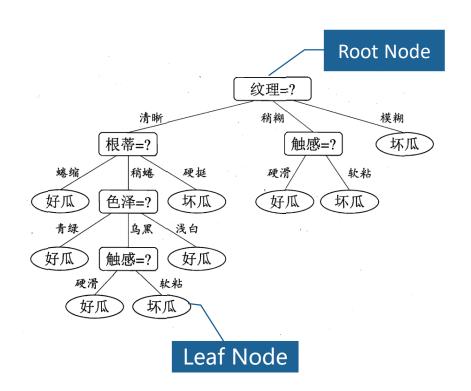


# **Decision Tree**

## Outline

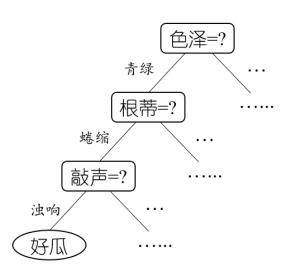
- > What's a decision tree
- The algorithm of decision tree
  - Information Gain
  - Gain ratio
  - Pruning tree
  - Continuous attributes
  - Missing values
  - Interpretability
- Summary

### **Decision Tree**



- Every non-leaf node represents a partition of an attribute
- ☐ The result of each partition either leads to a further decision problem or leads to the final conclusion
- Decision trees classify instances or examples by starting at the root of the tree and moving through branches until a leaf node
- The final conclusion of decision process corresponds to a target value

### How to Construct a Decision Tree



(1) Which attribute to start? (root)

(2) Which attribute to proceed?

(3) When to stop and obtain the target value?

# Decision Tree Algorithms

- The basic idea of decision tree algorithm:
  - Choose the best attribute(s) to split the remaining instances and make this attribute be a node
  - Repeat this process recursively for successor nodes
  - Stop when:
    - For the current node, all instances have same target value
    - Or there are no more attributes or the instances have the same values in all remaining attributes
    - Or there are no more instances

# Choosing Attributes

- One key problem of decision tree algorithm: attribute selection
- Different decision tree algorithms: different methods for attribute selection
- We will focus on the *ID3* (Interactive Dichotomize 3) algorithm [Ross Quinlan/1975]

# Information gain

- ID3 selects attributes according to their information gain
- Information gain is calculated from entropy
- Entropy is the measure of purity of a set Eg.
- Set1: 10 good watermelons
- Set2: 8 good watermelons and 2 bad watermelons
- Set3: 5 good watermelons and 5 bad watermelons

Purity: Set1 > Set2 > Set3

# Entropy

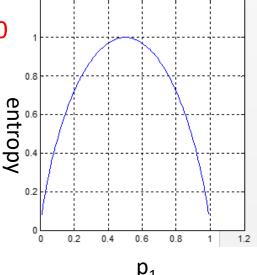
- In general, when p<sub>i</sub> is the fraction of instances labeled i,
   Entropy({p<sub>1</sub>,...,p<sub>k</sub>})=-sum(p<sub>i</sub>log(p<sub>i</sub>))
- Entropy of a set of instances relative to a binary classification is

Entropy=
$$-p_1\log(p_1)-(1-p_1)\log(1-p_1)$$

- If all the instances belong to the same class, entropy is 0
- Eg. Set1: 10 good watermelons

If the instances are equally mixed, entropy is 1

• Eg. Set2: 5 good watermelons, 5 bad watermelons



# Entropy

- Entropy is minimum when all the instances belong to the same class (highest purity)
- Entropy is maximum when the instances are equally mixed (lowest purity)
- The higher the purity, the smaller the entropy is; the lower the purity, the larger the entropy is.

## Information gain

- The information gain of an attribute is the expected reduction in entropy caused by partitioning on this attribute.
- *D<sup>i</sup>* is the subset of *D*, *a* is an attribute:

Gain(
$$D$$
,  $a$ )=Entropy( $D$ ) -  $\sum_{(i=1 \text{ to } k)} |D^i|/|D|$  Entropy( $D^i$ )

- Partitions: low entropy → high gain
- Eg.

D: 5 good watermelons, 5 bad watermelons

D1: 2 good watermelons, 1 bad watermelon

 $D^2$ : 3 good watermelons, 4 bad watermelons

Gain(D, a)= Entropy(D)-
$$\left(\frac{3}{10}$$
 Entropy(D<sup>2</sup>) +  $\frac{7}{10}$  Entropy(D<sup>2</sup>)

## The example

Ent(D)=-
$$\sum_{k=1}^{2} p_k \log_2 p_k$$
=- $(\frac{8}{17} \log_2 \frac{8}{17} + \frac{9}{17} \log_2 \frac{9}{17})$ =0.998

#### Training set

色泽:

Ent(D1)=-
$$(\frac{3}{6}\log_2\frac{3}{6} + \frac{3}{6}\log_2\frac{3}{6})$$
=1.000  
Ent(D<sup>2</sup>)=- $(\frac{4}{6}\log_2\frac{4}{6} + \frac{2}{6}\log_2\frac{2}{6})$ =0.918

