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Assignment: 02

**Course: Formal Method in software
Engineering**

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PROBLEM#01

Every crocodile is bigger than every alligator. Sam is a crocodile. But there is a snake, and Sam isn't bigger than that snake. Therefore, something is not an alligator.

- Use $C(x)$, $A(x)$, $B(x,y)$, s , $S(x)$

Predicate Logic

$$(\forall x) (\forall y)[C(x) \wedge A(y) \rightarrow B(x,y)] \wedge C(s) \wedge (\exists x)(S(x) \wedge [B(s,x)]') \rightarrow (\exists x)[A(x)]'$$

Question:

$$P(x): x + y \geq 6$$

Possible Solutions:

$$\text{Let } P(7,1) \quad P(7,1): (7) + (1) \geq 6 \quad \text{True propositional statement} \\ 8 \geq 6$$

$$\text{Let } P(3,2) \quad P(3,2): (3) + (2) \geq 6 \quad \text{False propositional statement} \\ 5 \not\geq 6$$

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PROBLEM#03

- Every real number has its corresponding negative.
- Translation: –
- Assume:
 - a real number is denoted as x and its negative as y
 - A predicate $P(x,y)$ denotes: " $x + y = 0$ "
 - Then we can write: $\forall x \exists y P(x,y)$

PROBLEM#04

- For all x and y, if x is a parent of y then y is a child of x
- Assume:
 - Parent(x,y) denotes “x is a parent of y”
 - Child(x,y) denotes “x is a child of y”
- Two equivalent ways to represent the statement:
 - $\forall x \forall y \text{ Parent}(x,y) \diamond \text{Child}(y,x)$
 - $\forall y \forall x \text{ Parent}(x,y) \diamond \text{Child}(y,x)$