

Lecture Study Guideline

You need to follow three steps to study

Step 1: Watch the topic related video uploaded on LMS.

Step 2: Read the lecture notes attached.

Step 3: Read the topic from course book and do practice of questions mention below.

Topic: Chain Rule

Step 1

Watch the topic related video uploaded on LMS.

Step 2

3.6 The Chain Rule:

$$\text{If } y = f(u) \text{ \& } u = g(x).$$

$$\text{Then } \frac{dy}{dx} = \frac{dy}{du} \cdot \frac{du}{dx}$$

Example Find dy/dx if $y = \cos(x^3)$.

$$\text{Sol: let } u = x^3 \Rightarrow y = \cos u$$

$$\Rightarrow \frac{dy}{dx} = \frac{dy}{du} \cdot \frac{du}{dx} = -\sin u \cdot 3x^2$$

$$\boxed{\frac{dy}{dx} = -3\sin(x^3)x^2}$$

Generalized Derivative Formulas

$$\frac{d}{dx}[f(u)] = f'(u) \cdot \frac{du}{dx}$$

Ex. 3.6.

$$\text{Q3. let } f(x) = x^5 \text{ \& } g(x) = 2x-3$$

Find $(f \circ g)(x)$ \& $(f \circ g)'(x)$.

$$\text{Sol: } (f \circ g)(x) = f(2x-3) = (2x-3)^5$$

$$\therefore (f \circ g)'(x) = \frac{d}{dx} (2x-3)^5$$

$$\text{let } u = 2x-3.$$

$$\Rightarrow (f \circ g)'(x) = \frac{d}{dx} u^5 = \frac{du^5}{du} \cdot \frac{du}{dx}$$

$$= 5u^4 \cdot 2.$$

$$= 10u^4 = 10(2x-3)^4$$

$$\text{Q 11 } y = f(x) = \frac{4}{(3x^2-2x+1)^3}$$

$$\text{let } u = 3x^2-2x+1$$

$$\Rightarrow \text{~~f(x)~~ } y = \frac{4}{u^3} = 4u^{-3}$$

$$\therefore \frac{dy}{dx} = \frac{dy}{du} \cdot \frac{du}{dx} = -3 \cdot 4u^{-4} \cdot \frac{d}{dx}(3x^2-2x+1)$$

$$= -12(3x^2-2x+1)^{-4} (6x-2)$$

$$23. \quad f(x) = \sqrt{\cos(5x)} \quad \text{let } u = 5x$$

$$\Rightarrow y = (\cos u)^{1/2} \therefore \frac{dy}{du} = \frac{dy}{du} \cdot \frac{du}{dx}$$

$$\Rightarrow \frac{dy}{du} = \frac{1}{2} \cos u^{-1/2} \cdot (-\sin u) \cdot 5$$

$$33. \quad y = \cos^3(\sin 2x)$$

$$\text{let } u = \sin 2x \Rightarrow y = \cos^3 u.$$

$$\frac{dy}{dx} = \frac{dy}{du} \cdot \frac{du}{dx} = 3\cos^2 u \cdot (-\sin u) \cdot 2\cos 2x.$$

$$30. \quad y = \frac{\sin x}{\sec(3x+1)} = \sin x \cdot \cos(3x+1)$$

Q 61 if $y = A \cos \omega t$

a) show that $\frac{d^2 y}{dt^2} = -\omega^2 y$

b) show that $T = 2\pi/\omega$ (Time req. to complete one oscillation)

c) Find f in terms of T .

Sol:

a) $\frac{dy}{dt} = -A\omega \sin \omega t$

$$\frac{d^2 y}{dt^2} = -A\omega^2 \cos \omega t = -\omega^2 y.$$

b) As period of \cos is 2π

$$\therefore \omega T = 2\pi \Rightarrow T = 2\pi/\omega$$

c) $f = 1/T$

Step 3: Read topic 3.6 from text book (Calculus by Howard Anton 8th edition)

Practice exercise 3.6 (Q.3, Q.4, Q.7 to Q.40, Q.51 to Q.54)