Ent(
$$D^3$$
)=- $(\frac{1}{5}\log_2\frac{1}{5} + \frac{4}{5}\log_2\frac{4}{5})$ =0.722

$$\sum_{\nu=1}^{3} \frac{|D^{\nu}|}{|D|} \operatorname{Ent}(D^{\nu}) = \frac{6}{17} \times 1.000 + \frac{6}{17} \times 0.918 + \frac{5}{17} \times 0.722 = 0.889$$

$$Gain(D, 色泽) = Ent(D) - \sum_{v=1}^{3} \frac{|D^{v}|}{|D|} Ent(D^{v})$$

=0.998-
$$(\frac{6}{17} \times 1.000 + \frac{6}{17} \times 0.918 + \frac{5}{17} \times 0.722)$$

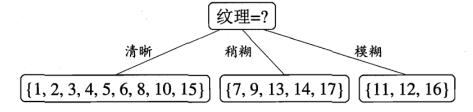
=0.109

_	编号	色泽	根蒂	敲声	纹理	脐部	触感	好瓜
_	1 .	青绿	蜷缩	浊响	清晰	凹陷	硬滑	- 是
	2	乌黑	蜷缩	沉闷	清晰	凹陷	硬滑	是
	3	乌黑	蜷缩	浊响	清晰	凹陷	硬滑	是
	4	青绿	蜷缩	沉闷	清晰	凹陷	硬滑	是
	5	浅白	蜷缩	浊响	清晰	凹陷	硬滑	是
	6	青绿	稍蜷	浊响	清晰	稍凹	软粘	是
	7	乌黑	稍蜷	浊响	稍糊	稍凹	软粘	是
-	8-	乌黑	稍蜷	浊响	清晰	稍凹	硬滑	是
	9	乌黑	稍蜷	沉闷	稍糊	稍凹	硬滑	否
	10	青绿	硬挺	清脆	清晰	平坦	软粘	否
	11	浅白	硬挺	清脆	模糊	平坦	硬滑	否
	12	浅白	蜷缩	浊响	模糊	平坦	软粘	否
	13	青绿	稍蜷	浊响	稍糊	凹陷	硬滑	否
39	14	浅白	稍蜷	沉闷	稍糊	凹陷	硬滑	否
	15	乌黑	稍蜷	浊响	清晰	稍凹	软粘	否
	16	浅白	蜷缩	浊响	模糊	平坦	硬滑	否
	17	青绿	蜷缩	,沉闷	稍糊	稍凹	硬滑	否
					_			

# The example

Gain(D, 色泽) = Ent(D) - 
$$\sum_{\nu=1}^{3} \frac{|D^{\nu}|}{|D|}$$
 Ent ( $D^{\nu}$ ) = 0.998-( $\frac{6}{17} \times 1.000 + \frac{6}{17} \times 0.918 + \frac{5}{17} \times 0.722$ ) = 0.109

#### Similarly:

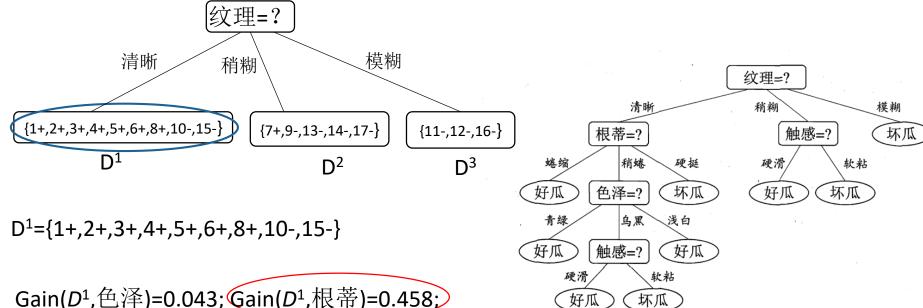


Gain(*D*,根蒂)=0.143; Gain(*D*,敲声)=0.141;

Gain(D,纹理)=0.381; Gain(D,脐部)=0.289;

Gain(*D*,触感)= 0.006

# The example



Gain(D<sup>1</sup>,色泽)=0.043; Gain(D<sup>1</sup>,根蒂)=0.458;

Gain(D<sup>1</sup>, 敲声)=0.331; Gain(D<sup>1</sup>, 脐部)=0.458;

Gain(*D*<sup>1</sup>,触感)= 0.458

### One limitation of ID3

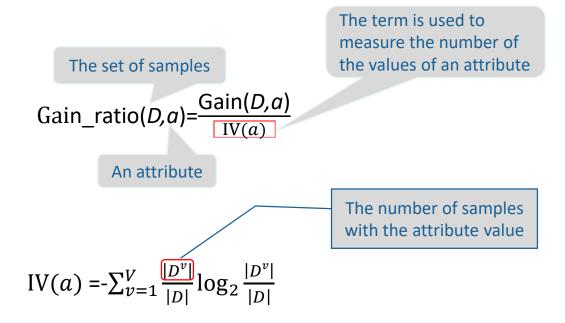
 ID3 tends to select the attribute with more values as the best attribute

