# Image Segmentation and Visualization

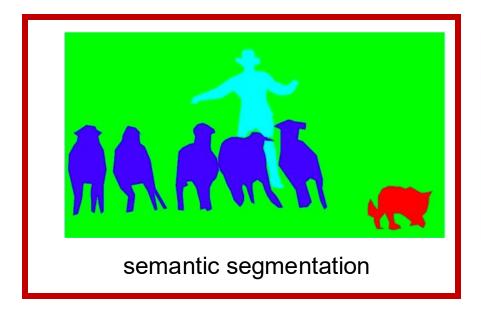
Xiaolong Wang

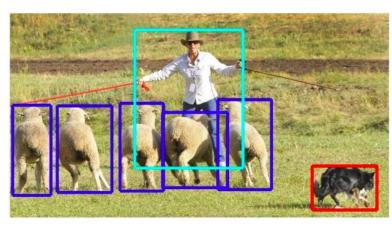
# Segmentation Problem and FCN

# The problem

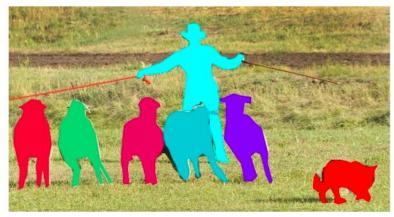


image classification



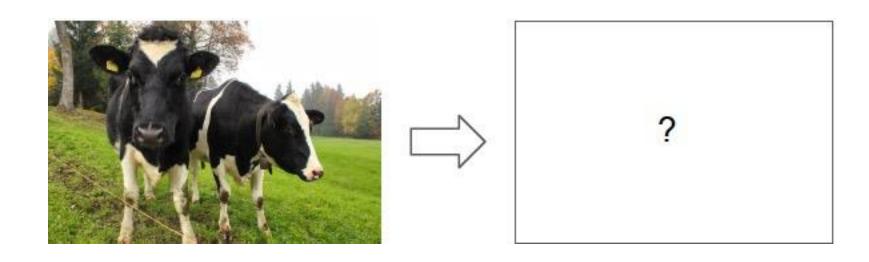


object detection



instance segmentation

# The problem



# Semantic Segmentation

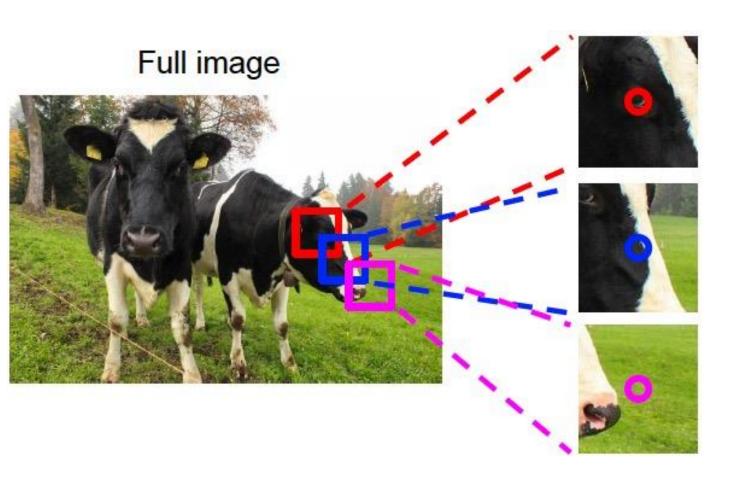
#### Full image



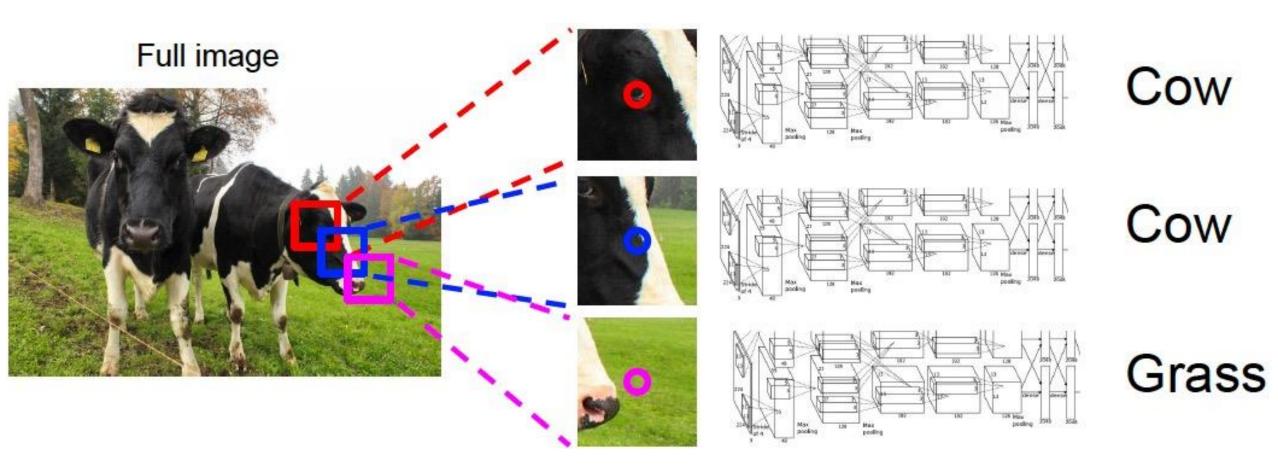
Simply staring one pixel is impossible to do the classification

Let's put in some context!

# Semantic Segmentation



# Semantic Segmentation

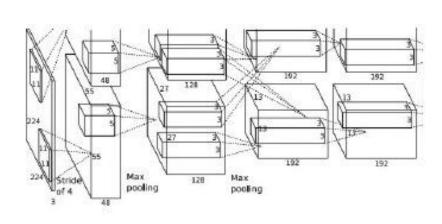


Time Consuming!

# Can we process the whole image at one time?

Full image







AlexNet input: 227 x 277 x 3

AlexNet Conv5: 13 x 13 x 128



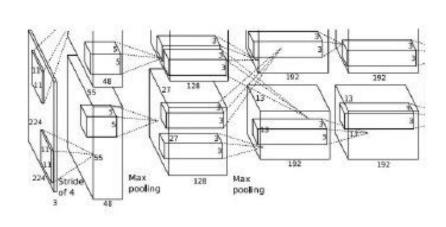
Output ? 13 x 13 x 21

Output is too small!

# Can we process the whole image at one time?

Full image





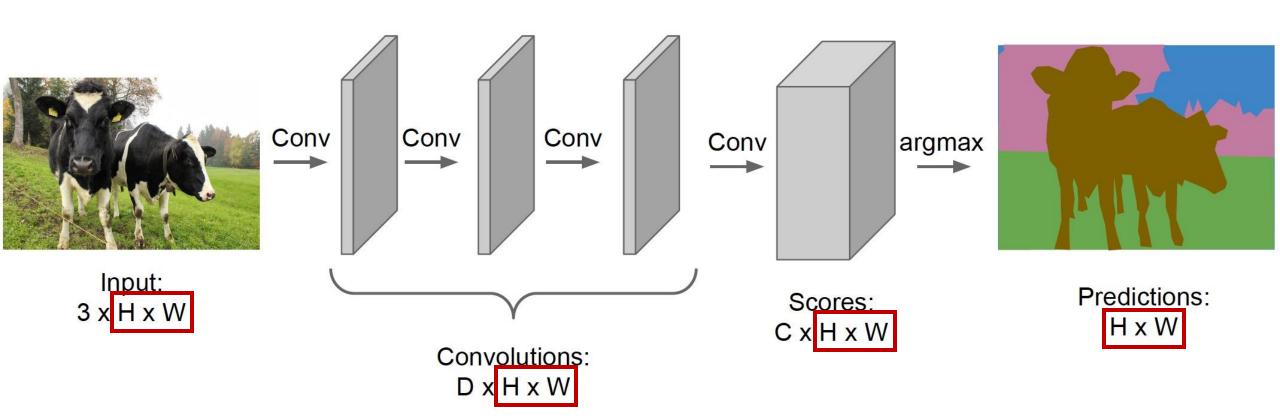


AlexNet input: 227 x 277 x 3

AlexNet Conv5: 13 x 13 x 128

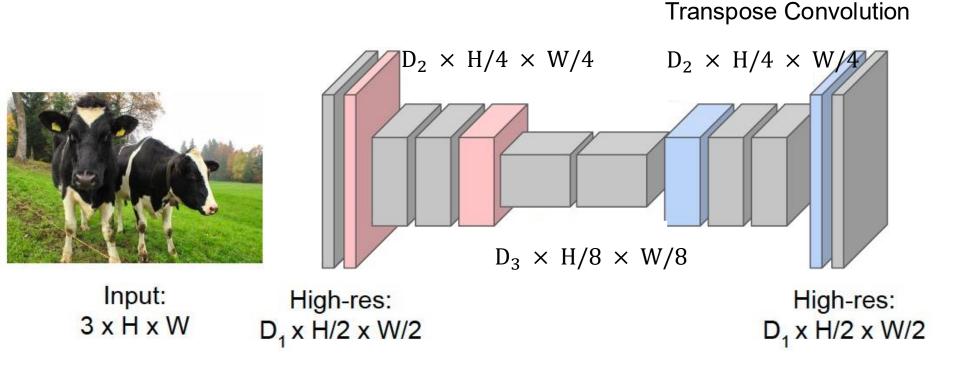


# Fully Convolutional Network



Convolution at original image resolution has high computation cost.

