

# Advanced Process Mining

Sommer term 2020

## Exercise sheet 3

DFG Limitations • DFG Soundness • DFG to PNG

# Limitations of the Directly-Follows Graph

## Exercise 1a

#	Trace
100	abcef
90	abecf
87	abdef
85	abedf
3	abef
1	abcdef

Draw a Directly-Follows Graph for the event log above.

# Limitations of the Directly-Follows Graph

## Exercise 1a

Given the event log. create a directly follows graph for traces observed:

1. Create a table with pairs of consecutive activities and their quantity

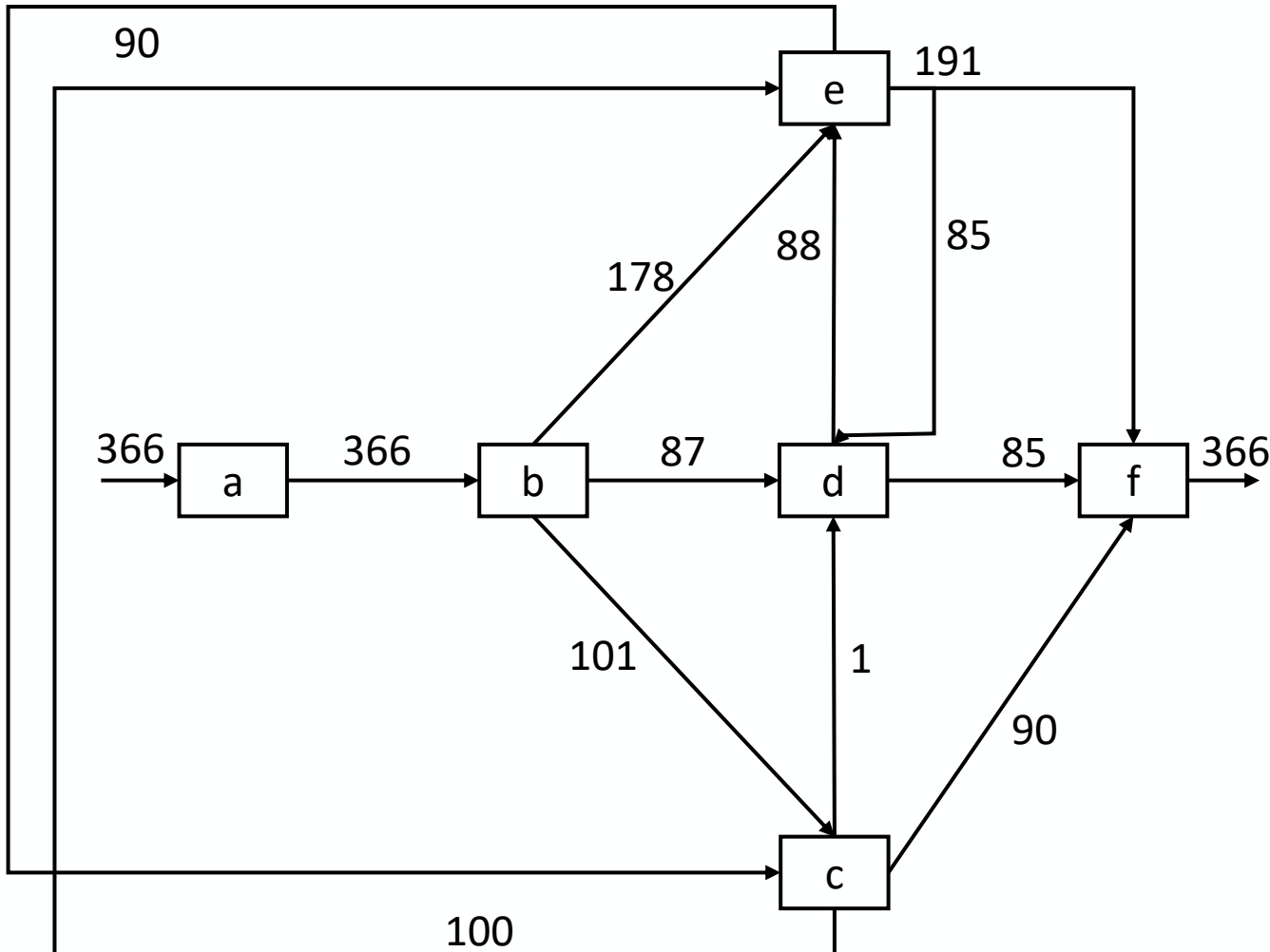
> <sub>L</sub>	a	b	c	d	e	f	E
s	366						
a		366					
b			101	87	178		
c				1	100	90	
d					88	85	
e			90	85		191	
f							366