> 如果我们把"编号"视为 西瓜的一个属性,它将会 被选择为最优属性。

編号	色泽	根蒂	敲声	纹理	脐部	触感	好瓜
1 1	青绿	蜷缩	浊响	清晰	凹陷	硬滑	 是
2	乌黑	蜷缩	沉闷	清晰	凹陷	硬滑	是
3	乌黑	蜷缩	浊响	清晰	凹陷	硬滑	是
4	青绿	蜷缩	沉闷	清晰	凹陷	硬滑	是
5	浅白	蜷缩	浊响	清晰	凹陷	硬滑	是
6	青绿	稍蜷	浊响	清晰	稍凹	软粘	是
7	乌黑	稍蜷	浊响	稍糊	稍凹	软粘	是
- 8	乌黑	稍蜷	浊响	清晰	稍凹	硬滑	是
9	乌黑	稍蜷	沉闷	稍糊	稍凹	硬滑	
10	青绿	硬挺	清脆	清晰	平坦	软粘	否
11	浅白	硬挺	清脆	模糊	平坦	硬滑	否
12	浅白	蜷缩	浊响	模糊	平坦	软粘	否
13	青绿	稍蜷	浊响	稍糊	凹陷	硬滑。	否
14	浅白	稍蜷	沉闷	稍糊	凹陷	硬滑	否
15	乌黑	稍蜷	浊响	清晰	稍凹	软粘	否
16	浅白	蜷缩	浊响	模糊	平坦	硬滑	否
17	青绿	蜷缩	,沉闷	稍糊	稍凹	硬滑	否
				0			

### Gain ratio

#### Gain ratio:



- Gain ratio tends to select the attribute with less values.
- C4.5 firstly selects these attributes whose information gain is higher than the average information gain, then chooses the attribute with highest gain ratio among these attributes.

## Pruning Trees

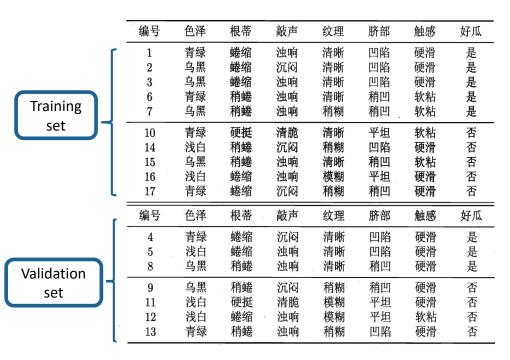
- Too many branches may cause overfitting.
- There is a technique for reducing the number of branches used in a tree – pruning
- Two types of pruning:
  - Pre-pruning (forward pruning)
  - Post-pruning (backward pruning)

# Pruning

Generalization ability is estimated by the accuracy on validation set

- Prepruning: we stop adding attributes during the process of building the decision tree
- Postpruning: we prune the attributes after the full decision tree has been built
- Prepruning & Postpruning: according to generalization ability

# Example of Prepruning

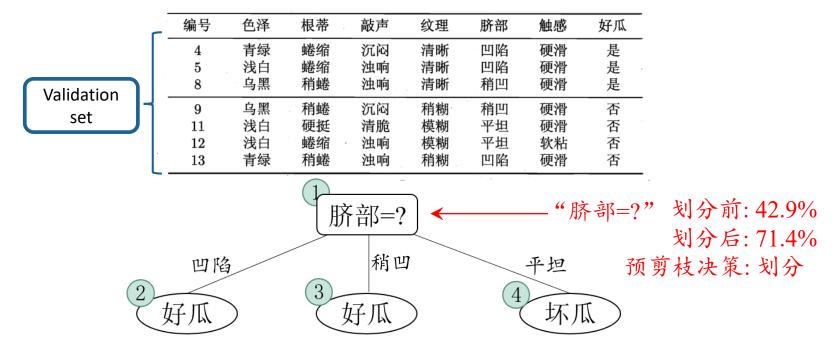


脐部=?

If stop adding this attribute and the label of the node is good:

Accuracy on validation set: 3/7=42.9%

# Example of Prepruning

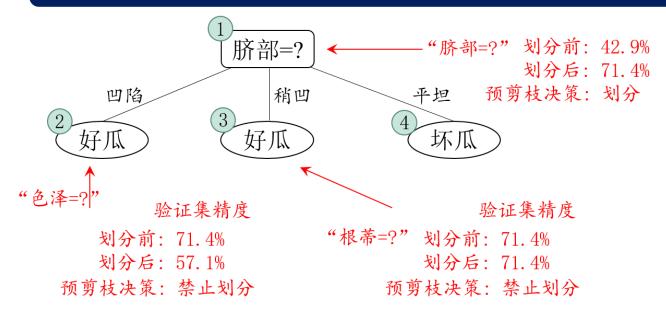


If don't stop adding this attribute:

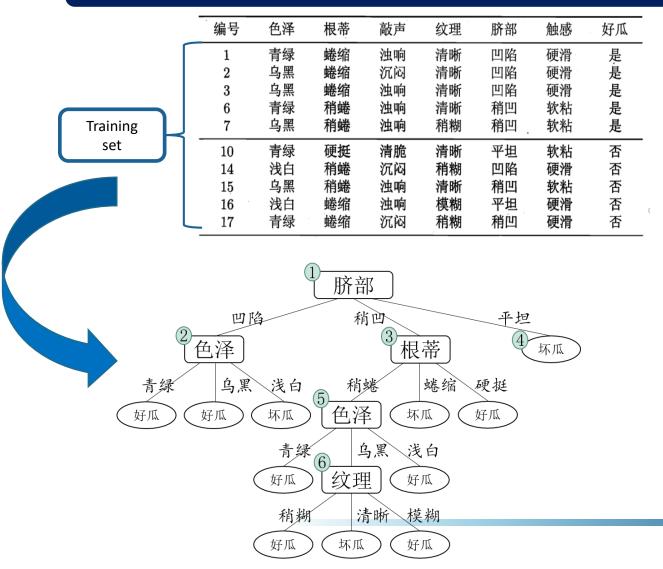
Accuracy on validation set:

