

# Oxford IB Physics Course Companion

Unofficial student made suggested solutions

By Noël M. Nimstad

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# 1 Topic A – Space, time and motion

## 1.1 Subtopic A.1 – Kinematics

### A1:P11 Question 1

a) The total distance is given as the sum of distance traveled during each translation,  $2.5 + 3.8 = 6.3$  [km]

b) Displacement is a vector quantity, thus taking the magnitude of the sum of the two vector displacements caused by the movement:

$$\begin{aligned}\left\| \begin{pmatrix} 2.5 \\ 0 \end{pmatrix} + \begin{pmatrix} 0 \\ 3.8 \end{pmatrix} \right\| &= \left\| \begin{pmatrix} 2.5 \\ 3.8 \end{pmatrix} \right\| \\ &= \sqrt{2.5^2 + 3.8^2} \approx 4.55 \text{ [km]}\end{aligned}$$

c) Since this scenario can be set up as a right angle triangle, with the boat as the hypothesis' outer vertex, using trigonometry the angle can be determined as:

$$\tan \theta = \frac{o}{a} \rightsquigarrow \theta = \tan^{-1} \frac{2.5}{3.8} \approx 33.3^\circ$$

### A1:P11 Question 2

a) 15 minutes corresponds to a 90 degree ( $\frac{\pi}{2}$  [rad]) rotation on a clock, or one quarter of its perimeter.

Therefore the distance travelled by the tip of the pointer must be:

$$s = \frac{2\pi r}{4} = \frac{15\pi}{2} \approx 23.6 \text{ [cm]}$$

The displacement however is the distance between the points  $\langle 0, 15 \rangle$  and  $\langle 15, 0 \rangle$ , thus using Pythagoras' theorem<sup>a</sup>:

$$s = \sqrt{15^2 + 15^2} = \sqrt{450} = 21.2 \text{ [cm]}$$

b) Analogously to part a) but for the 180 degrees ( $\pi$  [rad]) rotation resulting from 30 elapsed minutes:

$$s_{\text{distance}} = \frac{2\pi r}{2} = 15\pi \approx 47.1 \text{ [cm]}$$

$$s_{\text{displacement}} = \sqrt{0^2 + 30^2} = 30 \text{ [cm]}$$

### A1:P12 Question 3

Since they are headed in completely opposite directions,  $s_{\text{Ada}} + s_{\text{Matt}} = 580$  [m]. Ada's speed of  $20 \text{ [km h}^{-1}]$

is approximately  $5.56 \text{ [m s}^{-1}\text{]}$ , as found by dividing through by 3.6. Since  $s = \int v dt$ :

$$v_{\text{Ada}}t + v_{\text{Matt}}t = 580$$

$$5.56 \times 60 + v_{\text{Matt}} \times 60 = 580$$

$$\therefore v_{\text{Matt}} \approx 4.11 \text{ [m s}^{-1}\text{]} \equiv \boxed{14.8 \text{ [km h}^{-1}\text{]}}$$

### A1:P12 Question 4

First multiply the speed of light by the length of a light-year in seconds to obtain 1 [ly].

$$\begin{aligned} 1 \text{ [ly]} &= 3 \times 10^8 \text{ [m s}^{-1}\text{]} \times (60 \times 60 \times 24 \times 365) \text{ [s]} \\ &\approx 9.46 \times 10^{15} \end{aligned}$$

Then, find the conversion between 1 [au] and one light-year.

$$1 \text{ [au]} \approx \frac{1.5 \times 10^{11}}{9.46 \times 10^{15}} = 1.59 \times 10^{-5} \text{ [ly]}$$

Therefore,

$$5.5 \times 10^5 \text{ [au]} \approx \boxed{8.72 \text{ [ly]}}$$

### A1:P14 Question 5

a) Calculating the speed between stations A and B:

$$v = \frac{1000}{80} = 12.5 \text{ [m s}^{-1}\text{]}$$

Multiplying by 3.6 to obtain the speed in  $\text{[km h}^{-1}\text{]}$ :

$$v = 12.5 \times 3.6 = \boxed{45 \text{ [km h}^{-1}\text{]}}$$

b)  $\Delta y = 1800 - 1000 = 800 \text{ [m]}$

c) The train travels 800 [m] in 60 seconds, therefore, analogously to part a):

$$v = \frac{800}{60} \approx 13.3 \text{ [m s}^{-1}\text{]} = \boxed{47.9 \text{ [km h}^{-1}\text{]}}$$

### A1:P14 Question 6

a) i)

$$\frac{4 \text{ [m]}}{10 \text{ [m s}^{-1}\text{]}} = \boxed{0.4 \text{ [s]}}$$

ii) The ball traveled for a total of 0.9 [s]. If then, it took 0.4 [s] to the wall, then it took  $0.9 - 0.4 = 0.5 \text{ [s]}$ .