#	Trace
100	abcef
90	abecf
87	abdef
85	abedf
3	abef
1	abcdef

# Limitations of the Directly-Follows Graph

## Exercise 1a

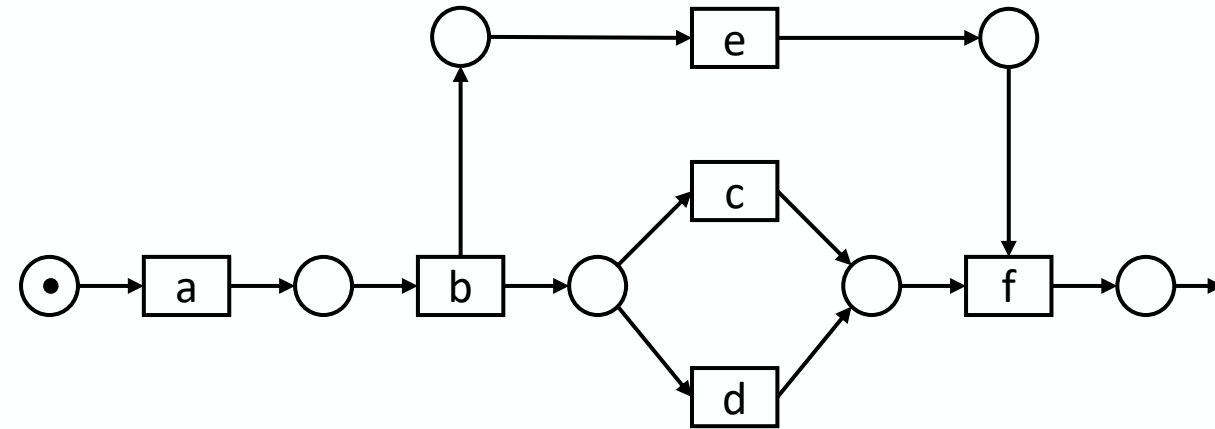
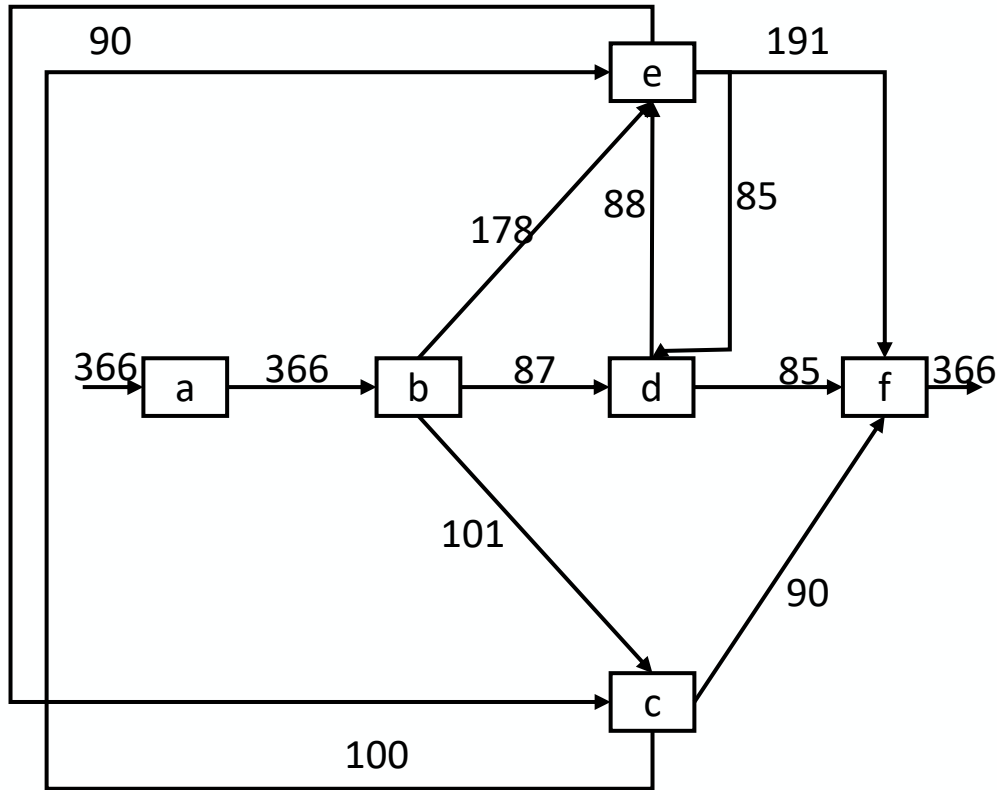
2. Draw the Directly-Follows Graph from the collected information in the table:



