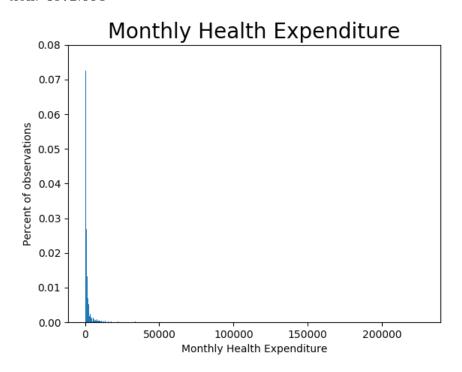
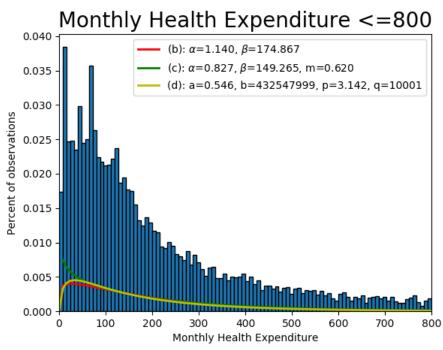
Problem Set 2

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Problem 1

(a) Mean: 720.278, Median: 172.210, Max: 227967.25, Min:0.01, Standard Deviation: 3972.664





The second histogram is preferred because the mean is around 720 and most of the data are concentrated below mean. In addition, it takes away outliers such as 227967.

- (b) $\hat{\alpha} = 1.13976691235, \hat{\beta} = 174.866836155, lnL = -56732.5986796$ The estimated gamma distribution is depicted in the graph above with the red line.
- (c) $\hat{\alpha} = 0.826528658566$, $\hat{\beta} = 149.264584308$, $\hat{m} = 0.618997875459$, lnL = -56732.5986796 The estimated generalized gamma distribution is depicted in the graph above with the green line.
- (d) $\hat{a} = 0.545045409007$, $\hat{b} = 432528268.017$, $\hat{p} = 3.16725263428$, $\hat{q} = 9999.89896562$, lnL = -56800.0038081

The estimated generalized beta 2 distribution is depicted in the graph above with the yellow line.

- (e) p-value with the gamma distribution: 1.0 p-value with the generalized gamma distribution: 1.0
- (f) Using the generalized beta 2 distribution, the probability that one has a monthly health care claim for more than \$1,000 is 0.01182126643710546. With the gamma distribution, it is 0.00457132368760782.

Please see the attached Jupyter Notebook for the detail and codes used. I suppose that my calculation for the generalized gamma distribution is wrong, because it provided the weird estimated line.