(1+1+1+1+1)/7=71.4% > 42.9%

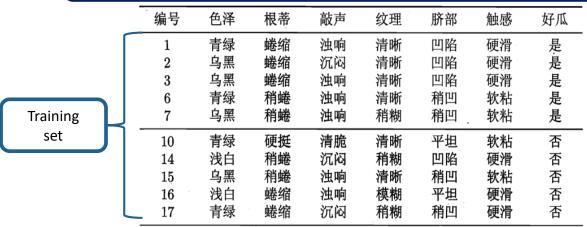
# Example of Prepruning

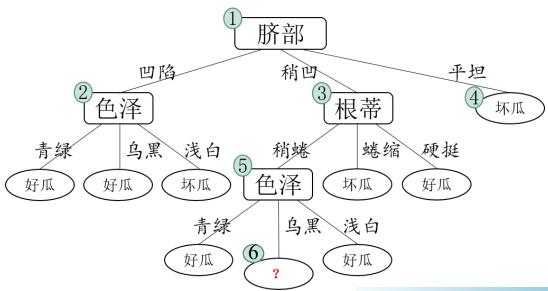


- Prepruning can reduce the risk of overfitting, but it may lead to underfitting.
- Sometimes attributes individually may cause the reduction of generalization ability, but combined, they may improve the generalization ability.



	编号	色泽	根蒂	敲声	纹理	脐部	触感	好瓜	
	4	青绿	蜷缩	沉闷	清晰	凹陷	硬滑	是	
Yo Parkers	5 8	浅白 乌黑	蜷缩 稍蜷	浊响 浊响	清晰 清晰	凹陷 稍凹	硬滑 硬滑	是是	
Validationset	9	乌黑	稍蜷	沉闷	稍糊	稍凹	硬滑	否	
Set	$\frac{11}{12}$	浅白 浅白	硬挺 蜷缩	清脆 浊响	模糊 模糊	平坦 平坦	硬滑 软粘	否否	
	13	青绿	稍蜷	浊响	稍糊	凹陷	硬滑	否	
	济部			<b>.</b>					
2 4 2 2	稍凹3	)		平坦 4					
色泽		根蒂		坏瓜					
青绿 乌黑 浅白	稍蜷	蜷约	宿硬投	£	$ \bar{\chi} $	计于节	点6,	剪枝前	Í
好瓜 好瓜 坏瓜	色泽 (	坏瓜	好瓜		弘	验证集	精度:	3/7=4	12.9%
青绿6	乌黑	浅白							
	文理?	好瓜	)	验证	E集精	度			
稍糊	清晰	模糊		一剪枝	前: 42	.9%			

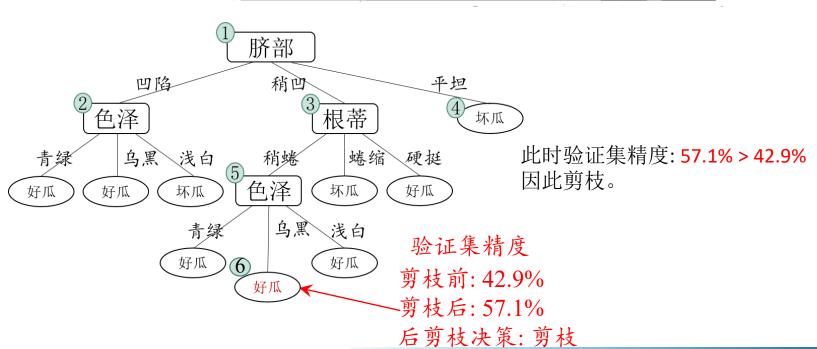




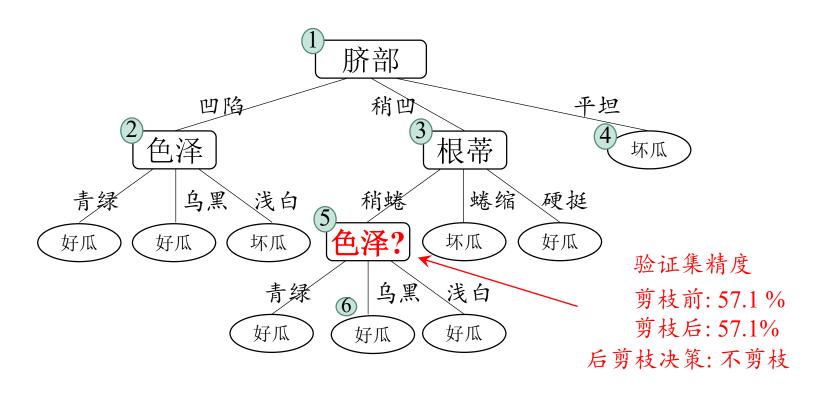
将对节点6进行剪枝,即将节点6替换为叶子节点,当前包含的训练样本为{7+,15-},标记为"好瓜"。