$>_L$	a	b	c	d	e	f	E
s	366						
a		366					
b			101	87	178		
c				1	100	90	
d					88	85	
e			90	85		191	
f							366

# Limitations of the Directly-Follows Graph

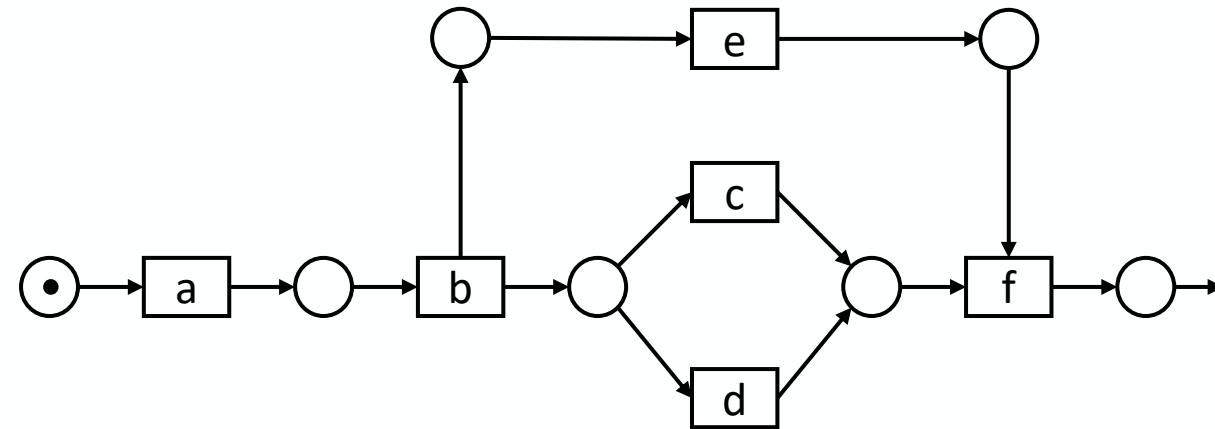
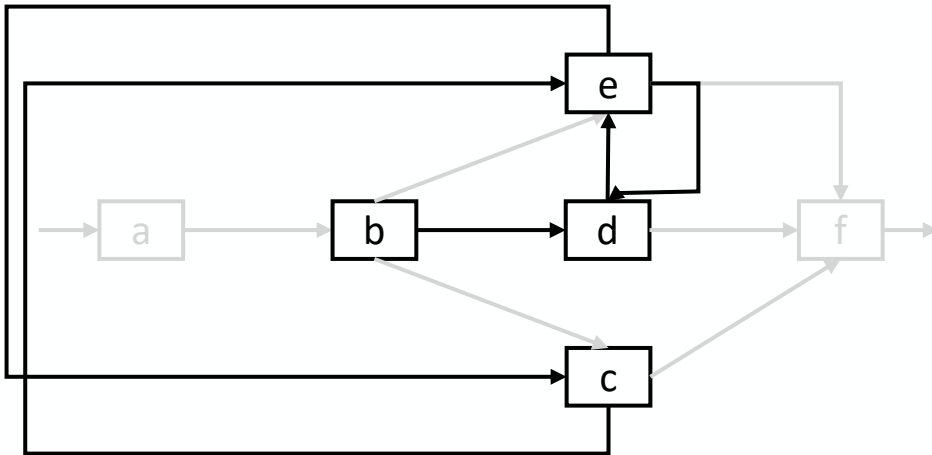
## Exercise 1b



