### Presentation Title

Sara Venkatraman
Statistics and Data Science, Cornell University

March 5, 2021

### Mercer's theorem

#### Eigendecomposition of a kernel

A continuous function  $K:([0,1]\times[0,1])\to\mathbb{R}$  is a *kernel* if it is:

- ▶ Symmetric: K(a, b) = K(b, a)
- Positive semi-definite:

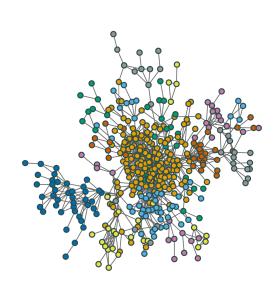
$$\sum_{i=1}^n \sum_{j=1}^n K(x_i, x_j) c_i c_j \geq 0$$

for all  $x_1, ..., x_n \in [0, 1]$  and  $c_1, ..., c_n \in \mathbb{R}$ 

Now define an integral operator on  $\mathcal{L}^2[0,1]$  using  $\mathcal{K}$ :

$$(T_K f)(x) = \int_0^1 K(x, s) f(s) \, \mathrm{d}s$$

# Example image



### References



## Paper 1 Title.

Paper 1 Authors. Journal Name Edition, Year.



### Paper 2 Title.

Paper 2 Authors.

arXiv:1234.56789.