1) up[u][i] = up[up[u][i-1]][i-1];
           else up[u][i] = -1;
57
       }
58
       for (int v: G[u]){
           if (v == p) continue;
           depth[v] = depth[u] + 1;
61
           dfs(v, u);
62
       }
63
```

```
64 }
65
   int LCA(int u, int v){
66
        if (depth[u] < depth[v]) swap(u, v);</pre>
67
       for (int i = L; i \ge 0; i --){
68
            if (up[u][i] != -1 && depth[up[u][i]] >= depth[v]){
69
                u = up[u][i];
70
            }
71
        }
72
        if (u == v) return u;
73
        for (int i = L; i \ge 0; i --){
74
            if (up[u][i] != up[v][i] \&\& up[u][i] != -1 \&\& up[v][i] != -1){
75
                u = up[u][i];
76
                v = up[v][i];
77
            }
78
        }
79
       return up[u][0];
80
81
82
    int dis(int u, int v){
83
        int cmm = LCA(u, v);
84
       // cout << u << " " << v << " " << cmm << "\n";
85
       return depth[u] + depth[v] - (2 * depth[cmm]);
86
87
88
    void uup(int u, int node){
89
       dist[u].insert({dis(u, node), node});
90
        for (int v: ct[u])
91
            uup(v, node);
92
93
94
    void update(int node){
95
        dist[node].insert({0, node});
96
        for (int v: ct[node])
97
            uup(v, node);
98
99
100
   int qup(int u, int node){
101
        int mn = dis(node, u) + dist[u].begin()->first;
102
       for (int v: ct[u]) mn = min(mn, qup(v, node));
103
        return mn;
104
105
106
```

```
int query(int node){
        int mn = dist[node].begin()->first;
108
        for (int v: ct[node]) mn = min(mn, qup(v, node));
109
        return mn;
110
   }
111
112
   int main()
113
   {
114
        ios::sync_with_stdio(0);cin.tie(0);
115
        int m; cin >> n >> m;
116
        L = log2(n);
117
        L(i, 1, n){
118
            int u, v; cin >> u >> v;
119
            u --; v --;
120
            G[u].push_back(v);
121
            G[v].push_back(u);
122
        }
123
        L(i, 0, n){
            dist[i].insert({inf, i});
125
        }
126
        build(0, n, -1);
127
        L(i, 0, L + 1) up[root][i] = -1;
        run(root, -1);
129
        update(0);
130
        L(_q, 0, m){
131
            int op, node; cin >> op >> node;
132
            if (op == 2){
133
                 cout << query(node-1) << '\n';</pre>
134
            } else {
135
                 update(node-1); // Log Log
136
            }
137
        }
138
139 }
```