

# Exercise Session – Gradient Descent

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# Goal

Provide the implementation of **gradient descent** algorithm for **polynomial functions**

$$f : \mathbb{R} \rightarrow \mathbb{R}$$

$$f(x) = a_0 + a_1x + a_2x^2 + \dots + a_nx^n = \sum_{k=0}^n a_kx^k$$

# Gradient Descent algorithm

- Find the minimum of  $f$  in a given interval  $[\inf, \sup]$
- Start from a given initial point  $x_0$
- Next candidate:

$$x_i = x_{i-1} - \delta f'(x_{i-1})$$

where  $\delta$  is a given constant

# Required methods

- `solve`, that finds the minimum of  $f$  in  $[\inf, \sup]$
- `solve_multistart`, that randomly picks an initial point in  $[\inf, \sup]$  at each iteration
- `solve_domain_decomposition`, that performs multistart after having split  $[\inf, \sup]$  in a given number of subintervals