The speed needed to travel 4 [m] in 0.5 [s] is:

$$\frac{4 \text{ [m]}}{0.5 \text{ [s]}} = \boxed{8 \text{ [m s}^{-1}\text{]}}$$

b)

Note that graph question solutions are not yet done due to lack of time.

**A1:P16 Question 7**

a) i) Imagining a straight line tangent to the curve (since  $v = \frac{ds}{dt}$ ), it goes roughly 6 [m] in 1 [s], therefore the velocity is  $\boxed{6 \text{ [m s}^{-1}\text{]}}$

ii) The tangent line at  $t = 5 \text{ [s]}$  goes approximately from  $\langle 2.5, 12.5 \rangle$  to  $\langle 10, 28 \rangle$ , thus

$$\Delta s = 28 - 12.5 = 15.5 \text{ [m]}$$

$$\Delta t = 10 - 2.5 = 7.5 \text{ [s]}$$

Therefore:

$$v = \frac{\Delta s}{\Delta t} = \frac{15.5}{7.5} \approx \boxed{2 \text{ [m s}^{-1}\text{]}}$$

b)

$$v = \frac{\Delta s}{\Delta t} = \frac{24}{12.5} = \boxed{1.92 \text{ [m s}^{-1}\text{]}}$$

**A1:P16 Question 8**

a) The perimeter of the track is  $s = \frac{2\pi r}{2} = 25\pi \text{ [m]}$ . Therefore, the average speed is:

$$v = \frac{25\pi}{19} \approx \boxed{4.13 \text{ [m s}^{-1}\text{]}}$$

b) For the velocity, we need the magnitude of the displacement which is 50 [m] since he went from one side of the circle to the other, one length of the diameter ( $2r$ ). Therefore, the average velocity is:

$$v = \frac{50}{19} \approx \boxed{2.63 \text{ [m s}^{-1}\text{]}}$$

**A1:P21 Question 9**

Since  $s = \int v dt$ , the sum of the squares under the graph is the distance travelled. Estimating using triangles ( $A = \frac{bh}{2}$ ):

$$\begin{aligned} s &= \frac{4 \times 1}{2} + \frac{2 \times 1}{2} + \frac{2 \times 3}{2} + 11 \\ &= 2 + 1 + 3 + 11 = 17 \text{ [m]} \end{aligned}$$

The triangles in this case underestimate the area, so rounding up we get 20 [m], making the answer  $\boxed{B}$ .

**A1:P21 Question 10**

The tangent line (since  $a = \frac{dv}{dt}$ ) goes from roughly  $\langle 0, 4 \rangle$  to  $\langle 4, 8 \rangle$ , thus:

$$\Delta v = 8 - 4 = 4$$

$$\Delta t = 4 - 0 = 4$$

$$a = \frac{\Delta v}{\Delta t} = \frac{4}{4} = 1 \text{ [m s}^{-1}\text{]}$$

Therefore the answer is A.

**A1:P21 Question 11**

At  $t = 4$  [s], the max speed has been reached. Since the object was accelerated previously, the average speed is below the max line, thus the answer is either A or C. The tangent line (since  $a = \frac{dv}{dt}$ ) at this point, however, is flat, meaning  $a_{\text{instant}} = 0$ . Thus the answer is A.

**A1:P21 Question 12**

If the velocity magnitude of the velocity is negative then it is moving in one direction, and if it is positive, then it moves in the oposite direction. Therefore, each time the velocity changes sign, the object is changing direction. The velocity changes sign twice, meaning the answer is B.

**A1:P22 Question 13**

**a)** Considering the absolute value of the graph, the velocity is first decreasing between  $t = 0$  [s] and  $1.5$  [s] and then increasing between  $t = 1.5$  [s] and  $2.5$  [s]. What happens however at  $t = 1.5$  [s] is that, with the change of sign (vide **A1:21 Question 12**), is that the direction of travel changes.

