

Design and Power Measurement of 2 And 8 Point FFT Using Radix-2 Algorithm for FPGA Implementation

Mayura Patrikar, Prof.Vaishali Tehre

Electronics and Telecommunication Department,G.H.Raisoni college of EngineeringNagpur,Maharashtra,India

Abstract: In Cooley-Tukey algorithm the Radix-2 decimation-in-time Fast Fourier Transform is the easiest form. The Fast Fourier Transform is the mostly used in digital signal processing algorithms. Discrete Fourier Transform (DFT) is computing by the FFT. DFT is used to convert a time domain signal into its frequency spectrum domain. FFT algorithms uses many applications for example, OFDM, Noise reduction, Digital audio broadcasting, Digital video broadcasting. It's used to design butterflies for different point FFT. In this paper given to design and power measurement 2 and 8 point FFT by using VHDL. Simulation and synthesis of design is done using Xilinx ISE 14.2.

Keywords: Fast Fourier transform (FFT), Discrete Fourier transform (DFT), DIT, Radix-2, VHDL, FPGA.

I. Introduction

Now a day field of digital signal processing is very important of transmission, there is a many growths in FFT algorithms which is way in designing a system. In this paper explains the implementation and simulation of 2and 8-point FFT using radix- 2 algorithm. Due to radix-2, FFT can achieve less time delay, beat down the area complication and, also reach cost dominant execution with minimum grow up time .

Fast Fourier Transform is an algorithm to compute Discrete Fourier Transform (DFT). DFT is used to convert a time domain signal into its frequency spectrum domain. DFT is computational tool that play a very determining role in many digital signal processing applications. The main importance of DFT in practical applications is due to a large extent on existences of computationally efficient algorithms, known as Fast Fourier Transform (FFT) algorithms, for counting the DFT. There are numerous isolated FFT algorithms implicating a large spectrum of calculated from effortless complicated calculation arithmetic to set theory and calculation theory. FFTs are algorithms for speedy calculated of discrete. Fourier transform of a information vector. The FFT is a DFT algorithm which decrease the count of calculations necessity for N point from $O(N^2)$ to $O(N \log N)$ everywhere log is the base-2 logarithm .

$$f_j = \sum_{k=0}^{n-1} x_k e^{-(2\pi i/n)jk} \quad j = 0, \dots, n-1.$$

In FPGA calculation there are two types of power

- Static Power- In static power spending the utilize of strength is minimum to keep the accelerator in power-up state.
- Dynamic Power- Dynamic power consumption is based on its switching activity.

II. Field Programmable Gate Arrays

From long period of time FPGAs architecture is used by the users. It have potential to mapped various applications on system. Figure 2.1 is basic FPGAs structure. It shows that FPGAs use fine grained technique to develop applications. FPGAs contain SRAM based memory which makes the system flexible. FPGA is very popular because of its flexibility.

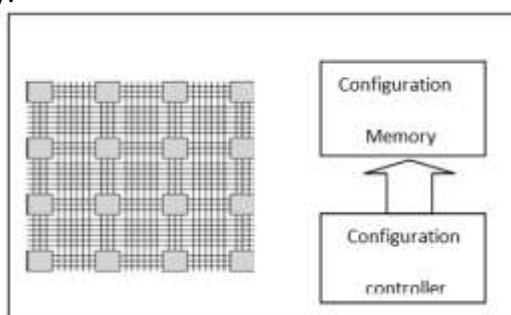


Fig.2.1: Basic architecture of FPGAs

III. Radix-2 Fast Fourier Transform Algorithm

Radix-2 algorithms are the most widely used in FFT algorithms. While counting DFT, we every time compute N-point DFT. The calculation N can be component as,

$$N=r_1, r_2, r_3, \dots, r_v \text{ ---(a)}$$

Here r is a prime,

$$\text{Now if } r_1=r_2=r_3=\dots=r_v=r$$

We can write,

$$N=r^v \text{ ---(b)}$$

Here r is denominated as radix (base) FFT algorithm and v is shows number of phases in FFT algorithm.