# Fully Convolutional Network





Predictions: H x W

Make the feature map small increases the receptive field

Make the feature map larger again increases the resolution

# The upsamling

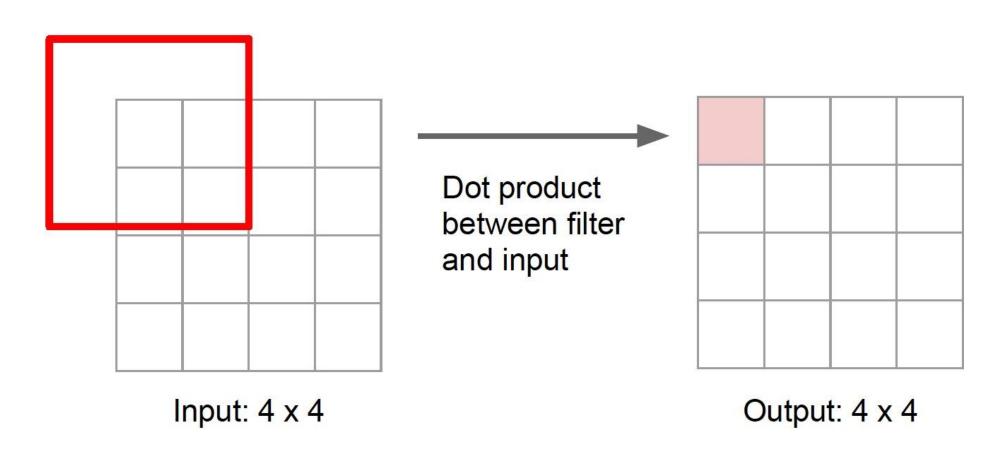
Upsampling Layer

Deconvolution Layer

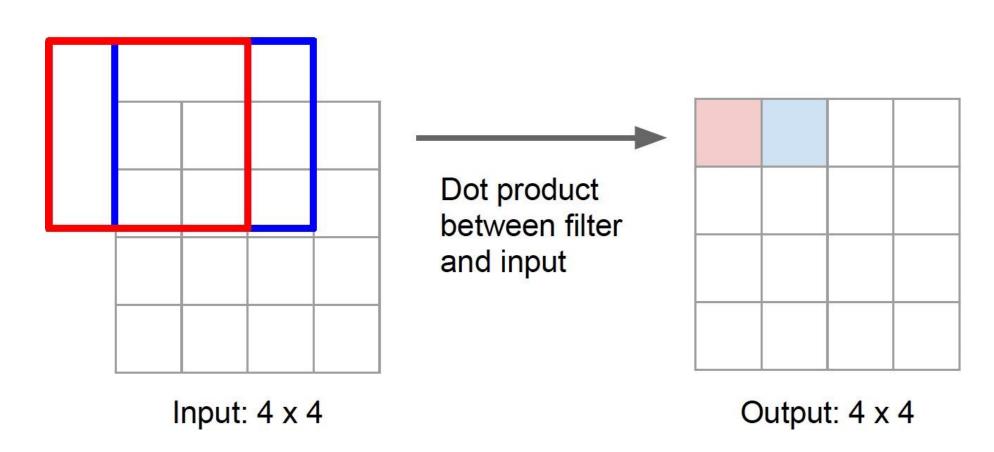
Transpose Convolution Layer

# **Transpose Convolution**

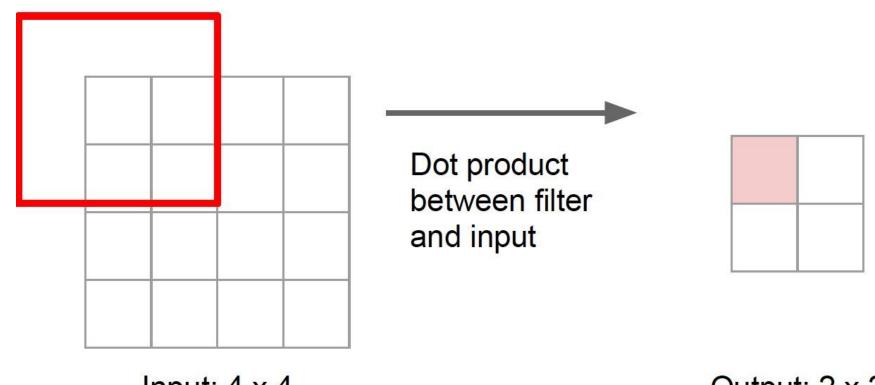
3 X 3 convolution with stride 1 and padding 1



3 X 3 convolution with stride 1 and padding 1

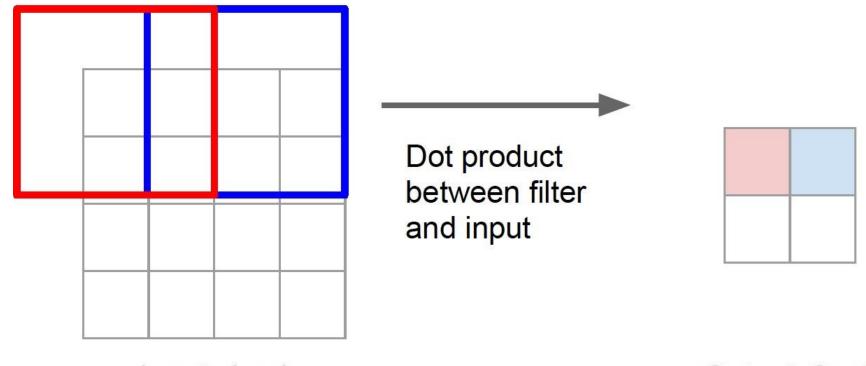


3 X 3 convolution with stride 2 and padding 1



Input: 4 x 4 Output: 2 x 2

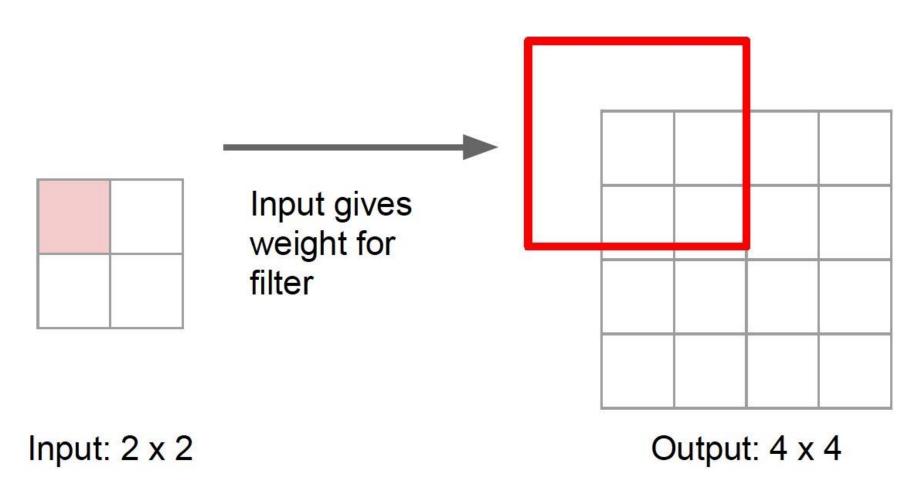
3 X 3 convolution with stride 2 and padding 1



