Learning to Play Board Games With Deep Reinforcement Learning Machine Learning Nanodegree - Capstone Report

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1 Definition

1.1 Project Overview

Reinforcement learning is the area of machine learning concerned with the idea of learning by interacting with an environment (Sutton and Barto, 1998). It has a long and notable history in games. The checkers program written by Samuel (1959) was the first remarkable application of temporal difference learning, and also the first significant learning program of any kind. It had the principles of temporal difference learning decades before it was described and analyzed. However, it was another game where reinforcement learning reached its first big success, when TD-GAMMON (Tesauro, 1995) reached world-class gameplay in Backgammon by training a neural network-based evaluation function through self-play.

Deep Learning (LeCun et al., 2015) is another branch of machine learning that allows computational models that are composed of multiple processing layers to learn representations of data with multiple levels of abstraction. Deep learning techniques have dramatically improved the state-of-the-art in areas such as speech recognition (Hinton et al., 2012), image recognition (Krizhevsky et al., 2012) and natural language processing (Colbert et al., 2011).

Recently, there have been several breakthroughs when combining reinforcement learning and deep learning. Mni et al. (2015) used a convolutional neural network trained with a variant of Q-learning and learned to play Atari 2600 games at a human-level. Last year, one of the biggest challenges for artificial intelligence was solved, when Google's DeepMind (Silver et al., 2016) created AlphaGo to beat the world's greatest Go player. AlphaGo used deep neural networks trained by a combination of supervised learning from human expert games, and reinforcement learning from games of self-play.

Developing strong game-playing programs for classic two-player games (e.g. Chess, Checkers, Go) is important in two respects: first, for humans that play the games looking for an intellectual challenge, and second, for AI researchers that use the games as testbeds for artificial intelligence. In both cases, the task for game programmers and AI researchers of writing strong game AI is a hard and tedious task that requires hours of trial and error adjustments and human expertise. Therefore, when a strong game-playing algorithm is created to play a specific game, it is rarely useful for creating an algorithm to play another game, since the domain knowledge is non-transferable. For this reason, there is enormous value in using machine learning to learn to play these games without using any domain knowledge.

1.2 Problem Statement

In this project we use deep reinforcement learning to create an agent that learns to play the game of Connect 4 by playing games against itself. We define the machine learning problem as follows:

- Task: Playing Connect 4.
- **Performance:** Winning percentage when playing against other agents, and accuracy of the predicted outcomes on the UCI Connect 4 dataset.

- Experience: Games played against itself.
- Target function: $Q^{\pi}: \mathcal{S} \times \mathcal{A} \to \mathbb{R}$, where \mathcal{S} is the set of *states* (board positions) and \mathcal{A} is the set of *actions* (moves), and \mathbb{R} represents the value of being in a state $s \in \mathcal{S}$, applying a action $a \in \mathcal{A}$, and following policy π thereafter.
- Target function representation: Deep neural network.

More specifically, we seek to build an agent that uses Q-learning via self-play to train a deep convolutional neural network to approximate the optimal action-value function:

$$Q^*(s, a) = \max_{\pi} Q^{\pi}(s, a), \forall s \in \mathcal{S}, a \in \mathcal{A}$$
(1)

which is the maximum sum of rewards achievable by a behavior policy π .

1.3 Metrics

- Winning percentage. Consists in playing a high number of games (e.g. 100,000) against other agents (e.g. Alpha-Beta player) using the trained deep neural network as the action-value function to take greedy actions.
- **Prediction accuracy.** The learned action-value function is used to predict the game-theoretic outcomes (win, loss or draw) of the board positions in the Connect 4 Data Set.

2 Analysis

2.1 Data Exploration and Visualization

In this project we use two environments and one dataset. The environments are the games of Tic-Tac-Toe and Connect 4, and the dataset is the UCI Connect 4 dataset.

2.1.1 Tic-Tac-Toe Environment

Tic-Tac-Toe [source] is a paper-and-pencil game for two players, X and O, who take turns marking the spaces in a 3x3 grid. The player who succeeds in placing three of their marks in a horizontal, vertical, or diagonal row wins the game. Figure 1 shows three Tic-Tac-Toe game positions: a win, a draw and a loss.

