

# Hypothesis Testing

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Fall 2020

## $\chi^2$ Example

Random sample of 500 U.S. adults: political affiliation and opinion on a tax reform. Dependent at a 5% level of significance?

Observed

	Favor	Indifferent	Oppose
<b>Dem</b>	138	83	64
<b>Rep</b>	64	67	84

Expected

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<b>Dem</b>	115.14	85.50	
<b>Rep</b>			

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<b>Rep</b>	86.86		

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$$4.539 + 0.073 + 4.914 + 6.016 + 0.097 + 6.514 = 22.152 \quad (1)$$

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```
>>> from scipy.stats.distributions import chi2
>>> 1 - chi2.cdf(22.15, 2)
1.5494894118783797e-05
>>> from scipy.stats import chisquare
>>> chisquare([138, 83, 64, 64, 67, 84],
...           [115.14, 85.5, 84.36, 86.86, 64.5, 63.64],
...           3)
Power_divergenceResult(statistic=22.152468645918482,
                        pvalue=1.5475780213)
```

# US vs. Japanese Mileage

## Read in Data

```
>>> import pandas as pd
>>> mpg = pd.read_csv("jp-us-mpg.dat", delim_whitespace=True)
>>> mpg.head()
```

	US	Japan
0	18	24.0
1	15	27.0
2	18	27.0
3	16	25.0
4	17	31.0

Is the average car in the US as efficient as the average car in Japan?

## Two-Tailed Two-Sample $t$ -test

- Compute means

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```
>>> from numpy import mean
>>> mean(mpg["Japan"].dropna())
30.481012658227847
>>> mean(mpg["US"].dropna())
20.14457831325301
```

- Compute sample variances

## Two-Tailed Two-Sample *t*-test

- Compute means

```
>>> from numpy import mean
>>> mean(mpg["Japan"].dropna())
30.481012658227847
>>> mean(mpg["US"].dropna())
20.14457831325301
```

- Compute sample variances

```
>>> from numpy import var
>>> us = mpg["US"].dropna()
>>> jp = mpg["Japan"].dropna()
>>> jp_var = var(jp) * len(jp) / float(len(jp) - 1)
>>> us_var = var(us) * len(us) / float(len(us) - 1)
```



## Degrees of Freedom

$$\nu = \frac{\left( \frac{s_1^2}{N_1} + \frac{s_2^2}{N_2} \right)^2}{\frac{\left( \frac{s_1^2}{N_1} \right)^2}{N_1 - 1} + \frac{\left( \frac{s_2^2}{N_2} \right)^2}{N_2 - 1}} \quad (2)$$

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$$\nu = 136.8750$$

## *t*-Statistic

$$T = \frac{(\bar{x}_1 - \bar{x}_2)}{\sqrt{\frac{s_1^2}{N_1} + \frac{s_2^2}{N_2}}} \quad (3)$$

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$$T = 12.94$$

*p*-value

## $p$ -value

```
>>> 2*(1.0 - t.cdf(abs(12.946), 136.8750))  
0.0
```