Compare the Directly-Follows Graph with the Petri net above.  
Does the DFG allow for behaviour that is not allowed according to the Petri net?

# Limitations of the Directly-Follows Graph

## Exercise 1b



The Directly-Follows Graph allows for a loop involving activities c, d and e. The Petri net from which the event log was created does not permit any loops involving activities c and d. According to the Petri net there is an exclusive choice between c and d.

# Limitations of the Directly-Follows Graph

## Exercise 1c

Explain the following thresholds:

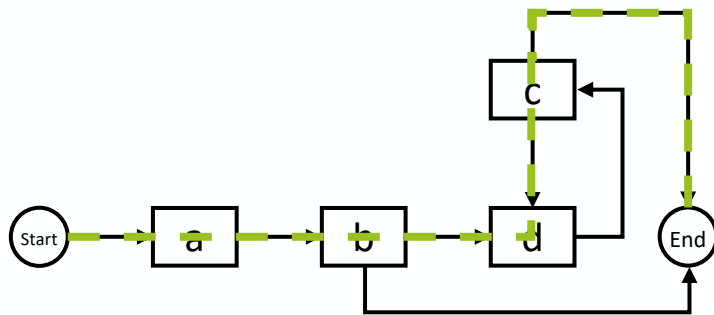
$\tau_{var}$	Defines the thresholds for the minimal number of traces for each variant included (based on $\#_L(\sigma)$ ).
$\tau_{act}$	Defines the minimal number of events for each activity included (based on $\#_L(a)$ ).
$\tau_{df}$	Defines the minimal number of direct successions for each relation included (based on $\#_L(a, b)$ ).

# Soundness in Directly-Follows Graphs

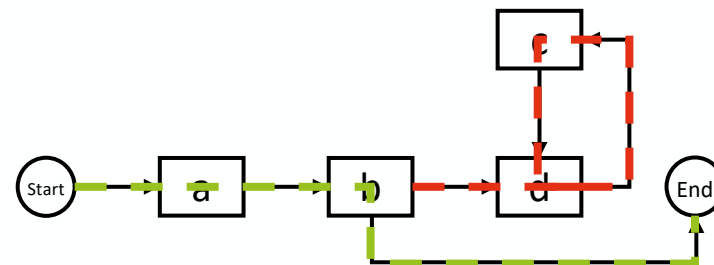
## Exercise 2a

Define soundness in DFG in a non-formal way.

A DFG with  $N$  (the set of nodes) and  $E$  (the set of edges) is sound, if every node  $x \in N$  is on a path from start to end.