Tic-Tac-Toe is an extremely simple game, nonetheless, is very useful to analyze simple concepts and to verify that the implementation of the learning algorithms are behaving as expected before moving into the Connect 4 environment, which is more complex because of its large state space.



Figure 1: Examples of a win, a loss and a draw in Tic-Tac-Toe.

2.1.2 Connect 4 Environment

Connect 4 [source] is a two-player board game of perfect information where pieces are dropped into the columns of a vertical 6×7 grid with the goal of forming a straight line of 4 connected pieces. There are at most seven actions per state, since placing a piece in a column is a legal action only if that column has at least one empty location. In this project we use pieces of two colors: Yellow for the first player, and Red for the second player. Figure 2 shows three Connect 4 game positions: a win, a draw and a loss:



Figure 2: Examples of a win, a loss and a draw in Connect Four.

2.1.3 UCI Connect 4 Data Set

As part of the testing phase, we will use the $Connect\ 4$ $Data\ Set^1$ that is available from the UCI Machine Learning Repository (Hettich and Merz, 1998). A partial view of the dataset is presented in Table 1. The dataset has a total of 67,557 instances, representing all legal 8-ply positions in Connect 4 in which neither player has won yet, and which the next move is not forced. Each instance is described by 42 features, one for each space in the 6×7 board, and can belong to one of the classes $\{x, o, b\}$, where x is the first player, o is the second player, and b is empty. The outcome class is the game theoretical value for the first player, and can belong to one of the classes $\{win, loss, draw\}$. There are 44,473 wins, 16,635 losses and 6,449 draws [source]. Figure 3 shows a visual representation of five randomly selected instances of the data set. As we can see, all game positions have eight pieces in the board, representing all legal 8-ply positions [source].

¹https://archive.ics.uci.edu/ml/datasets/Connect-4

		Features															Target	
No.	a1	a2	a3	a4	a5	a6	b1	b2		f5	f6	g1	$\mathbf{g}2$	$\mathbf{g}3$	g4	$\mathbf{g5}$	g6	outcome
0	b	b	b	b	b	b	b	b		b	b	b	b	b	b	b	b	win
1	b	b	b	b	b	b	b	b		b	b	b	b	b	b	b	b	win
2	b	b	b	b	b	b	О	b		b	b	b	b	b	b	b	b	win
3	b	b	b	b	b	b	b	b		b	b	b	b	b	b	b	b	win
4	О	b	b	b	b	b	b	b		b	b	b	b	b	b	b	b	win
67552	x	x	b	b	b	b	О	X		b	b	О	O	x	b	b	b	loss
67553	x	X	b	b	b	b	О	b		b	b	O	X	O	O	X	b	draw
67554	x	x	b	b	b	b	О	О		b	b	О	X	x	O	b	b	loss
67555	x	O	b	b	b	b	О	b		b	b	O	X	O	X	X	b	draw
67556	x	О	О	О	X	b	О	b		b	b	x	b	b	b	b	b	draw

Table 1: UCI Connect 4 Dataset. Each row represents a different board position, and each feature represents a specific cell in the board. The target is the outcome of the game for the first player, assuming perfect play.



Figure 3: Five randomly selected instances of the UCI Connect 4 Data Set. The outcome of each board position is from the point of view of the firs player (Yellow discs).

2.2 Algorithms and Techniques

2.2.1 Markov Decision Process

A Markov decision process (MDP) consist of four elements:

