Dividimos y No Conquistamos (D&!C)

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1 Template

1.1 C++ Template

```
#include <bits/stdc++.h>
   using namespace std;
2
   #define L(i, j, n) for (int i = (j); i < (int)n; i ++)
   #define SZ(x) int((x).size())
   #define ALL(x) begin(x),end(x)
   #define vec vector
   #define pb push_back
   #define eb emplace_back
   using ll = long long;
   using ld = long double;
13
   void solve(){}
15
   int main(){
       ios::sync_with_stdio(0);cin.tie(0);
17
       int TT = 1:
18
       //cin >> TT:
19
       while (TT--) {
20
           solve();
21
       }
^{22}
23 | }
```

1.2 Fast Python

```
import os, sys, io
finput = io.BytesIO(os.read(0, os.fstat(0).st_size)).readline
fprint = sys.stdout.write
```

2 Search

2.1 Ternary

```
// Minimo de 'f' en '(l,r)'.
template<class Fun>ll ternary(Fun f, ll l, ll r) {
  for (ll d = r-l; d > 2; d = r-l) {
    ll a = l + d/3, b = r - d/3;
    if (f(a) > f(b)) l = a; else r = b;
}
```

```
return 1 + 1:
   }
8
   // para error < EPS, usar iters=log((r-1)/EPS)/log(1.618)</pre>
9
   template<class Fun>double golden(Fun f, double 1, double r, int iters){
     double const ratio = (3-sqrt(5))/2;
11
     double x1=1+(r-1)*ratio, x2=r-(r-1)*ratio, f1=f(x1), f2=f(x2);
12
     while (iters--) {
13
       if (f1 > f2) l=x1, x1=x2, f1=f2, x2=r-(r-1)*ratio, f2=f(x2);
14
                     r=x2, x2=x1, f2=f1, x1=1+(r-1)*ratio, f1=f(x1);
15
     }
16
     return (1+r)/2;
17
18 }
                       2.2 Simulated Annealing
   using my_clock = chrono::steady_clock;
   struct Random {
     mt19937_64 engine;
     Random(): engine(my_clock::now().time_since_epoch().count()) {}
     template<class Int>Int integer(Int n) {return integer<Int>(0, n);} //
         '[0,n)'
     template<class Int>Int integer(Int 1, Int r)
6
       {return uniform_int_distribution{1, r-1}(engine);} // '[1,r)'
7
     double real() {return uniform_real_distribution{}(engine);} // '[0,1)'
8
   struct Timer {
     using time = my_clock::time_point;
11
     time start = my_clock::now();
12
     double elapsed() { // Segundos desde el inicio.
13
       time now = my_clock::now();
14
       return chrono::duration<double>(now - start).count();
15
16
   } timer;
17
   template<class See,class Upd>struct Annealing {
     using energy = invoke_result_t<See>;
19
     energy curr, low;
20
     See see;
21
     Upd upd:
22
     Annealing(See _see, Upd _upd): see{_see}, upd{_upd}
23
       \{\text{curr} = \text{low} = \text{see}(), \text{upd}();\}
24
     void simulate(double s, double mult=1) { // Simula por 's' segundos.
25
       double t0 = timer.elapsed();
26
       for (double t = t0; t-t0 < s; t = timer.elapsed()) {</pre>
27
```

```
energy near = see();
28
         auto delta = double(curr - near);
29
         if (delta >= 0) upd(), curr = near, low = min(low, curr);
30
         else {
31
           double temp = mult * (1 - (t-t0)/s);
32
           if (exp(delta/temp) > rng.real()) upd(), curr = near;
33
34
35
36
37
   auto see = [&] -> double {
38
       1 = rng.integer(gsz);r = rng.integer(gsz);
39
       swap(groups[1], groups[r]);
40
       int ans = 0, rem =0;
41
       L(i,0,gsz){
42
           if (groups[i] > rem) {
43
               rem = x;
44
                ans ++;
45
           }
46
           rem -= groups[i];
47
       }
48
       swap(groups[1], groups[r]);
49
       return ans;
50
51
s2 | auto upd = [&] {swap(groups[1], groups[r]);};
```

3 Data structures

3.1 BIT

```
#define LSO(S) (S & -S)
   struct BIT {
2
       vec<int> B;
3
       int n;
4
       BIT(int n = 1): B(n + 1), n(n+1){}
5
       BIT(vec<int> &v): B(SZ(v)+1), n(SZ(v)+1) {
6
           LI(i, 1, n){
7
               B[i] += v[i-1]:
               if (i + LSO(i) \le n){
9
                   B[i + LSO(i)] += B[i];
10
               }
11
           }
12
       }
13
```

```
void update(int i, int x){
14
            while (i \le n){
15
                B[i] += x;
16
                i += LSO(i);
17
            }
18
19
       int sum(int i){
20
            int res = 0;
21
            while (i > 0){
22
                res += B[i];
                i = LSO(i);
24
25
            return res;
26
27
       int range_sum(int 1, int r){
28
            return sum(r) - sum(1 - 1);
       }
30
31 };
                               3.2 BIT - 2D
1 #define LSO(S) (S & -S)
int f[N][N]; // Initial Matrix
   struct BIT {
       vec<vec<int>> B;
       int n:
5
       BIT(int n_{=} = 1): B(n_{+} + 1, \text{vec} < \text{int} > (n_{+} + 1)), sz(n_{-}) \{ // N * N * \log(N) \}
6
            * log(N);
            for (int i = 1; i <= n_; i ++)
7
                for (int j = 1; j \le n_{j} + +)
8
                    add(i, j, f[i-1][j-1]);
9
10
       void add(int i, int j, int delta){ // log(N) * log(N)
11
            for (int x = i; x \le n; x += LSO(x))
12
                for (int y = j; y \le n; y += LSO(y))
13
                    B[x][y] += delta;
14
15
       int sum(int i, int j){ // log(N) * log(N)
16
            int tot = 0:
17
            for (int x = i; x > 0; x -= LSO(x))
18
                for(int y = j; y > 0; y = LSO(y))
19
                    tot += B[x][y];
20
            return tot;
21
```

```
}
                                                                                                for (int j = 0; j + (1 << i) <= n; <math>j ++) {
                                                                                 10
23 };
                                                                                 11
                                                                                                        ]); // change op
                                3.3 DSU
                                                                                                }
                                                                                 12
                                                                                            }
                                                                                 13
struct DSU {
                                                                                 14
       vec<int> par, sz; int n;
2
                                                                                        int get(int 1, int r) {
                                                                                 15
       DSU(int n = 1): par(n), sz(n, 1), n(n) { iota(ALL(par), 0); }
3
                                                                                            int bit = log2(r - 1 + 1);
                                                                                 16
       int find(int a){return a == par[a] ? a : par[a] = find(par[a]);}
4
                                                                                 17
       void join(int a, int b){
5
                                                                                        }
                                                                                 18
           a=find(a);b=find(b);
6
                                                                                 19 };
           if (a == b) return;
           if (sz[b] > sz[a]) swap(a,b);
                                                                                                             3.6 Segment tree
           par[b] = a;
9
           sz[a] += sz[b];
10
                                                                                  #define LC(v) (v<<1)</pre>
       }
11
                                                                                    #define RC(v) ((v<<1)|1)
12 |};
                                                                                    #define MD(L, R) (L+((R-L)>>1))
                                                                                    struct node {
                        3.4 Index Compession
                                                                                        ll mx:
                                                                                        11 cant; };
   template<class T>
                                                                                    struct ST {
   struct Index{ // If only 1 use Don't need to copy T type
                                                                                        vec<node> st;
       vec<T> d;
                                                                                        vec<ll> lz; int n;
       int sz;
                                                                                 10
       Index(const vec<T> &a): d(ALL(a)){
                                                                                            build(1, 0, n - 1);}
           sort(ALL(d)); // Sort
                                                                                        node merge(node a, node b){
                                                                                 11
           d.erase(unique(ALL(d)), end(d)); // Erase continuous duplicates
                                                                                            if (a.mx == oo) return b;
                                                                                 12
           sz = SZ(d); }
                                                                                            if (b.mx == oo) return a;
                                                                                 13
       inline int of(T e) const{return lower_bound(ALL(d), e) - begin(d);}
                                                                                 14
           // get index
                                                                                 15
       inline T at(int i) const{return d[i];} // get value of index
                                                                                 16
11 | };
                                                                                        void build(int v, int L, int R){
                                                                                 17
                            3.5 Sparse Table
                                                                                            if (L == R){
                                                                                 18
                                                                                                st[v] = \{0, 1\};
                                                                                 19
   struct SPT {
                                                                                            } else {
                                                                                 20
       vec<vec<int>> st;
                                                                                                int m = MD(L, R);
2
                                                                                 21
       int K;
                                                                                                build(LC(v), L, m);
                                                                                 22
3
       SPT(vec<int> &a): K(0) {
                                                                                                build(RC(v), m + 1, R);
                                                                                 23
           int n = SZ(a):
                                                                                 24
           while((1<<K)<=n) K ++;
                                                                                            }
                                                                                 25
                                                                                        }
           st = vec<vec<int>>(K, vec<int>(n));
                                                                                 26
           L(i,0,n) st[0][i] = a[i];
                                                                                        void push(int v, int L, int R){
                                                                                 27
           L(i,1,K) {
```

```
st[i][j] = min(st[i-1][j], st[i-1][j+(1 << (i-1))
return min(st[bit][1], st[bit][r - (1<<bit) + 1]); // change op
```

```
ST(int n = 1): st(4 * n + 10, {oo, oo}), lz(4 * n + 10, 0), n(n) {
           if (a.mx == b.mx) return {a.mx, a.cant + b.cant};
           return {max(a.mx, b.mx), a.mx > b.mx ? a.cant : b.cant};
               st[v] = merge(st[LC(v)], st[RC(v)]);
           if (lz[v]){
28
```

```
if (L != R){
29
                    st[LC(v)].mx += lz[v]; // Apply to left
30
                    st[RC(v)].mx += lz[v]; // And right
31
                    lz[LC(v)] += lz[v];
32
                    lz[RC(v)] += lz[v];
33
                }
34
                lz[v] = 0;
35
           }
36
       }
37
       void update(int v, int L, int R, int gl, int gr, ll w){
38
           if (ql > R || qr < L) return;
39
           push(v, L, R);
40
           if (ql == L \&\& qr == R){
41
                st[v].mx += w;
42
                lz[v] += w;
43
                push(v, L, R);
44
                return;
45
           }
46
           int m = MD(L, R):
47
           update(LC(v), L, m, ql, min(qr, m), w);
48
           update(RC(v), m + 1, R, max(m + 1, ql), qr, w);
49
           st[v] = merge(st[LC(v)], st[RC(v)]);
50
       }
51
       node query(int v, int L, int R, int ql, int qr){
52
           if (ql > R || qr < L) return {oo, oo};
53
           push(v, L, R);
54
           if (ql == L && qr == R) return st[v];
55
           int m = MD(L, R);
56
           return merge(query(LC(v), L, m, ql, min(m, qr)), query(RC(v), m
57
                + 1, R, max(m + 1, ql), qr);
58
       node query(int 1, int r){return query(1, 0, n - 1, 1, r);}
59
       void update(int 1, int r, ll w){update(1, 0, n - 1, 1, r, w);}
60
61 | };
```