Input: 4 x 4 Output: 2 x 2

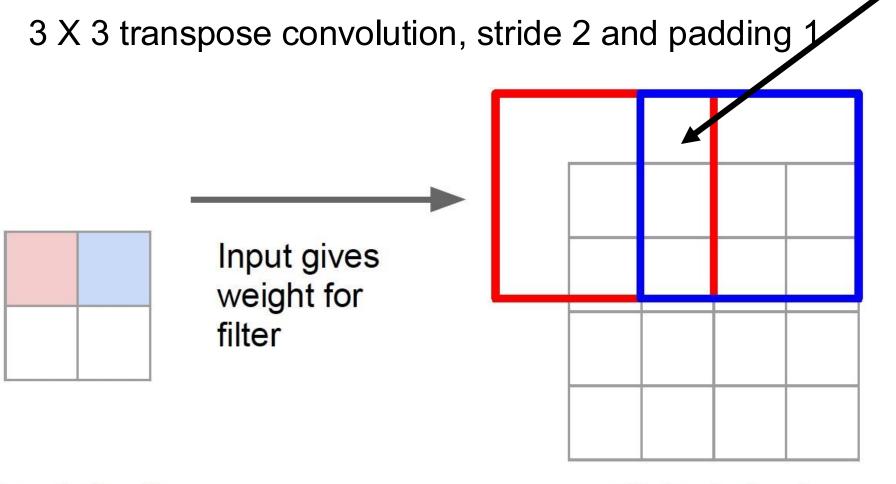
# **Transpose Convolution**

3 X 3 transpose convolution, stride 2 and padding 1



# **Transpose Convolution**

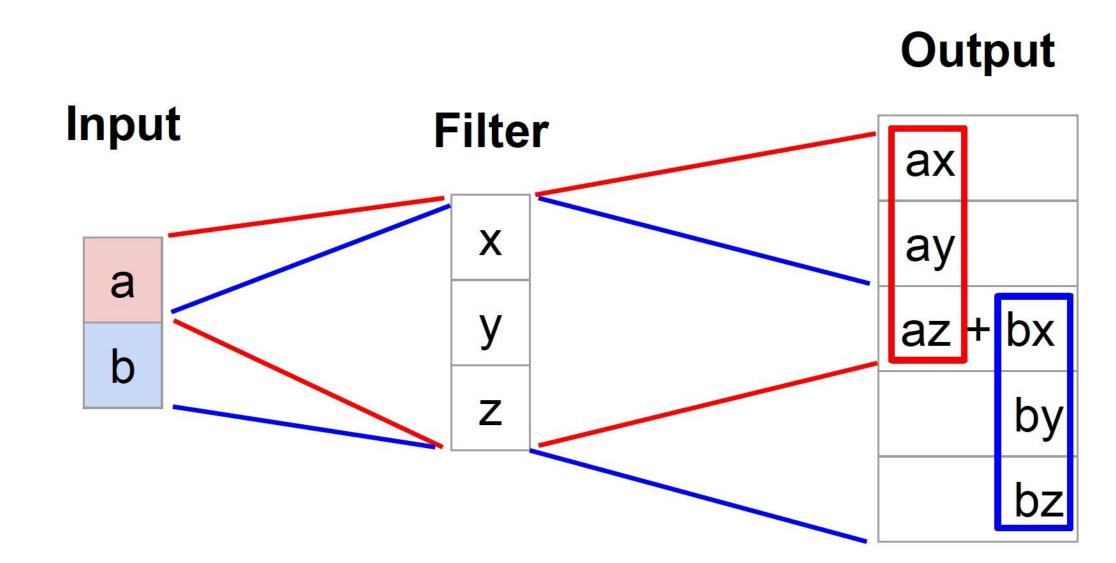
Sum over the overlapping region



Input: 2 x 2

Output: 4 x 4

## 1D Transpose Convolution Example



#### 2D Convolution

Regular convolution (stride 1, pad 0)

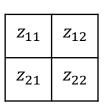
$x_{11}$	<i>x</i> <sub>12</sub>	<i>x</i> <sub>13</sub>	<i>x</i> <sub>14</sub>
$x_{21}$	$x_{22}$	$x_{23}$	$x_{24}$
$x_{31}$	<i>x</i> <sub>32</sub>	$x_{33}$	$x_{34}$
$x_{41}$	<i>x</i> <sub>42</sub>	<i>x</i> <sub>43</sub>	<i>x</i> <sub>44</sub>

#### Matrix-vector form:

$$\begin{bmatrix} w_{11} & w_{12} & w_{13} & 0 & w_{21} & w_{22} & w_{23} & 0 & w_{31} & w_{32} & w_{33} & 0 & 0 & 0 & 0 \\ 0 & w_{11} & w_{12} & w_{13} & 0 & w_{21} & w_{22} & w_{23} & 0 & w_{31} & w_{32} & w_{33} & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & w_{11} & w_{12} & w_{13} & 0 & w_{21} & w_{22} & w_{23} & 0 & w_{31} & w_{32} & w_{33} & 0 \\ 0 & 0 & 0 & 0 & 0 & w_{11} & w_{12} & w_{13} & 0 & w_{21} & w_{22} & w_{23} & 0 & w_{31} & w_{32} & w_{33} \\ 0 & 0 & 0 & 0 & 0 & w_{11} & w_{12} & w_{13} & 0 & w_{21} & w_{22} & w_{23} & 0 & w_{31} & w_{32} & w_{33} \\ \end{bmatrix} \begin{bmatrix} x_{11} \\ x_{12} \\ x_{13} \\ x_{14} \\ \vdots \\ x_{44} \end{bmatrix} = \begin{bmatrix} z_{11} \\ z_{12} \\ z_{21} \\ z_{22} \end{bmatrix}$$

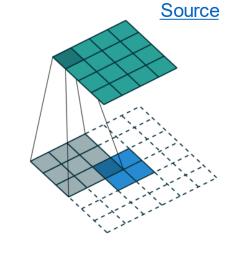
4x4 input, 2x2 output

## Transpose Convolution



 $x_{11} \\ x_{12}$ 

<i>x</i> <sub>11</sub>	<i>x</i> <sub>12</sub>	<i>x</i> <sub>13</sub>	<i>x</i> <sub>14</sub>
<i>x</i> <sub>21</sub>	<i>x</i> <sub>22</sub>	<i>x</i> <sub>23</sub>	<i>x</i> <sub>24</sub>
<i>x</i> <sub>31</sub>	x <sub>32</sub>	<i>x</i> <sub>33</sub>	<i>x</i> <sub>34</sub>
<i>x</i> <sub>41</sub>	<i>x</i> <sub>42</sub>	<i>x</i> <sub>43</sub>	<i>x</i> <sub>44</sub>



$\left( w_{11} \right)$	0	0	0	
$w_{12}$	$w_{11}$	0	0	
$w_{13}$	$w_{12}$	0	0	
0	$W_{13}$	0	0	
$w_{21}$	0	$w_{11}$	0	
$w_{22}$	$w_{21}$	$w_{12}$	$w_{11}$	
$w_{23}$	$w_{22}$	$w_{13}$	$w_{12}$	
0	$W_{23}$	0	$w_{13}$	
$w_{31}$	0	$w_{21}$	0	
$w_{32}$	$w_{31}$	$W_{22}$	$w_{21}$	
$W_{33}$	$W_{32}$	$w_{23}$	$w_{22}$	
0	$W_{33}$	0	$w_{23}$	
0	0	$w_{31}$	0	
0	0	$W_{32}$	$w_{31}$	
0	0	$W_{33}$	$w_{32}$	
0	0	0	$w_{33}$	

$$\begin{pmatrix}
z_{11} \\
z_{12} \\
z_{21} \\
z_{22}
\end{pmatrix} = \begin{pmatrix}
x_{13} \\
x_{24} \\
x_{23} \\
x_{24} \\
x_{31} \\
x_{32} \\
x_{33} \\
x_{34} \\
x_{41} \\
x_{42} \\
x_{43} \\
x_{44}
\end{pmatrix}$$

2x2 input, 4x4 output

*Not* an inverse of the original convolution operation, simply reverses dimension change!

#### $W_{32}$ $w_{31}$ Trans $w_{22} | w_{21}$ $w_{11}$ $w_{13}$ $w_{12}$

$z_{11}$	z <sub>12</sub>
z <sub>21</sub>	Z <sub>22</sub>

	<i>w</i> <sub>11</sub>	<i>w</i> <sub>12</sub>	<i>w</i> <sub>13</sub>
*T	<i>w</i> <sub>21</sub>	<i>w</i> <sub>22</sub>	$W_{23}$
	w <sub>31</sub>	<i>w</i> <sub>32</sub>	W <sub>33</sub>

=

 $x_{11} = w_{11} z_{11}$ 

<i>x</i> <sub>11</sub>	<i>x</i> <sub>12</sub>	<i>x</i> <sub>13</sub>	<i>x</i> <sub>14</sub>
<i>x</i> <sub>21</sub>	<i>x</i> <sub>22</sub>	<i>x</i> <sub>23</sub>	<i>x</i> <sub>24</sub>
<i>x</i> <sub>31</sub>	x <sub>32</sub>	<i>x</i> <sub>33</sub>	<i>x</i> <sub>34</sub>
<i>x</i> <sub>41</sub>	x <sub>42</sub>	<i>x</i> <sub>43</sub>	<i>x</i> <sub>44</sub>