- S is the set of *states* (state space).
- \mathcal{A} is the set of actions (action space). The set of actions that are available in some particular state $s_t \in \mathcal{S}$ is denoted $\mathcal{A}(s_t)$.
- $T: \mathcal{S} \times \mathcal{A} \times \mathcal{S} \to \mathbb{R}$ is the transition function, which is the probability given we are in state $s_t \in \mathcal{S}$, take action $a_t \in \mathcal{A}(s_t)$ and we will transition to state $s_{t+1} \in \mathcal{S}$.
- $R: \mathcal{S} \times \mathcal{A} \times \mathcal{S} \to \mathbb{R}$ is the reward function, which is the immediate reward received when in state $s_t \in \mathcal{S}$ action $a_t \in \mathcal{A}$ is taken and the MDP transitions to state $s_{t+1} \in \mathcal{S}$. However, it is also possible to define it either as $R: \mathcal{S} \times \mathcal{A} \to \mathbb{R}$ or $R: \mathcal{S} \to \mathbb{R}$. The first one gives rewards for performing an action a_t in a particular state s_t , and the second gives rewards when transitioning to state s_{t+1} .

2.2.2 Environment

In the reinforcement learning problem an agent does not have access to the dynamics (reward and transition function) of the MDP. However, it interacts with an *environment* by way of three signals: a *state*, which describes the state of the environment, an *action*, which allows the agent to have some impact on the environment, and a *reward*, which provides the agent with feedback on its immediate performance.

2.2.3 Policy

In an MDP, the agent acts according to a policy π , which maps each state $s \in \mathcal{S}$ to an action $a \in \mathcal{A}(s)$. A policy that specifies a unique action to be performed is called a *deterministic* policy, and is defined as $\pi : \mathcal{S} \to \mathcal{A}$.

The interaction between the policy used by the agent and the environment works as follows. First, it starts at an *initial state* s_0 . Then, the policy π selects an action $a_0 = \pi(s_0)$ from the set of available actions $\mathcal{A}(s_0)$, and the action is executed. The environment transitions to a new state s_1 based on the transition function T with probability $T(s_0, a_0, s_1)$, and a reward $r_0 = R(s_0, a_0, s_1)$ is received. This process continues, producing a trajectory of experience $s_0, a_0, s_1, r_1, a_1, s_2, r_2, a_2, \ldots$, and the process ends in a terminal state s_T and is restarted in the initial state.

We use three types of policies in this project:

- Random. Selects actions uniformly at random.
- Greedy. Selects the max action, which is the greedy action with the highest value,

$$\pi_{\text{greedy}}(s) = \underset{a \in \mathcal{A}(s)}{\operatorname{argmax}} Q(s, a)$$
(2)

• ϵ -greedy. Selects the best action for a proportion $1 - \epsilon$ of the trials, and another action is randomly selected (with uniform probability) for a proportion,

$$\pi_{\epsilon}(s) = \begin{cases} \pi_{\text{rand}}(s, a) & \text{if } rand() < \epsilon \\ \pi_{\text{greedy}}(s, a) & \text{otherwise} \end{cases}$$
 (3)

where $\epsilon \in [0,1]$ and rand() returns a random number from a uniform distribution $\in [0,1]$.

2.2.4 Value Functions

Most of the algorithms for solving MDPs (computing optimal policies) do it by learning a *value function*. A value function estimates what is good for an agent over the long run. It estimates the expected outcome from any given state, by summarising the total amount of reward that an agent can expect to accumulate into a single number. Value functions are defined for particular policies.

Two types of value functions exist: state value functions and action value functions. In this project, however, we only focus in the latter.

The action value function (or Q-function), is the expected return after selecting action a in state s and then following policy π ,

$$Q^{\pi}(s,a) = \mathbb{E}_{\pi} \left[R_t | s_t = s, a_t = a \right] \tag{4}$$

The *optimal value function* is the unique value function that maximises the value of every state, or state-action pair,

$$Q^*(s,a) = \max_{\pi} Q^{\pi}(s,a), \forall s \in \mathcal{S}, a \in \mathcal{A}$$
 (5)

An optimal policy $\pi^*(s, a)$ is a policy that maximises the action value function from every state in the MDP,

$$\pi^*(s, a) = \operatorname*{argmax}_{\pi} Q^{\pi}(s, a) \tag{6}$$

2.2.5 Q-learning

One of the most basic and popular methods to estimate action-value functions is the Q-learning algorithm (Watkins, 1989) [source]. It is model-free online off-policy algorithm, whose main strength is that it is able to compare the expected utility of the available actions without requiring a model of the environment. Q-learning works by learning an action-value function that gives the expected utility of taking a given action in a given state and following a fixed policy thereafter. The update rule uses action-values and a built-in max-operator over the action-values of the next state in order to update $Q(s_t, a_t)$ as follows,

$$Q(s_t, a_t) \leftarrow Q(s_t, a_t) + \alpha [r_{t+1} + \gamma \max_{a} Q(s_{t+1}, a) - Q(s_t, a_t)]$$
 (7)