3.7 Segment Tree Iterativo

```
struct STI {
vec<11> st;
int n, K;
STI(vec<11> &a): n(SZ(a)), K(1) {
    while(K<=n) K<<=1;
st.assign(2*K, 0); // 0 default</pre>
```

```
L(i,0,n) st[K+i] = a[i];
            for (int i = K - 1; i > 0; i --) st[i] = st[i*2] + st[i*2+1];
8
       }
9
       void upd(int pos, ll w) {
10
            pos += K;
11
            st[pos] += w;
12
            while((pos>>=1) > 0) st[pos] = st[pos * 2] + st[pos * 2 + 1];
13
14
       11 query(int 1, int r) { // [1, r)
15
           11 \text{ res} = 0;
16
           1 += K; r += K;
17
            while (1 < r) {
18
                if (1 & 1) res += st[1++]:
19
                if (r & 1) res += st[--r]:
20
                1>>=1:r>>=1:
21
            }
22
            return res;
23
       }
25 };
```

3.8 Policy Based

```
#include <ext/pb_ds/assoc_container.hpp>
using namespace __gnu_pbds;
template<typename Key, typename Val=null_type>
using indexed_set = tree<Key, Val, less<Key>, rb_tree_tag,
tree_order_statistics_node_update>;
// indexed_set<char> s;
// char val = *s.find_by_order(0); // acceso por indice
// int idx = s.order_of_key('a'); // busca indice del valor
template<class Key,class Val=null_type>using htable=gp_hash_table<Key,
Val>;
// como unordered_map (o unordered_set si Val es vacio), pero sin metodo count
```

4 Graph

4.1 Bellman Ford

```
struct Edge {int a, b, cost;};
vector<Edge> edges;
int solve(int s) // Source
{
```

```
for (int &id = nxt[i]; id < g[i].size(); id++) {</pre>
10
          int j = g[i][id];
11
         if (mb[j] == -1 or (dist[mb[j]] == dist[i]+1 and dfs(mb[j]))) {
12
            ma[i] = j, mb[j] = i;
13
           return true;
14
15
       }
16
       return false;
17
     }
18
     bool bfs() {
19
       for (int i = 0; i < n; i++) dist[i] = n;
20
       queue<int> q;
21
       for (int i = 0; i < n; i++) if (ma[i] == -1) {
22
         dist[i] = 0:
         q.push(i);
24
       }
25
       bool rep = 0;
26
       while (q.size()) {
         int i = q.front(); q.pop();
28
         for (int j : g[i]) {
           if (mb[j] == -1) rep = 1;
30
            else if (dist[mb[j]] > dist[i] + 1) {
31
              dist[mb[j]] = dist[i] + 1;
32
              q.push(mb[j]);
34
35
       }
36
       return rep;
37
38
     int matching() {
39
       int ret = 0;
40
       for (auto& i : g) shuffle(ALL(i), rng);
41
       while (bfs()) {
42
         for (int i = 0; i < n; i++) nxt[i] = 0;
         for (int i = 0; i < n; i++)
44
            if (ma[i] == -1 \text{ and } dfs(i)) \text{ ret++};
45
       }
46
       return ret:
47
48
     vec<int> cover[2]; // if cover[i][j] = 1 -> node i, j is part of cover
49
     int konig() {
50
       cover[0].assign(n,1); // n left size
51
       cover[1].assign(m,0); // m right size
52
```

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```
vector<int> d(n, INF);
5
       d[s] = 0;
6
       for (int i = 0; i < n - 1; ++i)
           for (Edge e : edges)
8
               if (d[e.a] < INF)
9
                   d[e.b] = min(d[e.b], d[e.a] + e.cost);
10
11 }
                                 4.2 SCC
  vec<int> dfs_num(N, -1), dfs_low(N, -1), in_stack(N);
  int dfs_count = 0;
   int numSCC = 0;
  stack<int> st;
   void dfs(int u){
     dfs_low[u] =dfs_num[u] =dfs_count++;
     st.push(u);
     in_stack[u] = 1;
     for(int v: G[u]) {
       if (dfs_num[v] == -1) dfs(v);
10
       if (in_stack[v]) dfs_low[u] = min(dfs_low[u], dfs_low[v]);
11
12
     if (dfs num[u] == dfs low[u]){
13
       numSCC ++:
14
       while(1){
15
         int v = st.top(); st.pop();
16
         in_stack[v] = 0;
17
         if (u == v) break;
18
19
    }
20
21
```

4.3 Bipartite Matching Hopcroft-Karp - With Konig

```
mt19937 rng((int) chrono::steady_clock::now().time_since_epoch().count()
    );
struct hopcroft_karp {
    int n, m; // n is Left Partition Size, m is Right Partition Size
    vec<vec<int>> g;
    vec<int> dist, nxt, ma, mb;
    hopcroft_karp(int n_, int m_) : n(n_), m(m_), g(n),
        dist(n), nxt(n), ma(n, -1), mb(m, -1) {}
    void add(int a, int b) { g[a].pb(b); }
    bool dfs(int i) {
```

while(true){

28

