# The results of CAV can not directly extend to NRA theory

```
in[1]:= verifyResult[precondition_, invariant_, guardcond_, loopcond_,
      postcondition_, f_, vars_, domain_] := Module[{ce1, ce2, ce3},
      ce1 = FindInstance[Not[Implies[domain && precondition, invariant]], vars];
                        ce2 = Table[FindInstance[Not[Implies[domain && invariant &&
           表格    求解
                               … 塩涵
             guardcond ≤ 0 && And @@ (LessEqual[#, 0] & /@ Flatten[{loopcond[i]]}]),
                            上逻辑与 上小于等于
            invariantnext = invariant /. Table[vars[j]] \rightarrow f[i][j], {j, 1, Length[vars]}]]],
         vars], {i, 1, Length[loopcond]}];
      ce3 = FindInstance[
        Not[Implies[domain && invariant && guardcond > 0, postcondition]], vars];
      Print[ce1, ce2, ce3];
      If[Length[Flatten[Join[ce1, ce2, ce3]]] == 0,
               压平
      [… [长度
       Print["Verified."],
       打印
       Print["Numerical Error Deteced."]
      ];
     1
```

### cohendiv

```
\label{eq:localization} $$\inf_{\{\cdot\}^{=}}$ vars2 = \{vx, vy, vq, vr, vd\};$ $$domain2 = And @@ Table[vars2[i]]^2 - 50^2 \le 0, \{i, 1, Length[vars2]\}];$ $$ $$ [wardcond2 = -1;$ $$loopcond2 = {-vr + vy};$ $$ f2 = \{\{vy, vd, vr - vy * vd, vq + vd, vx\}\};$ $$ precond2 = vr - vx \le 0 && -vr + vx \le 0 && -vq \le 0;$ $$ postcond2 = 1 \ge 0;$ $$ inv2 = vx = vq * vy + vr;$ $$ verifyResult[precond2, inv2, guardcond2, loopcond2, postcond2, f2, vars2, domain2];$ $$$ $$$ \{\{\{vx \to -\frac{2}{21}, vy \to -\frac{1}{7}, vq \to -\frac{2}{15}, vr \to -\frac{4}{35}, vd \to \frac{2}{105}\}\}\}$$$ Numerical Error Deteced.
```

## fermat2

In[2]:=

```
vars6 = {rr, u, v, r, n};
        domain6 = And @@ Table [vars6[i]^2 - 50^2 \le 0, {i, 1, Length[vars6]}];
        guardcond6 = -1;
        loopcond6 = \{-r+1, r\};
        f6 = \{\{rr, u, 2+v, r-v, n\}, \{rr, 2+u, v, r+u, n\}\};
        precond6 = -1 - 2 rr + u \le 0 \&\& 1 + 2 rr - u \le 0 \&\& -1 + v \le 0 \&\&
             1 - v \le 0 \& n + r - rr^2 \le 0 \& - n - r + rr^2 \le 0 \& n \ge (rr - 1)^2 + 1 \& n \le r^2;
        postcond6 = 1 \ge 0;
        inv6 = 4 n = u^2 - v^2 - 2 * u + 2 * v
        verifyResult[precond6, inv6, guardcond6, loopcond6, postcond6, f6, vars6, domain6];
Out[9]= 4 n == -2 u + u^2 + 2 v - v^2
       \Big\{\Big\{rr\to -\frac{1}{2}\text{, }u\to \text{0, }v\to \text{1, }r\to -\frac{15}{4}\text{, }n\to 4\Big\}\Big\}\Big\{\Big\{\Big\{rr\to -5\text{0, }u\to -\frac{92}{25}\text{, }v\to -\frac{138}{25}\text{, }r\to \text{1, }n\to -\frac{644}{125}\Big\}\Big\}\text{, }r\to \text{1, }r\to -\frac{644}{125}\Big\}\Big\}
           \left\{\left\{rr \to -50, u \to -\frac{92}{25}, v \to -\frac{138}{25}, r \to -50, n \to -\frac{644}{125}\right\}\right\}\right\} {}
        Numerical Error Deteced.
```

#### lcm

```
ln[*]:= vars12 = {a, b, x, y, u, v, c};
       domain12 = And @@ Table[vars12[i]^2 - 100^2 \le 0, {i, 1, Length[vars12]}];
                         逻辑与【表格
       guardcond12 = \{ -x + y \}, \{ x - y \} \};
       loopcond12 = \{-1\};
       f12 = \{ \{a, b, x - y, y, u, u + v, c\}, \{a, b, x, -x + y, u + v, v, c\} \};
       precond12 = -a + x \le 0 \&\& a - x \le 0 \&\& -b + y \le 0 \&\& b - y \le 0 \&\&
             -b + u \le 0 \&\& b - u \le 0 \&\& v \le 0 \&\& -v \le 0 \&\& -a b + c \le 0 \&\& a b - c \le 0;
       postcond12 = -c + u x + v y \le 0 & c - u x - v y \le 0;
       inv12 = u * y + v * y == a * b;
       verifyResult[precond12, inv12,
          guardcond12, loopcond12, postcond12, f12, vars12, domain12];
       \{ \{ a \rightarrow -11, b \rightarrow -5, x \rightarrow -11, y \rightarrow -5, u \rightarrow -5, v \rightarrow 0, c \rightarrow 55 \} \}
         \{\,\{\,\{\,a\rightarrow 0\,\text{, }b\rightarrow 0\,\text{, }x\rightarrow -1\,\text{, }y\rightarrow -1\,\text{, }u\rightarrow -1\,\text{, }v\rightarrow 1\,\text{, }c\rightarrow -100\,\}\,\}\,\}\,\{\,\}
       Numerical Error Deteced.
```

# ex\_sqrt

```
In[*]:= vars18 = {su, t, n, a};
      domain18 =
          su \geq -100 \;\&\& \; su \leq 100 \;\&\& \; t \geq -100 \;\&\& \; t \leq 100 \;\&\& \; a \geq -100 \;\&\& \; a \leq 100 \;\&\& \; n \geq 0 \;\&\& \; n \leq 100 \;;
       guardcond18 = {-1};
      loopcond18 = \{su - n\};
      f18 = \{ \{ su + t + 2, t + 2, n, a + 1 \} \};
       precond18 = a \le 0 \&\& -a \le 0 \&\& su - 1 \le 0 \&\& 1 - su \le 0 \&\& t - 1 \le 0 \&\& 1 - t \le 0 \&\& n \ge 0;
       postcond18 = a^2 - n \le 0 \& n - (a + 1)^2 \le 0;
      inv181 = su = (a + 1) * (a + 1);
      verifyResult[precond18, inv181,
          guardcond18, loopcond18, postcond18, f18, vars18, domain18];
       \{\;\}\;\{\;\{\,\{\,su\rightarrow0\,\text{, }t\rightarrow-100\,\text{, }n\rightarrow0\,\text{, }a\rightarrow-1\}\,\}\,\}\;\{\;\}
      Numerical Error Deteced.
```