

*Mathematica* for the constantly busy:  
A guide along a glorious journey  
2nd Edition

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## Part I

# Introduction

*Mathematica* is a beautiful machine that is capable of doing outstanding things for the world of science. It can solve terrible integrals in a fraction of a second, solve differential equations faster than you can say “quidditch”, and even make some quite perfect plots. While there are other programs out there that also do math on a very efficient level and are great for certain scenarios, like Matlab, STATA, R, Geometer’s sketchpad, I believe *Mathematica* can do just about anything you could ever want for any scenario if you really wanted to make it.

Here we will explore some of the basics of the glory that is *Mathematica*, ranging from doing simple arithmetic to solving differential equations and then plotting them in 3D.

This guide is meant to be either a quick reference, or a guide along the journey that is *Mathematica*.

Before we begin, I would like to point out the in program help dialog can easily be reached by simply pressing the F1 key at any time. If the cursor is on a command, it will automatically go to the page of that command.

## Part II

# Syntax

### 1 Capitalizing functions

The first letter of each word in every function in Mathematica is capitalized.

e.g. Plot, ListPlot, DSolve, FindSequenceFunction, etc.

### 2 Brackets

- **Square brackets**

Square brackets, `[ ... ]`, are used to enclose everything that is needed to work a function.

e.g. `Plot[ ... ]`

- **Parenthesis**

Parenthesis are used for multiplication.

e.g.

$$x(x + 1) = x^2 + x$$

- **Curly brackets**

Curly brackets are to group things, like sets and "function machinery".

e.g. Let  $V$  be a vector space spanned by the set  $\{v_1, v_2, v_3\}$  or `Table[k, {k, 3, 10}]`

### 3 Function Format

When using a function that calls for an argument and bounds, it usually take its arguments in the form

`function[expression, {variable, lower_bound, upper_bound}]`

#### 3.1 Semicolons

When a semicolon, `;`, is at the end of a function or line, it suppresses the output of that command.

For example, when you want to have a large set of astronomical data that consists of 5 columns with over 7000 entries in each column stored in memory, you can simply import the data, then put a semicolon after it, and it won't display the entire set of data. (When the set is big enough, *Mathematica* will shorten it down to a little display window)

#### 3.2 Strings

When something is inside quotation marks, `" ... "`, they make it into a string, otherwise known as just text. This is needed for some options in functions like `ColorFunction -> "Temperature"`.

### 3.3 Comments

Commenting in *Mathematica* can be done by simply enclosing whatever you want in "( \* ... \* )".

### 3.4 The equals symbol

There are multiple uses for the equals symbol in *Mathematica*, as well as other coding languages.

#### 3.4.1 Programming Declaration

"=" is used to define the left side as the right side.

For example,

$$x = 2$$

means x is now defined as the value 2;

or

$$P = ax^3 + bx^2 + cx + d$$

means P is now the above polynomial.

#### 3.4.2 Mathematical equality

"==" is used to denote mathematical equality.

For example,

$$2 == 2$$

will return True because 2 does indeed equal 2.

#### 3.4.3 Delayed definition

:=" is used to define a variable on the left with an expression on the right each time it runs.

For example,

$$f[x_] := \sin[\cos[x]]$$

means "f[x]" is now a function of the variable x which will be ran and displayed each time. (More on this later.)

#### 3.4.4 Clear

The "Clear" function is used to clear any function or variable of its declaration, and is used by "Clear[...]"

You can clear multiple things at once by putting them all in the function argument and separated by a comma.

Another way of clear, or unsetting variables is to use "unset", which is just "=."

For example, if  $x = 42$ , then we can clear it by using " $x = .$ ".

## 4 Spaces

Spaces between 2 things in *Mathematica* imply a multiplication between those 2 things.

For example,

$$x\ y = x * y$$

## 5 Special Numbers

*Mathematica* also knows almost all the special numbers out there, like  $\pi$ ,  $e$  and  $\infty$  (Is  $\infty$  a number?) , etc. Here we'll see how to get these "exact" values. First, to typeset almost anything in *Mathematica*, you can push the escape key, type the name of the thing you want, then press escape again.