```
auto go = [&](auto&& me, int u) -> void {
                                                                                              i = -1:
53
                                                                                  29
                                                                                             L(k, 0, n) if(!sn[k] and (j == -1 or ds[k] < ds[j])) j = k;
         cover[0][u] = false;
                                                                                  30
54
         for (auto v : g[u]) if (!cover[1][v]) {
                                                                                              sn[j] = 1; i = vR[j];
55
                                                                                  31
           cover[1][v] = true;
                                                                                              if(i == -1) break;
56
                                                                                  32
           me(me,mb[v]);
                                                                                              L(k, 0, n) if(!sn[k]){
                                                                                  33
57
                                                                                                auto new_ds = ds[j] + cs[i][k] - u[i]-v[k];
58
                                                                                  34
                                                                                               if(ds[k] > new_ds) ds[k]=new_ds, dad[k]=j;
       };
59
                                                                                  35
       L(u,0,n) if (ma[u] < 0) go(go,u);
60
                                                                                  36
       return size;
                                                                                           }
61
                                                                                  37
                                                                                           L(k, 0, n) if (k!=j \text{ and } sn[k])
62
                                                                                              auto w = ds[k]-ds[j]; v[k] += w, u[vR[k]] -= w;
63 | };
                                                                                  39
                                                                                  40
                             4.4 Hungarian
                                                                                           usl += ds[i]:
                                                                                  41
                                                                                           while (dad[i] >= 0) { int d = dad[i]; vR[i] = vR[d]; vL[vR[i]] = i;
                                                                                  42
                                                                                                i = d: 
  using vi = vec<int>;
                                                                                           vR[j] = s; vL[s] = j;
   using vd = vec<ld>;
                                                                                         }
   const ld INF = 1e100;
                           // Para max asignacion, INF = 0, y negar costos
                                                                                  44
                                                                                         ld value = 0; L(i, 0, n) value += cs[i][vL[i]], ans.pb({i, vL[i]});
   bool zero(ld x) {return fabs(x) < 1e-9;} // Para int/ll: return x==0;
                                                                                         return value:
   vec<pii> ans; // Guarda las aristas usadas en el matching: [0..n)x[0..m)
                                                                                  46
                                                                                      }
                                                                                  47
   struct Hungarian{
                                                                                  48 };
     int n; vec<vd> cs; vi vL, vR;
7
     Hungarian(int N, int M) : n(max(N,M)), cs(n,vd(n)), vL(n), vR(n){
8
                                                                                                              4.5 Flow - Dinics
       L(x, 0, N) L(y, 0, M) cs[x][y] = INF;
9
10
     void set(int x, int y, ld c) { cs[x][y] = c; }
                                                                                   1 struct Dinic {
11
     ld assign(){
                                                                                       bool scaling = false; // com scaling -> O(nm log(MAXCAP)),
12
       int mat = 0; vd ds(n), u(n), v(n); vi dad(n), sn(n);
                                                                                       int lim:
                                                                                                                    // com constante alta
13
       L(i, 0, n) u[i] = *min_element(ALL(cs[i]));
                                                                                       struct edge {
14
       L(j, 0, n){
                                                                                         int to, cap, rev, flow;
                                                                                   5
15
         v[i] = cs[0][i]-u[0];
                                                                                         bool res;
16
                                                                                   6
         L(i, 1, n) v[j] = min(v[j], cs[i][j] - u[i]);
                                                                                         edge(int to_, int cap_, int rev_, bool res_)
17
                                                                                            : to(to_), cap(cap_), rev(rev_), flow(0), res(res_) {}
                                                                                   8
18
       vL = vR = vi(n, -1);
                                                                                       };
                                                                                  9
19
       L(i,0, n) L(j, 0, n) if (vR[j] == -1 \text{ and } zero(cs[i][j] - u[i] - v[j])
                                                                                       vec<vec<edge>> g;
                                                                                  10
20
           ){
                                                                                       vec<int> lev, beg;
                                                                                  11
         vL[i] = j; vR[j] = i; mat++; break;
                                                                                       11 F;
                                                                                  12
21
                                                                                       Dinic(int n) : g(n), F(0) {}
                                                                                  13
^{22}
                                                                                       void add(int a, int b, int c) {
       for(: mat < n: mat ++){
23
                                                                                  14
         int s = 0, j = 0, i;
                                                                                         g[a].emplace_back(b, c, g[b].size(), false);
                                                                                  15
24
         while(vL[s] != -1) s++;
                                                                                         g[b].emplace_back(a, 0, g[a].size()-1, true);
                                                                                  16
25
         fill(ALL(dad), -1); fill(ALL(sn), 0);
26
                                                                                  17
         L(k, 0, n) ds[k] = cs[s][k]-u[s]-v[k];
                                                                                       bool bfs(int s, int t) {
                                                                                  18
27
```

19

lev = vector<int>(g.size(), -1); lev[s] = 0;

64 }

return cut;

```
beg = vector<int>(g.size(), 0);
20
       queue<int> q; q.push(s);
^{21}
       while (q.size()) {
^{22}
         int u = q.front(); q.pop();
23
         for (auto& i : g[u]) {
24
           if (lev[i.to] != -1 or (i.flow == i.cap)) continue;
25
           if (scaling and i.cap - i.flow < lim) continue;</pre>
26
           lev[i.to] = lev[u] + 1;
27
           q.push(i.to);
28
29
       }
30
       return lev[t] != -1;
31
32
     int dfs(int v, int s, int f = oo) {
33
       if (!f or v == s) return f;
34
       for (int& i = beg[v]; i < g[v].size(); i++) {
35
         auto& e = g[v][i];
36
         if (lev[e.to] != lev[v] + 1) continue;
37
         int foi = dfs(e.to, s, min(f, e.cap - e.flow));
38
         if (!foi) continue;
39
         e.flow += foi, g[e.to][e.rev].flow -= foi;
40
         return foi;
41
       }
42
       return 0;
43
     }
44
     11 max_flow(int s, int t) {
45
       for (lim = scaling ? (1<<30) : 1; lim; lim /= 2)
46
         while (bfs(s, t)) while (int ff = dfs(s, t)) F += ff;
47
       return F;
48
     }
49
50
   vec<pair<int, int>> get_cut(Dinic& g, int s, int t) {
51
     g.max_flow(s, t);
52
     vec<pair<int, int>> cut;
53
     vec<int> vis(g.g.size(), 0), st = {s};
54
     vis[s] = 1:
55
     while (st.size()) {
56
       int u = st.back(); st.pop_back();
57
       for (auto e : g.g[u]) if (!vis[e.to] and e.flow < e.cap)</pre>
58
         vis[e.to] = 1, st.push_back(e.to);
59
60
     for (int i = 0; i < g.g.size(); i++) for (auto e : g.g[i])
61
       if (vis[i] and !vis[e.to] and !e.res) cut.emplace_back(i, e.to);
62
```

```
4.6 Flow - MinCostMaxFlow
```

```
_1 // 0(nm + f * m log n)
2 // const ll oo = (ll)1e18:
   template<typename T> struct mcmf {
     struct edge {
       int to, rev, flow, cap; // para, id da reversa, fluxo, capacidade
       bool res; // se eh reversa
       T cost; // custo da unidade de fluxo
       edge(): to(0), rev(0), flow(0), cap(0), cost(0), res(false) {}
       edge(int to_, int rev_, int flow_, int cap_, T cost_, bool res_)
         : to(to_), rev(rev_), flow(flow_), cap(cap_), res(res_), cost(
             cost_) {}
    };
11
     vec<vec<edge>> g;
12
     vec<int> par_idx, par;
     T inf:
     vec<T> dist:
15
     mcmf(int n) : g(n), par_idx(n), par(n), inf(numeric_limits<T>::max()
         /3) {}
    void add(int u, int v, int w, T cost) { // de u pra v com cap w e
17
         custo cost
       edge a = edge(v, g[v].size(), 0, w, cost, false);
18
       edge b = edge(u, g[u].size(), 0, 0, -cost, true);
19
       g[u].push_back(a);
       g[v].push_back(b);
21
22
     vec<T> spfa(int s) { // nao precisa se nao tiver custo negativo
23
       deque<int> q;
24
       vec<bool> is_inside(g.size(), 0);
25
       dist = vec<T>(g.size(), inf);
26
       dist[s] = 0;
27
       q.push_back(s);
28
       is_inside[s] = true;
29
       while (!q.empty()) {
30
         int v = q.front();
31
         q.pop_front();
32
         is_inside[v] = false;
33
         for (int i = 0; i < g[v].size(); i++) {</pre>
34
           auto [to, rev, flow, cap, res, cost] = g[v][i];
35
```