**b) i)** The velocity decreases along a straight line, meaning acceleration is constant. Calculating the slope of the line between 2 nice points:

$$a = \frac{\Delta v}{\Delta t} = \frac{-2}{1.5} \approx \boxed{-1.33 \text{ [m s}^{-2}\text{]}}$$

**ii)** The positive and negatibe parts between  $t = 0.5$  [s] and  $2.5$  [s] will cancel out, thus we only need to compute the area under the curve (since  $s = \int v dt$ ) between  $t = 0$  [s] and  $0.5$  [s]. To compute this we need to know the coordinates of the point  $\langle 0.5, ? \rangle$ . Since we know  $a \approx -1.33 \text{ [m s}^{-2}\text{]}$ , we can compute:

$$v_{0.5} \approx v_0 - 1.33 \times 0.5$$

$$= 1.335 \text{ [m s}^{-1}\text{]}$$

Therefore summing the rectangle and triangle below the curve:

$$s = 0.5 \times 1.335 + \frac{(2 - 1.335) \times 0.5}{2} \approx \boxed{0.834 \text{ [m]}}$$

c)

Note that graph question solutions are not yet done due to lack of time.

### A1:P25 Question 14

a) Note that if the cart is returning to its origin, then the distance travelled  $s$  is 0. Using  $s = ut + \frac{1}{2}at^2$ :

$$\begin{aligned} 0 &= ut + \frac{1}{2}at^2 \\ &= 3t - 0.5 \times 1.8t^2 \\ \implies 0.9t^2 &= 3t \end{aligned}$$

Dividing by  $t$  discards the solution of  $t = 0$  (since division by 0 is not mathematically allowed), however this solution is trivial (when the cart begins travelling it is at its origin):

$$\begin{aligned} 0.9t &= 3 \\ \therefore t &= \frac{3}{0.9} \approx [3.33 \text{ s}] \end{aligned}$$

b) When the velocity  $v$  is 0 the distance is maximum, since after the velocity changes sign (by passing zero), the object starts moving in the opposite direction. Using  $v^2 = u^2 + 2as$ :

$$\begin{aligned} 0 &= 3^2 - 2 \times 1.8s \\ \implies s &= \frac{9}{3.6} = [2.5 \text{ m}] \end{aligned}$$

### A1:P25 Question 15

a) Converting  $100 \text{ km h}^{-1}$  to  $\text{m s}^{-1}$  by dividing by 3.6 means:

$$v = \frac{100}{3.6}$$

Then using  $v = u + at$ :

$$\begin{aligned} \frac{100}{3.6} &= 0 + 16a \\ \implies a &= \frac{100}{3.6 \times 16} \approx [1.74 \text{ ms}^{-2}] \end{aligned}$$

b) Converting  $250 \text{ km h}^{-1}$  to  $\text{m s}^{-1}$  by dividing by 3.6 means:

$$v = \frac{250}{3.6}$$

Using  $v^2 = u^2 + 2as$  and the acceleration from a) we derive:

$$\begin{aligned}\frac{250^2}{3.6^2} &= 0 + 2 \times \frac{100}{57.6} s \\ \implies s &= \frac{250^2 \times 57.6}{200 \times 3.6^2} \approx [1400 \text{ [m]}]\end{aligned}$$

### A1:P25 Question 16

Using  $v^2 = u^2 + 2as$ :

$$\begin{aligned}12^2 &= u^2 + 2 \times (-4.3) \times 25 \\ \implies u &= \sqrt{12^2 + 8.6 \times 25} \approx [18.9 \text{ [m s}^{-1}]\boxed{\text{]}}\end{aligned}$$

### A1:P25 Question 17

a) To reach maximum velocity and be able to stop in time, the train must accelerate the first half of the distance and then immediately start de-accelerating. Therefore  $s = 360$ . Then using  $v^2 = u^2 + 2as$ :

$$\begin{aligned}v^2 &= 0 + 2 \times 1.3 \times 360 \\ \implies v &= \sqrt{720 \times 1.3} \approx [30.6 \text{ [m s}^{-1}]\boxed{\text{]}}\end{aligned}$$

b) The time is minimised if the velocity is maximised. Since the travel is symmetrical, considering the first half ( $s = 360$ ) with maximum acceleration and using  $s = ut + \frac{1}{2}at^2$ :

$$\begin{aligned}360 &= 0 + \frac{1}{2} \times 1.3 \times t^2 \\ \implies t &= \sqrt{\frac{720}{1.3}}\end{aligned}$$

