

Study Guideline

You need to follow three steps to study

Step 1: Watch the video link given in the start of the topic.

Step 2: Read the lecture notes attached.

Step 3: Read the topic from course book and do practice questions mention.

Topic: Techniques of differentiation

Step 1

<https://www.youtube.com/watch?v=esxNDR1epeq>

You can also watch other videos related to topic.

Step 2

3.3. Techniques of Differentiation.
Exercise set. 3.3.

Find dy/dx

Q 6. $y = \sqrt{2}x + (1/\sqrt{2})$

sol.

$$\frac{dy}{dx} = \sqrt{2}$$

Q 11. $f(x) = -3x^8 + 2\sqrt{x}$

sol. $f'(x) = 24x^{-7} + \frac{1}{\sqrt{x}}$

Q. 23. $y = (1-x)(1+x)(1+x^2)(1+x^4)$. at $x=1$

sol. $y = (1-x^2)(1+x^2)(1+x^4)$
 $= (1-x^4)(1+x^4)$

$$y = (1-x^8)$$

$$\therefore \frac{dy}{dx} = -8x^7$$

$$\therefore \left. \frac{dy}{dx} \right|_{x=1} = -8.$$

Q 33

Step 3: Read topic 3.3 from text book (Calculus by Howard Anton 8th edition)

Practice exercise 3.3 (Q.1 to Q.24, Q.37 to Q.38)

Topic: Product and Quotient Rule

Step 1

<https://www.youtube.com/watch?v=esxNDR1epeo>

You can also watch other videos related to topic.

Step 2

3.4 The product & quotient Rules

Product rule

$$\frac{d}{dx} [f(x) \cdot g(x)] = f(x)g'(x) + g(x) \cdot f'(x)$$

Quotient rule

$$\frac{d}{dx} \left[\frac{f(x)}{g(x)} \right] = \frac{g(x)f'(x) - f(x)g'(x)}{(g(x))^2}$$

Exercise set 3.4

Find all values of x at which the tangent line to the given curve is:

23 $y = \frac{x^2 - 1}{x + 2}$; horizontal.

sol.

$$y' = \frac{(x+2)(2x) - (x^2-1)}{(x+2)^2} = \frac{2x^2 + 4x - x^2 + 1}{(x+2)^2}$$

$$= \frac{x^2 + 4x + 1}{(x+2)^2} = \frac{(x+2)^2 - 3}{(x+2)^2} = 1 - \frac{3}{(x+2)^2}$$

when tangent line is horizontal $\Rightarrow \frac{dy}{dx} = 0$

$$\Rightarrow 0 = x^2 + 4x + 1 \Rightarrow \boxed{x = -2 \pm \sqrt{3}}$$

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Q 25 ~~parallel to~~ $y = \frac{x^2+1}{x+1}$, parallel to line $y=x$.

if tangent line is \parallel to $y=x$

$$\Rightarrow \frac{dy}{dx} = 1.$$

Q 26 perpendicular to $y=x$

$$\Rightarrow \frac{dy}{dx} = -1.$$

Q 27, 28 Try yourself!

Step 3: Read topic 3.4 from text book (Calculus by Howard Anton 8th edition)

Practice exercise 3.4 (Q.1 to Q.16, Q.23 to Q.28)