```
if (flow < cap and dist[v] + cost < dist[to]) {</pre>
                                                                                               while (u != s){
36
                                                                                     78
              dist[to] = dist[v] + cost;
                                                                                                 mn_flow = min(mn_flow,
37
                                                                                     79
                                                                                                   g[par[u]][par_idx[u]].cap - g[par[u]][par_idx[u]].flow);
38
                                                                                     80
              if (is_inside[to]) continue;
                                                                                                 u = par[u];
39
                                                                                     81
              if (!q.empty() and dist[to] > dist[q.front()]) q.push_back(to)
                                                                                               }
40
                                                                                     82
                                                                                               ret += pot[t] * mn_flow;
                                                                                     83
              else q.push_front(to);
                                                                                               u = t;
                                                                                     84
41
              is_inside[to] = true;
                                                                                               while (u != s) {
42
           }
                                                                                                 g[par[u]][par_idx[u]].flow += mn_flow;
43
                                                                                                 g[u][g[par[u]][par_idx[u]].rev].flow -= mn_flow;
44
       }
                                                                                                 u = par[u];
45
                                                                                     88
       return dist;
                                                                                     89
46
                                                                                               f += mn_flow;
                                                                                     90
47
     bool dijkstra(int s, int t, vec<T>& pot) {
                                                                                     91
48
       priority_queue<pair<T, int>, vec<pair<T, int>>, greater<>> q;
                                                                                             return make_pair(f, ret);
                                                                                     92
49
       dist = vec<T>(g.size(), inf);
50
                                                                                     93
       dist[s] = 0;
                                                                                          // Opcional: retorna as arestas originais por onde passa flow = cap
                                                                                     94
51
       q.emplace(0, s);
                                                                                           vec<pair<int,int>> recover() {
52
                                                                                     95
       while (q.size()) {
                                                                                             vec<pair<int,int>> used;
                                                                                     96
53
                                                                                            for (int i = 0; i < g.size(); i++) for (edge e : g[i])</pre>
         auto [d, v] = q.top();
54
         q.pop();
                                                                                               if(e.flow == e.cap && !e.res) used.push_back({i, e.to});
55
         if (dist[v] < d) continue;</pre>
                                                                                            return used;
56
         for (int i = 0; i < g[v].size(); i++) {</pre>
                                                                                          }
57
                                                                                     100
                                                                                    <sub>101</sub> |};
           auto [to, rev, flow, cap, res, cost] = g[v][i];
58
           cost += pot[v] - pot[to];
59
                                                                                                                       4.7 2 Sat
           if (flow < cap and dist[v] + cost < dist[to]) {</pre>
60
              dist[to] = dist[v] + cost;
61
              q.emplace(dist[to], to);
                                                                                      1 | struct TwoSat {
62
             par_idx[to] = i, par[to] = v;
                                                                                             int n, v_n;
63
                                                                                      2
64
                                                                                             vec<bool> vis, assign;
                                                                                      3
         }
                                                                                            vec<int> order, comp;
65
                                                                                      4
       }
66
                                                                                             vec<vec<int>> g, g_t;
                                                                                     5
       return dist[t] < inf:
                                                                                             TwoSat(int n_): n(n_{-}), v_{-}n(2 * n_{-}), vis(v_{-}n), assign(n_{-}), comp(v_{-}n)
67
                                                                                      6
                                                                                                 , -1), g(v_n), g_t(v_n) {
68
     pair<int, T> min_cost_flow(int s, int t, int flow = (int)1e9) {
                                                                                                 order.reserve(v_n);
69
                                                                                     7
       vec<T> pot(g.size(), 0);
                                                                                             }
70
                                                                                      8
       pot = spfa(s); // mudar algoritmo de caminho minimo aqui
71
                                                                                             void add_disj(int a, bool na, int b, bool nb) { // negated_a,
                                                                                     9
       int f = 0:
                                                                                                 negated b
72
       T ret = 0;
                                                                                                 a = 2 * a ^na:
73
                                                                                     10
       while (f < flow and dijkstra(s, t, pot)) {</pre>
                                                                                                 b = 2 * b ^ nb;
74
                                                                                     11
         for (int i = 0; i < g.size(); i++)
75
                                                                                                 int neg_a = a ^1;
                                                                                     12
           if (dist[i] < inf) pot[i] += dist[i];</pre>
                                                                                                 int neg_b = b^1;
76
                                                                                     13
         int mn_flow = flow - f, u = t;
77
                                                                                                 g[neg_a].pb(b);
                                                                                     14
```

```
g[neg_b].pb(a);
15
           g_t[a].pb(neg_b);
16
           g_t[b].pb(neg_a);
17
       }
18
       void dfs1(int u){
19
           vis[u] = 1;
20
           for (int v: g[u]) if (!vis[v]) dfs1(v);
21
           order.pb(u);
^{22}
       }
23
       void dfs2(int u, int cc) {
24
           comp[u] = cc;
25
           for (int v: g_t[u]) if (comp[v] == -1) dfs2(v, cc);
26
       }
27
       bool solve() {
28
           order.clear();
29
           vis.assign(v_n, 0);
30
           L(i,0, v_n) if (!vis[i]) dfs1(i);
31
           comp.assign(v_n, - 1);
32
           int cc = 0:
33
           L(i, 0, v_n) \{
34
                int v = order[v_n - 1 - i];
35
                if (comp[v] == -1) dfs2(v, cc ++);
36
           }
37
           assign.assign(n, false);
38
           for (int i = 0; i < v_n; i += 2) {
39
                if (comp[i] == comp[i+1]) return false;
40
                assign[i / 2] = comp[i] > comp[i + 1];
41
^{42}
           return true;
43
44
45 };
```

4.8 Euler Tour

```
// Directed version (uncomment commented code for undirected)
struct edge {
   int y;

// list<edge>::iterator rev;
   edge(int y):y(y){}

};

list<edge> g[N];

void add_edge(int a, int b){
   g[a].push_front(edge(b));//auto ia=g[a].begin();
```

```
g[b].push_front(edge(a));auto ib=g[b].begin();
         ia->rev=ib;ib->rev=ia;
11
   }
12
   vec<int> p;
13
   void go(int x){
       while(g[x].size()){
           int y=g[x].front().y;
           //g[y].erase(g[x].front().rev);
           g[x].pop_front();
18
           go(y);
19
20
       p.push_back(x);
21
   }
22
   vec<int> get_path(int x){ // get a path that begins in x
   // check that a path exists from x before calling to get_path!
       p.clear();go(x);reverse(p.begin(),p.end());
       return p;
26
27 }
```

5 Trees

5.1 Heavy Light Decomposition

```
int ans[N], par[N], depth[N], head[N], pos[N];
   vec<int> heavy(N, - 1);
   int t = 0:
   vec<int> g[N];
   int dfs(int u) {
       int size = 1;
       int max_size = 0;
       for (int v: g[u]) if (v != par[u]) {
           par[v] = u;
9
           depth[v] = depth[u] + 1;
10
           int cur_size = dfs(v);
11
           size += cur_size;
12
           if (cur_size > max_size) {
13
               max_size = cur_size;
14
               heavy[u] = v;
15
           }
16
       }
17
       return size;
18
   }
19
20 | void decompose(int u, int h){
```

return u;

int build(int u){

removed[c] = 1;

int c = centroid(u, -1, getSize(u, -1));

13 | }

14

15

16

17

31

32

33

34

35 }

}

return jump[0][u];

```
head[u] = h:
                                                                                          for (int v: G[c]) if (!removed[v]) { build(v); }
21
       pos[u] = t ++;
                                                                                   19
                                                                                          return c;
^{22}
                                                                                  20 }
       if (heavy[u] != -1){ decompose(heavy[u], h); }
23
       for (int v: G[u]) if (v != par[u] && v != heavy[u]) {
^{24}
           decompose(v, v);
                                                                                                     5.3 LCA - Binary exponentiation
25
       }
26
27
   int query(int a, int b) {
                                                                                   vec<int> g[N];
28
       int resp = -1;
                                                                                   _{2} int K; // K should be (1<<K) > n
29
       for (; head[a] != head[b]; b = par[head[b]]){ // Subi todo el heavy
                                                                                     int jump[20][N];
30
           path y a su padre // Next
                                                                                      int depth[N];
           if (depth[head[a]] > depth[head[b]]) swap(a, b);
31
           resp = max(resp, st.query(pos[head[b]], pos[b])); // pos[head[b]
32
                                                                                      void dfs(int u, int p){
               ]] < pos[b]
                                                                                          for (int v: g[u]) if (v != p) {
                                                                                   7
       }
                                                                                              jump[0][v] = u;
33
                                                                                   8
       if (depth[a] > depth[b]) swap(a, b); // Una vez misma path(head)
34
                                                                                              L(i, 1, K + 1) {
                                                                                   9
           entonces es una query [a,b]
                                                                                                  jump[i][v] = -1;
                                                                                   10
       resp = max(resp, st.query(pos[a], pos[b]));
35
                                                                                                  if (jump[i - 1][v] != -1) {
                                                                                  11
       return resp;
                                                                                                      jump[i][v] = jump[i - 1][jump[i - 1][v]];
36
37
                                                                                  13
   dfs(root);
                                                                                              }
38
decompose(root, root);
                                                                                              depth[v] = depth[u] + 1;
                                                                                  15
                                                                                              dfs(v, u);
                                                                                  16
                               5.2 Centroid
                                                                                          }
                                                                                  17
                                                                                      }
                                                                                  18
  int sz[N];
                                                                                   19
   bool removed[N];
                                                                                      int LCA(int u, int v){
   int getSize(int u, int p){
                                                                                          if (depth[u] < depth[v]) swap(u, v); // Make u the deepest
                                                                                  21
3
                                                                                          for (int i = K; i \ge 0; i \longrightarrow 0 // make them same depth
       sz[u] = 1;
4
                                                                                  22
       for(int v: G[u]) if (v != p && !removed[v]){
                                                                                              if (jump[i][u] != -1 && depth[jump[i][u]] >= depth[v]){
5
                                                                                  23
           sz[u] += getSize(v, u);
                                                                                                  u = jump[i][u];
6
                                                                                  24
                                                                                              }
7
                                                                                  25
       return sz[u];
                                                                                          }
8
                                                                                  26
                                                                                          if (u == v) return u; // u is parent of v
9
                                                                                  27
                                                                                          for (int i = K; i \ge 0; i --){
   int centroid(int u, int p, int tz){
                                                                                  28
10
       for (int v: g[u])
                                                                                              if (jump[i][u] != jump[i][v] && jump[i][u] != -1 && jump[i][v]
                                                                                  29
11
           if (v != p \&\& !removed[v] \&\& sz[v] * 2 > tz) return centroid(v,
                                                                                                  !=-1){}
12
                                                                                                  u = jump[i][u];
                                                                                  30
                                                                                                  v = jump[i][v];
```

5.4 LCA - Const Time

