

Dylan's PHYS211 Notes

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Week 1

Vector review

$v, |\vec{v}|$ Magnitude

θ above \hat{i} , Direction

The primary method to add or subtract

$$\vec{A} + \vec{B} = \vec{C} = (\vec{A}_i + \vec{B}_i) + (\vec{A}_j + \vec{B}_j)$$

$$\vec{C}_i = \vec{A}_i + \vec{B}_i$$

$$\vec{C}_j = \vec{A}_j + \vec{B}_j$$

Multiplying vectors

Scalar / Dot Product

$$\vec{A} = c\hat{i} + c\hat{j} + c\hat{k}$$

$$\vec{B} = b\hat{i} + b\hat{j} + b\hat{k}$$

$$\vec{A} \cdot \vec{B} = (\vec{A}_i + \vec{B}_i) + (\vec{A}_j + \vec{B}_j) + (\vec{A}_k + \vec{B}_k)$$

Cross Product

$$\vec{A} = c\hat{i} + c\hat{j} + c\hat{k}$$

$$\vec{B} = b\hat{i} + b\hat{j} + b\hat{k}$$

$$\vec{A} \times \vec{B} = A_j B_k - A_k B_j \hat{i} + A_k B_i - A_i B_k \hat{j} + A_i B_j - A_j B_i \hat{k}$$

Lecture 1:

Syllabus

Day

Lecture 2:

Learning

$$\vec{r}(t) = ct\hat{i} + (ct - gt^2/2)\hat{j} + 0\hat{k}$$

$$\vec{v}(t) = \frac{d\vec{r}}{dt} = \frac{dr_x}{dt}\hat{i} + \frac{dr_y}{dt}\hat{j} + 0$$

$$c\hat{i} + (c - gt)\hat{j}$$

$$\vec{a} = (-g)\hat{j}$$

Kinematics Review



Figure 1: Display of vectors

Position : $\vec{r}(t)$

Length / distance : $r = |\vec{r}(t)|$

Displacement : $\Delta\vec{r}$

Velocity :

$$\vec{v}_{avg} = \frac{\vec{r}(t + \delta t) - \vec{r}(t)}{\Delta t}$$

Instantaneous Velocity :

$$\vec{v}(t) = \lim_{\Delta t \rightarrow 0} \frac{\vec{r}(t + \Delta t) - \vec{r}(t)}{\Delta t} = \frac{d}{dt}\vec{r}(t)$$

Acceleration :

$$\vec{a}(t) = \frac{d}{dt}\vec{v}(t) = \frac{d}{dt^2}\vec{r}(t)$$

Example problem : Find velocity (Accelerations) from position (velocity)

Example : Suppose that the position of a particle is given by $\vec{r} = A(e^{\alpha t}\hat{i} + e^{-\alpha t}\hat{j})$, where A and α are constants. Find the velocity and sketch the trajectory.

$$\vec{r} = A(e^{\alpha t}\hat{i} + e^{-\alpha t}\hat{j})$$

Velocity would follow from a simple derivative :

$$\frac{d}{dt}\vec{r} = A(\alpha e^{\alpha t}\hat{i} - \alpha e^{-\alpha t}\hat{j})$$

We can factor out :

$$\vec{v} = A\alpha(e^{\alpha t}\hat{i} - e^{-\alpha t}\hat{j})$$

we can sketch this graph by just looking at the behaviors of the graph at its extremes.

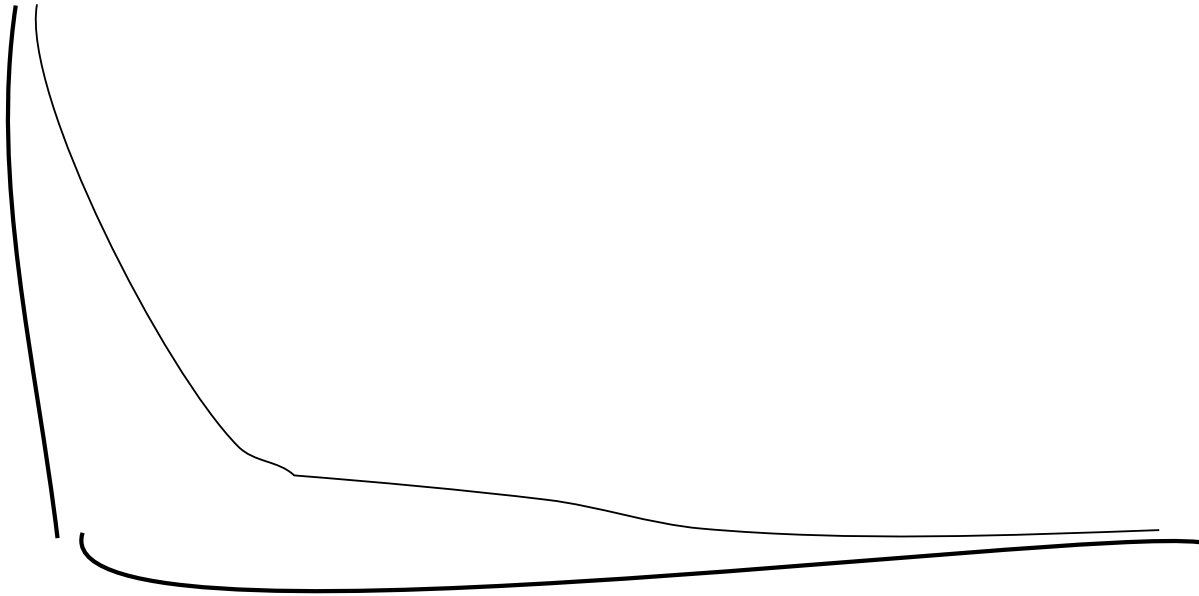


Figure 2: Sample decay graph

A table-tennis ball is released near the surface of the moon with initial velocity $\vec{v}_0 = (0, 5, 3) \text{ m/s}$. It accelerates downward with acceleration $\vec{a} = (0, 0, -1.6) \text{ m/s}^2$. Find its velocity at $t = 5\text{s}$

This is just a simple function of units :

$$5\text{s} \left(-1.6 \text{ m/s}^2 \hat{k} \right)$$

$$25 \cdot -1.6 = -40$$

Simple addition then :

$$3 - 40 = -37$$

The balls velocity at 5 seconds is :

$$\vec{v}(5) = (0, 5, -37)$$

This can also be done more formally, aka the "correct" way :

$$\vec{v}(t) = \int \vec{a}(t) dt, \int_{t_0}^{t_f} \frac{d\vec{v}}{dt} dt = \vec{v}_f - \vec{v}_0$$

$$\begin{aligned}\int_{t_0}^{t_f} \vec{a}(t) dt &= \int_{t_0}^{t_f} (0, 0, a_z) dt = (0, 0, a_z)t \Big|_{t_0}^{t_f} \\ &= (0, 0, a_z(t_f - t_i)) =\end{aligned}$$