- $\pi$  can be represented in *Mathematica* by either "Pi" or with escape, "p"
- $e$  can be represented by either "E" or with escape by "ee"
- $\infty$  can be represented by either "Infinity" or with escape by "inf"
- $i$  can be represented by either "I" or with escape by "ii"

## 6 Domains

*Mathematica* also knows about domains other than the conventional reals. These are represented as:

- The complexes,  $\mathbb{C}$ , are represented as "Complexes"
- The rationals,  $\mathbb{Q}$ , are represented as "Rationals"
- The integers,  $\mathbb{Z}$ , are represented as "Integers"
- The primes,  $\mathbb{P}$ , are represented as "Primes"
- The reals,  $\mathbb{R}$ , are represented as "Reals"

## 7 Exercises

Here will be a few exercises and problems to help with learning *Mathematica*. Most of these will work in any version of *Mathematica*, but some may only work in versions 8-10.

1. Correctly enter the name of a function in the *Mathematica* catalog.
2. Make a function that multiplies the variable by a special constant.
3. Clear the function from the previous problem and make a function of two variables. Then make function that take a set as an argument.

## Part III

# Math! (Not factorial)

## 8 Arithmetic

To do arithmetic in *Mathematica*, all you have to do is type the numbers you want to add, subtract, multiply, or divide, in the form you want to compute, and hold "Shift" and press "Enter".

For example,

input:  $2 + 2$   
Shift + Enter  
output: 4

Now, the real learning part here is the action of the Shift+Enter motion. In *Mathematica* 8 and later versions, commands can be done by also pushing the Enter button on the numeric keypad.

## 9 Algebra

### 9.1 Solve

*Mathematica* has a beautiful function that when given an equation and a desired variable in that equation it will solve that equation for that variable. Imaginatively enough, this function is called Solve.

For example

input:  $\text{Solve}[ax^2 + bx + c == 0, x]$   
output:  $x \rightarrow \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$

Note: There are also variations on Solve to do slightly different things. For instance, there is also "NSolve" which numerically finds solutions to equations.

### 9.2 Trigonometry

*Mathematica* of course also has all your trig functions, Sin, Cos, Tan, their reciprocals, and their inverses.

Note: *Mathematica* automatically takes the argument of these function to be in radians. If you want the argument to be in degrees, simply put "Degree" after the argument but still inside the function. e.g.

$$\sin\left[\frac{\pi}{2}\right] = \sin[90 \text{ Degree}]$$

Remember, these are functions so they need to be capitalized, but they are not here because  $\text{\LaTeX}$  uses them in lowercase.



### 9.3 Sum

*Mathematica* can certainly do both indefinite and definite sums even to infinity (Series)!

To take a definite sum we simply use

$$\text{Sum}[\text{exp}, \{\text{variable}, \text{lower\_bound}, \text{upper\_bound}\}]$$

For example

In:  $\text{Sum}[p^2, \{p, 10\}]$   
Out: 385

### 9.4 Logarithms

*Mathematica* can use logarithms of any base, but its standard "Log" function automatically uses base  $e$ .

To take a logarithm, we use

$$\text{Log}[b, v]$$

where "b" is the base of the logarithm, and "v" is the thing you're taking the log of.

## 10 Calculus

### 10.1 Derivatives

Differentiating in *Mathematica* is actually quite easy. When you want to differentiate an expression you can simply use

$$D[f, x]$$

where f is the function you want to differentiate and x is the variable you want to differentiate with respect to.

**Note:** "D" gives the partial derivative of the function, so "f" doesn't have to be single variable.

"D" has a few variations that include multiple derivatives, and vector derivatives (gradients).

### 10.2 Integrals

For all those pesky indefinite integrals that would need several by parts, you can do it in a snap with the mathing power of *Mathematica* using "Integrate"!