, ,	-3

_					
1	/ W <sub>11</sub>	0	0	0 /	١
	$w_{12}$	$w_{11}$	0	0	
	$w_{13}$	$w_{12}$	0	0	
	0	$W_{13}$	0	0	
	$w_{21}$	0	$w_{11}$	0	
	$w_{22}$	$w_{21}$	$w_{12}$	$w_{11}$	
	$w_{23}$	$w_{22}$	$W_{13}$	$w_{12}$	
	0	$W_{23}$	0	$w_{13}$	
	$w_{31}$	0	$w_{21}$	0	
	$w_{32}$	$w_{31}$	$W_{22}$	$w_{21}$	
	$W_{33}$	$W_{32}$	$W_{23}$	$w_{22}$	
	0	$W_{33}$	0	$w_{23}$	
	0	0	$w_{31}$	0	
	0	0	$W_{32}$	$w_{31}$	
	0	0	$W_{33}$	$w_{32}$	
	0	0	0	$W_{33}$	
	\			/	

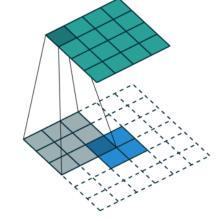
$$\begin{pmatrix}
z_{11} \\
z_{12} \\
z_{21} \\
z_{22}
\end{pmatrix} = \begin{pmatrix}
z_{11} \\
z_{22} \\
z_{23} \\
z_{24} \\
z_{31} \\
z_{32} \\
z_{33} \\
z_{34} \\
z_{41} \\
z_{42} \\
z_{43} \\
z_{44} \\
z_{44} \\
z_{45} \\
z_{$$

$$egin{array}{c} x_{11} \\ x_{12} \\ x_{13} \\ x_{14} \\ x_{21} \\ x_{22} \\ x_{23} \\ x_{24} \\ x_{31} \\ x_{32} \\ x_{33} \\ x_{34} \\ x_{41} \\ x_{42} \\ x_{43} \\ x_{44} \\ \end{pmatrix}$$

# Trans $\begin{bmatrix} w_{33} & w_{32} & w_{31} \\ w_{23} & w_{22} & w_{21} \end{bmatrix}$ Convolution $\begin{bmatrix} w_{13} & w_{12} & w_{11} \\ w_{13} & w_{12} & w_{11} \end{bmatrix}$

z <sub>11</sub>	Z <sub>12</sub>
z <sub>21</sub>	Z <sub>22</sub>

<i>x</i> <sub>11</sub>	<i>x</i> <sub>12</sub>	<i>x</i> <sub>13</sub>	<i>x</i> <sub>14</sub>
<i>x</i> <sub>21</sub>	<i>x</i> <sub>22</sub>	<i>x</i> <sub>23</sub>	<i>x</i> <sub>24</sub>
<i>x</i> <sub>31</sub>	x <sub>32</sub>	<i>x</i> <sub>33</sub>	<i>x</i> <sub>34</sub>
<i>x</i> <sub>41</sub>	<i>x</i> <sub>42</sub>	<i>x</i> <sub>43</sub>	<i>x</i> <sub>44</sub>



_						
	$\left( w_{11} \right)$	0	0	0	/	$x_{11}$
	$w_{12}$	$w_{11}$	0	0		$x_{12}$
	$w_{13}$	$w_{12}$	0	0		$x_{13}$
	0	$W_{13}$	0	0		$x_{14}$
	$w_{21}$	0	$w_{11}$	0		$x_{21}$
	$w_{22}$	$w_{21}$	$W_{12}$	$w_{11}$	$  (z_{11})  $	$x_{22}$
	<i>w</i> <sub>23</sub>	$w_{22}$	$W_{13}$	$w_{12}$		$x_{23}$
	0	$W_{23}$	0	$w_{13}$	$\begin{vmatrix} z_{12} \\ z_{12} \end{vmatrix} =$	$x_{24}$
	<i>w</i> <sub>31</sub>	0	$w_{21}$	0	$  z_{21}  $	$x_{31}$
	$w_{32}$	$w_{31}$	$w_{22}$	$w_{21}$	$  Z_{22}  $	$x_{32}$
	$W_{33}$	$W_{32}$	$w_{23}$	$w_{22}$		
	0	$W_{33}$	0	$w_{23}$		$x_{33}$
	0	0	$w_{31}$	0		$x_{34}$
	0	0	$W_{32}$	$w_{31}$		$x_{41}$
	0	0	$W_{33}$	$W_{32}$		$x_{42}$
	0	0	0	$W_{33}$	)	$x_{43}$
					<i>'</i>	$\chi_{44}$

$$\begin{array}{c|c}
x_{11} \\
x_{12} \\
x_{13} \\
x_{14} \\
x_{21} \\
x_{22} \\
x_{23} \\
x_{24} \\
x_{31} \\
x_{32} \\
x_{33} \\
x_{34} \\
x_{41} \\
x_{42} \\
x_{43} \\
\end{array}$$

#### $W_{31}$ prodution Transpo $w_{21}$

 $W_{12}$  $w_{11}$ 

<i>z</i> <sub>11</sub>	<i>z</i> <sub>12</sub>
<i>z</i> <sub>21</sub>	Z <sub>22</sub>

 $_*T$ 

<i>w</i> <sub>11</sub>	<i>w</i> <sub>12</sub>	<i>w</i> <sub>13</sub>
<i>w</i> <sub>21</sub>	<i>w</i> <sub>22</sub>	$w_{23}$
<i>w</i> <sub>31</sub>	$w_{32}$	$W_{33}$

 $x_{14}$  $x_{21}$ 

 $x_{22}$  $x_{23}$ 

 $x_{24}$ 

 $x_{31}$ 

 $\chi_{32}$ 

 $\chi_{33}$ 

 $x_{34}$ 

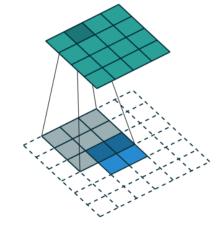
 $x_{41}$ 

 $x_{42}$ 

 $x_{43}$ 

 $x_{44}$ 

<i>x</i> <sub>11</sub>	x <sub>12</sub>	<i>x</i> <sub>13</sub>	<i>x</i> <sub>14</sub>
<i>x</i> <sub>21</sub>	<i>x</i> <sub>22</sub>	$x_{23}$	<i>x</i> <sub>24</sub>
<i>x</i> <sub>31</sub>	x <sub>32</sub>	<i>x</i> <sub>33</sub>	<i>x</i> <sub>34</sub>
<i>x</i> <sub>41</sub>	x <sub>42</sub>	<i>x</i> <sub>43</sub>	x <sub>44</sub>



/	$w_{11}$	0	0	0	<u> </u>	$\int x_{11}$
			^	^		

 $W_{33}$ 

$w_{12}$	$w_{11}$	U	U
$W_{13}$	$w_{12}$	Ü	Ü
0	$W_{13}$	0	0
$w_{21}$	0	$w_{11}$	0
$w_{22}$	$w_{21}$	$w_{12}$	$w_{11}$
$w_{23}$	$w_{22}$	$w_{13}$	$w_{12}$

$$\begin{pmatrix} z_{11} \\ z_{12} \\ z_{21} \\ z_{22} \end{pmatrix} =$$

Convolve input with *flipped* filter
$$x_{12}$$

$$x_{13}$$

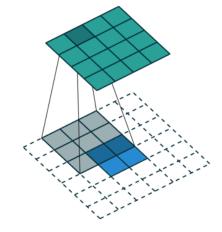
$$x_{13}$$

$$x_{14} = w_{12}z_{11} + w_{11}z_{12}$$



$z_{11}$	z <sub>12</sub>
$z_{21}$	Z <sub>22</sub>

x <sub>11</sub>	x <sub>12</sub>	<i>x</i> <sub>13</sub>	<i>x</i> <sub>14</sub>
x <sub>21</sub>	<i>x</i> <sub>22</sub>	<i>x</i> <sub>23</sub>	<i>x</i> <sub>24</sub>
x <sub>31</sub>	x <sub>32</sub>	<i>x</i> <sub>33</sub>	x <sub>34</sub>
<i>x</i> <sub>41</sub>	<i>x</i> <sub>42</sub>	<i>x</i> <sub>43</sub>	<i>x</i> <sub>44</sub>



)	0	0	$(x_{11})$	Convolve input with <i>flipped</i> filter
	Λ	Λ	24	

$$x_{12} = w_{12}z_{11} + w_{11}z_{12}$$

	$^{-12}$
	$x_{13}$
	$x_{14}$
	$x_{21}$
$Z_{11}$	$x_{22}$
$z_{12}$	$x_{23}$
	$x_{24}$
$Z_{21}$	$x_{31}$
$Z_{22}$	$x_{32}$
	$x_{33}$
	$x_{34}$
	$x_{41}$
	$x_{42}$
	$x_{43}$
	$x_{44}$