Since this was only half the distance, the total minimum travel time is  $2t$ :

$$2t = 2\sqrt{\frac{720}{1.3}} \approx [47.1 \text{ [s]}\boxed{\text{]}}$$

### A1:P25 Question 18

a) Since we know the distance, initial velocity (0), and time, we can derive the acceleration through the SUVAT equation  $s = ut + \frac{1}{2}at^2$ :

$$\begin{aligned}12 &= 0 + 0.5a \times 4^2 \\ \implies a &= \frac{12}{0.5 \times 4^2} = \frac{12}{8} = 1.5 \text{ [m s}^{-2}]\end{aligned}$$

Then using  $v = u + at$  we find the velocity at  $t = 2$  is:

$$v = 0 + 1.5 \times 2 = 3 \text{ [m s}^{-1}\text{]}$$

The answer matching this is D.

b)

Note that graph question solutions are not yet done due to lack of time.

#### A1:P34 Question 19

If both projectiles reach the same height, that means that the vertical component of the initial velocity was the same, since:

$$\begin{aligned} u_{1y}t - \frac{1}{2}gt^2 &= \max y = u_{2y}t - \frac{1}{2}gt^2 \\ \implies u_{1y} &= u_{2y} \end{aligned}$$

If the vertical component of the initial velocity is the same, then the time taken to reach the ground is the same. This is because both are experiencing the same gravitational pull. Thus the answer is B.

#### A1:P34 Question 20

The horizontal distance travelled is proportional to the height  $s \propto h$  since the time taken to hit the ground is proportional to the height  $t_{\text{final}} \propto h$ . The time taken to hit the ground  $s_y = -h$ , with 0 initial vertical velocity, can be computed as:

$$\begin{aligned} -h &= 0 - \frac{1}{2}gt_{\text{final}}^2 \\ \implies t_{\text{final}} &= \sqrt{\frac{2h}{g}} \end{aligned}$$

Note that the negative solution was discarded as it is physically impossible. Thus we derive that:

$$t_{\text{final}} \propto \sqrt{h}$$

Then, we compute that horizontal distance travelled (with initial horizontal velocity  $u$ , with no or negligible air resistance) as:

$$s = ut + 0$$

Therefore, the final distance travelled is  $s$  evaluated at  $t_{\text{final}}$ , meaning:

$$s \propto \sqrt{h}$$

Thus to reach a distance of  $2s$ , we need a height of  $4h$ , since  $\sqrt{4h} = 2\sqrt{h}$ . This means the answer is D.

**A1:P34 Question 21**

Using  $s = ut + \frac{1}{2}at^2$ :

$$\begin{aligned}s &= -4t - \frac{1}{2}gt^2 \\ &= -4 \times 1.9 - \frac{g}{2}(1.9)^2 \approx -25.3 \text{ [m]}\end{aligned}$$

This is the displacement of the object over that time, so the tower's height is  $h = -s = 25.3$  [m]. The closest answer is therefore **D**.

**A1:P34 Question 22**

The time to hit the floor is given by, as derived in **A1:P34 Question 20**:

$$t_{\text{final}} = \sqrt{\frac{2h}{g}}$$

The horizontal displacement is then given through  $s = ut + \frac{1}{2}at^2$  (noting air resistance is negligible, providing 0 acceleration):

$$\begin{aligned}s &= vt_{\text{final}} \\ &= v \sqrt{\frac{2h}{g}}\end{aligned}$$

The answer is therefore **C**.

**A1:P34 Question 23**

**a)** The maximum height is reached when the vertical velocity is 0, since the changing of a sign changes the direction of motion, making the height of the ball strictly decrease post that point. Therefore, using  $v = u + at$ :

$$\begin{aligned}0 &= u_y - gt_{\text{max}} \\ u_y &= gt_{\text{max}} = 0.9g \approx 8.84 \text{ [m s}^{-1}\text{]}\end{aligned}$$

**b)** Noting there is no air resistance, the horizontal velocity can be computed using  $s = ut + \frac{1}{2}at^2$  as:

$$\begin{aligned}16 &= 0.9u_x + 0 \\ \implies u_x &= \frac{16}{0.9} \approx 17.8 \text{ [m s}^{-1}\text{]}\end{aligned}$$