To integrate something, we use

$$\text{Integrate}[f, x]$$

where "f" is the integrand, and "x" is the variable with which you are integrating with respect to.

For example

$$\begin{aligned} \text{input: } & \text{Integrate}\left[\frac{1}{x^3+1}, x\right] \\ \text{output: } & -\frac{1}{6}\log(x^2-x+1) + \frac{1}{3}\log(x+1) + \frac{\tan^{-1}\left(\frac{2x-1}{\sqrt{3}}\right)}{\sqrt{3}} \end{aligned}$$

To do a definite integral, you would do the same thing, but put the variable and bounds in curly brackets.

e.g. `Integrate[log[x], {x, -10, 10}]`

## 11 Linear Algebra

### 11.1 Making Matricies

There are 2 ways to make matricies in *Mathematica*, typesetting or using sets. Using sets is easier to enter, but doesn't look as pretty. I like the sets method.

In *Mathematica* sets are used as vectors, matricies and tensors. It all depends on how many levels there are.

For example, the set

$$\{v_1, v_2, v_3\}$$

is a vector, while the set of sets

$$\{\{u_{1,1}, u_{1,2}, u_{1,3}\}, \{u_{2,1}, u_{2,2}, u_{2,3}\}, \{u_{3,1}, u_{3,2}, u_{3,3}\}\}$$

is a 3 x 3 matrix.

### 11.2 Matrix Arithmetic

Matrix Arithmetic is probably just as you would expect, when you add them, they add as they should, component wise. Same for subtraction. When multiplying matrices, you need to use `."` instead of `"*"`, otherwise it will multiply component wise.

### 11.3 Matrix Operations

*Mathematica* of course also has the capability to do many matrix operations, like taking the inverse, transpose, determinant, etc.

#### 11.3.1 Inverse

When taking the inverse of a matrix, it's actually pretty simple using `"Inverse"`. (Imagine that!)

To take the inverse of a matrix, you simply use `"Inverse[...]"`. Remember, you can only take the inverse of a square matrix.

For example, let B be the matrix

$$\begin{pmatrix} b_{1,1} & b_{1,2} \\ b_{2,1} & b_{2,2} \end{pmatrix}$$

Then

$$\begin{array}{l} \text{in: } \text{Inverse}[B] \\ \text{out: } \left( \begin{array}{cc} \frac{b_{2,2}}{-b_{1,2}b_{2,1}+b_{1,1}b_{2,2}} & -\frac{b_{1,2}}{-b_{1,2}b_{2,1}+b_{1,1}b_{2,2}} \\ -\frac{b_{2,1}}{-b_{1,2}b_{2,1}+b_{1,1}b_{2,2}} & \frac{b_{1,1}}{-b_{1,2}b_{2,1}+b_{1,1}b_{2,2}} \end{array} \right) \end{array}$$

### 11.3.2 Transpose

Similar to "Inverse", "Transpose" is as easy as it should be. Simply write "Transpose[...]", where the argument of "Transpose" is a list.

### 11.3.3 Determinant

Amazingly enough, you can simply find the determinant of a square matrix using "Det[...]".

### 11.3.4 Row Reducing

To quickly row reduce a matrix, simply use "RowReduce[...]" where the argument is a matrix.

## 11.4 Eigen-stuff

Another very useful thing *Mathematica* is great for is finding the eigen: values, vectors, and space, of a matrix.

The syntax for the functions "Eigenvalues", "Eigenvectors", "Eigensystem" is all the same. "Eigen-thing[...]" will give you the desired result for the input square matrix.

Note, "Eigensystem" will give a set of sets where the first element in each set is an eigenvalue and the second element is the corresponding eigenvector.

Another note, *Mathematica* will give each eigenvalue as if it were distinct. i.e. It will display multiple of the same eigenvalue if that value has multiplicity greater than zero.

### 11.5 NullSpace

To find the set of vectors that span the null space of a matrix A, we use "NullSpace[A]".