The agent makes a step in the environment from state s_t to s_{t+1} using action a_t while receiving reward r_t . The update takes place on the action-value a_t in the state s_t from which this action was executed. This version of Q-learning works well for tasks with a small a state-space, since it uses arrays or tables with one entry for each state-action pair. In many cases in which there are far more states than could possibly be entries in a table we need to use function approximation.

2.2.6 Approximate Q-learning

Approximate Q-learning consists in parameterizing an approximate action-value function, $Q(s, a; \theta_i) \approx Q(s, a)$, in which θ_i are the parameters (weights) of the action-value function at iteration i.

2.2.7 Experience Replay

Reinforcement learning is known to be unstable or even to diverge when a nonlinear function approximator such as a neural network is used to represent the action-value function. One trick is to make it work is to use experience replay, which consists in storing the experiences (s_t, a_t, r_t, s_{t+1}) . During the training of approximate Q-learning random minibatches from the replay memory are used instead of the most recent transition. This breaks the similarity of subsequent training samples, which otherwise might drive the network into a local minimum.

2.2.8 Self-play

Self-play is by far the most popular training method. It is a single policy $\pi(s, a)$ that is used by both players in a two-player game, $\pi_1(s, a) = \pi_2(s, a) = \pi(s, a)$. The first reason for its popularity is that training is quickest if the learner's opponent is roughly equally strong, and that definitely holds for self-play. As a second reason for popularity, there is no need to implement or access a different agent with roughly equal playing strength. However, self-play has several drawbacks, with the main one being that a single opponent does not provide sufficient exploration (Szita, 2011).

2.3 Benchmark

- Random agent. This benchmark consists in playing against an agent that takes uniformly random moves. This is the most basic benchmark, but first we have to be sure that our learned evaluation function can play better than a random agent before moving into a harder benchmark. Also, this will help us to detect bugs in the code and algorithms: if a learned value function does not play significantly better than a random agent, is not learning. The idea is to test against this benchmark using Alpha-beta pruning at 1, 2 and 4-ply search.
- Connect 4 Data Set. This dataset will be used as the main benchmark. The learned value function will be used to predict the game-theoretic outcomes (win, loss or draw) for the first player in the 67,557 instances of the dataset.

3 Methodology

3.1 Data Preprocessing

In this project data preprocessing is not necessary because all the learning came from two reinforcement learning simulators.

3.2 Implementation

3.2.1 Game

The first part of the implementation was to implement both two games: Tic-Tac-Toe and Connect 4. The idea was to design them first in a way that is independent of reinforcement learning. The following is the abstract Game interface for both [source].

```
class Game(object):
   def copy(self):
        '''Returns a copy of the game.'''
        pass
    def cur_player(self):
        Returns the index of the player in turn, starting with 0:
        0 (Player 1), 1 (Player 2), etc.
        pass
    def is_over(self):
        '''Returns True if the game is over.'''
        return len(self.legal_moves()) == 0
    def legal_moves(self):
        '''Returns a list of legal moves for the player in turn.'''
        pass
    def make_move(self, move):
        '''Makes one move for the player in turn.'''
        pass
    def outcomes(self):
        '''Returns a list of outcomes for each player at the end of the game.'''
        pass
    def reset(self):
        '''Restarts the game.'''
        pass
```

Once we had the Game interface well defined we implemented both Tic-Tac-toe [source] and Connect 4 [source].