Using Pythagoras theorem, we get that the total initial velocity is:

$$u = \sqrt{u_x^2 + u_y^2} = \sqrt{17.8^2 + 8.84^2} \approx 19.9 \text{ [m s}^{-1}\text{]}$$

c) Solving the equation  $u \sin \theta = u_y$  (or  $u \cos \theta = u_x$ ) gives:

$$\begin{aligned}\sin \theta &\approx \frac{8.84}{19.9} \\ \implies \theta &\approx \sin^{-1} \frac{8.84}{19.9} \approx 0.4603 \dots \text{ [rad]}\end{aligned}$$

Converting to degrees (using  $\theta_{\text{deg}} = \frac{180\theta_{\text{rad}}}{\pi}$ ):

$$\theta \approx \boxed{26.4^\circ}$$

d) Using  $s = ut + \frac{1}{2}at^2$ :

$$\begin{aligned}\max h &= u_y t_{\max} - \frac{1}{2}gt_{\max}^2 \\ &= 8.84 \times 0.9 - \frac{g}{2}0.9^2 \approx \boxed{3.98 \text{ [m]}}\end{aligned}$$

#### A1:P34 Question 24

Since there is 0 initial vertical velocity, the time to reach the net is (using  $s = ut + \frac{1}{2}at^2$ ):

$$\begin{aligned}0.9 - 2.7 &= 0 - \frac{1}{2}gt_{\text{final}}^2 \\ \implies t_{\text{final}} &= \sqrt{\frac{2 \times 1.8}{g}} \quad (\text{Negative solution not possible}) \\ &\approx 0.605 \text{ [s]}\end{aligned}$$

Then to derive the initial horizontal velocity (with assumed 0 acceleration), we use  $s = ut + \frac{1}{2}at^2$  again:

$$\begin{aligned}12 &= u_x t_{\text{final}} + 0 \\ \implies u_x &\approx \frac{12}{0.605} \approx \boxed{19.8 \text{ [m s}^{-1}\text{]}}\end{aligned}$$

#### A1:P34 Question 25

a) The initial vertical velocity  $u \sin \theta$  is approximately  $0.628 \text{ [m s}^{-1}\text{]}$ . Then using  $s = ut + \frac{1}{2}at^2$  and checking for approximate equality at  $t = 0.3 \text{ [s]}$ :

$$\begin{aligned}-0.25 &\approx 0.628 \times 0.3 - \frac{1}{2}g(0.3)^2 \\ -0.25 &\approx -0.2535 \quad \checkmark\end{aligned}$$

b) i) The initial horizontal velocity  $u \cos \theta$  is approximately  $8.98 \text{ [m s}^{-1}\text{]}$ . Using  $s = ut + \frac{1}{2}at^2$  with assumed 0 acceleration:

$$s \approx 8.98 \times 0.3 + 0 = \boxed{2.69 \text{ [m]}}$$

ii) Only the vertical velocity is changing (due to the assumed 0 horizontal acceleration). Therefore, using

$v = u + at$ :

$$v_{\text{final}} \approx 0.628 - 0.3g = -2.32 \text{ [m s}^{-1}\text{]}$$

Then using Pythagoras theorem to calculate the total final velocity:

$$v = \sqrt{v_x^2 + v_y^2} = \sqrt{8.98^2 + (-2.32)^2} \approx \boxed{9.27 \text{ [m s}^{-1}\text{]}}$$

c) i)

Note that graph question solutions are not yet done due to lack of time.

ii)

Note that graph question solutions are not yet done due to lack of time.

## 1.2 Subtopic A.2 – Forces and momentum

### A2:P46 Question 1

Disregarding the initial moment, in which force is applied to propell the object, the only force acting on the object is gravity pull. Gravitational pull is always directed downwards, meaning the answer is D.

Note that what is 0 isn't the force, but the velocity (since the sign is changing).

### A2:P46 Question 2

Ignore all vertical movement. Using  $v^2 = u^2 + 2as$  (with  $v = 0$  since the pellet comes to rest):

$$\begin{aligned} 0 &= 200^2 + 2a \times 0.1 \\ \implies a &= -\frac{40000}{0.2} = -200000 \text{ [m s}^{-2}\text{]} \end{aligned}$$

Then using Newton's second law ( $F \stackrel{\text{N2}}{=} ma$ ), and only considering the magnitude (ignoring the – sign):

$$F = 0.002 \times 200000 = 400 \text{ [N]}$$

Thus, the answer is C.