### 11.6 Norm

To know the magnitude, or Norm, of a number, vector or matrix, you simply use "Norm[...]".

Note, this includes complex numbers.

### 11.7 Dimension

To know the dimension of a matrix we simply do

$$\text{Dimensions}[...]$$

This will give the length 2 set whose first element is the number of rows the matrix has and the second element is the number of columns the matrix has.

## 11.8 Solving matrix equations

To solve a matrix equation, we can use "LinearSolve". "LinearSolve" take 2 arguments, a  $n \times m$  matrix  $A$  and a vector  $b \in \mathbb{R}^m$ , where  $A\vec{x} = \vec{b}$ . In practice, the function takes the form

LinearSolve[A,b]

## 11.9 LeastSquares

Just like solving the matrix equation, we can also use the least squares method by using

LeastSquares[A,b]

where  $A$  is a matrix and  $b$  is the solution to the equation  $A\vec{x} = \vec{b}$ .

## 12 Differential Equations

*Mathematica* is also perfect for linear ordinary differential equations with constant coefficients, but also does a pretty good job against other kinds as well!

### 12.1 Solving ordinary differential equations

When you have a really nasty differential equation and you completely have forgotten how to solve even the simplest form, you can use *Mathematica's* function "DSolve".

To use "DSolve" we write the form

DSolve[eqn,y[x],x]

where *eqn* is the equation we want to solve,  $y[x]$  is the function we're solving for, and  $x$  is the independent variable of the desired function.

If you want to find the "pure" function solution  $y$  you can use

DSolve[eqn,y,x]

### 12.2 Solving partial differential equations

It doesn't stop at ordinary differential equations though, *Mathematica* can even do partial differential equations in a snap!

To solve a partial differential equation in *Mathematica*, we still use "DSolve" but now we use

DSolve[eqn,y[x],{ $x_1, x_2, \dots$ }]

### 12.3 Numerically solving ordinary differential equations

There is also "NDSolve" which solve differential equations numerically and is used

NDSolve[eqn,y[x], { $x$ , lower bound ,upper bound }]

It should be noted *Mathematica* does best with linear ordinary differential equations with constant coefficients, but can do most with non-constant coefficients up to second order.

## 12.4 Using the solution

If you want to use the solution to the differential equation in something else, we can easily use the `replace` command.

Say we get a pure function solution  $y$  to a differential equation, and now we want to use that equation in another equation  $y(x) + \sin(y(x))$ . To easily substitute the solution  $y(x)$  into the equation, we would use

$$y(x) + \sin(y(x))/.y \rightarrow DSolve[eqn, y, x]$$

This will replace every instance of the character  $y$  with the solution and simplify.

## 13 Exercises

1. Find the result of  $1,000,000 - 2^{12} + 8^7 * 5^{-3}/9$ .
2. Analytically solve an algebraic equation. Ex:  $\pi x^2 + ex + \phi = x$
3. Numerically solve a trigonometric equation.
4. Add the first 100 natural numbers. Ex:  $1 + 2 + 3 + \dots + 100$
5. Make a function that adds the previous two values of the function up to a certain amount of times.
6. Find the closed form solution to the series of an infinite degree polynomial. Ex:  $1 + x + x^2 + \dots$
7. Find the derivative of the solution to the previous problem.
8. Find the derivative of the factorial function.
9. Find the integral of the solution to #6.
10. Create a  $2 \times 2$  matrix, a vector in  $\mathbb{R}^2$ . Then multiply them.
11. Find the determinant of the inverse of the transpose of a matrix of your choice.
12. Row reduce a  $10 \times 10$  matrix of odd numbers.
- 13.

## Part IV

# Data! (Not the Android)

Not only can *Mathematica* do awesome symbolic and numeric computations, it can also handle massive amounts of data!

## 14 Reading in data

First, we need to import the data, with guess what, "Import".

To use "Import" we enter

```
Import["file.format"]
```

Now here the quotations are necessary and the file either needs to be in the same folder as your notebook, or you need to specify the entire path in the file name.

