

The result for wensely is  $0 = 0, 0 = 0, 0 = 0$

```
Needs["RISC`fastZeil`"];
```

需要

```
Needs["RISC`Dependencies`"];
```

需要

```
(*Load Aligator*)
```

```
<< Aligator`
```

```
Aligator[WHILE[(d ≥ e), IF[(P < a + b), b := b / 2;  
  d := d / 2, a := a + b;  
  y := y + d / 2;  
  b := b / 2;  
  d := d / 2]]]
```

Fast Zeilberger Package version 3.61

written by Peter Paule, Markus Schorn, and Axel Riese

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Johannes Kepler University, Linz, Austria

Package FindRelations version 0.29

written by Manuel Kauers and Burkhard Zimmermann

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Package Dependencies version 0.30

written by Manuel Kauers and Burkhard Zimmermann

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Aligator.m

Automated Loop Invariant Generation by Algebraic Techniques Over the Rationals.

Package written by Laura Kovacs and Andreas Humenberger – © TU Wien – V 0.6 (2017-02-03)

```
Out[4]= {-b[5] × d[0] + b[0] × d[5], a[0] × d[5] - a[5] × d[5] + 2 b[5] (-y[0] + y[5]),  
  a[0] × d[0] - a[5] × d[0] + 2 b[0] (-y[0] + y[5]) }
```

(this means  $bd = bd$ ,  $ad = ad + 2b(y - y)$ ,  $ad = ad + 2b(-y + y)$ )

Our environment is correctly configured

```
In[5]:= Aligator[WHILE[y > 0, t1 := t2;
  t2 := a;
  a := 5 (n + 2) t2 + 6 (n^2 + 3 n + 2) t1;
  b := 2 b;
  c := 3 (n + 2) c;
  d := (n + 2) d], LoopCounter → n, IniVal → {t1 := 1;
  t2 := 1;
  a := 1;
  b := 1;
  c := 1;
  d := 1}]
```

Method is complete!

```
Out[5]= { (7 a - 138 b c)^2 - 256 d^2, a - 23 b c + t2,
  49 a^2 - 1104 a b c - 256 d^2 + 828 b c t2, - 256 d^2 + (a - 6 t2)^2, -a + 6 t1 + 5 t2 }
```