Validation set

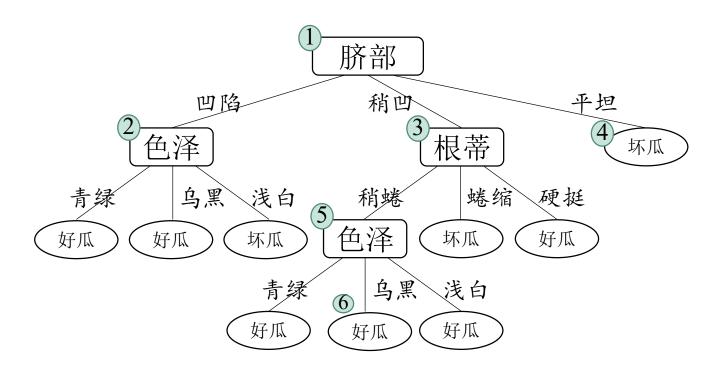
- 1	编号	色泽	根蒂	敲声	纹理	脐部	触感	好瓜
	4 5	青绿 浅白	蜷缩 蜷缩	沉闷 浊响	清晰 清晰	凹陷 凹陷	硬滑 硬滑	是是
	8	乌黑	稍蜷	浊响	清晰	稍凹	硬滑	是
	9	乌黑	稍蜷	沉闷	稍糊	稍凹	硬滑	否
	11	浅白	硬挺	清脆	模糊	平坦	硬滑	否
	12	浅白	蜷缩	浊响	模糊	平坦	软粘	否
	13	青绿	稍蜷	浊响	稍糊	凹陷	硬滑	否



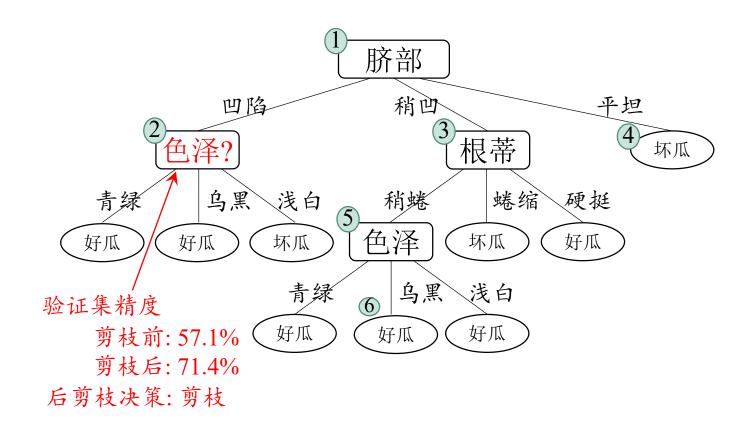
对于节点5:



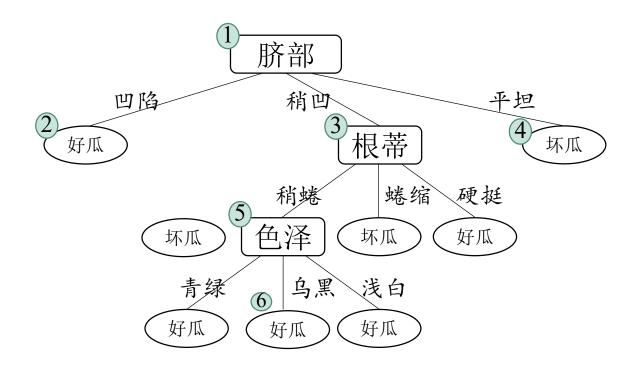
对于节点5:



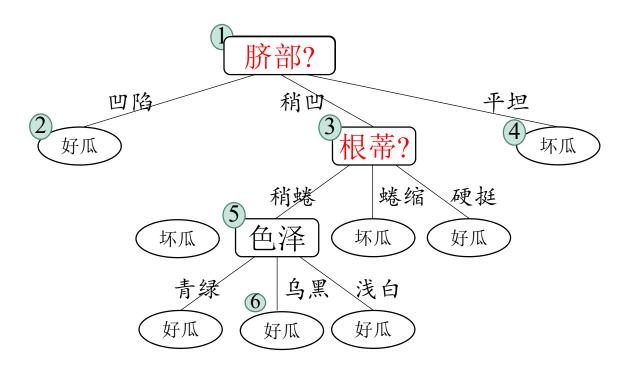
#### 对于节点2:



#### 对于节点2:

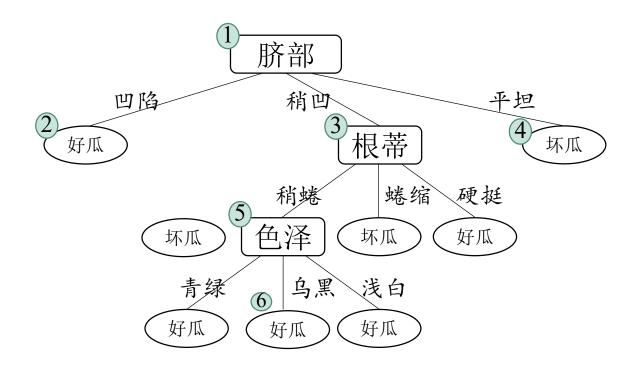


同理,先后把节点3和节点1替换为叶子节点,验证集精度均未提升,保留分支。



# Example of Pruning

最终得到的后剪枝树:



# Postpruning

- Advantages:
  - Compared to prepruning, the under-fitting risk of postpruning is low.
  - The generalization ability of postpruning is typically better than that of prepruning.
- Disadvantages:
  - The computational time is expensive.