### A2:P47 Question 3

The average acceleration is computed using  $v = u + at$  as:

$$\begin{aligned} 15 &= 0 + 0.01a \\ \implies a &= \frac{15}{0.01} = 1500 \text{ [m s}^{-2}\text{]} \end{aligned}$$

Then using Newton's second law ( $F \stackrel{N2}{=} ma$ ):

$$F = 0.058 \times 1500 = \boxed{87 \text{ [N]}}$$

#### A2:P47 Question 4

a) First convert the speed units to  $[\text{m s}^{-1}]$  by dividing through by 3.6:

$$\begin{cases} v = 12.5 \text{ [m s}^{-1}] \\ u = 22.2 \text{ [m s}^{-1}] \end{cases}$$

Then using  $v^2 = u^2 + 2as$ :

$$\begin{aligned} 12.5^2 &= 22.2^2 + 36a \\ \implies a &= \frac{12.5^2 - 22.2^2}{36} \approx -9.35 \text{ [m s}^{-2}] \end{aligned}$$

Therefore, the average force (only considering magnitude) must be:

$$F \stackrel{N2}{=} ma \approx 1200 \times 9.35 \approx \boxed{11220 \text{ [N]}}$$

b) Using  $v = u + at$ :

$$\begin{aligned} 12.5 &\approx 22.2 - 9.35t \\ \implies t &\approx \frac{12.5 - 22.2}{-9.35} \approx \boxed{1.04 \text{ [s]}} \end{aligned}$$

#### A2:P47 Question 5

a) Noting that Newton's second law states  $F \stackrel{N2}{=} ma$ , we see that:

$$a = \frac{F}{m} = \frac{400}{11000} = \frac{2}{55} \text{ [m s}^{-2}]$$

Then using  $v = u + at$  (and noting that since it was stationary at  $t = 0, u = 0$ ):

$$v = 0 + \frac{2}{55} \times 8 \approx \boxed{0.291 \text{ [m s}^{-1}]}$$

b) Using  $s = ut + \frac{1}{2}at^2$ :

$$\begin{aligned} s &= 0 + \frac{1}{2} \frac{2}{55} \times 8^2 \\ &= \frac{64}{55} \approx \boxed{1.16 \text{ [m]}} \end{aligned}$$

#### A2:P47 Question 6

**a)** The force acting on the electron is only acting along the vertical. Thus, if there is no force acting horizontally, then there is no acceleration horizontally. Without acceleration, the velocity remains constant (Newton's first law).

**b) i)** The time taken for the electron to travel the 25 [cm] is given by:

$$t = \frac{0.25 \text{ [m]}}{8 \times 10^6 \text{ [m s}^{-1}\text{]}} = 3.125 \times 10^{-8}$$

We then calculate the acceleration acting on the electron using Newton's second law:

$$a \stackrel{\text{N2}}{=} \frac{F}{m} = \frac{6.4 \times 10^{-17}}{9.11 \times 10^{-31}} = \frac{6.4}{9.11} \times 10^{14} \text{ [m s}^{-2}\text{]}$$

Finally using  $s = ut + \frac{1}{2}at^2$ :

$$\begin{aligned} s &= 0 + \frac{1}{2} \frac{6.4}{9.11} \times 10^{14} \times (3.125 \times 10^{-8})^2 \\ &\approx \boxed{3.43 \text{ [cm]}} \end{aligned}$$

**ii)** Using  $v = u + at$  we get a vertical velocity of:

$$\begin{aligned} v_y &= 0 + \frac{6.4}{9.11} \times 10^{14} \times 3.125 \times 10^{-8} \\ &\approx 2.2 \times 10^6 \text{ [m s}^{-1}\text{]} \end{aligned}$$

Then using  $\tan \theta = \frac{v_y}{v_x}$  ( $v_x$  is the velocity stated in the question):

$$\theta = \tan^{-1} \frac{2.2 \times 10^6}{8 \times 10^6} \approx \boxed{15.4^\circ}$$

### A2:P47 Question 7

**a)**

Note that graph question solutions are not yet done due to lack of time.

If there is no acceleration, then no force other than gravity is acting on the person. Thus the scale, measuring force, will show just the weight force:

$$F_g \stackrel{\text{N2}}{=} mg = 75 \times 9.82 \approx \boxed{737 \text{ [N]}}$$

**b)**

Note that graph question solutions are not yet done due to lack of time.