I usually like to set my data as the variable "Data" so I can use it easily in later commands.

Import can take many different formats of files, but the main one we'll focus on is CSV (Excel) since many it is usually the format scientific data is taken in for our purposes.

**Important Note:** If you don't want to see the data remember to put a semicolon after the closing square bracket.

## 15 Handling Data

We don't just want to read in a bunch of data and not do anything with it! Now we can look at the data.

### 15.1 Length

To find how many elements there are in the first level of your data, we simply use

```
Length[...]
```

### 15.2 Depth

To find how many levels there are in the data, we simply use

```
Depth[...]
```

Now, since *Mathematica* automatically make the data into one big set, the depth is how many indices are needed to specify the location of an element in the set + 1.

### 15.3 Select

Let's say you only want the data that meet certain criteria, then you would use the "Select" by

Select[Data, criteria]

For example, to find the evens out of  $Data = \{1, 2, 4, 7, 6, 2\}$ , we use.

in: Select[Data, EvenQ]  
out: {2, 4, 6, 2}

If we want to find the data that match a more abstract criteria we can use pure functions. For example, to find the data that is greater than 2, we use

In: Select[Data, # > 2 &]  
Out: {4, 7, 6}

In this case, the # is used to denote the element of the set that is being tested and the & is used to make the expression a pure function.

### 15.4 Indices

To actually look at an element in the set, or piece of data in the set, we can use double square brackets, "[[" and "]]".

To make good looking opening index brackets we use (Escape) [[ (Escape). The same goes for closing brackets.

So, to see the  $a$ -th element in the  $b$ -th set in Data, we say

Data[[b]][[a]]

For example, let  $Data = \{\{1, 2\}, \{3, 4\}\}$ .  
Then

In: Data[[2]][[1]]  
Out: 3

This can be extended to higher (deeper?) depths by adding more indices with brackets.

### 15.5 Flatten

Let's say you have a set with multiple levels, but you want the data to be all on the first level. In this case, we can use "Flatten".

To use "Flatten" we simply say

Flatten[...]

## Part V

# Important Functions

Out of all the functions *Mathematica* has to offer, I have a few that I think are particularly important and useful because they have been just that in my experience. I'm sure there are a lot of other really amazing functions and commands that *Mathematica* has to offer, but I only have a little bit of experience with it. This is why I encourage you to explore on your own to find the wonders of *Mathematica* for yourself.

## 16 Plot

### 16.1 Basic Plotting

Plotting is a very big deal in the science world. With the help of *Mathematica* and it's gigantic library of options, you can make the best plots.

The basic Plot function is rather simple to deal with since it takes the form

$$\text{Plot}[f[x], \{x, lb, ub\}]$$

where "lb" and "ub" are the lower and upper bounds respectively.

"Plot" in this form will still give you a beautiful plot of whatever function you give it to graph, but it could be better. Let's check out some of the options ol' Stephen gave us.

### 16.2 "Plot" Options

To implement "Plot" options, they need to be in the function, but after everything the function needs.

For example

$$\text{Plot}[x^2, \{x, -1, 1\}, \text{"Options go here each separated by a comma"}]$$

#### 16.2.1 Labeling Axes

To label your axes and not just have some random graph, use "AxesLabel".

"AxesLabel" take the form

$$\text{AxesLabel} \rightarrow \{x, y\}$$

where x is the label for the "x" axis and "y" is the label for the y axis.

When "AxesLabel" just points to "y", *Mathematica* will just label the "y" axis.

#### 16.2.2 Coloring your plot

To color your plot you can use "ColorFunction". Since there are quite a few implementations for "ColorFunction", I will let you explore these on your own.



### 16.2.3 Smoothness

*Mathematica* actually makes its plots by connecting a finite number of points, because it's a computer and they can't deal with infinities. Since this is how plots are made, you can set the number of points *Mathematica* uses to plot using, imaginatively enough, "PlotPoints".

