# Number Systems

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# Positional Number Systems

# Positional Number Systems

- In positional number system, some number b is selected as base and symbols or digits are assigned to numbers between 0 and b-1
- The value of each digit in a number can be determined using
  - **≻**The *digit*
  - ➤ The *position of the digit* in the number
  - The base of the number system (where the base is defined as the total number of digits available in the number system)

## **Decimal Number System**

- In decimal number system *base is 10* and the basic symbol or *digits* are 0,1,2,3,4,5,6,7,8,9
- Each digit in the number is associated with a power of 10, according to its position in the number.
- Example:  $3942 = 3x10^3 + 9x10^2 + 4x10^1 + 2x10^0$

**Binary Number System** 

- The base is 2
- The digits are 0 and 1
- Example:  $11010=1\times2^4+1\times2^3+0\times2^2+1\times2^1+0\times2^0$

# Hexadecimal Number System

- The base is **16**
- The digits are 0,1,2,3,4,5,6,7,8,9,A,B,C,D,E,F
- The hex letters A through F denote numbers ten to fifteen, respectively.
- Example:  $1A = 1 \times 16^1 + 10 \times 16^0$

# Conversion between Number Systems

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Hexadecimal to Decimal

#### **Convert 8A2D**<sub>h</sub> to decimal

$$8A2D_h = 8x16^3 + Ax16^2 + 2x16^1 + Dx16^0$$
  
=  $8x16^3 + 10x16^2 + 2x16^1 + 13x16^0$   
=  $8x16^3 + 10x16^2 + 2x16^1 + 13x16^0$   
=  $32768 + 2560 + 32 + 13$   
=  $35373_d$ 

Binary to Decimal

# **Convert 1101**<sub>b</sub> to decimal

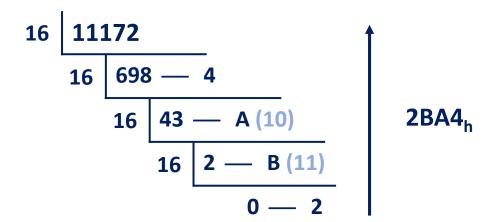
$$1101_{b} = 1 \times 2^{3} + 1 \times 2^{2} + 0 \times 2^{1} + 1 \times 2^{0}$$

$$= 8 + 4 + 0 + 1$$

$$= 13_{d}$$

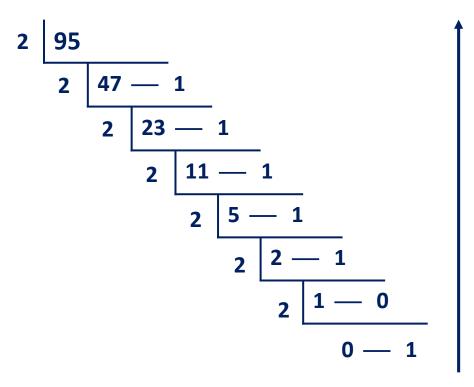
Decimal to Hexadecimal

## **Convert 11172**<sub>d</sub> to hexadecimal



# Decimal to Binary

# **Convert 95<sub>d</sub> to binary**



1011111<sub>b</sub>

# Hexadecimal to Binary

## **Convert 2B3C**<sub>h</sub> to binary

2	В	3	С
0010	1011	0011	1100

2B3C<sub>h</sub> = 10101100111100<sub>b</sub>

## Convert 1110101010<sub>b</sub> to hexadecimal

#### **11 1010 1010**

0011	1010	1010
3	Α	Α

Binary to Hexadecimal

 $1110101010_{b} = 3AA_{h}$ 

# Hexadecimal Addition and Subtraction

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#### Add 5B39<sub>h</sub> and 7AF4<sub>h</sub>.

• 9+4 = 13. In Hex, we represent 13 as  $D_h$ .

3+F meaning 3+15=18. In Hex, we represent 18<sub>d</sub> as 12<sub>h</sub>. So, we place 2 and have 1 as carry.