3.2.2 Markov Decision Process

Next, the interface for an MDP [source]:

```
class MDP(object):
   def states(self):
        '''Returns a list of all states. Not generally possible for large MDPs.'''
        pass
   def start_state(self):
        '''Returns the initial state.'''
       pass
   def actions(self, state):
        '''Returns a list of possible actions in the given state.'''
        pass
   def transitions(self, state, action):
        Returns a dict of (next_state: probability) key/values, where 'next_state' is
        reachable from 'state' by taking 'action'. The sum of all probabilities should
        be 1.0. Not available in reinforcement learning.
        pass
   def reward(self, state, action, next_state):
       Returns the reward of being in 'state', taking 'action', and ending up
        in 'next_state'. Not available in reinforcement learning.
       pass
   def is_terminal(self, state):
        '''.Returns True if the given state is terminal.'''
        pass
```

3.2.3 Markov Decision Process for Games

We also created two helper classes:

source

```
def __init__(self, game):
    self._game = game
    self._states = {}
def actions(self, state):
    return [None] if state.is_over() else state.legal_moves()
def is_terminal(self, state):
    return state.is_over()
def reward(self, state, action, next_state):
    '''Returns the utility from the point of view of the first player.'''
    return utility(next_state, 0) if next_state.is_over() else 0
def start_state(self):
    return self._game.copy()
def states(self):
    if not self._states:
        def generate_states(game):
            '''Generates all the states for the game'''
            if game not in self._states:
                self._states[game] = game
            for move in game.legal_moves():
                new_game = game.copy().make_move(move)
                generate_states(new_game)
        generate_states(self._game)
    return self._states
def transitions(self, state, action):
    if state.is_over():
        return [(state, 1.0)]
    new_game = state.copy().make_move(action)
    return [(new_game, 1.0)]
```

And also, FixedGameMDP [source], which converts a Game into an MDP by using a fixed opponent for one of the players in the game:

```
def reward(self, game, move, next_game):
    return utility(next_game, self._agent_idx) if next_game.is_over() else 0
def start_state(self):
   new_game = self._game.copy()
    if not new_game.is_over() and new_game.cur_player() == self._opp_idx:
        chosen_move = self._opp_player.choose_move(new_game)
        new_game.make_move(chosen_move)
    return new_game
def transitions(self, game, move):
    if game.is_over():
        return []
    new_game = game.copy().make_move(move)
    if not new_game.is_over() and new_game.cur_player() == self._opp_idx:
        chosen_move = self._opp_player.choose_move(new_game)
        new_game.make_move(chosen_move)
    return [(new_game, 1.0)]
```

3.2.4 Environment

A reinforcement learning environment [source] for interacting with an MDP. The main idea is that it restricts access to the transition and reward functions. It needs to interact with the environment to transition to another state and receive rewards.

```
class Environment(object):
    def __init__(self, mdp):
        self._mdp = mdp
        self._cur_state = self._mdp.start_state()
    def actions(self, state):
        '''Returns the available actions in the given state.'''
        return self._mdp.actions(state)
    def cur_state(self):
        '''Returns the current state.'''
        return self._cur_state.copy()
    def do_action(self, action):
        Performs the given action in the current state.
        Returns (reward, next_state).
        prev = self.cur_state()
        transitions = self._mdp.transitions(self.cur_state(), action)
        for next_state, prob in transitions:
            self._cur_state = next_state
```

```
reward = self._mdp.reward(prev, action, self.cur_state())
return reward, self.cur_state()

def is_terminal(self):
    return self._mdp.is_terminal(self.cur_state())

def reset(self):
    '''Resets the current state to the start state.'''
    self._cur_state = self._mdp.start_state()
```

3.2.5 Learner

We define an episodic learner. It is basically an interface for algorithms that learn a value function by interacting with an environment in an episodic way.

```
class Learner(object):
    def __init__(self, env, n_episodes=1000):
        self.env = env
        self.n_episodes = n_episodes
    def train(self, callbacks=None):
        '''Trains the model for a fixed number of episodes.'''
        callbacks = CallbackList(callbacks)
        callbacks.on_train_begin()
        for episode in range(self.n_episodes):
            callbacks.on_episode_begin(episode)
            self.env.reset()
            self.episode()
            callbacks.on_episode_end(episode, self.qfunction)
        callbacks.on_train_end(self.qfunction)
    @abc.abstractmethod
    def episode(self):
        pass
```