To make your plot as smooth or as jagged as you want, you can use

$$\text{PlotPoints} \rightarrow \#$$

where  $\#$  is the number of desired plot points.

Having a high number of plot points will certainly make your plot as "smooth", or as accurate to the original function, as possible.

**Note:** There is a point at which the plot will not change due to the number of plot points. Also, the run time of the code is proportional to the number of plot points.

### 16.2.4 How much you see

"Plot" intrinsically takes bounds on which to plot the function, but you can set the plot to show more of the viewing window with "PlotRange".

To use "PlotRange" we say

$$\text{PlotRange} \rightarrow \left\{ \left\{ \begin{array}{c} -x \\ x \end{array} \right\}, \left\{ \begin{array}{c} -y \\ y \end{array} \right\} \right\}$$

where "-x" and "x" are the left and right x axis plot bounds respectively, and "-y" and "y" are the bottom and top plot bounds respectively.

### 16.2.5 Colors!

To make your plot not just a thing blue line, we can use "PlotStyle".

Like "ColorFunction", "PlotStyle" has a lot of options, so I will cover what I think are the most important that I know.

To implement "PlotStyle" we use

$$\text{PlotStyle} \rightarrow \{\text{Thickness}[t], \text{Color}\}$$

where "t" is the thickness of the line of your function, (Generally you would want this around .01 for a good solid line, but try it at other values to see what happens.) and "Color" is the color you want your plot to be. *Mathematica* knows almost all colors by name, but can also recognize colors with specific RGB values. RGB valued colors are represented by "RGB[r,g,b]" where "r" is the red portion of the color, "g" is the green portion of the color, and "b" is the blue portion of the color.

## 16.3 3D Plotting

*Mathematica* can also make beautiful 3D plots using "Plot3D".

"Plot3D" is almost the exact same as its 2D counterpart, including its options, except for

it needing 2 variables to bound the plot.

To use "Plot3D" we enter

```
Plot3D[ f[x,y], {x, xmin, xmax}, {y, ymin, ymax} ]
```

where "f" is the function to be plotted, "x" is one of the function's variables, "xmin" and "xmax" are the lower and upper bound of the x-axis respectively, "y" is the other variable of the function, and "ymin" and "ymax" are the lower and upper bounds of the y-axis respectively.

## 17 We make table

"Table" is such a beautiful function because it holds so much power in such a tiny little container. With "Table", we can make enormous sets or sets, or do math with entries in a set with entries of another set, and so on.

### 17.1 Making simple sets

Like I said before, we can make sets with "Table" by entering

```
Table[ expr, {k, kmin, kmax} ]
```

where "expr" is some expression involving "k" and the expression will be generated *kmax* – *kmin* times starting at "kmin" and ending at "kmax", incrementing in steps of 1.

For example, we will make a simple set of the naturals from 1 to 10.

To do this we use

```
In: Table[k, {k, 1, 10}]  
Out: {1, 2, 3, 4, 5, 6, 7, 8, 9, 10}
```

Now if you're starting at 1, you can actually drop it from the function so it reads

```
In: Table[k, {k, 10}]
```

Too simple? How about

```
In: Table[Fibonacci[n], {n, 3, 10}]  
Out: {2, 3, 5, 8, 13, 21, 34, 55}
```

We can even have it take different step sizes by simply adding the step size to the end of the bounds!

```
In: Table[Fibonacci[n], {n, 3, 100, 17}]  
Out: {2, 6765, 24157817, 86267571272, 308061521170129, 1100087778366101931}
```

Now we get the Fibonacci numbers from 3 to 100 in steps of 17.  
 Now let's see what happens when we put curly brackets around the bounds.

In: `Table[Fibonacci[n], {n, {3, 100, 17}}]`  
 Out: `{2, 354224848179261915075, 1597}`

Oh! It made a table of the 3rd, 100th, and 17th Fibonacci numbers! So this tells you can make "Table" iterate on values denoted in the given set.