# Transpos



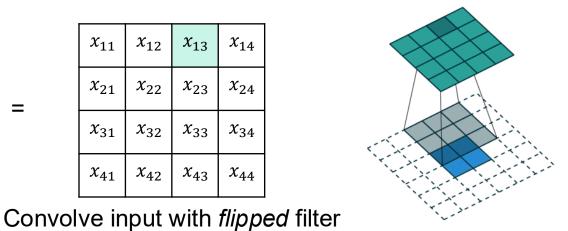
<i>w</i> <sub>13</sub>	<i>w</i> <sub>12</sub>	$w_{11}$

$z_{11}$	z <sub>12</sub>
z <sub>21</sub>	Z <sub>22</sub>

<i>w</i> <sub>11</sub>	<i>w</i> <sub>12</sub>	<i>w</i> <sub>13</sub>
w <sub>21</sub>	w <sub>22</sub>	<i>W</i> <sub>23</sub>
w <sub>31</sub>	<i>w</i> <sub>32</sub>	W <sub>33</sub>

_	_	
=	=	

<i>x</i> <sub>11</sub>	<i>x</i> <sub>12</sub>	<i>x</i> <sub>13</sub>	<i>x</i> <sub>14</sub>
<i>x</i> <sub>21</sub>	<i>x</i> <sub>22</sub>	<i>x</i> <sub>23</sub>	<i>x</i> <sub>24</sub>
<i>x</i> <sub>31</sub>	x <sub>32</sub>	<i>x</i> <sub>33</sub>	<i>x</i> <sub>34</sub>
<i>x</i> <sub>41</sub>	x <sub>42</sub>	x <sub>43</sub>	x <sub>44</sub>



$$\begin{array}{ccccccc} w_{23} & w_{22} & w_{13} & w_{12} \\ 0 & w_{23} & 0 & w_{13} \\ w_{31} & 0 & w_{21} & 0 \\ w_{32} & w_{31} & w_{22} & w_{21} \end{array}$$

U	U	$w_{31}$	U
0	0	$w_{32}$	$w_{31}$
0	0	$w_{33}$	$w_{32}$

$$\begin{pmatrix} x_{11} \\ x_{12} \end{pmatrix}$$

$$x_{13}$$
 $x_{14}$ 

$$= \begin{array}{c|c} x_{21} \\ x_{22} \\ x_{23} \\ x_{24} \\ x_{31} \\ x_{32} \end{array}$$

 $z_{11}$ 

 $Z_{12}$ 

 $z_{21}$ 

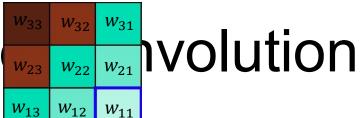
 $Z_{22}$ 

$$x_{23}$$
 $x_{24}$ 
 $x_{31}$ 
 $x_{32}$ 
 $x_{33}$ 
 $x_{34}$ 
 $x_{41}$ 
 $x_{42}$ 
 $x_{43}$ 

 $x_{44}$ 

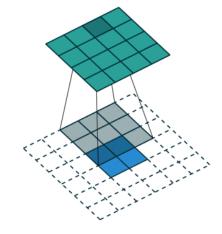
$$x_{13} = w_{13}z_{11} + w_{12}z_{12}$$

# Transpos



Z <sub>11</sub>	Z <sub>12</sub>
z <sub>21</sub>	Z <sub>22</sub>

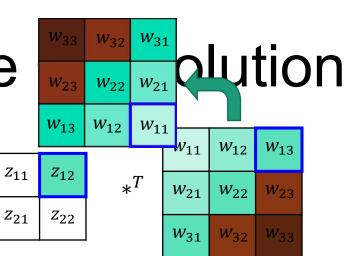
x <sub>11</sub>	<i>x</i> <sub>12</sub>	<i>x</i> <sub>13</sub>	<i>x</i> <sub>14</sub>
x <sub>21</sub>	<i>x</i> <sub>22</sub>	<i>x</i> <sub>23</sub>	<i>x</i> <sub>24</sub>
x <sub>31</sub>	x <sub>32</sub>	<i>x</i> <sub>33</sub>	x <sub>34</sub>
<i>x</i> <sub>41</sub>	<i>x</i> <sub>42</sub>	<i>x</i> <sub>43</sub>	<i>x</i> <sub>44</sub>



$$x_{13} = w_{13}z_{11} + w_{12}z_{12}$$

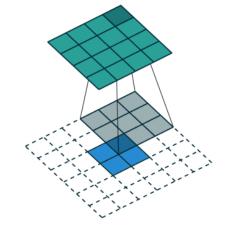
$$egin{array}{c} x_{11} \\ x_{12} \\ \hline x_{13} \\ \hline x_{14} \\ x_{21} \\ x_{22} \\ x_{23} \\ x_{24} \\ x_{31} \\ x_{32} \\ x_{33} \\ x_{34} \\ x_{41} \\ x_{42} \\ x_{43} \\ x_{44} \\ \hline \end{array}$$

# Transpose



 $x_{11}$ 

x <sub>11</sub>	<i>x</i> <sub>12</sub>	<i>x</i> <sub>13</sub>	<i>x</i> <sub>14</sub>
x <sub>21</sub>	<i>x</i> <sub>22</sub>	<i>x</i> <sub>23</sub>	<i>x</i> <sub>24</sub>
x <sub>31</sub>	x <sub>32</sub>	<i>x</i> <sub>33</sub>	x <sub>34</sub>
x <sub>41</sub>	x <sub>42</sub>	<i>x</i> <sub>43</sub>	x <sub>44</sub>



olve input with *flipped* filter

$$\begin{pmatrix} w_{11} & 0 & 0 & 0 \\ w_{12} & w_{11} & 0 & 0 \\ w_{13} & w_{12} & 0 & 0 \\ 0 & w_{13} & 0 & 0 \\ \end{pmatrix}$$

$$\begin{pmatrix} w_{21} & 0 & w_{11} & 0 \\ w_{22} & w_{21} & w_{12} & w_{11} \\ w_{23} & w_{22} & w_{13} & w_{12} \\ 0 & w_{23} & 0 & w_{13} \\ w_{31} & 0 & w_{21} & 0 \\ w_{32} & w_{31} & w_{22} & w_{21} \\ w_{33} & w_{32} & w_{23} & w_{22} \\ 0 & w_{33} & 0 & w_{23} \\ 0 & 0 & w_{31} & 0 \\ 0 & 0 & w_{32} & w_{31} \\ 0 & 0 & w_{33} & w_{32} \\ 0 & 0 & 0 & w_{33} \end{pmatrix}$$

$$x_{12}$$
 $x_{13}$ 
 $x_{14}$ 
 $x_{21}$ 
 $x_{22}$ 
 $x_{23}$ 
 $x_{24}$ 
 $x_{31}$ 
 $x_{32}$ 
 $x_{33}$ 
 $x_{34}$ 
 $x_{41}$ 
 $x_{42}$ 
 $x_{43}$ 

 $x_{44}$ 

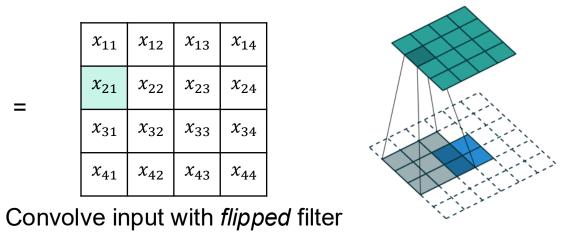
$$x_{14} = w_{13} z_{12}$$

#### $W_{31}$ Trans nvelution $W_{13}$ $w_{11}$ $W_{12}$

$z_{11}$	$z_{12}$
$z_{21}$	$Z_{22}$

<i>w</i> <sub>11</sub>	w <sub>12</sub>	<i>w</i> <sub>13</sub>
<i>w</i> <sub>21</sub>	<i>w</i> <sub>22</sub>	$W_{23}$
<i>w</i> <sub>31</sub>	$w_{32}$	$W_{33}$

<i>x</i> <sub>11</sub>	<i>x</i> <sub>12</sub>	<i>x</i> <sub>13</sub>	<i>x</i> <sub>14</sub>
<i>x</i> <sub>21</sub>	<i>x</i> <sub>22</sub>	<i>x</i> <sub>23</sub>	<i>x</i> <sub>24</sub>
<i>x</i> <sub>31</sub>	x <sub>32</sub>	<i>x</i> <sub>33</sub>	<i>x</i> <sub>34</sub>
<i>x</i> <sub>41</sub>	x <sub>42</sub>	<i>x</i> <sub>43</sub>	<i>x</i> <sub>44</sub>