3.2.6 Tabular Q-learning

asdf asd fas fas df a.

```
class QLearning(Learner):
    '''Tabular Q—learning'''
    def __init__(self, env, policy, qfunction, learning_rate=0.1, discount_factor=1.0):
        super(QLearning, self).__init__(env, **kwargs)
        self.policy = policy
        self.qfunction = qfunction
        self.learning_rate = learning_rate
        self.discount_factor = discount_factor
    def best_qvalue(self, state):
        return max_qvalue(state, self.env.actions(state), self.qfunction)
    def episode(self):
        while not self.env.is_terminal():
            state = self.env.cur_state()
            action = self.policy.action(state)
            reward, next_state = self.env.do_action(action)
            best_qvalue = self.best_qvalue(next_state)
            target = reward + (self.discount_factor * best_qvalue)
            td_error = target - self.qfunction[state, action]
            {\tt self.qfunction[state, action] += self.learning\_rate * td\_error}
```

3.2.7 Approximate Q-learning

```
state = self.env.cur_state()
action = self.policy.action(state)
reward, next_state = self.env.do_action(action)
if self.experience_replay:
    self.memory.add((state, action, reward, next_state))
    state, _, reward, next_state = random.choice(tuple(self.memory))
best_qvalue = self.best_qvalue(next_state)
update = reward + (self.discount_factor * best_qvalue)
self.qfunction.update(state, update)
```

3.3 Experiments

In order to create a strong agent to play Connect 4 we had to go step by step with a series of experiments. aasdf as fas dfas fsad f asdasdf as fas dfas fsad f asd.

3.3.1 Estimate Tic-Tac-Toe Q-values using tabular Q-learning versus fixed opponent

The goal of the first experiment [source] is to verify that the implementation of the Q-learning algorithm is correct. It consisted in using tabular Q-learning to estimate the Q-values of a simple Tic-Tac-Toe board position, shown in Figure 4. We modeled this scenario as an MDP in which a move by nature is made for the second player using a fixed Alpha-Beta agent that makes optimal moves. The position is set as the initial state, s_0 , and it has five available actions, $\mathcal{A}(s_0) = \{1, 2, 4, 6, 9\}$. This position is very close to the end of the game, which allows us to develop intuition of the expected Q-values from the game-theoretic point of view. For instance, we can clearly identify that the best available action is 9, which leads to an eventual win for the first player assuming optimal actions thereafter. On the other hand, any other action (i.e. 1, 2, 4 or 6) would lead to a loss, assuming perfect play from the opponent. The rewards given by the MDP are +1 for a win for the first player, -1 for a win for the second player, and 0 for a draw.



Figure 4: Initial state

We ran the experiment with $\alpha=0.1$ (learning rate), $\gamma=1.0$ (discount factor), and a $\pi_{\rm rand}$ (uniformly random) behavior policy. After approximately 800 episodes of training the Q-values converged to the expected, presented in Figure 5. As we can see, the expected future rewards are: 1.0 for action 9, and -1.0 for all other actions (i.e. 1, 2, 4 or 6). These are exactly the values we were looking for, which suggests that our implementation of Q-learning is correct.

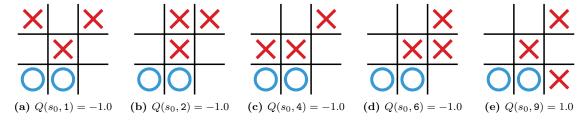


Figure 5

Figure 6 shows the predicted state-action values during training. It is interesting to see how the value of $Q(s_0, 9)$ takes more time to converge than the other Q-values. This is probably because taking action 9 results in an eventual, but not immediate win, and it requires making another move (either 1 or 6) to win. Also, is worth mentioning why we used a $\pi_{\rm rand}$ as the behavior policy instead of something like π_{ϵ} . Q-learning is an off-policy algorithm, which means we can use one policy for sampling (behavor policy), while estimating the value function for another one (target policy). And in an MDP as small as this, a simple $\pi_{\rm rand}$ policy is effective.