Sound



Unsound

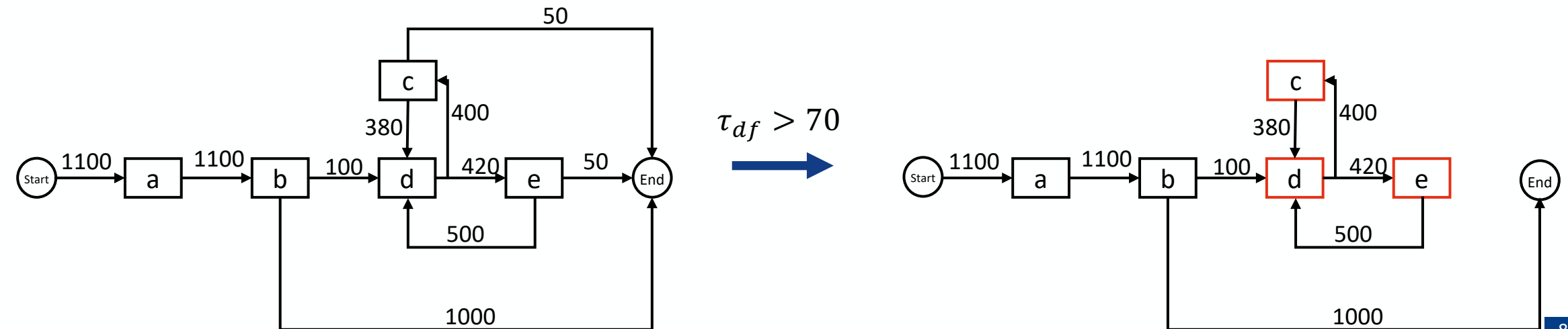


# Soundness in Directly-Follows Graphs

## Exercise 2b

How can a sound DFG be turned into an unsound Graph?

To reduce the complexity of a DFG, edges might be filtered out, possibly resulting in deadlocks and an unsound Graph.



In order to compute performance measures, each transition has to be modelled as a start and end event.

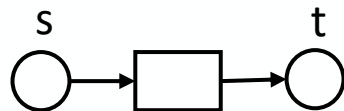
Source: DFM consisting of  $(N, E)$

Target: PN consisting of  $(P, T, F)$

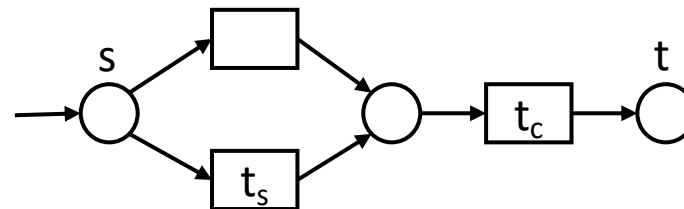
For each edge  $(s, t) \in E$  subgraphs will be created.

There is a differentiation between the *end node* and the other nodes:

If  $t$  is *end*

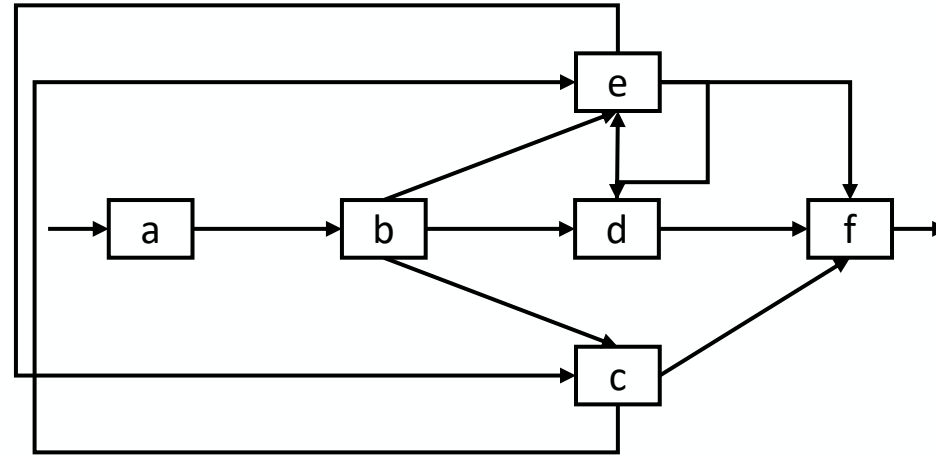


If  $t$  is not *end*



# Transformation from DFG to PN

## Exercise 3



Transform the DFG above into a Petri net.

Model each transition as a combination of start and end event.

# Transformation from DFG to PN

## Exercise 3