### Continuous Attribute

- Each non-leaf node represents the partition of the attribute (easy for discrete attributes).
- **C4.5** use Bi-partition to process continuous attributes:
  - Find a threshold  $T_a$  to change continuous attribute  $A_c$  to discrete attribute  $A_d$  which has two values

$$A_{d} = \begin{cases} true, & if Ac < Ta \\ false, & otherwise \end{cases}$$

How to choose the threshold T<sub>3</sub>?

### Continuous Attribute

Training set

$$\{a^1, a^2, ..., a^n\}$$

$$T_{a} = \left\{ \frac{a^{i} + a^{i+1}}{2} \middle| 1 \le i \le n - 1 \right\}$$
 (Possible partitions)

$$\begin{aligned} & \operatorname{Gain}(D, a) = \max_{t \in Ta} \operatorname{Gain}(D, a, t) \\ & = \max_{t \in Ta} \operatorname{Ent}(D) - \sum_{\lambda \in \{-, +\}} \frac{|D_t^{\lambda}|}{|D|} \operatorname{Ent}(D_t^{\lambda}) \end{aligned}$$

We choose the threshold corresponding to the partition with highest information gain.

## Missing value

	编号	色泽	根蒂	敲声	纹理	脐部	触感	好瓜
	1		蜷缩	浊响	清晰	凹陷	硬滑	是
	. 2	乌黑	蜷缩	沉闷	清晰	凹陷		是
	3	乌黑	蜷缩	_	清晰	凹陷	硬滑	是
	4	青绿	蜷缩	沉闷	清晰	凹陷	硬滑	是
	5	-	蜷缩	浊响	清晰	凹陷	硬滑	是
	6	青绿	稍蜷	浊响	清晰	_	软粘	是
	7	乌黑	稍蜷	浊响	稍糊	稍凹	软粘	是
Training	8	乌黑	稍蜷	浊响	_	稍凹	硬滑	是是
set	9	乌黑	_	 沉闷	 稍糊	 稍凹	硬滑	
	10	青绿	硬挺	清脆	_	平坦	软粘	否
	11	浅白	硬挺	清脆	模糊	平坦	- ,	否
	12	浅白	蜷缩	_	模糊	平坦	软粘	否
	13		稍蜷	浊响	稍糊	凹陷	硬滑	否
	14	浅白	稍蜷	沉闷	稍糊	凹陷	硬滑	否
	15	乌黑	稍蜷	浊响	清晰	-,	软粘	否 否
	16	浅白	蜷缩	浊响	模糊	平坦	硬滑	否
L	17	青绿		沉闷	稍糊	稍凹	硬滑	否

Q1: How to select the attribute when some values are missed?

Q2: Given the partitioning attribute, how to partition these examples which miss values on the attribute?

### Missing value

- $ightharpoonup \widetilde{D}$  which is the subset of D contains the samples which have values on the attribute a
- $ightharpoonup \widetilde{D^v}$  which is the subset of  $\widetilde{D}$  contains the samples which have value  $a^v$  on the attribute a
- $ightharpoonup \widetilde{D_k}$  which is the subset of  $\widetilde{D}$  contains the samples labeled K

We assign a weight  $\omega_x$  for each sample x.

 $\blacksquare$  The weight ratio of the samples which have values on the attribute a:

$$\rho = \frac{\sum_{x \in \widetilde{D}} \omega_x}{\sum_{x \in D} \omega_x}$$

■ The weight ratio of the samples labeled K in  $\widetilde{D}$ :

$$\widetilde{p_k} = \frac{\sum_{x \in \widetilde{D_k}} \omega_x}{\sum_{x \in \widetilde{D}} \omega_x} \quad (1 \le k \le |y|)$$

Q1: How to select the attribute when some values are missed!

lacksquare The weight ratio of the samples which have value  $a^v$  on the attribute a in  $\widetilde{D}$  :

$$\widetilde{r_v} = \frac{\sum_{x \in \widetilde{D^v}} \omega_x}{\sum_{x \in \widetilde{D}} \omega_x} \quad (1 \le v \le V)$$

### Missing value

Then,

Gain(
$$D$$
,  $a$ )= $\rho \times$  Gain( $\widetilde{D}$ ,  $a$ )  
=  $\rho \times (\text{Ent}(\widetilde{D}) - \sum_{v=1}^{V} \widetilde{r_v} \text{Ent}(\widetilde{D^v}))$ 

$$\operatorname{Ent}(\widetilde{D}) = -\sum_{k=1}^{|\mathcal{Y}|} \widetilde{p_k} \log_2 \widetilde{p_k}$$

#### As for Q2:

- 1. For the sample x which has value on the attribute a, we put x in its corresponding child node, and its weight does not change  $(\omega_x)$ .
- 2. For the sample x which misses value on the attribute a, we put it in all child nodes, and it weight changes to  $\widetilde{r_v}$  \* $\omega_x$