$\left( w_{11} \right)$	0	0	0 /	<b>)</b>
$w_{12}$	$w_{11}$	0	0	
$w_{13}$	$w_{12}$	0	0	
0	$W_{13}$	0	0	
<i>w</i> <sub>21</sub>	0	$w_{11}$	0	
w <sub>22</sub>	$w_{21}$	$w_{12}$	$w_{11}$	$\left(z_{11}\right)$
$w_{23}$	$w_{22}$	$w_{13}$	$w_{12}$	
0	$w_{23}$	0	$w_{13}$	$  z_{12}  $
<i>w</i> <sub>31</sub>	0	$w_{21}$	0	$   z_{21}$
$w_{32}$	$w_{31}$	$w_{22}$	$w_{21}$	$  z_{22}  $
$w_{33}$	$w_{32}$	$w_{23}$	$w_{22}$	
0	$W_{33}$	0	$w_{23}$	
0	0	$w_{31}$	0	

 $w_{32}$ 

 $w_{31}$ 

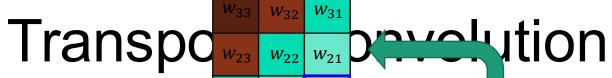
 $W_{32}$ 

 $W_{33}$ 

$$egin{array}{c} x_{12} \\ x_{13} \\ x_{14} \\ \hline x_{21} \\ x_{22} \\ x_{23} \\ x_{24} \\ x_{31} \\ x_{32} \\ x_{33} \\ x_{34} \\ x_{41} \\ x_{42} \\ x_{43} \\ x_{44} \\ \hline \end{array}$$

 $x_{11}$ 

$$x_{21} = w_{21}z_{11} + w_{11}z_{21}$$



 $W_{12}$  $w_{11}$ 

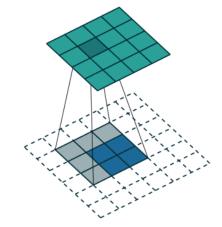
Z <sub>11</sub>	Z <sub>12</sub>
Z <sub>21</sub>	z <sub>22</sub>

\*T

<i>w</i> <sub>11</sub>	<i>w</i> <sub>12</sub>	<i>w</i> <sub>13</sub>
<i>w</i> <sub>21</sub>	<i>w</i> <sub>22</sub>	W <sub>23</sub>
<i>w</i> <sub>31</sub>	$w_{32}$	$W_{33}$

<i>x</i> <sub>11</sub>	<i>x</i> <sub>12</sub>	<i>x</i> <sub>13</sub>	<i>x</i> <sub>14</sub>
<i>x</i> <sub>21</sub>	<i>x</i> <sub>22</sub>	<i>x</i> <sub>23</sub>	<i>x</i> <sub>24</sub>
<i>x</i> <sub>31</sub>	x <sub>32</sub>	<i>x</i> <sub>33</sub>	<i>x</i> <sub>34</sub>
<i>x</i> <sub>41</sub>	x <sub>42</sub>	<i>x</i> <sub>43</sub>	<i>x</i> <sub>44</sub>

Convolve input with flipped filter



$$\begin{vmatrix} w_{11} & 0 & 0 & 0 \\ w_{12} & w_{11} & 0 & 0 \\ w_{13} & w_{12} & 0 & 0 \\ 0 & w_{13} & 0 & 0 \\ \cdots & & & & 0 \end{vmatrix}$$

$W_{22}$	$w_{21}$	$w_{12}$	$w_{11}$
$w_{23}$	$w_{22}$	$w_{13}$	$W_{12}$
0	$w_{23}$	0	$W_{13}$
$w_{31}$	0	$w_{21}$	0

$$egin{array}{ccccc} w_{32} & w_{31} & w_{22} & w_{21} \\ w_{33} & w_{32} & w_{23} & w_{22} \\ 0 & w_{33} & 0 & w_{23} \\ \end{array}$$

0	0	$w_{31}$	0
0	0	$w_{32}$	$w_{31}$
0	0	$W_{33}$	$W_{32}$

$$0 0 0 w_{33} w_{32}$$

$$\begin{cases}
 x_{11} \\
 x_{12} \\
 x_{13}
 \end{cases}$$

 $x_{14}$  $x_{21}$ 

 $x_{22}$ 

$z_{11}$	
$z_{12}$	_
$z_{21}$	

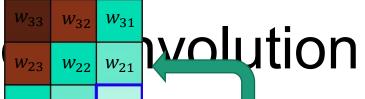
 $Z_{22}$ 

$$egin{array}{c} x_{23} \\ x_{24} \\ x_{31} \\ x_{32} \\ x_{33} \\ x_{34} \\ x_{41} \\ x_{42} \\ x_{43} \\ \end{array}$$

 $x_{44}$ 

$$x_{22} = w_{22}z_{11} + w_{21}z_{12} + w_{12}z_{21} + w_{11}z_{22}$$

# Transpos



 $*^T$ 

w13	W12	VV
Z <sub>1.1</sub>	Z <sub>12</sub>	

 $egin{array}{cccc} z_{12} & & & & & & \\ z_{1} & z_{22} & & & & & \\ \end{array}$ 

<i>w</i> <sub>11</sub>	<i>w</i> <sub>12</sub>	<i>w</i> <sub>13</sub>
w <sub>21</sub>	w <sub>22</sub>	<i>w</i> <sub>23</sub>
<i>w</i> <sub>31</sub>	$w_{32}$	W <sub>33</sub>

 $x_{11}$ 

 $x_{12}$ 

 $x_{13}$ 

 $x_{14}$ 

 $x_{21}$ 

 $x_{22}$ 

 $x_{23}$ 

 $x_{24}$ 

 $x_{31}$ 

 $\chi_{32}$ 

 $\chi_{33}$ 

 $\chi_{34}$ 

 $x_{41}$ 

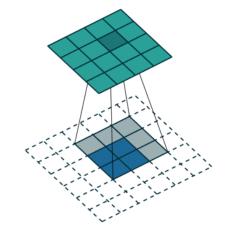
 $x_{42}$ 

 $\chi_{43}$ 

 $x_{44}$ 

_	_
	=
	=

<i>x</i> <sub>11</sub>	<i>x</i> <sub>12</sub>	<i>x</i> <sub>13</sub>	<i>x</i> <sub>14</sub>
<i>x</i> <sub>21</sub>	<i>x</i> <sub>22</sub>	<i>x</i> <sub>23</sub>	<i>x</i> <sub>24</sub>
<i>x</i> <sub>31</sub>	x <sub>32</sub>	<i>x</i> <sub>33</sub>	<i>x</i> <sub>34</sub>
<i>x</i> <sub>41</sub>	x <sub>42</sub>	<i>x</i> <sub>43</sub>	<i>x</i> <sub>44</sub>