1+B+A = 22. In hex, we represent 22<sub>d</sub> as 16<sub>h</sub>. So, we place 6 and have 1 as carry.

**Hexadecimal Addition** 

Hexadecimal Addition continued..

• Now, 1+5+7=13 which is  $D_h$  is hex.

• Thus  $5B39_h + 7AF4_h = D62D_h$ 

**Hexadecimal Subtraction** 

Subtract BA94<sub>h</sub> from D26F<sub>h</sub>.

# Binary Addition and Subtraction

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**Binary Addition** 

Add  $1001_b$  and  $1100_b$ .

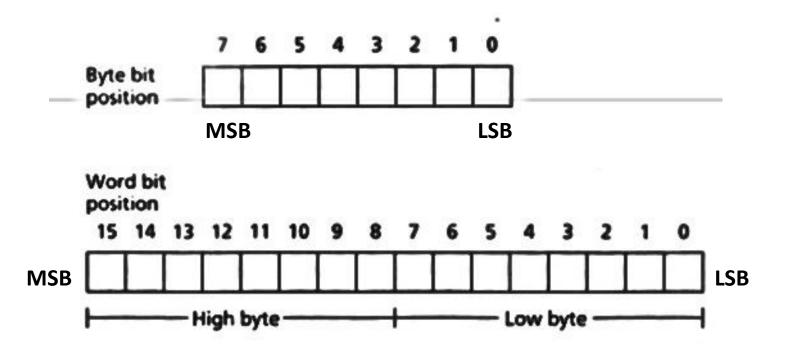
# How integers are represented in the computer?

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Most Significant Bit (MSB) is the leftmost bit.
 In a word, the msb is bit 15; in a byte it is 7.

Least Significant Bit (LSB) is the rightmost bit. That is, bit 0.

MSB and LSB



One's Complement

The one's complement of an integer is obtained by *complementing each bit*; that is, replace each 0 by a 1 and each 1 by a 0.

**Example 2.6 Find the one's complement of 5 = 0000000000000101.** 

Solution: 5 = 000000000000101

One's complement of 5 = 1111111111111010

## Two's Complement

To get the two's complement of an integer, just add 1 to its one's complement.

**Example 2.7 Find the two's complement of 5.** 

**Solution:** 

One's complement of 5 = 1111111111111010

+ 1

Two's complement of 5 = 11111111111111111 = FFFB<sub>h</sub>

Note that, As 5 and it's two's complement add up to 0, the two's complement of 5 is the correct representation of -5.

Two's complement of two's complement of a number gives the number itself.

### **Unsigned Integers**

- Represents a magnitude, so it is never negative.
- appropriate for representing quantities that can never be negative, such as addresses of memory locations, counters, and ASCII character codes
- none of the bits are needed to represent the sign, and so all 8 bits in a byte, or 16 bits in a word, are available to represent the number.
- The largest unsigned integer that can be stored in a byte is  $11111111 = FF_h = 255$ . This is not a very big number, so we usually store integers in words.
- The number is odd if the LSB is 1.
- The number is even if the LSB is 0.

# Signed Integers

- It can either be *positive or negative*.
- Most significant bit (MSB) is reserved for sign: 0 for positive and 1 for negative
- Negative integers are stored in a computer as two's complement

Signed Integers

Example 2.9: Show how the decimal integer -97 would be represented (a) in 8 bits, and tb) in 16 bits. Express the answers in hex.

# Subtraction as Two's Complement Addition

The advantage of two's complement representation of negative integers in the computer is that subtraction can be done by bit complementation and addition, and circuits that add and complement bits are easy to design.

Example 2.10: Suppose AX contains 5ABC<sub>h</sub> and BX contains 21FC<sub>h</sub>.

Find the difference of AX minus BX by using complementation and addition.

# **Decimal Interpretation**

#### **Unsigned Decimal Interpretation**

#### **Binary to decimal conversion**

#### **Signed Decimal Interpretation**

- If MSB is 0 then signed decimal is same as unsigned decimal
- If MSB is 1 take two's complement and convert it to decimal