#### Training set

				_			
编号	色泽	根蒂	敲声	纹理	脐部	触感	好瓜
1		蜷缩	浊响	清晰	凹陷	硬滑	 是
2	乌黑	蜷缩	沉闷	清晰	凹陷		是
3	乌黑	蜷缩	_	清晰	凹陷	硬滑	是
4	青绿	蜷缩	沉闷	清晰	凹陷	硬滑	是
5	_	蜷缩	浊响	清晰	凹陷	硬滑	是
6	青绿	稍蜷	浊响	清晰	_	软粘	是
7	乌黑	稍蜷	浊响	稍糊	稍凹	软粘	是
8	乌黑	稍蜷	浊响	_	稍凹	硬滑	是
9	乌黑	_	 沉闷	 稍糊	 稍凹	硬滑	
10	青绿	硬挺	清脆	_	平坦	软粘	否
11	浅白	硬挺	清脆	模糊	平坦	_	否
12	浅白	蜷缩	_	模糊	平坦	软粘	否
13		稍蜷	浊响	稍糊	凹陷	硬滑	否
14	浅白	稍蜷	沉闷	稍糊	凹陷	硬滑	否
15	乌黑	稍蜷	浊响	清晰	_	软粘	否
16	浅白	蜷缩	浊响	模糊	平坦	硬滑	否
17	青绿		沉闷	稍糊	稍凹	硬滑	否

- 学习开始时,根结点包含样本集中 全部17个样本,各样本的权值均初 始化为1
- 以"色泽"属性为例,在色泽属性有取值的样本为14个:

$$\widetilde{D}$$
={2+,3+,4+,6+,7+,8+,9-,10-, 11-,12-,14-,15-,16-,17-}

$$\operatorname{Ent}(\widetilde{D}) = -\sum_{k=1}^{2} \widetilde{p_k} \log_2 \widetilde{p_k}$$

$$=-(\frac{6}{14}\log_2\frac{6}{14}+\frac{8}{14}\log_2\frac{8}{14})=0.985$$

Training set

色泽:
$$\widetilde{D}$$
={2+,3+,4+,6+,7+,8+,9-,10-,11-,12-,14-,15-,16-,17-}

编号	色泽	根蒂	敲声	纹理	脐部	触感	好瓜
1		蜷缩	浊响	清晰	凹陷	硬滑	 是
. 2	乌黑	蜷缩	沉闷	清晰	凹陷		是
3	乌黑	蜷缩	_	清晰	凹陷	硬滑	是
4	青绿	蜷缩	沉闷	清晰	凹陷	硬滑	是
5	-	蜷缩	浊响	清晰	凹陷	硬滑	是
6	青绿	稍蜷	浊响	清晰	_	软粘	是
7	乌黑	稍蜷	浊响	稍糊	稍凹	软粘	是
8	乌黑	稍蜷	浊响	_	稍凹	硬滑	是
9	乌黑	_	 沉闷	稍糊	———— 稍凹	硬滑	否
10	青绿	硬挺	清脆	_	平坦	软粘	否
11	浅白	硬挺	清脆	模糊	平坦	_	否
12	浅白	蜷缩	_	模糊	平坦	软粘	否
13	_	稍蜷	浊响	稍糊	凹陷	硬滑	否
14	浅白	稍蜷	沉闷	稍糊	凹陷	硬滑	否
15	乌黑	稍蜷	浊响	清晰		软粘	否
16	浅白	蜷缩	浊响	模糊	平坦	硬滑	否
17	青绿		沉闷	稍糊	稍凹	硬滑	否

青绿: 
$$\widetilde{D}^1$$
={4+,6+,10-,17-}

乌黑: 
$$\widetilde{D}^2$$
={2+,3+,7+,8+,9-,15-}

浅白: 
$$\widetilde{D}^3$$
={11-,12-14-,16-}

Ent 
$$(\widetilde{D}^1)$$
=- $(\frac{2}{4}\log_2\frac{2}{4} + \frac{2}{4}\log_2\frac{2}{4})$ =1.000

Ent 
$$(\widetilde{D}^2)$$
 =  $-(\frac{4}{6}\log_2\frac{4}{6} + \frac{2}{6}\log_2\frac{2}{6})$  = 0.918

Ent 
$$(\widetilde{D}^3)$$
=- $(\frac{0}{4}\log_2\frac{0}{4} + \frac{4}{4}\log_2\frac{4}{4})$ =0.000

$$\sum_{v=1}^{3} \widetilde{r_{v}} \operatorname{Ent}(\widetilde{D^{v}}) = \frac{4}{14} \times 1.000 + \frac{6}{14} \times 0.918 + \frac{4}{14} \times 0.000 = 0.679$$

色泽:  $\widetilde{D}$ ={2+,3+,4+,6+,7+,8+,9-,10-,11-,12-,14-,15-,16-,17-}

#### Information gain:

Gain(
$$\widetilde{D}$$
, 色泽)=Ent( $\widetilde{D}$ )- $\sum_{v=1}^{3} \widetilde{r_{v}}$ Ent( $\widetilde{D^{v}}$ )
=0.985-( $\frac{4}{14} \times 1.000 + \frac{6}{14} \times 0.918 + \frac{4}{14} \times 0.000$ )
=0.306

我们这里把含有色泽属性样本集的权重所占的比例考虑进去(每个样本的初始权重为1):

 $\tilde{D}$ 含有14个样本,每个样本的权重为1,所以 $\tilde{D}$ 总权重为14;训练集D共包含17个样本,每个样本的权重为1,所以训练集D的总权重为17; $\tilde{D}$ 所占权重比例为 $\frac{14}{17}$ :

$$Gain(D, 色泽) = \rho \times Gain(\widetilde{D}, 色泽) = \frac{14}{17} \times 0.306 = 0.252$$

#### Similarly,

Gain(D,色泽)=0.252; Gain(D,根蒂)=0.171;

Gain(D, 敲声)=0.145; Gain(D, 纹理)=0.424;

Gain(D,脐部)=0.289; Gain(D,触感)= 0.006.