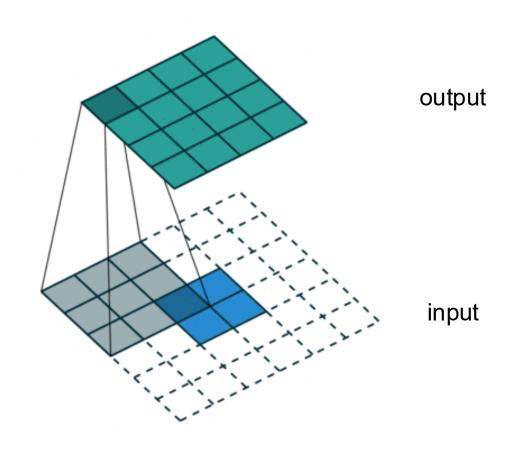


Convolve input with flipped filter

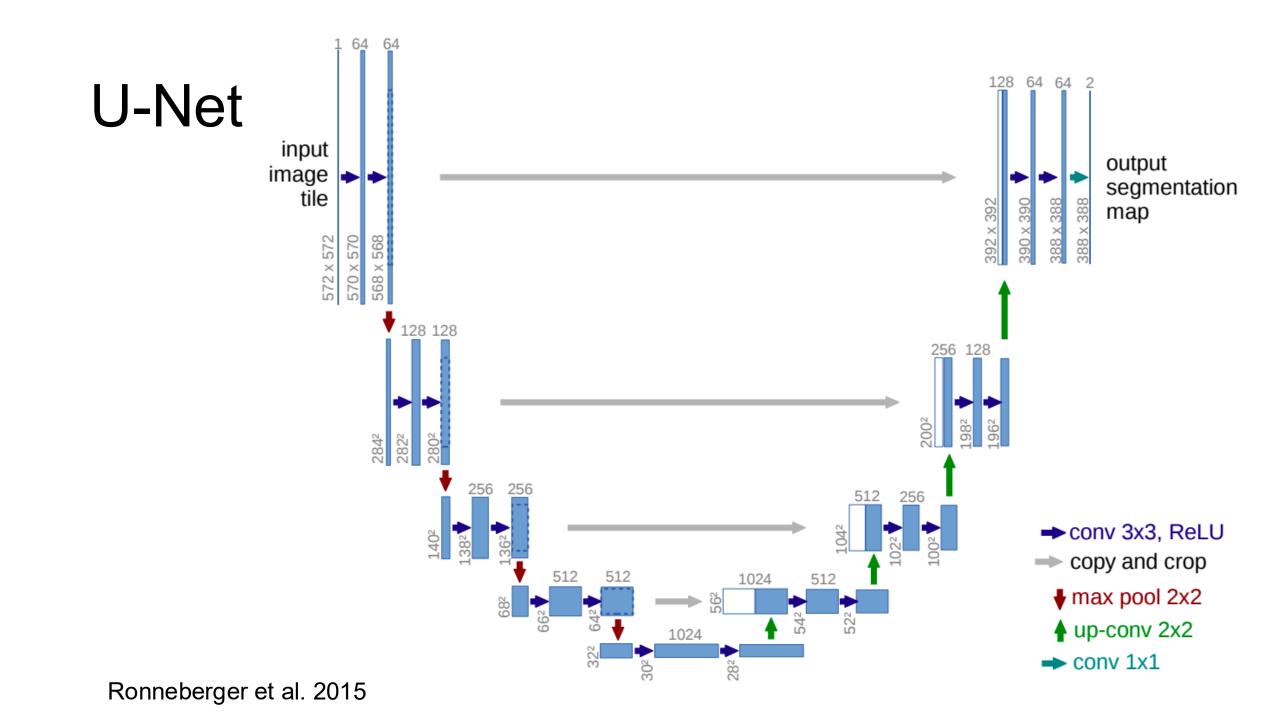
$$\begin{pmatrix} w_{11} & 0 & 0 & 0 \\ w_{12} & w_{11} & 0 & 0 \\ w_{13} & w_{12} & 0 & 0 \\ 0 & w_{13} & 0 & 0 \\ w_{21} & 0 & w_{11} & 0 \\ w_{22} & w_{21} & w_{12} & w_{11} \\ \hline & w_{23} & w_{22} & w_{13} & w_{12} \\ \hline & 0 & w_{23} & 0 & w_{13} \\ w_{31} & 0 & w_{21} & 0 \\ w_{32} & w_{31} & w_{22} & w_{21} \\ w_{33} & w_{32} & w_{23} & w_{22} \\ 0 & w_{33} & 0 & w_{23} \\ 0 & 0 & w_{31} & 0 \\ 0 & 0 & w_{32} & w_{31} \\ 0 & 0 & w_{33} & w_{32} \\ 0 & 0 & 0 & w_{33} \end{pmatrix} = \begin{bmatrix} Z_{11} \\ Z_{21} \\ Z_{22} \end{bmatrix} =$$

$$x_{23} = w_{23}z_{11} + w_{22}z_{12} + w_{13}z_{21} + w_{12}z_{22}$$

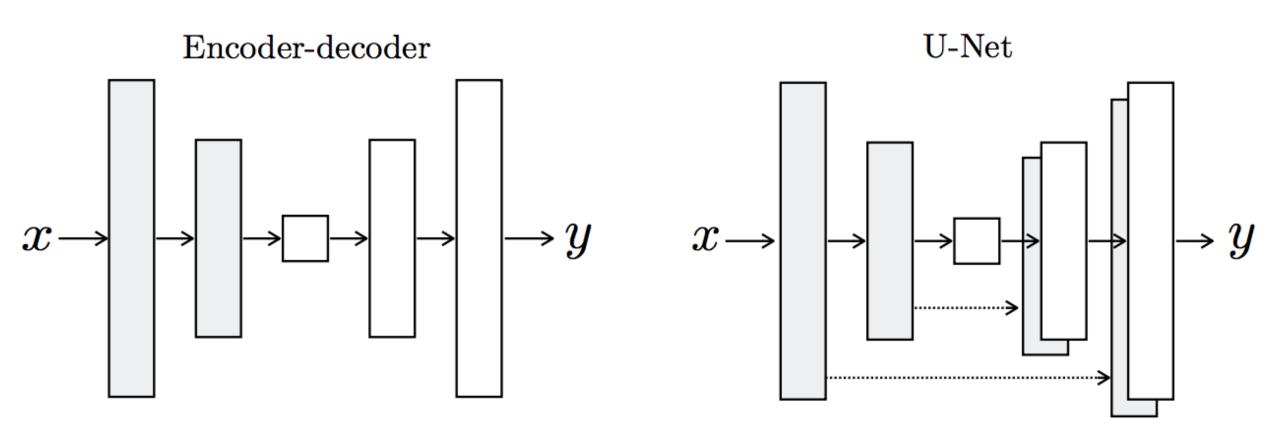
# **Transpose Convolution**



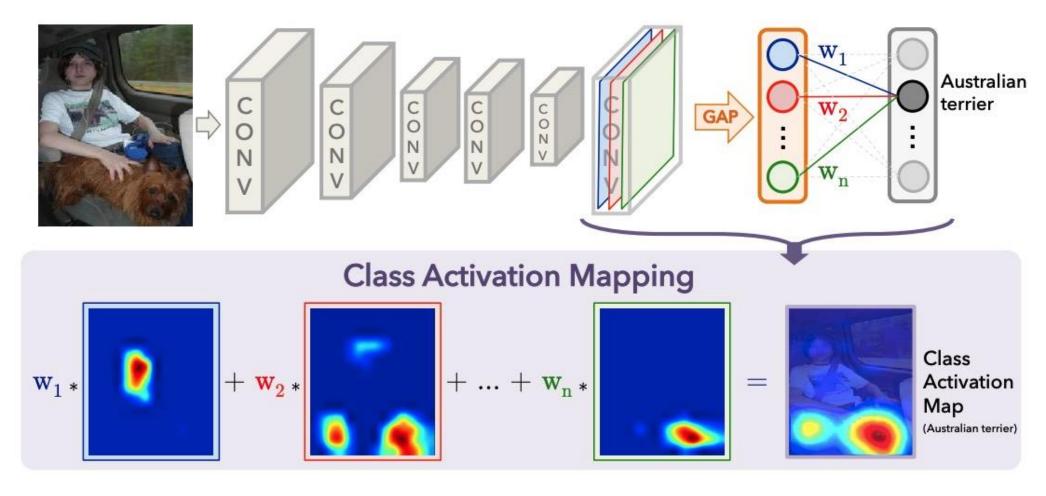
# Advanced Techniques in Segmentation



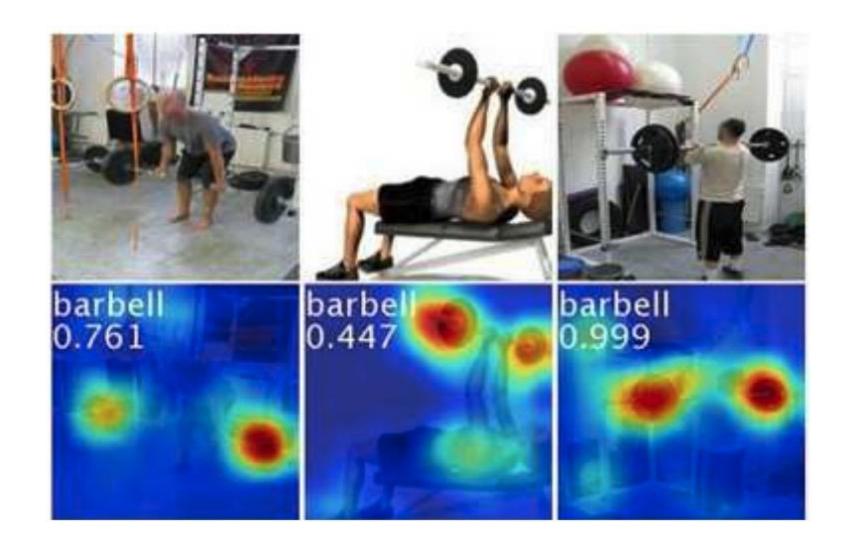
## **U-Net**



# Visualizing Deep Networks using "Saliency map"



Zhou et al. 2016







# Visualizing Deep Networks by maximizing activation

### Visualization by optimization

 We can synthesize images that maximize activation of a given neuron.