Radix denotes base and if it's value is '2' then it is said as radix-2 FFT algorithm. put the value of r=2,

$$N=2^v \text{ ----(c)}$$

If we are computing 2 point DFT then N=2

$$2=2^v$$

$$V=1$$

Therefore, designed for 2 point DFT, convenient are single stage of FFT Algorithm.

If we are computing two point DFT then N=8

$$8=2^v$$

$$V=3$$

Therefore, for 8 point DFT, convenient are 3 stages of FFT algorithm.

In Fast Fourier transform algorithms, a butterfly structure is a part of a calculation that jointly the outcome of compact discrete Fourier transforms (DFTs) during a massive DFT, or conversely (demolition a massive DFT above during sub transforms). The title "butterfly" move nearer from a structure of the data-flow representation in radix-2 case, as detailed beneath. The before time event in imprint of the period is idea to be in a 1969 MIT technical report. The similar formation may as well be establish in the Viterbi algorithm, utilized for locating the very similarly series of mystic states. Twiddle factor fundamentally mentioned to the root of unity difficult multiplier continual in butterfly manipulations of cooley-Tukey FFT Algorithm. Twiddle factor can as well be applied for every information free multiplier continual in FFT.

IV. Implementation of Dit-2 Point FFT Algorithm Using VHDL Code In Xilinx

In several years hardware design language has become an integral part of the industry for designing of the low level as well as high level hardware design as it is the most compatible language hence is widely used by the vendors due to its functionality of being interchangeable that it can be functioned as per the users choice it widely used for the efficient synthesis of the FPGA as its supports annexation of technology precise modules .

In the below figure 4.1, find the 2 point FFT algorithm for radix-2.

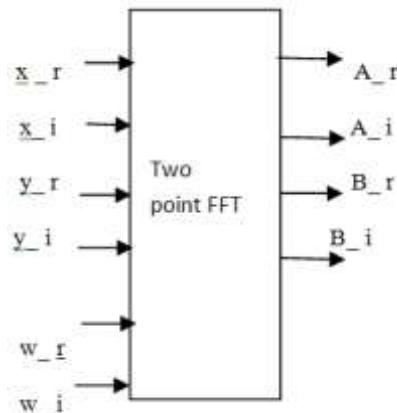


Fig.4.1: Basic block of 2 point FFT

In the above figure 4.1 shown the two point FFT algorithm. This figure has two input and one twiddle factor. x and y are the inputs, w is twiddle factor, these are imaginary and real forms. A and B are output those are also imaginary and real forms. Which Collect all the input and twiddle forms write the code in VHDL and perform the operation in Xilinx 14.2