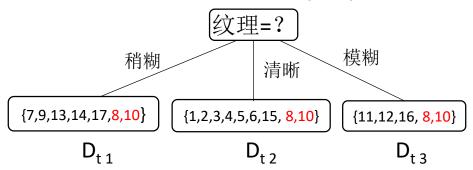
✓ 纹理(15个样本):{1, 2, 3, 4, 5, 6, 7, 9, 11, 12, 13, 14, 15, 16, 17}

其中: 稍糊(5个样本): {7,9,13,14,17}

清晰(7个样本): {1,2,3,4,5,6,15}

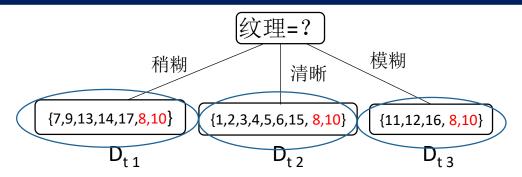
模糊(3个样本): {11,12,16}

✔ 缺失纹理属性取值的样本: {8,10}

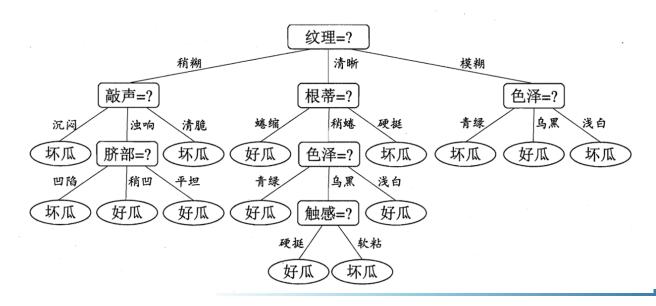


选择纹理属性后,我们把在纹理属性上有取值的样本划分到三个分支,权重不变;同时把在纹理属性上没有取值的样本**8**,**10**同时放进三个分支,在三个子节点的权重调整为 $\tilde{r}_v$ \* $\omega_x$ , 即  $\frac{5}{15}$ ,  $\frac{7}{15}$ ,  $\frac{3}{15}$ 。则:

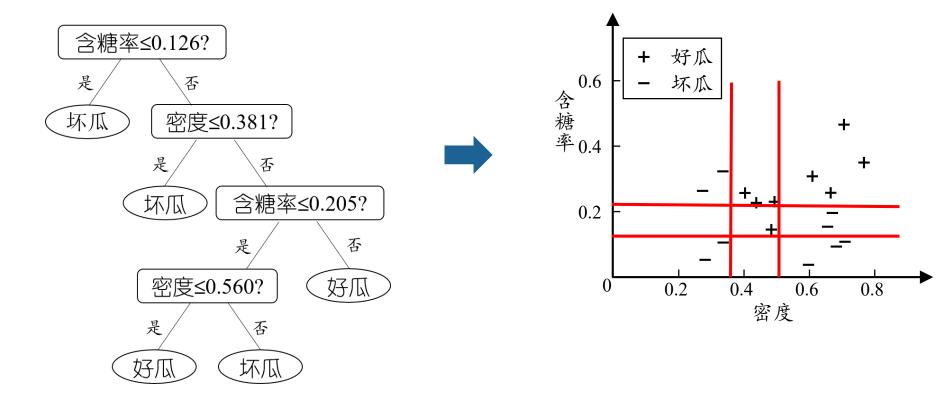
- 1.  $D_{t_1}$ 各个样本权重为: 样本7,9,13,14,17的权重为1, 样本8,10的权重为 $\frac{5}{15}$
- 2.  $D_{t2}$ 各个样本权重为: 样本1,2,3,4,5,6,15的权重为1, 样本8,10的权重为 $\frac{7}{15}$
- 3.  $D_{t3}$ 各个样本权重为: 样本1,2,3,4,5,6,15的权重为1, 样本8,10的权重为 $\frac{3}{15}$



对于后续节点同理:



## Interpretability

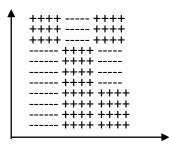


- The boundaries of classification are axis-parallel
- But for too complex problems, they may have too many small segments.

## Summary

#### Strengths

- can generate understandable rules
- perform classification without much computation
- provide a clear indication of which attributes are most important for prediction or classification
- Treat well rectangular regions



#### Weaknesses

- The trees may suffer from error propagation
- Do not treat well non-rectangular regions

### RESOURCES

- C4.5 package: http://www.rulequest.com/Personal/c4.5r8.tar.gz
- Wikipedia page for decision tree: http://en.wikipedia.org/wiki/Decision\_tree\_learning
- Random Forests (Leo Breiman and Adele Cutler): http://www.stat.berkeley.edu/~breiman/RandomForests/
- ICCV 2013 tutorial:

Decision Forests and Fields for Computer Vision: http://research.microsoft.com/enus/um/cambridg e/projects/iccv2013tutorial/

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Thanks!