```
1 | struct LCA {
       vec<int> depth, in, euler;
2
       vec<vec<int>> g, st;
       int K, n;
       inline int Min(int i, int j) {return depth[i] <= depth[j] ? i : j;}</pre>
       void dfs(int u, int p) {
           in[u] = SZ(euler);
7
           euler.pb(u);
           for (int v: g[u]) if (v != p){
9
                depth[v] = depth[u] + 1;
10
                dfs(v, u);
11
                euler.pb(u);
12
           }
13
14
       LCA(int n_{-}): depth(n_{-}), g(vec<vec<int>>(n_{-})), K(0), n(n_{-}), in(n_{-}) {
15
            euler.reserve(2 * n); }
       void add_edge(int u, int v) {g[u].pb(v);}
16
       void build(int root){
17
           dfs(root, -1):
18
            int ln = SZ(euler);
19
            while((1<<K)<=ln)K++;
20
            st = vec<vec<int>> (K, vec<int>(ln));
21
           L(i,0,ln) st[0][i] = euler[i];
22
           for (int i = 1; (1 << i) <= ln; i ++) {
23
                for (int j = 0; j + (1 << i) <= ln; <math>j ++) {
24
                    st[i][j] = Min(st[i-1][j], st[i-1][j + (1 << (i-1))]);
25
26
           }
27
       }
28
       int get(int u, int v) {
29
            int su = in[u];
30
            int sv = in[v]:
31
           if (sv < su) swap(sv, su);
32
           int bit = log2(sv - su + 1);
33
           return Min(st[bit][su], st[bit][sv - (1<<bit) + 1]);</pre>
34
35
<sub>36</sub> |};
```

6 Dynamic Programming

6.1 Knapsack

```
int knapsack(vector<int>& values, vector<int>& weights, int W) {
       int n = values.size():
       vector<vector<int>> dp(n + 1, vector<int>(W + 1, 0));
4
       for(int i = 1; i <= n; i++) {
5
           for(int w = 0; w \le W; w++) {
6
                if(weights[i-1] <= w) {</pre>
7
                    dp[i][w] = max(dp[i-1][w],
                                  dp[i-1][w-weights[i-1]] + values[i-1]);
9
                } else {
10
                    dp[i][w] = dp[i-1][w];
11
12
           }
13
14
       return dp[n][W];
15
16 }
```

6.2 LIS

```
vector<int> getLIS(vector<int>& arr) {
       int n = arr.size();
       vector<int> dp(n + 1, INT_MAX); // dp[i] = smallest value that ends
3
            an LIS of length i
       vector<int> len(n);
                                        // Length of LIS ending at each
4
           position
       dp[0] = INT_MIN;
5
       for(int i = 0; i < n; i++) {
6
           int j = upper_bound(dp.begin(), dp.end(), arr[i]) - dp.begin();
7
           dp[j] = arr[i];
8
           len[i] = j;
9
       }
10
       // Find maxLen and reconstruct sequence
11
       int maxLen = 0;
12
       for(int i = n-1; i \ge 0; i--) maxLen = max(maxLen, len[i]);
13
       vector<int> lis:
14
       for(int i = n-1, currLen = maxLen; i \ge 0; i--) {
15
           if(len[i] == currLen) {
16
               lis.push_back(arr[i]);
17
               currLen--;
18
```

```
}
                                                                                                 end = i;
19
                                                                                  16
       }
                                                                                             }
                                                                                  17
20
       reverse(lis.begin(), lis.end());
                                                                                         }
                                                                                  18
^{21}
                                                                                         return {maxSoFar, {start, end}}; // max, 1, r
       return lis;
                                                                                  19
^{22}
                                                                                  20 }
23 | }
                                Edit Distance
                           6.3
                                                                                                                      Strings
  int editDistance(string& s1, string& s2) {
                                                                                                                 7.1 Hashing
       int n = s1.length(), m = s2.length();
2
       vector<vector<int>> dp(n + 1, vector<int>(m + 1));
3
                                                                                  static constexpr ll ms[] = {1'000'000'007, 11'000'000'403};
       for(int i = 0; i <= n; i++) dp[i][0] = i;
4
                                                                                     static constexpr 11 b = 500'000'000;
       for(int j = 0; j \le m; j++) dp[0][j] = j;
5
                                                                                     struct StrHash { // Hash polinomial con exponentes decrecientes.
       for(int i = 1; i <= n; i++) {
6
                                                                                       vec<11> hs[2], bs[2];
           for(int j = 1; j <= m; j++) {
7
                                                                                       StrHash(string const& s) {
               if(s1[i-1] == s2[j-1]) {
8
                                                                                         int n = SZ(s);
                                                                                  6
                   dp[i][j] = dp[i-1][j-1];
9
                                                                                         L(k, 0, 2) {
                                                                                  7
               } else {
10
                                                                                           hs[k].resize(n+1), bs[k].resize(n+1, 1);
                                                                                  8
                   dp[i][j] = 1 + min({dp[i-1][j], // deletion}
11
                                                                                           L(i, 0, n) {
                                      dp[i][j-1],
                                                     // insertion
12
                                                                                             hs[k][i+1] = (hs[k][i] * b + s[i]) % ms[k];
                                      dp[i-1][j-1]}); // replacement
13
                                                                                             bs[k][i+1] = bs[k][i] * b
                                                                                                                                 % ms[k];
               }
14
                                                                                           }
                                                                                  12
           }
15
                                                                                         }
       }
16
                                                                                  14
       return dp[n][m];
17
                                                                                       ll get(int idx, int len) const { // Hashes en 's[idx, idx+len)'.
                                                                                 15
18 }
                                                                                         11 h[2]:
                                                                                  16
                               6.4 Kadane
                                                                                         L(k, 0, 2) {
                                                                                 17
                                                                                           h[k] = hs[k][idx+len] - hs[k][idx] * bs[k][len] % ms[k];
                                                                                  18
                                                                                           if (h[k] < 0) h[k] += ms[k];
  pair<int, pair<int,int>> kadane(vector<int>& arr) {
                                                                                  19
       int maxSoFar = arr[0], maxEndingHere = arr[0];
2
                                                                                 20
       int start = 0, end = 0, s = 0;
                                                                                         return (h[0] << 32) | h[1];
                                                                                 21
3
                                                                                  22
4
       for(int i = 1; i < arr.size(); i++) {</pre>
                                                                                     };
                                                                                  23
5
           if(maxEndingHere + arr[i] < arr[i]) {</pre>
6
                                                                                 24
               maxEndingHere = arr[i];
                                                                                     pll union_hash(vec<pll> hs, vec<ll> lens){ //use arrays makes it slower
7
               s = i;
                                                                                       11 len = 0;
8
                                                                                 26
           } else {
                                                                                      for(int i = hs.size()-1; i > 0; i--){
                                                                                 27
9
               maxEndingHere += arr[i];
                                                                                         len += lens[i]:
10
                                                                                 28
           }
                                                                                         pll& [11, 12] = hs[i];
                                                                                 29
11
                                                                                        pll\& [r1, r2] = hs[i-1];
12
           if(maxEndingHere > maxSoFar) {
                                                                                         11 = ((11 * binpow(b, len, ms[0])) \% ms[0] + r1) \% ms[0];
13
               maxSoFar = maxEndingHere;
                                                                                         12 = ((12 * binpow(b, len, ms[1])) \% ms[1] + r2) \% ms[1];
14
                                                                                 32
               start = s;
                                                                                 33
                                                                                      }
15
```

 $while((n - i) >= (m - j)){$

if(pat[j] == sec[i]){

i++;

j++;

12

13

14

15

16

L(i, 1, n) {