V. Implementation of DIT 8 Point FFT Algorithm Using VHDL Code In Xilinx

In this below figure shown the block diagram of 8point FFT algorithm for radix-2

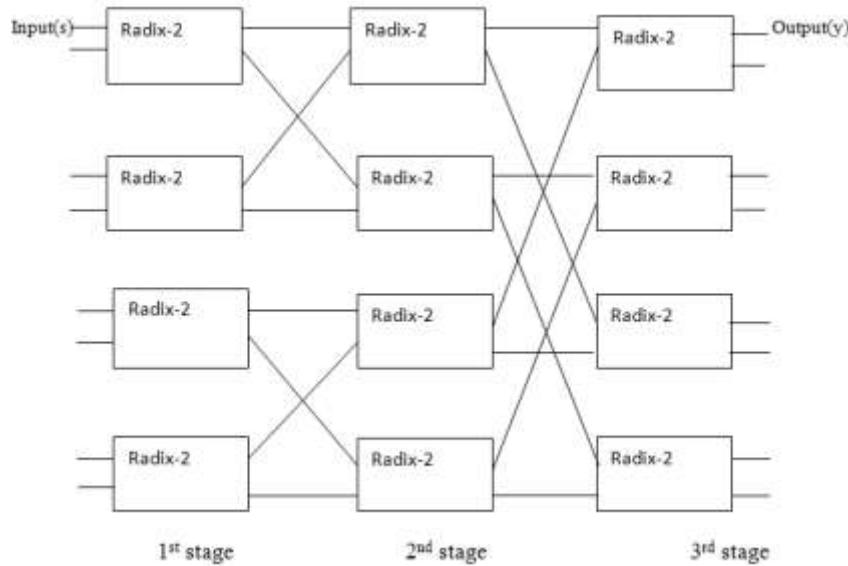


Fig.5.1: Block Diagram of 8 point FFT using 3 stage Butterfly Units

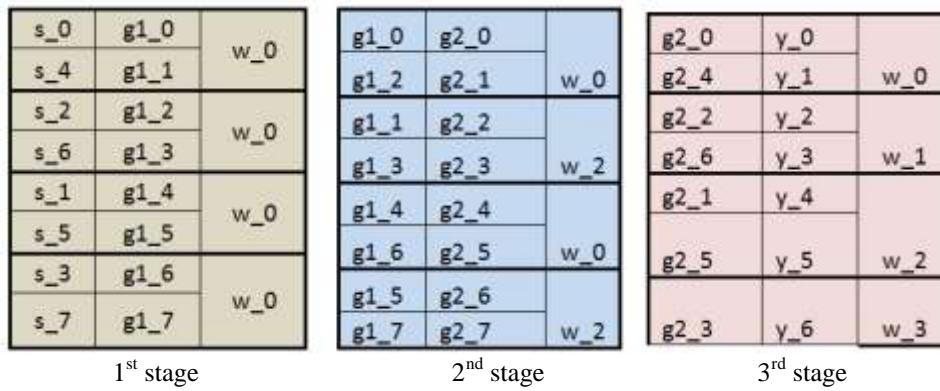


Fig.5.2: Internal structure of 8 point FFT Butterfly units

In the above figure 5.1 shows 8 point FFT algorithm in butterfly structure. This structure have three stages. In Fig.5.2 shown the internal operation of three stages 8 point FFT algorithm. Depend on internal structure write the code in VHDL and perform the operation in XILINX 14.2 tools.

VI. Simulation And Results

The RTL block thus acquired for the DIT domain by using radix-2 ,2 point FFT algorithm RTL view is shown fig.6.1 and simulation result shown in figure 6.2.

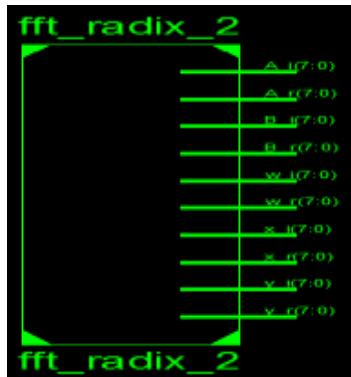


Fig.6.1: RTL View of 2 point FFT

Name	Value
$t_0[7:0]$	00000110
$t_1[7:0]$	00000100
$b_0[7:0]$	00000100
$b_1[7:0]$	00000100
$w_0[7:0]$	00000011
$w_1[7:0]$	00000011
$w_2[7:0]$	00000000
$x_0[7:0]$	00001010
$x_1[7:0]$	00000011
$y_0[7:0]$	00000010
$y_1[7:0]$	00000010
$product_1[15:0]$	00000000000010
$product_2[15:0]$	00000000000001

Fig.6.2: simulation result of 2 point FFT

The RTL block thus acquired for the DIT domain by using radix-2 ,8 point FFT algorithm is demonstrate fig.6.3 and Internal Architecture of 8 point FFT butterfly component shown in figure 6.4.