The force driving the elevator upwards will push against the person in the elevator. By Newton's third

law, the person will then experience an equal force, but in the opposite direction. Since the force on the elevator acts upwards, the force on the person acts downwards with an acceleration of  $2 \text{ [m s}^{-2}\text{]}$ .

The magnitude of the force acting downwards on the person is given as:

$$F_{\downarrow} \stackrel{\text{N2}}{=} ma = 75 \times 2 = 150 \text{ [N]}$$

Therefore the magnitude of the resultant force  $F_R$  is given as ( $F_g$  was computed in a)):

$$F_R = F_g + F_{\downarrow} \approx 737 + 150 = \boxed{887 \text{ [N]}}$$

### A2:P54 Question 8

a) Let the force of tension in each string be denoted  $F_t$ . Combined, the vertical component of both string's tension ( $F_t \sin \theta$ ) force,  $2F_t \sin \theta$ , must balance the weight force of the object,  $F_g$ . The weight force of the object is given as:

$$F_g \stackrel{\text{N2}}{=} mg = 2g \approx 19.6 \text{ [N]}$$

Then to derive the angle  $\theta$ , splitting the  $150^\circ$  in to two gives  $75^\circ$ . Then, in consideration of the right angle triangle on the side towards the weight, we get the angle  $\theta = 90 - 75 = 15^\circ$ . Finally, we solve the equation:

$$\begin{aligned} 2F_t \sin 15^\circ &= F_g \\ F_t &= \frac{19.6}{2 \sin 15^\circ} \approx \boxed{37.9 \text{ [N]}} \end{aligned}$$

b) The threads can only support a certain amount of tension. As the angle (let this be called  $\phi$ ) between the strings increases, the angle  $\theta$  decreases. This is because (as demonstrated in a)):

$$\theta = 90 - \frac{\phi}{2}$$

The equation for the force of tension is proportional to (as demonstrated in a)):

$$\begin{aligned} F_t &\propto \frac{1}{\sin \theta} = \frac{1}{\sin 90 - \frac{\phi}{2}} \\ &= \frac{1}{\cos \frac{\phi}{2}} \\ \therefore F_t &\propto \frac{1}{\cos \phi} \end{aligned}$$

As  $\phi$  increases towards  $180^\circ$ ,  $\cos \phi$  increases as well, meaning the force of tension, too, increases. Thus by increasing the angle, the threads are more likely to break.

### A2:P54 Question 9

a)

Note that graph question solutions are not yet done due to lack of time.

b) The tension in each string has to support the weight force pulling on it. For the upper string, both A ( $m_A = M$ ) and B ( $m_B = 2M$ ) pull on it. Therefore:

$$\begin{aligned} F_{t\text{up}} &= F_{gA} + F_{gB} \\ &\stackrel{\text{N2}}{=} Mg + 2Mg = \boxed{3Mg} \end{aligned}$$

For the second string, only the weight of B is pulling on it, thus:

$$F_{t\text{down}} = F_{gB} = \boxed{2Mg}$$

### A2:P54 Question 10

a) i) To form a  $40^\circ$  angle, the angle formed between the bob, the vertical and the end point of F if placed at the end of the weight force must be  $40^\circ$ . We therefore solve the equation:

$$\begin{aligned} \tan 40^\circ &= \frac{F}{0.5} \\ \implies F &\approx 0.839 \times 0.5 \approx \boxed{0.420 \text{ [N]}} \end{aligned}$$

ii) To stay in equilibrium and not break, the magnitude of the tension force in the string must be equal to the magnitude of the resultant. We thus calculate the magnitude of the resultant, using Pythagoras' theorem, as:

$$F_R \approx \sqrt{0.5^2 + 0.420^2} = \boxed{0.653 \text{ [N]}}$$

b) Since the forces remain unchanged, but there is no tension to hold them back anymore, the bob starts accelerating along the resultant. It thus moves away from the wall at the same direction the equilibrium was in ( $40^\circ$  away from the negative vertical).

### A2:P59 Question 11

When a spring is cut in half, the spring constant doubles, thus  $k' = 2k$ . Then, when placed in parallel, the total spring constant is the sum of the individual spring constants, thus:

$$k_{\text{total}} = k' + k' = 4k$$

Using Hooke's law, we know that since the object is in equilibrium:

$$\begin{aligned} F_g &\stackrel{\text{N2}}{=} mg = F_h = -kL \\ \implies mg &= -kL \end{aligned}$$

Applying the new total spring constant:

$$mg = -k'L' = -4kL'$$

Since both equations equal  $mg$ :

$$\begin{aligned} -kL &= -4kL' \\ \implies L' &= \frac{L}{4} \end{aligned}$$

The answer is thus A. We also conclude that for some spring constant  $k' = nk$ , the extension of the new system is  $L' = \frac{L}{n}$ .