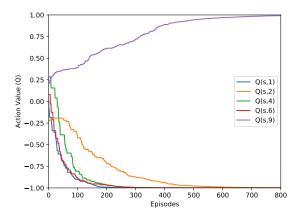


Figure 6: The predicted Q-values during the training phase of tabular Q-learning using Alpha-Beta as a fixed opponent.

3.3.2 Estimate Tic-Tac-Toe Q-values using tabular Q-learning via self-play

In this experiment [source] we also used tabular Q-learning to estimate the Q-values of the same position described in Section 3.3.1. This time, however, we used self-play, which consists in playing games against itself. Self-play is a good alternative when we do not have a strong opponent or one of roughly equal playing strength to train against. This is the case in Connect 4 because we cannot use the Alpha-Beta algorithm to search the full tree, given its large state-space and game tree complexity. To use Alpha-Beta we would need to use a heuristic evaluation function, which is what we are trying to create with deep reinforcement learning anyway. Nevertheless, we are trying to validate that our self-play implementation is working in Tic-Tac-Toe before moving to Connect 4.

We ran this experiment using the same parameters: $\alpha = 0.1$, $\gamma = 1.0$, and a $\pi_{\rm rand}$ behavior policy. Once again, the Q-values converged to the expected: 1.0 for action 9, and -1.0 for all other actions. However, in Figure 7 we can observe how this time the Q-values took 3,500 episodes to converge, which is around four times slower than when training against a strong fixed opponent. This is understandable, since the opponent was itself, i.e., an agent that makes uniformly random moves and provides less direct feedback.

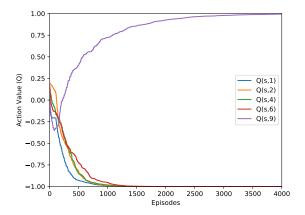


Figure 7: The predicted Q-values during the training phase of tabular Q-learning via self-play.

3.3.3 Use Q-function to Play Tic-Tac-Toe versus a Random agent

In this experiment [source] we used tabular Q-learning via self-play to learn the Q-values of all game states of Tic-Tac-Toe, and used them to play the game against a random player. In order to do that we set the starting state of the MDP as the empty board. We evaluated the performance as training progressed by having a π_{greedy} policy (using the Q-function being learned) play 1,000 matches every 1,000 episodes against a player that makes uniformly random moves.

The results are presented in Figure 8. We can observe how after around 70,000 episodes it learned to play the game almost perfectly against a random player. While the random opponent is obviously a weak opponent, is a simple test to verify that we can use the learned Q-values to play the game.



Figure 8: Win/Loss/Draw percentages of playing 1,000 games every 1,000 episodes between a greedy player that uses the learned Q-function against a Random player.

4 Results

4.1 Model Evaluation and Validation

4.1.1 Learning to Play Connect 4 using Q-learning with a Deep Neural Network

Once that we validated that our implementation of Q-learning is working and showed that it can learn a tabular value function to play Tic-Tac-Toe we moved into the more complex Connect 4. In this game, storing the Q-values for every board position in a lookup table is not feasible because of its huge state space. Instead of using tabular Q-learning, we used approximate Q-learning [source] with a deep neural network (DNN) [source]. This approach consists in parameterizing an approximate action-value function, $Q(s, a; \theta_i) \approx Q(s, a)$, in which θ_i are the weights of the neural network.

In some games it can be more efficient to consider the afterstate value $V(s \circ a)$, which is the state reached after taking action a in state s, instead of the Q-value Q(s,a) (Sutton and Barto, 1998). We used this approach by using a DNN that takes the state of the board in the input layer, as shown in Figure 9, and outputs the value of being in that state, V(s). After the input layer, we used convolutions with 4 layers of 64 filters of size 3×3 and rectified linear non-linearities. In addition to the convolutions, we added a densely-connected layer with 256 units. Finally, the output layer has only one unit that fires the value of the given board with a tanh activation function to keep it in the range [-1, +1].