• Find image x maximizing target activation f(x) subject to natural image regularization penalty R(x):

$$x^* = \arg\max_{x} f(x) - \lambda R(x)$$

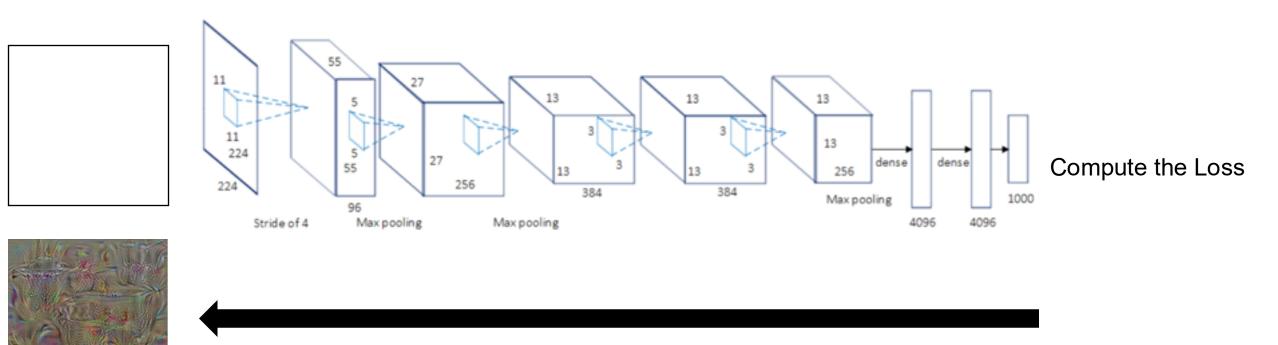
#### Visualization by optimization

- Maximize  $f(x) \lambda R(x)$ 
  - f(x) is score for a category before softmax
  - R(x) is L2 regularization
  - Perform gradient ascent starting with zero image, add dataset mean to result



Simonyan et al. 2014

#### Visualization by optimization

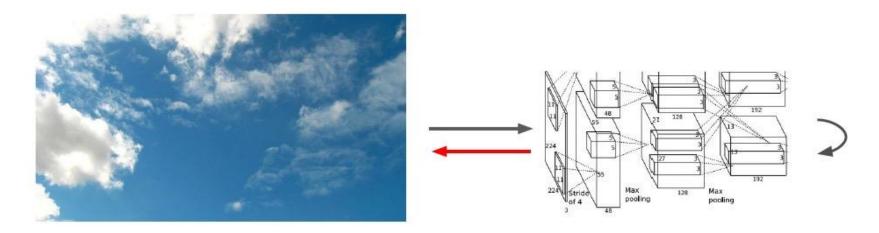


BP the gradients, but do not train the network

Keep adding/aggregating the gradients under constraint R(x)

### Google DeepDream

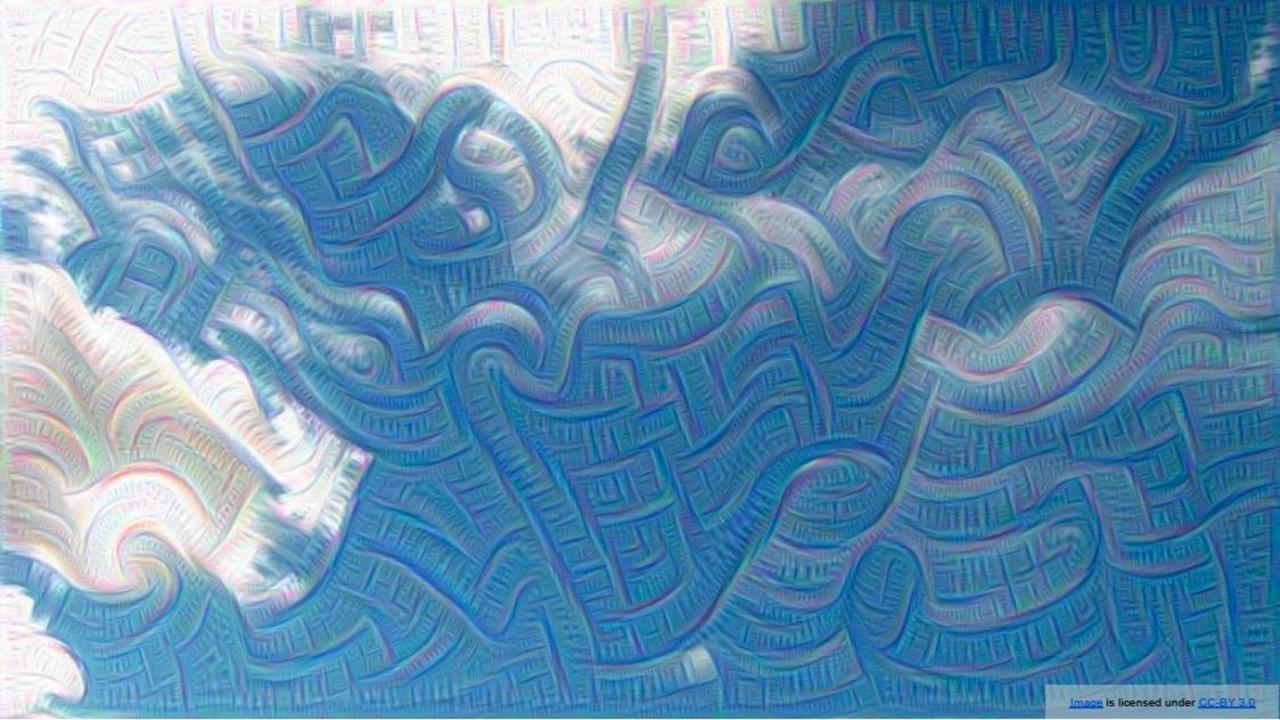
Amplify one layer instead of just one neuron.

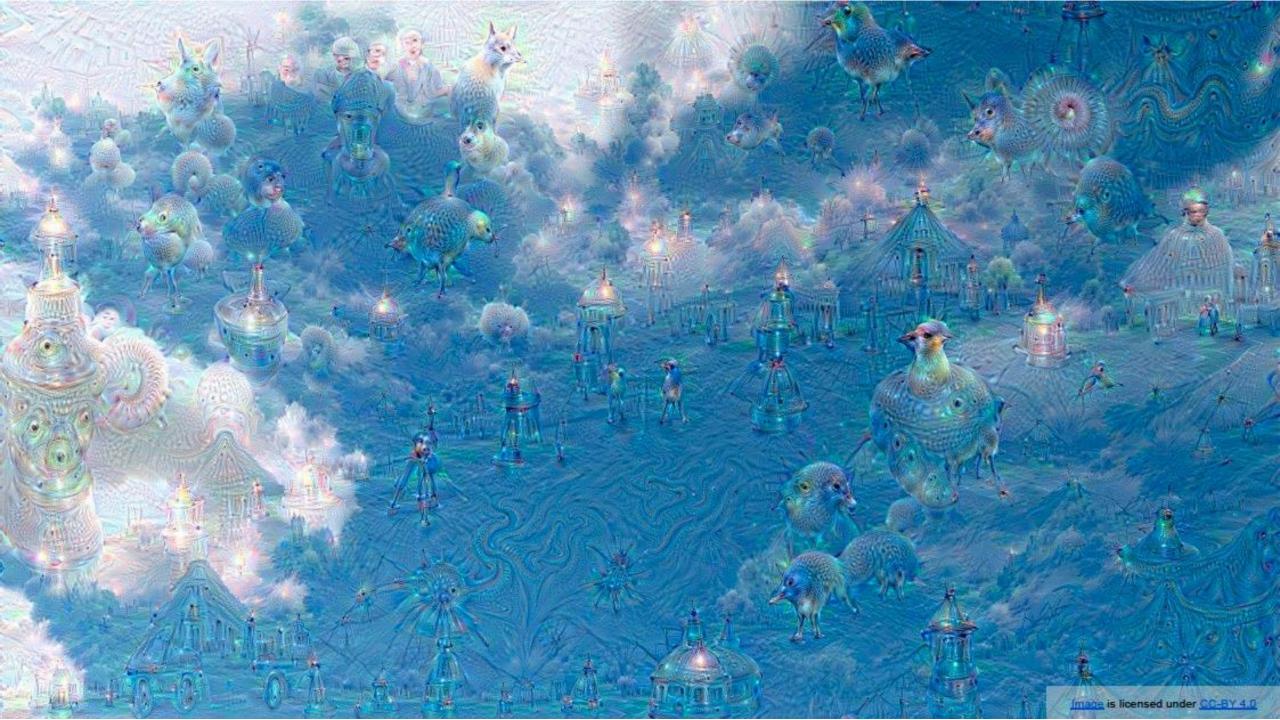


#### Choose an image and a layer in a CNN; repeat:

- 1. Forward: compute activations at chosen layer
- 2. Set gradient of chosen layer equal to its activation Equivalent to maximizing  $\sum_{i} f_{i}^{2}(x)$
- 3. Backward: Compute gradient w.r.t. image
- 4. Update image (with some tricks)





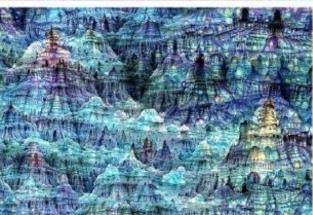


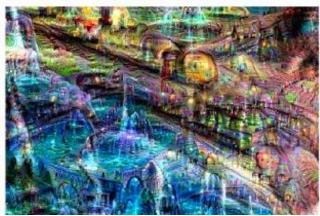
















#### **Next Class**

**Object Detection**