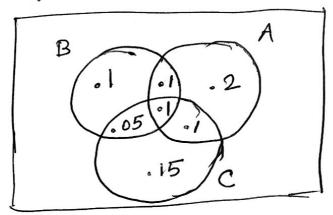
## Problem Sheet 2.

1. Let A, B and C be three events with probabilities given below:



Find P(AIB), P(CIB), P(B/AUC) and P(B (Anc).

Ams. 4/4, 3/4, 5/14 and 1/2.

2. A family Ras five children. We pick one at remdom and find that the child it a girl. What is the prob. That all children are girls?

3. I have 3 logs that each Contourn 100 marbles.
Bag I Contains 75 red and 25 blue marbles.

Bag 2 how 60 ved and 40 blue monbles. Bay 3 Ras 45 red and 55 blue manbles.

- I choose me bog at random and pick a marble from the Chosen bag, also at wordown.
- i) What is the prob. That the chosen marble is red?
- 12) of the chosen marble is red, what is the prob. that bag I was chosen?

  Ams. 0.6 and 5/12.
- 4, If A and B one two independent events, Show that A and B' are indep.
- 5. A box contains 2 coins, nother of them being fake with  $P(\{H\}) = 1$ . A coin is picked at rondom set and toksed twice.

  Let  $A = \{ \text{ the 1st tols vesselts in an H} \}$   $B = \{ \text{ the 2rd tols } \}$   $C = \{ \text{ good Coin is picked } \}$ .

- i) Show that A and B one and dependent.
  ii) Show that A and B are conditionally independent given C.
- 6. Let a fair die de volled once let  $A = \{1, 2\}, B = \{2, 4, 6\} \& C = \{1, 4\}$ 
  - i) Show that A and B are independent.
  - ii) Show that A and B are NOT conditionally independent given C.
- 7. Let  $C_1, C_2, \ldots, C_n$  be a partition on a Sample space &  $\Omega$  and let A and B be two events such that
  - (a) A&B are cond. indep. given C;
  - (b) B is imdep. Ball Ci's, Show that A and B are indep. Himt: Use total prob. for AnB.
  - 8. A box contains 3 coins: 2 fair coins and one fake with P(H) = 1.

- A Coim is picked at random and tossed 1) What is prob. B getting head?
- ii) If head is obtained, what is the prob. That it is a fake coim.

  Ans. 2/3 and 1/2.
- 9. Let  $x_1, x_2 \in \{1,2,3,4,5\}$  and  $X = x_1 + x_2$ . Find the  $\beta m f$   $\delta he$  ne narrable X.
- 10. A loin with  $P(H) = \beta$  ( 0'< \beta < 1) is torsed

  Prepeatedly until a head is obtained

  for the 1st time. Let Y be the no. B coin

  Rese tokked needed. Find the \beta for y.

  Ans. \beta (y) = \S (1-\beta)^{y-1}\beta for \quad y = 1,2,...

  O otherwise.