### A2:P59 Question 12

The spring constant of a system connected in series is given by:

$$\begin{aligned} \frac{1}{k'} &= \frac{1}{k_1} + \frac{1}{k_2} \\ &= \frac{1}{k} + \frac{1}{2k} = \frac{3}{2k} \\ \therefore k' &= \frac{2k}{3} \end{aligned}$$

We define using Newton's second law and Hooke's law the total extension  $L$  by:

$$\begin{aligned} F_g &\stackrel{\text{N2}}{=} mg = F_h = -k'L = -\frac{2k}{3}L \\ \implies mg &= -\frac{2k}{3}L \end{aligned}$$

The extension of the first spring is similarly given as:

$$mg = -kL_1$$

Equating both expressions:

$$\begin{aligned} -kL_1 &= -\frac{2k}{3}L \\ \implies L_1 &= \frac{2L}{3} \end{aligned}$$

Thus the answer fitting the total spring constant and extension is D.

### A2:P61 Question 13

Let the density of object 1 and 2 be denoted  $\rho_1$  and  $\rho_2$ , and the density of water  $\rho_w$ . Dividing both sides

of the ratio  $\frac{\rho_1}{\rho_2}$  by  $\rho_w$  gives:

$$\frac{\rho_1}{\rho_2} \stackrel{\text{let}}{=} r = \frac{\frac{\rho_1}{\rho_2}}{\rho_w}$$

The fraction of an object's volume which is below water is given as:

$$V' = \frac{\rho_o}{\rho_w}$$

We know 75% of the volume of object 1 is below the water, and 50% for object 2. Thus:

$$r = \frac{75\%}{50\%} = 1.5$$

This makes the answer A.

#### A2:P61 Question 14

**a)** The percentage of the volume of the cuboid under the water is the ratio between the submerged height and the total height. Therefore the percentage is given by:

$$\frac{2 \text{ [cm]}}{10 \text{ [cm]}} = 20\%$$

We then get the density of object using the fact that the ratio between an object's density and the fluid's density is the percentage of its submerged volume:

$$0.2 = \frac{\rho_o}{\rho_w} \implies \rho_o = 0.2\rho_w$$

Finally, we calculate mass using  $m = V\rho$ :

$$\begin{aligned} m &= 0.25 \times 0.25 \times 0.1 \times 0.2\rho_w \\ &= 0.00125\rho_w = 0.00125 \times 10^3 = \boxed{1.25 \text{ [kg]}} \end{aligned}$$

**b)** To sink, the whole 10 [cm] has to be submerged. The new mass is given as:

$$m = 1.25 + 4 = 5.25 \text{ [kg]}$$

We then need to calculate the new density of the cuboid, which is done as (using the volume computed in **a)**):

$$\rho_o = \frac{m}{V} = \frac{5.25}{0.25 \times 0.25 \times 0.1} = \frac{5.25}{0.00625} = 840 \text{ [kg m}^{-3}\text{]}$$

Finally, we compute the ratio of the object's density and the water's density:

$$\frac{\rho_o}{\rho_w} = \frac{840}{1000} \leq 1$$

Since the ratio is less than 1, all of the volume will not be submerged, making the object stay afloat.

### A2:P62 Question 15

To float in equilibrium, the density of the balloon + the density of the gas have to be equal to the density of air. Therefore:

$$\rho_a = \rho_b + \rho_g$$

The density of the balloon  $\rho_b$  (sans gas) is computed as:

$$\rho_b = \frac{m}{V} = \frac{0.014}{\frac{4}{3}\pi 0.15^3} \approx 0.990 \text{ [kg m}^{-3}\text{]}$$

Since the density of air  $\rho_a$  was given, we simply solve the original equation:

$$1.2 = 0.99 + \rho_g \implies \rho = 1.2 - 0.99 = \boxed{0.21 \text{ [kg m}^{-3}\text{]}}$$

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$$a^2 + b^2 = c^2$$

## **2 Topic B – The particulate nature of matter**

### **2.1 Subtopic B.1 – Thermal energy transfers**