```
34
     return hs[0];
35
36 }
                             7.2 Prefix Trie
  struct Trie {
       map<char, int> ch;
2
       bool eee;
3
       Trie(): eee(0) {}
   |};
5
   vec<Trie> t;
6
   void initTrie(){t.clear();t.pb(Trie());}
   void insert(string &word) {
       int v = 0;
9
       for(char c : word) {
10
           if(!t[v].ch[c]) {
11
               t[v].ch[c] = SZ(t);
12
               t.pb(Trie());
13
           }
14
           v = t[v].ch[c];
15
       }
16
       t[v].eee = 1;
17
18 }
                                7.3 KMP
  vec<int> kmp(string pat, string sec){ //geeks4geeks implementation with
       some changes
     int m = pat.length();
2
     int n = sec.length();
     cout << m << "_{\sqcup}" << n << endl;
5
     vec<int> lps = getLps(pat);
6
     vec<int> res;
8
     int i = 0;
9
     int j = 0;
10
11
```

```
if(j == m){
17
         res.push_back(i - j);
18
         j = lps[j - 1];
19
20
       else{
21
         if(i < n && pat[j] != sec[i]){</pre>
22
           if(j != 0) j = lps[ j - 1 ];
23
           else i = i + 1;
24
         }
25
     }
27
28
     return res;
29
30 }
                                 7.4 LPS
vec<int> getLps(string pat){ //geek4geeks implementatio with some
     vec<int> lps(pat.length(), 0);
     int len = 0;
     int i = 1;
     lps[0] = 0;
     while(i < pat.length()){</pre>
       if(pat[i] == pat[len]){
         len++;
8
         lps[i] = len;
         i++;
10
11
       else //pat[i] != pat[len]
12
13
         lps[i] = 0;
14
         i++;
16
     }
17
     return lps;
19 }
                           7.5 Z-FUNCTION
template<class Char=char>vec<int> zfun(const basic_string<Char>& w) {
     int n = SZ(w), l = 0, r = 0; vec < int > z(n);
     z[0] = w.length();
```

```
if (i <= r) {z[i] = min(r - i + 1, z[i - 1]);}
while (i + z[i] < n && w[z[i]] == w[i + z[i]]) {++z[i];}
if (i + z[i] - 1 > r) {1 = i, r = i + z[i] - 1;}
}
return z;
}

7.6 Manacher

| struct Manacher {
```

```
vec<int> p;
2
     Manacher(string const& s) {
3
       int n = SZ(s), m = 2*n+1, l = -1, r = 1;
4
       vec < char > t(m); L(i, 0, n) t[2*i+1] = s[i];
5
       p.resize(m); L(i, 1, m) {
6
         if (i < r) p[i] = min(r-i, p[l+r-i]);
         while (p[i] \le i \&\& i \le m-p[i] \&\& t[i-p[i]] == t[i+p[i]]) ++p[i];
         if (i+p[i] > r) l = i-p[i], r = i+p[i];
9
10
     } // Retorna palindromos de la forma {comienzo, largo}.
11
     pii at(int i) const {int k = p[i]-1; return pair{i/2-k/2, k};}
12
     pii odd(int i) const {return at(2*i+1);} // Mayor centrado en s[i].
     pii even(int i) const {return at(2*i);} // Mayor centrado en s[i-1,i].
14
<sub>15</sub> | };
```

7.7 Aho-Corasick

```
bool vis[N], r[N];
  struct ACvertex {
     map<char,int> next,go;
     int p,link;
4
     char pch;
5
     vec<int> leaf;
     ACACvertex(int p=-1, char pch=-1):p(p),pch(pch),link(-1){}
7
8
   vec<ACvertex> t;
   void aho_init(){ //do not forget!!
     t.clear();t.pb(ACvertex());
11
12
   void add_string(string &s, int id){
13
     int v=0;
14
    for(char c:s){
15
       if(!t[v].next.count(c)){
16
         t[v].next[c]=t.size();
17
```

```
t.pb(ACvertex(v,c));
18
19
       v=t[v].next[c];
20
21
     t[v].leaf.pb(id);
22
23
   int go(int v, char c);
   int get_link(int v){ // Failure link
     if(t[v].link<0)</pre>
       if(!v||!t[v].p)t[v].link=0;
       else t[v].link=go(get_link(t[v].p),t[v].pch);
28
     return t[v].link;
29
30
   int go(int v, char c){ // state = go(state, ch) this state is ACvertex
     if(!t[v].go.count(c))
32
       if(t[v].next.count(c))t[v].go[c]=t[v].next[c];
33
       else t[v].go[c]=v==0?0:go(get_link(v),c);
34
     return t[v].go[c];
35
36
   void proc(int x){
37
       if (x == -1|| vis[x]) return;
       vis[x] = 1;
39
       L(i,0,SZ(t[x].leaf)) r[t[x].leaf[i]] = 1;
       proc(get_link(x));
41
42 }
                                 Suffix-Array
| #define RB(x) ((x) < n ? r[x] : 0)
   void csort(vec<int>& sa, vec<int>& r, int k) {
     int n = SZ(sa);
     vec<int> f(max(255, n)), t(n);
     L(i,0, n) ++f[RB(i+k)];
     int sum = 0;
6
     L(i,0, \max(255, n)) f[i] = (sum += f[i]) - f[i];
    L(i,0, n) t[f[RB(sa[i]+k)]++] = sa[i];
     sa = t:
9
10
   vec<int> compute_sa(string& s){ // O(n*log2(n))
     int n = SZ(s) + 1, rank;
     vec<int> sa(n), r(n), t(n);
13
     iota(all(sa), 0);
```

```
L(i,0, n) r[i] = s[i];
15
     for (int k = 1; k < n; k *= 2) {
16
       csort(sa, r, k), csort(sa, r, 0);
17
       t[sa[0]] = rank = 0;
18
       L(i, 1, n) {
19
         if(r[sa[i]] != r[sa[i-1]] || RB(sa[i]+k) != RB(sa[i-1]+k)) ++rank;
20
         t[sa[i]] = rank;
21
       }
22
       r = t;
23
       if (r[sa[n-1]] == n-1) break;
24
25
     return sa; // sa[i] = i-th suffix of s in lexicographical order
26
27
    vec<int> compute_lcp(string& s, vec<int>& sa){
     int n = SZ(s) + 1, K = 0;
29
     vec<int> lcp(n), plcp(n), phi(n);
30
     phi[sa[0]] = -1;
31
     L(i, 1, n) phi[sa[i]] = sa[i-1];
32
     L(i.0.n) {
33
       if (phi[i] < 0) { plcp[i] = 0; continue; }</pre>
34
       while(s[i+K] == s[phi[i]+K]) ++K;
35
       plcp[i] = K;
36
       K = \max(K - 1, 0);
37
38
     L(i,0, n) lcp[i] = plcp[sa[i]];
39
     return lcp; // lcp[i] = longest common prefix between sa[i-1] and sa[i
41 }
```

8 Math

8.1 Euclidean Extended

```
ll extendedGCD(ll a, ll b, ll &x, ll &y) {
       if (b == 0) {
2
           x = 1;
3
           v = 0;
4
           return a;
5
       }
6
       ll x1, y1;
       ll gcd = extendedGCD(b, a % b, x1, y1);
8
       x = y1;
9
       y = x1 - (a / b) * y1;
10
```

```
return gcd;
11
   }
12
13
   bool findSolutionWithConstraints(ll a, ll b, ll c, ll x_min, ll y_min,
14
       ll &x, ll &v) {
       ll g = extendedGCD(a, b, x, y);
16
       if (c % g != 0) return false;
17
18
       x *= c / g;
19
       y *= c / g;
20
21
       // Ajustamos las variables a/g y b/g para mover las soluciones
22
       a /= g;
23
       b /= g;
24
25
       if (x < x_min) {
26
           ll k = (x_min - x + b - 1) / b; // Redondeo hacia arriba
           x += k * b:
28
           v -= k * a;
       } else if (x > x_min) {
           11 k = (x - x_min) / b;
           x -= k * b;
           v += k * a;
33
       }
34
35
       if (y < y_min) {
36
           ll k = (y_min - y + a - 1) / a; // Redondeo hacia arriba
37
38
           y -= k * a;
39
       } else if (y > y_min) {
40
           11 k = (y - y_min) / a;
41
           x -= k * b:
42
43
           y += k * a;
       }
44
45
       return x >= x_min && y >= y_min;
46
47 }
                            8.2 Euler Totient
```

```
#include <bits/stdc++.h>
using namespace std;
```

```
3 typedef long long 11;
4
   vector<ll> compute_totients(ll n) {
       vector<ll> phi(n + 1);
       for (ll i = 0; i <= n; i++) {
8
           phi[i] = i;
9
       }
10
11
       for (ll i = 2; i <= n; i++) {
12
           if (phi[i] == i) { // i es primo
13
               for (ll j = i; j <= n; j += i) {
14
                    phi[j] = phi[j] * (i - 1) / i;
15
               }
16
           }
17
       }
18
19
       return phi;
20
21 }
```

8.3 Josephus

