

### Problem 3

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#### RSA encryption scheme

**Given:**

Public key( $n, e$ ) = (15151, 17)

Ciphertext =  $y = 832$

- **Find the prime factorization of  $n$**

$$n = 15151 = p * q = 109 * 139$$

The prime factorizations are  $p = 109$  and  $q = 139$

- **Compute  $\phi(n)$**

$$\phi(n) = (p-1)(q-1) = 108 * 138 = \underline{14904}$$

- **Finding the private key  $d$**

Know that  $e = 17$

To find  $d$ , we use the formula:

$$e^{-1} \bmod (\phi(n))$$

$$d = 17^{-1} \bmod 14904 = \underline{6137}$$

- **Decrypting ciphertext  $y$**

You get a plaintext by decrypting the ciphertext

$$\text{plaintext} = y^d \bmod n$$

$$832^{6137} \bmod 15151 = \underline{1781}$$