## 17.2 Plotting your data

- **1 to 2 elements**

To plot the data, or elements of a set, as points with elements of your data being the coordinates of each point, we use "ListPlot".

To use "ListPlot", we enter

`ListPlot[Data]`

If the data is a set of individual elements, those elements will be plotted in order with indices corresponding to successive naturals 1, 2, ...

If the data is a set of sets with 2 elements, the first element in each set will be the x-coordinate and the second element will be the y-coordinate.

- **More than 2 elements**

When dealing with data that has more than 2 elements in each set, or has more 2 levels, we need to make a table of the just elements we want. To do this, we need to use the indices of the elements in the data, `Data[[a]][[b]]`.

e.g. If we want to make a plot of the data from the 1st and 3rd elements in each set within "Data", we would say

`ListPlot[ Table[ {Data[[t]][[1]],Data[[t]][[3]]}, {t, Length[Data]} ]`

Maybe an application would be helpful.

### Mapping the Universe

Let's say you have a set of data from the SDSS (Sloan Digital Sky Survey) that is comprised of right ascension, declination, redshift, apparent magnitude in the green band, and apparent magnitude in the red band, of distant galaxies. Then you want to make a map of the galaxies.

First let each galaxy be its own set consisting of the 5 measurements in the order presented above. e.g.

$$g_1 = \{ra_1, de_1, z_1, g_1, r_1\}$$

where  $g_1$  is the first galaxy,  $ra$  is the right ascension,  $de$  is the declination,  $z$  is the redshift,  $g$  is the apparent magnitude in the green band, and  $r$  is the apparent magnitude in the red band.

Then, ignoring the astronomy, we would use something along the lines of

```
x = Table [  $\frac{1}{72}(c \text{ Data}[[s]][[3]]) \cos(\text{Data}[[s]][[1]] \text{ Degree} - 185 \text{ Degree}), \{s, 3, \text{Length}[\text{Data}]\} ] ;$ 
y = Table [  $\frac{1}{72}(c \text{ Data}[[s]][[3]]) \sin(\text{Data}[[s]][[1]] \text{ Degree} - 185 \text{ Degree}), \{s, 3, \text{Length}[\text{Data}]\} ] ;$ 
ListPlot [Table[{x[[q]], y[[q]]}, {q, 1, Length[x]}]]
```

For "ListPlot" there are similar variations of it like "ListLinePlot" which connects successive points together with a line.

## 18 Simplifying

One of the best functions in *Mathematica* is "FullSimplify". With "FullSimplify", you can input an expression or equation and it will go through every identity and standard reduction it has and apply it to the expression until it has reached the simplest form of the expression.

For example,

```
input: FullSimplify [  $i \sin^3[\theta] + \cos^3[\theta] + i \sin[\theta] \cos^2[\theta] + \sin^2[\theta] \cos[\theta]$  ]
output:  $e^{i\theta}$ 
```

Another version of this function is just "Simplify". This version goes through much fewer possible reductions, but is a lot faster.

## 19 Manipulate

Another key function in *Mathematica* is "Manipulate" which allows you to, well, manipulate anything you want. This applies to plots, graphics, and almost anything you can think of.

To use "Manipulate", we can enter

```
Manipulate[ stuff, {var, varmin, varmax} ]
```

where "stuff" is an expression which has the variable "var" acting on it in some way, and "varmin" and "varmax" are the minimum and maximum of "var" respectively.

For example

```
Manipulate[Plot[  $\gamma x^2$ , {x, -1, 1}, PlotRange -> {-1, 1} ], { $\gamma$ , -1, 1} ]
```

gives us the power to manipulate the curvature of the produced parabola from "Plot".

## Part VI

# Conclusion

*Mathematica* is also used here in our very own back pocket by some faculty in both physics and math in their research.

These are just the tip of the power of *Mathematica* and almost all of the functions have more to them than presented here. More information on each of these can be found by searching them in the *Mathematica* dialog or from "reference.wolfram.com/language" where all the past and newest features of *Mathematica* are.

Have fun!

*Nate Chapman*