```
1 #include <iostream>
   using namespace std;
   typedef long long 11;
   ll josephus_iterative(ll n, ll k) {
6
       11 result = 0;
       for (ll i = 2; i <= n; ++i) {
8
           result = (result + k) % i;
9
10
       return result;
11
12
13
14
   ll josephus_recursive(ll n, ll k) {
15
16
       if (n == 1)
17
           return 0;
18
19
       return (josephus_recursive(n - 1, k) + k) % n;
20
21 | }
```

```
22
23
   11 josephus_power_of_2(11 n) {
24
25
       11 power = 1;
26
       while (power <= n) {</pre>
27
           power <<= 1;
28
29
       power >>= 1;
32
       return 2 * (n - power);
33
34 }
                               8.4 Mobius
#include <bits/stdc++.h>
   using namespace std;
   typedef long long 11;
   vector<ll> compute_mobius(ll n) {
       vector<ll> mu(n + 1, 1);
7
       vector<bool> is_prime(n + 1, true);
8
9
       for (ll i = 2; i <= n; i++) {
10
           if (is_prime[i]) { // i es un primo
11
               for (ll j = i; j <= n; j += i) {
12
                   mu[j] *= -1; // Multiplicamos por -1 para cada primo
13
                   is_prime[j] = false;
14
15
               for (ll j = i * i; j <= n; j += i * i) {
16
                    mu[j] = 0; // Si tiene un cuadrado de un primo, se pone
17
               }
18
           }
19
       }
20
21
22
       return mu;
   }
23
24
25
26 | 11 mobius(11 x) {
```

26

```
11 count = 0:
                                                                                               j ^= bit;
27
                                                                                   27
       for (ll i = 2; i * i <= x; i++) {
                                                                                   28
28
           if (x \% (i * i) == 0)
                                                                                               if (i < j)
                                                                                   29
29
               return 0;
                                                                                                   swap(a[i], a[j]);
30
                                                                                    30
           if (x \% i == 0) {
                                                                                           }
                                                                                   31
31
                count++;
32
                                                                                   32
                x /= i;
                                                                                           for (int len = 2; len <= n; len <<= 1) {
                                                                                   33
33
           }
                                                                                               int wlen = invert ? root_1 : root;
34
                                                                                    34
       }
                                                                                               for (int i = len; i < root_pw; i <<= 1)</pre>
35
                                                                                    35
                                                                                                    wlen = (int)(1LL * wlen * wlen % mod);
36
       if (x > 1) count++;
37
                                                                                   37
                                                                                               for (int i = 0; i < n; i += len) {
38
                                                                                    38
       return (count % 2 == 0) ? 1 : -1;
                                                                                                   int w = 1:
39
                                                                                    39
40 }
                                                                                                   for (int j = 0; j < len / 2; j++) {
                                                                                                        int u = a[i+j], v = (int)(1LL * a[i+j+len/2] * w % mod);
                                 8.5 NTT
                                                                                                        a[i+j] = u + v < mod ? u + v : u + v - mod;
                                                                                                        a[i+j+len/2] = u - v >= 0 ? u - v : u - v + mod;
                                                                                                        w = (int)(1LL * w * wlen % mod);
   #include <bits/stdc++.h>
                                                                                                   }
   using namespace std;
                                                                                    45
                                                                                               }
   using cd = complex<double>;
                                                                                           }
   typedef long long 11;
                                                                                    47
   const 11 mod = 998244353;
                                                                                           if (invert) {
   const 11 root = 31;
                                                                                    49
                                                                                               int n_1 = inverse(n, mod);
   const ll root_1 = inverse(root, mod);
                                                                                               for (auto & x : a)
   const ll root_pw = 1 << 23;</pre>
                                                                                   51
                                                                                                    x = (int)(1LL * x * n_1 \% mod);
                                                                                    52
9
                                                                                           }
   ll inverse(ll a, ll m) {
                                                                                    53
       11 \text{ res} = 1, \exp = m - 2;
                                                                                    54
11
       while (exp) {
                                                                                    55
12
                                                                                       vector<ll> multiply(vector<ll> const &a, vector<ll> const &b) {
           if (exp % 2 == 1) res = (1LL * res * a) % m;
13
                                                                                           vector<ll> fa(a.begin(), a.end()), fb(b.begin(), b.end());
           a = (1LL * a * a) % m;
                                                                                   57
14
                                                                                           11 n = 1;
                                                                                    58
           exp /= 2;
15
                                                                                           while (n < a.size() + b.size())</pre>
       }
16
                                                                                               n <<= 1:
                                                                                    60
       return res;
17
                                                                                           fa.resize(n);
18
                                                                                           fb.resize(n);
19
   void ntt(vector<ll> & a, bool invert) {
20
                                                                                           ntt(fa, false);
       int n = a.size():
21
                                                                                           ntt(fb, false);
22
                                                                                           for (ll i = 0; i < n; i++)
       for (int i = 1, j = 0; i < n; i++) {
23
                                                                                               fa[i] = (fa[i] * fb[i]) % mod;
           int bit = n \gg 1;
                                                                                   67
24
                                                                                           ntt(fa, true);
           for (; j & bit; bit >>= 1)
                                                                                   68
25
                j ^= bit;
                                                                                   69
```

