FP-Growth

Given

Transactional Database

| TransactionID | Items included |
|---------------|----------------|
| T1 | ABDE |
| T2 | BCE |
| T3 | ABDE |
| T4 | ABCE |
| T5 | ABCDE |
| T6 | BCD |

minSupport = 3.

Task a: Find all frequent itemsets using FP-Growth

Overview FP-Growth

For a given transactional database

- Derive set of frequent 1-itemsets L
- Rearrange transactions in L-order
- Create FP-Tree from L-ordered transactions
- Create header table (items in decreasing frequency, node links)
- Mine FP-Tree
 - bottom to top through header table, for each (frequent) item:
 - create conditional pattern bases
 - create conditional FP-Tree
 - create frequent pattern combinations

1.1 Scan DB, derive frequent 1-itemsets

| Item (1-itemset) | frequency | frequent? |
|------------------|-----------|-----------|
| A | 4 | yes |
| В | 6 | у |
| С | 4 | у |
| D | 4 | у |
| Е | 5 | у |

 $L = \{B, E, A, C, D\}$

L-order refers to frequency beginning with the most frequent and decreasing. Additionally using lexicographical order on item(set)s of same frequency here.

1.2 Rearrange transactions following L-order

| TransactionID | Items included | L-ordered |
|---------------|----------------|-----------|
| T1 | ABDE | BEAD |
| T2 | BCE | BEC |
| T3 | ABDE | BEAD |
| T4 | ABCE | BEAC |
| T5 | ABCDE | BEACD |
| Т6 | BCD | BCD |

2 Create FP-Tree and Header Table

Header Table (L-ordered); see pictures of all (Conditional) FP-Trees below

| Item (1-itemset) | frequency | node link |
|------------------|-----------|-----------|
| В | 6 | green |
| Е | 5 | pink |
| A | 4 | blue |
| С | 4 | gray |
| D | 4 | yellow |

3 Mine the FP-Tree

| Item | Cond. Pattern Base | Conditional FP-Tree | Frequent Pattern Comb. |
|------|--|-------------------------|--|
| D | {{B, E, A : 2}, {B, E, A, C : 1}, {B, C : 1}} | < B: 4, E: 3, A: 3 > | {B, D : 4} {E, D : 3} {A, D : 3}, {B, E, D : 3}, {B, A, D : 3} {E, A, D : 3} {B, E, A, D : 3} |
| С | {{B, E, A : 2}, {B, E : 1} {B : 1} } | < B: 4, E: 3 | {B, C : 4} {E, C : 3} {B, E, C : 3} |
| A | {B, E: 4} | < B : 4, E : 4 > | {B, A : 4} {E, A : 4} {B, E, A : 4} |
| Е | {B:5} | <b:5></b:5> | {B, E: 5} |

Frequent Itemsets:

{B} {E} {A} {C} {D}

 $\{B, E\} \{B, A\} \{B, C\} \{B, D\} \{E, A\} \{E, D\} \{E, C\} \{A, D\}$

{B, E, A} {B, E, C} {B, E, D} {E, A, D}

{B, E, A, D}

Task b

Closed frequent itemsets

- frequent itemset
- there is no proper superset, that has the same support count

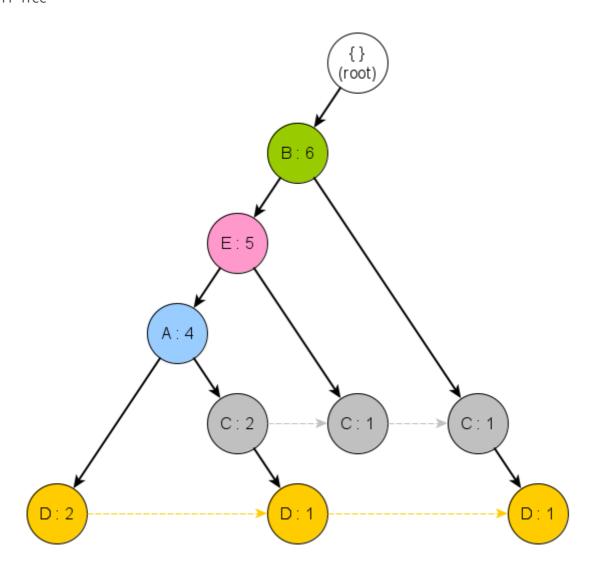
 $\{B\} \{B, E\} \{B, C\} \{B, D\} \{B, E, A\} \{B, E, C\} \{B, E, A, D\}$

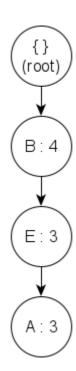
Maximal frequent itemsets

- frequent itemset
- there is no proper superset, that is frequent

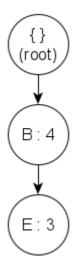
{B, E, C} {B, E, A, D}

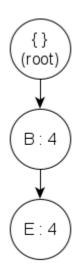
FP Tree



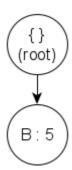


CFPT(C)





CFPT(E)



Additional Exercise

Found in Han, Kamber, Pei: Data Mining, 3rd edition, p. 257. (Example 6.5, referring to database on page 250 (table 6.1))

| TID | Items |
|-----|----------------|
| T1 | i1, i2, i5 |
| T2 | i2, i4 |
| T3 | i2, i3 |
| T4 | i1, i2, i4 |
| T5 | i1, i3 |
| T6 | i2, i3 |
| T7 | i1, i3 |
| Т8 | i1, i2, i3, i5 |
| Т9 | i1, i2, i3 |

minSupport = 2

You could also try for minSupport = 3 and see the differences.