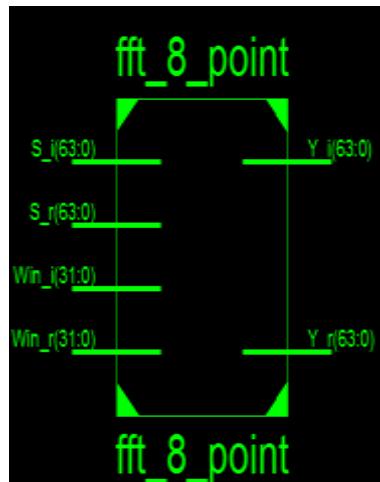


Fig.6.3: RTL View of 8 point FFT

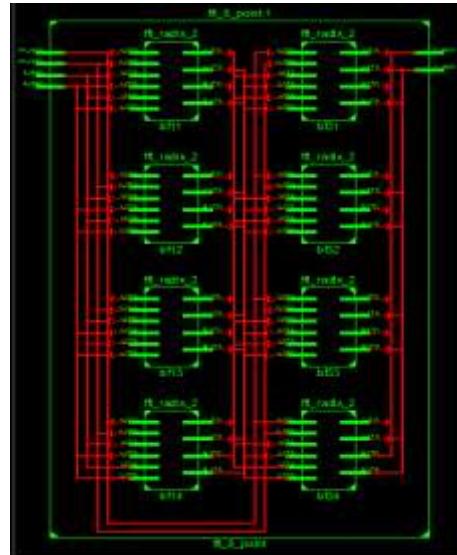


Fig.6.4: Internal Architecture of 8 point FFT

VII. Power Result

The power result shows the overall power performance of 2 and 8 point FFT algorithm. Table shows the static and dynamic power results of 2 and 8 point FFT algorithm.

FFT Length	Static Power	Dynamic Power	Total Power
2 point	0.020w	0.013w	0.033w
8 point	0.449w	0.160w	0.609w

Table: Power results of FFTS

VIII. Conclusion

In this paper we have designed 2 and 8 point FFT design using Radix-2algorithm and their simulation and synthesis are finished in VHDL using Xilinx 14.2 tool. This work demonstrate the design of 2 and 8 bit radix-2 DIT FFT is implemented in the FPGA .

The simulation of 2 bit radix-2 FFT is finished and outcome is received in Isim window. The power result of 2 bit and 8 bit radix-2 FFT are done and outcomes acquired in Xilinx XPower Analyzer, we have got two types power first static power and dynamic power.

Acknowledgements

First and foremost, I would like to thank God for blessing me with enthusiasm, courage, knowledge and energy to help me finish my project. I am thankful to my project supervisor Prof. Vaishali A. Tehre, with a heartfelt gratitude for the valuable and persistent guidance given by her through formal information, discussion, support and timely inspiration. She not only encouraged me throughout this venture but also took great pains in going through the project carefully and suggested corrections, which greatly improved the quality of project.

References

- [1]. Harpreet Kaur , Tarandip Singh 'Design and Simulation of 32-Point FFT Using Mixed Radix Algorithm for FPGA Implementation International Journal of Engineering Trends and Applications (IJETA) – Volume 2 Issue 3, May-June 2015.
- [2]. Remya Ramachandran,Vanmathi.k."simulation of radix-2 fast fourier transform using Xilinx" Remya Ramachandran et al. / International Journal of Computer Science Engineering (IJCSE) ISSN
- [3]. Waqar Hussain, Tapani Ahonen, Roberto Airolidi, Jari Nurmi "Energy and Power Estimation of Coarse-Grain Reconfigurable Array based Fast Fourier Transform Accelerators" 2012 - ieeexplore.ieee.org
- [4]. Prof.Vaishali Tehre Pooja pantwane "Low power coarse grain architecture for SoC" International conference on Quality up-gradating in engineering ,science & Technology (ICQUEST-2016).
- [5]. Alan V. Oppenheim, Ronald W. Schafer, and John R. Buck, Discrete-Time Signal Processing, 2nd edition (Upper Saddle River, NJ: Prentice Hall, 1989)
- [6]. Jump up^ C. J. Weinstein (1969-11-21). Quantization Effects in Digital Filters (Report). MIT Lincoln Laboratory. p. 42. Retrieved 2015-02-10. This computation, referred to as a 'butterfly'
- [7]. Jump up^ Cipra, Barry A. (2012-06-04). "FFT and Butterfly Diagram". mathoverflow.net. Retrieved 2015-02-10.

- [8]. W. M. Gentleman and G. Sande, "Fast Fourier transforms—for fun and profit," Proc. AFIPS 29, 563–578 (1966). doi:10.1145/1464291.1464352
- [9]. Ahmed Saeed, M. Elbably, G. Abdelfadeel, and M. I. Eladawy; "Efficient FPGA implementation of FFT/IFFT Processor"; International journal of circuits, Systems and Signal Processing, Issue 3, Volume 3, 2009.

Books:

- [10]. S.S.Limaye "VHDL A Design Oriented Approach"
- [11]. Dr. Sanjay Sharma "Digital signal processing" with Matlab programs