```
vector<ll> result(n):
                                                                                        for (int i = 0; i < a.size(); i++) in[i] = C(fa[i], 0);
70
                                                                                 35
       for (ll i = 0; i < n; i++)
                                                                                         for (int i = 0; i < b.size(); i++) in[i].imag(fb[i]);</pre>
71
                                                                                 36
           result[i] = fa[i];
72
                                                                                 37
       return result;
                                                                                        fft(in);
73
                                                                                 38
74 }
                                                                                        for (C\& x : in) x *= x;
                                                                                        for (int i = 0; i < n; i++) out[i] = in[-i & (n - 1)] - conj(in[i]);
                                 8.6 FFT
                                                                                               // Corregido aqui
                                                                                        fft(out);
   typedef long long 11;
                                                                                         vll res(a.size() + b.size() - 1);
   typedef complex<double> C;
                                                                                        for (int i = 0; i < res.size(); i++) {</pre>
   typedef vector<double> vd;
                                                                                 44
                                                                                             res[i] = llround(imag(out[i]) / (4 * n));
   typedef vector<ll> vll;
                                                                                 45
                                                                                        }
   const double PI = acos(-1);
                                                                                 46
                                                                                        return res;
                                                                                 47
                                                                                 48 }
   void fft(vector<C>& a) {
       int n = a.size(), L = 31 - __builtin_clz(n);
8
                                                                                                                   8.7 Rho
       static vector<C> R(2, 1);
9
       static vector<C> rt(2, 1);
10
       for (static int k = 2; k < n; k *= 2) {
                                                                                  1 //RECOMENDADO USAR UNSIGNED LONG LONG
           R.resize(n); rt.resize(n);
                                                                                  static inline ll mulmod(ll a, ll b, ll m) {
           auto x = polar(1.0, PI / k);
                                                                                        return (ll)((__int128)a * b % m);
13
           for (int i = k; i < 2 * k; i++)
                                                                                    }
                                                                                  4
14
               rt[i] = R[i] = i & 1 ? R[i / 2] * x : R[i / 2];
15
                                                                                    static inline ll powmod(ll b, ll e, ll m) {
16
       vector<int> rev(n):
                                                                                        11 r = 1:
17
                                                                                  7
       for (int i = 0; i < n; i++) rev[i] = (rev[i / 2] | (i & 1) << L) /
                                                                                        while (e) {
                                                                                  8
18
           2;
                                                                                             if (e \& 1) r = mulmod(r, b, m);
                                                                                  9
       for (int i = 0; i < n; i++) if (i < rev[i]) swap(a[i], a[rev[i]]);
                                                                                             b = mulmod(b, b, m);
                                                                                 10
19
       for (int k = 1; k < n; k *= 2)
                                                                                             e >>= 1;
                                                                                 11
20
           for (int i = 0; i < n; i += 2 * k) for (int j = 0; j < k; j++) {
                                                                                        }
                                                                                 12
21
               auto x = (double*)&rt[j + k], y = (double*)&a[i + j + k];
                                                                                 13
                                                                                         return r;
22
               C z(x[0] * y[0] - x[1] * y[1], x[0] * y[1] + x[1] * y[0]);
                                                                                    }
                                                                                 14
23
               a[i + j + k] = a[i + j] - z;
                                                                                 15
^{24}
               a[i + j] += z;
                                                                                    // RNG rapido
25
           }
                                                                                    static inline ll splitmix64(ll x) {
26
                                                                                        x += 0x9e3779b97f4a7c15ULL;
27
                                                                                        x = (x ^ (x >> 30)) * 0xbf58476d1ce4e5b9ULL;
28
   vll multiply(const vll& a, const vll& b) {
                                                                                        x = (x ^ (x >> 27)) * 0x94d049bb133111ebULL;
29
       if (a.empty() || b.empty()) return {};
                                                                                        return x \hat{} (x >> 31);
                                                                                 21
30
                                                                                 22 }
       vd fa(a.begin(), a.end()), fb(b.begin(), b.end());
31
       int L = 32 - \_builtin\_clz(fa.size() + fb.size() - 1), n = 1 << L;
                                                                                 static ll rng_state = 0x1234567890abcdefULL ^ chrono::
32
       vector<C> in(n), out(n);
                                                                                         high_resolution_clock::now().time_since_epoch().count();
33
                                                                                 static inline ll rnd() { return splitmix64(rng_state += 0
34
```

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```
x9e3779b97f4a7c15ULL); }
                                                                                               if (witness(a)) return false;
                                                                                   64
                                                                                   65
25
   // trial division pequena para acelerar
                                                                                           return true;
                                                                                    66
   static const int SMALL_P_MAX = 1000;
                                                                                       }
                                                                                   67
   static vector<int> small_primes;
                                                                                    68
                                                                                       ll pollard_rho(ll n) {
29
   static void sieve_small() {
       vector<bool> is(SMALL_P_MAX + 1, true);
                                                                                           while (true) {
31
       is[0] = is[1] = false;
32
       for (int i = 2; i * i \le SMALL_P_MAX; ++i) if (is[i])
33
           for (int j = i * i; j <= SMALL_P_MAX; j += i) is[j] = false;</pre>
                                                                                               11 y = x;
34
                                                                                   74
       for (int i = 2; i <= SMALL_P_MAX; ++i) if (is[i]) small_primes.
                                                                                               11 d = 1;
35
                                                                                   75
           push_back(i);
                                                                                   76
36
37
       bool isPrime(ll n) {
38
       if (n < 2) return false;
39
       // divide por primos pequenos
40
       for (int p : small_primes) {
41
           if ((11)p * (11)p > n) break;
42
           if (n \% p == (11)0) return n == (11)p;
43
       }
                                                                                               return d;
44
       if (n < 4) return true; // 2,3
                                                                                           }
45
                                                                                    86
       // Miller-Rabin deterministico para 64-bit
                                                                                       }
                                                                                    87
46
       11 d = n - 1, s = 0;
47
       while ((d \& 1) == 0) d >>= 1, ++s;
48
       auto witness = [&](ll a) -> bool {
                                                                                           if (n == 1) return;
49
           if (a % n == 0) return false;
50
                                                                                   91
           11 x = powmod(a \% n, d, n);
51
           if (x == 1 \mid | x == n - 1) return false;
52
           for (int i = 1; i < s; ++i) {
                                                                                   94
53
                                                                                           }
               x = mulmod(x, x, n);
54
                                                                                   95
               if (x == n - 1) return false;
                                                                                           if (n == 1) return:
55
56
           return true; // es testigo: n compuesto
                                                                                           11 d = pollard_rho(n);
57
                                                                                           fact(d, F);
       };
58
       // Bases correctas para 64-bit
                                                                                           fact(n / d, F);
59
                                                                                   100
       for (11 a : {2ULL, 3ULL, 5ULL, 7ULL, 11ULL, 13ULL, 17ULL, 19ULL, 23
                                                                                   101 }
60
           ULL,
                     325ULL, 9375ULL, 28178ULL, 450775ULL, 9780504ULL,
61
                         1795265022ULL}) {
           if (a == 0) continue;
62
           if (a % n == 0) continue;
63
```

```
if ((n & 1ULL) == OULL) return 2ULL;
       ll c = (rnd() \% (n - 1)) + 1; // [1..n-1]
       11 x = (rnd() \% (n - 2)) + 2; // [2..n-1]
       // limite de iteraciones para evitar lazos raros
        for (int it = 0; it < 1'000'000 \&\& d == 1; ++it) {
            x = (mulmod(x, x, n) + c) \% n;
            y = (mulmod(y, y, n) + c) \% n;
           y = (mulmod(y, y, n) + c) \% n;
            ll diff = x > y ? x - y : y - x;
            d = std::gcd(diff, n);
        if (d == 1 || d == n) continue;
void fact(ll n, map<ll,int> &F) {
    if (isPrime(n)) { F[n]++; return; }
   for (int p : small_primes) {
       if ((11)p * (11)p > n) break;
        while (n \% p == 0) \{ F[p] ++; n /= p; \}
   if (isPrime(n)) { F[n]++; return; }
                           8.8 Simpson
```

```
| | ld simpsonRule(function<ld(ld)> f, ld a, ld b, int n) {
      // Asegurarse de que n sea par
```

```
if (n % 2 != 0) {
3
           n++;
4
       }
5
       1d h = (b - a) / n;
6
       1d s = f(a) + f(b);
8
       // Suma de terminos interiores con los factores apropiados
9
       for (int i = 1; i < n; i++) {
10
           1d x = a + i * h;
11
           s += (i \% 2 == 1 ? 4.0L : 2.0L) * f(x);
12
13
       // Multiplica por h/3
14
       return (h / 3.0L) * s;
15
16
   // Ejemplo: integrar la funcion x^2 entre 0 y 3
   auto f = [\&](ld x){return x * x;};
   1d a = 0.0L, b = 3.0L;
   int n = 1000; // numero de subintervalos
ld resultado = simpsonRule(f, a, b, n);
```

9 Geometry

9.1 Convex Hull

```
typedef pair<11, 11> Point;
  11 cross_product(Point 0, Point A, Point B) {
       return (A.first - O.first) * (B.second - O.second) - (A.second - O.
           second) * (B.first - O.first);
4
   vector<Point> convex_hull(vector<Point>& points) {
5
       sort(points.begin(), points.end());
6
       points.erase(unique(points.begin(), points.end()), points.end());
7
       vector<Point> hull:
8
       // Parte inferior
9
       for (const auto& p : points) {
10
           while (hull.size() >= 2 && cross_product(hull[hull.size() - 2],
11
               hull[hull.size() - 1], p) < 0)
               hull.pop_back();
12
           if (hull.empty() || hull.back() != p) {
13
               hull.push_back(p);
14
           }
15
       }
16
       // Parte superior
17
```

```
int t = hull.size() + 1:
18
       for (int i = points.size() - 1; i >= 0; --i) {
19
           while (hull.size() >= t && cross_product(hull[hull.size() - 2],
20
               hull[hull.size() - 1], points[i]) < 0)</pre>
               hull.pop_back();
21
           if (hull.empty() || hull.back() != points[i]) {
22
               hull.push_back(points[i]);
23
           }
24
       }
25
       hull.pop_back();
26
       return hull;
27
28 }
                             9.2 Operations
1 | 11 cross_product(pair<11, 11> P1, pair<11, 11> P2, pair<11, 11> P3) {
       ll x1 = P2.first - P1.first:
       11 y1 = P2.second - P1.second;
       11 \times 2 = P3.first - P1.first;
       11 y2 = P3.second - P1.second;
5
       return x1 * y2 - y1 * x2;
6
   }
7
   double distancia(pair<11, 11> P1, pair<11, 11> P2) {
       return sqrt((P2.first - P1.first) * (P2.first - P1.first) +
                    (P2.second - P1.second) * (P2.second - P1.second));
10
11
   11 dot_product(pair<11, 11> P1, pair<11, 11> P2, pair<11, 11> P3) {
12
       11 x1 = P2.first - P1.first;
13
       11 v1 = P2.second - P1.second;
14
       11 \times 2 = P3.first - P1.first;
15
       11 y2 = P3.second - P1.second;
       return x1 * x2 + y1 * y2;
17
18 }
                           9.3 Polygon Area
typedef pair<11, 11> Point;
   double polygon_area(const vector<Point>& polygon) {
       ll area = 0:
3
       int n = polygon.size();
4
       for (int i = 0; i < n; ++i) {
5
           11 j = (i + 1) \% n;
6
           area += (polygon[i].first * polygon[j].second - polygon[i].
7
```

second * polygon[j].first);

```
}
       return abs(area) / 2.0;
10 }
                           9.4 Ray Casting
  typedef pair<11, 11> Point;
  |bool is_point_in_polygon(const vector<Point>& polygon, Point p) {
       bool inside = false;
3
       int n = polygon.size();
      for (int i = 0, j = n - 1; i < n; j = i++) {
5
          if ((polygon[i].second > p.second) != (polygon[j].second > p.
               second) &&
               p.first < (polygon[j].first - polygon[i].first) * (p.second</pre>
7
                   - polygon[i].second) /
                         (polygon[j].second - polygon[i].second) + polygon[
                             i].first) {
               inside = !inside;
9
          }
10
       }
11
      return inside;
12
13 }
```