

# 5.

## Exercício 5.1

a)

$$f[x_, y_, z_] = x^2 + 2y^2 + 3z^2; \text{ ponto} = \{1, 1, 1\}$$

$$\{1, 1, 1\}$$

$$f @ @ \text{ ponto}$$

$$6$$

$$\text{Grad}f[x_, y_, z_] = \text{Grad}[f[x, y, z], \{x, y, z\}]$$

$$\{2x, 4y, 6z\}$$

Reta normal

$$y = -1 + 2x$$

$$z = -2 + 3x$$

Plano tangente

$$z = \frac{1}{3} (6 - x - 2y)$$

b)

$$f[x_, y_, z_] = xyz^2; \text{ ponto} = \{1, 1, 1\}$$

$$\{1, 1, 1\}$$

$$f @ @ \text{ ponto}$$

1

$$\text{Gradf}[\mathbf{x}_-, \mathbf{y}_-, \mathbf{z}_-] = \text{Grad}[\mathbf{f}[\mathbf{x}, \mathbf{y}, \mathbf{z}], \{\mathbf{x}, \mathbf{y}, \mathbf{z}\}]$$

$$\{y z^2, x z^2, 2 x y z\}$$

Reta normal

$$y = x$$

$$z = -1 + 2x$$

Plano tangente

$$z = \frac{1}{2} (4 - x - y)$$

c)

$$\mathbf{f}[\mathbf{x}_-, \mathbf{y}_-, \mathbf{z}_-] = \mathbf{x}^2 + 3 \mathbf{y}^3 + \text{Sin}[\mathbf{x} \mathbf{y}] - \mathbf{z}; \text{ponto} = \{1, 0, 1\};$$

$$\mathbf{f} @ \text{ponto}$$

$$0$$

$$\text{Gradf}[\mathbf{x}_-, \mathbf{y}_-, \mathbf{z}_-] = \text{Grad}[\mathbf{f}[\mathbf{x}, \mathbf{y}, \mathbf{z}], \{\mathbf{x}, \mathbf{y}, \mathbf{z}\}]$$

$$\{2x + y \cos[xy], 9y^2 + x \cos[xy], -1\}$$

Reta normal

$$y = \frac{1}{2} (-1 + x)$$

$$z = \frac{3}{2} - \frac{x}{2}$$

Plano tangente

$$z = -1 + 2x + y$$

d)

```
f[x_, y_, z_] = Exp[x y z]; ponto = {1, 1, 0};
```

```
f @@ ponto
```

```
1
```

```
Gradf[x_, y_, z_] = Grad[f[x, y, z], {x, y, z}]
```

```
{e^{y z} y z, e^{y z} x z, e^{y z} x y}
```

Reta normal

$$x = 1$$

$$y = 1$$

Plano tangente

$$z = 0$$

## Exercício 5.2

a)

```
f[x_, y_, z_] = x^3 + x y z; ponto = {2, 2, 1}
```

```
{2, 2, 1}
```

```
f @@ ponto
```

```
12
```

```
Gradf[x_, y_, z_] = Grad[f[x, y, z], {x, y, z}]
```

```
{3 x^2 + y z, x z, x y}
```

Reta normal

$$y = \frac{12 + x}{7}$$

$$z = \frac{3}{7} + \frac{2x}{7}$$

## Plano tangente

$$z = \frac{1}{2} (18 - 7x - y)$$

b)

Não

## Exercício 5.3

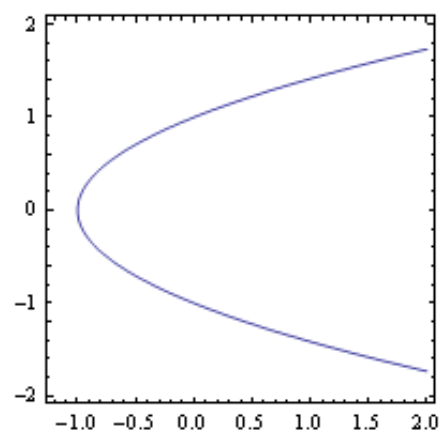
a)

$$f(x, y) = x - y^2; \quad A = \{-1, 0\};$$

$$f|_A$$

$$-1$$

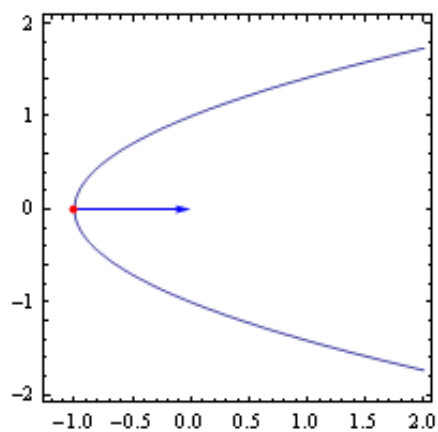
$$x = -1 + y^2$$



b)

$$\text{Grad} f(x, y) = \text{Grad}[f(x, y), \{x, y\}]$$

$$\{1, -2y\}$$



c)

```
Print["z = ", f @@ A + Gradf @@ A. ({x, y} - A)]
```

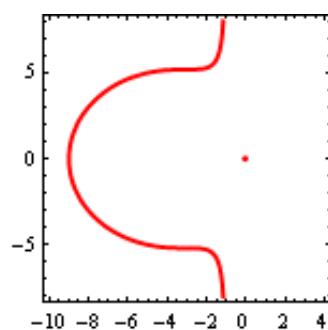
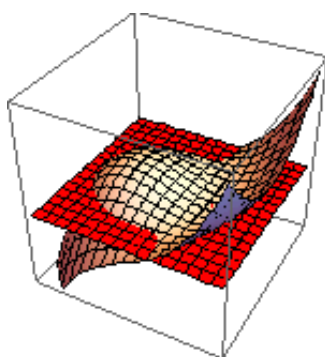
```
z = x
```

## Exercício 5.4

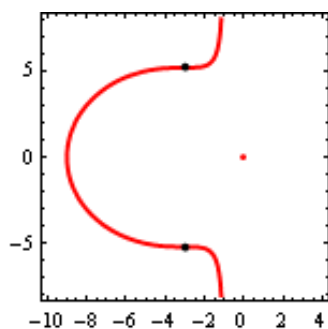
```
f[x_, y_] = x (x^2 + y^2) + 9 x^2 + y^2;
```

```
Grad[f[x, y], {x, y}]
```

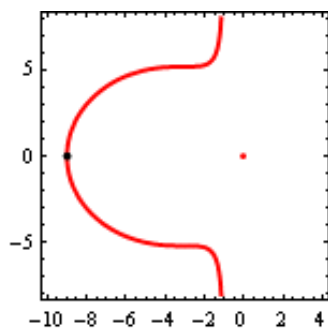
```
{18 x + 3 x^2 + y^2, 2 y + 2 x y}
```



$$\{ \{-3, -3\sqrt{3}\}, \{-3, 3\sqrt{3}\} \}$$



$$\{ \{-9, 0\} \}$$



### Exercício 5.5

$$\{ \{0, 1\}, \left\{ \frac{2}{3}, -\frac{1}{3} \right\} \}$$

### Exercício 5.6

$$\left\{ \left\{ \frac{2}{3}, -\frac{4}{3} \right\}, \{2, 0\} \right\}$$

### Exercício 5.7

$$f[x_, y_, z_] = x^2 + y^2 + z^2;$$

$$z = \frac{5 + y}{2}$$

e

$$x = \frac{5 - y}{2}$$

## Exercício 5.8

$$\text{ArcCos}\left[\sqrt{\frac{2}{3}}\right]$$

Created with the Wolfram Language