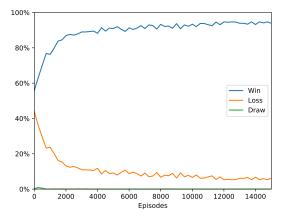
Figure 9: Feature extraction of a Connect 4 board

4.1.2 Training and Evaluation

In this experiment [source] our goal was to learn to play Connect 4 starting from 8-ply positions from the UCI Connect 4 dataset (Section 2.1.3). In these positions we already know the game-theoretical outcome of the game assuming perfect play from both players, however, we did not use the outcome for training (no supervised learning), only for evaluation. This helped us to start every episode of Q-learning training from different board positions, which is helpful to learn to generalize by seeing all kinds of board positions.

This experiment consisted in using approximate Q-learning [source] with a deep neural network [source]. In Figure 10 we can see how the quality of the target policy improved during training. The policy was evaluated during training every 500 episodes by playing 3,000 games against a random player starting from randomly selected 8-ply positions from the UCI Connect 4 dataset. The first 1,000 games started from positions where the outcome is a win for the first player assuming perfect play from both sides. Figure 10a shows how the policy improved from a 56% to a 94% win rate after 15,000 episodes. This makes sense because the matches started from favorable positions with higher probability of winning for the first player. The next 1,000 games started from game-theoretical draw positions (Figure 10b). As expected, the win rate at the beginning was 50%, but then it went up to 92%. Good improvement, but a little lower win rate than when starting from favorable positions. Finally, the last 1,000 games (Figure 10c) started from unfavorable positions that are guaranteed wins for the second player under optimal play from both sides. In this case the win rate before the policy begins learning is 45%, but then it went up to a 90% win rate. This was also expected, since we started at a disadvantage.

While the previous evaluation was made against a weak random player, we can see that the Q-learning is learning a value function for Connect 4 using a deep neural network as a function approximator.



(a) Starting from game theoretical win positions for player 1

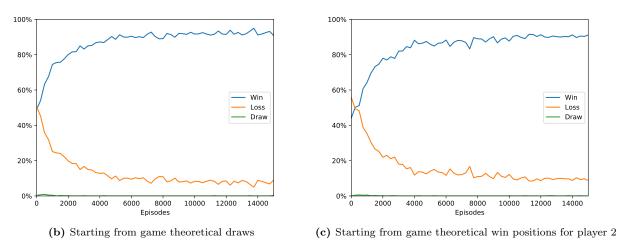


Figure 10: Performance of the policy during training learned during trained evaluated starting from winning, draws, and loss positions assuming perfect play.

Content

4.2 Justification

Content.

5 Conclusion

5.1 Free-Form Visualization

Content.

5.2 Reflection

The most difficult aspect of this project was that is extremely hard to stabilize reinforcement learning with non-linear function approximators via self-play. There are plenty of tricks that can be used and hyperparameters that need to be tuned to get it to work, such as:

- **Q-learning**: exploration policy (random?, ϵ -greedy?), discount factor, learning rate, number of episodes.
- Experience Replay: batch size, experience pool size.
- **Deep Neural Network**: mlp? convnets? number of layers, number of filters, number of kernels, optimizer (vanilla sgd, adam, rprop), learning rate, pooling, activation functions, etc.
- ϵ -greedy: fixed ϵ ? decrease ϵ ? initial value for ϵ ?, how many episodes to decrease it? final value?

All these techniques and parameters were selected by trial and error, and no systematic grid search was done due to the high computational cost.

5.3 Improvement

As in most projects, there are way too many aspects that can be improved. But in my opinion the three most important are:

- 1. **Better benchmarks:** In most of this project we used simple benchmarks, such as playing against random players. While testing against random is probably the first thing to test against (if you can't beat a random player your learning algorithm is not working), it would be better to find a few heuristics and better players that can be used for testing.
- 2. **Incorporate other RL techniques:** The field of RL has been advancing fast in recent years. There are a few new and old techniques that I would like to try, such as asynchronous RL, double Q-learning, prioritized experience replay.
- 3. Benchmark: dsfasdfas.

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