

---

## **Abstract**

Content

---

# 1. Introduction

Theoreticians have briefed the significance of the mixing properties of binary liquid alloys from both the scientific and the technological points of view. A precise understanding of the mixing properties and phase diagrams of the alloy system is elementary to establish a good arrangement between the experimental results, theoretical approaches, and empirical models for liquid alloys with a miscibility gap. All liquid binary alloys can be grouped into two distinct classes that either exhibit positive deviation (usually called segregating systems) or negative deviation (i.e. short-ranged ordered alloys) from Raoult's law or the additive rule of mixing. If the deviations are considerably large, they may conduct either phase separation or compound formation in the binary system.

There are liquid alloys, however, which do not belong exclusively to any of the above two classes. For instance, the excess Gibbs energy of mixing ( $G_M^{xs}$ ) for Cd-Na, and Ag-Ge is negative at certain compositions, while positive at other compositions. In liquid alloys such as Au-Bi, Bi-Cd, and Bi-Sb, the enthalpy of mixing  $H_M$  is a positive quantity but  $G_M^{xs}$  is negative. Bi-Pb has positive  $H_M$  and  $G_M^{xs}$  in the solid phase as against the negative values of  $H_M$  and  $G_M^{xs}$  in the liquid phase. Systems such as Au-Ni and Cr-Mo exhibit immiscibility in the solid phase which is not visible in the interrelated liquid phase. Systems such as Ag-Te show intermetallic phases and large negative  $H_M$  values in the liquid phase concurrently with a liquid miscibility gap.

Systems such as Al-Bi, Al-In, Al-Pb, Bi-Ga, Bi-Zn, Cd-Ga, Ga-Pb, Ga-Hg, Pb-Zn, Pb-Si and Cu-Pb, etc, are represented by liquid miscibility gaps and exhibit enormous positive  $H_M$ . Their properties in the liquid phase tend to vary markedly as a role of composition (c), temperature (T), and pressure (p). The long-wavelength limit ( $q \rightarrow 0$ ) of the composition-composition structure factors,  $S_{cc}(0)$  diverges as the composition and temperature approach the critical values  $c \rightarrow c_c$ , and  $T \rightarrow T_c$ .  $S_{cc}(0)$ , which can instantly be obtained from thermodynamic functions (either acquired by taking the first composition derivative of the activity or through the second derivative of the Gibbs function), is very useful for establishing the immiscibility and the degree of segregation in binary liquid alloys. Additional thermodynamic, structural, and transport properties are also found to alter anomalously in the area of  $c_c$  and  $T_c$ .

A provided unary system is expressed by two pairs of independent variables, namely the mechanical degrees of freedom (pressure (p) or volume ( $\Omega$ )) and the thermal degrees of freedom (temperature (T) or entropy (S)). The preference of independent variables is mostly a concern of free option; yet, there are four possibilities for creating such pairs have one mechanical and one thermal variable, say (S,  $\Omega$ ), (S, p), (T,  $\Omega$ ) and (T, p). These pairs guide to thermodynamic functions such as internal energy  $E(S, \Omega)$ , enthalpy  $H(S, p)$ , Helmholtz energy  $F(T, \Omega)$ , and Gibbs energy  $G(T, p)$ , respectively.

The enthalpy, H, merging the internal energy E to the mechanical degrees of freedom (p,  $\Omega$ ) is

$$H = E + p\Omega \quad (1)$$

or in differential form,

$$dH = \delta Q + \Omega dp \quad (2)$$

where

$$\delta Q = dE + pd\Omega$$

The Helmholtz energy, F, relates E to the thermal degrees of freedom (S, T), i.e.

$$F = E - TS \quad (3)$$

or,

$$dF = -SdT - pd\Omega \quad (4)$$

In the case of reversible isothermal and isochoric processes (T,  $\Omega$  = constant),  $dF = 0$ , i.e. F remains invariant. Similarly, the Gibbs function establishes a relation between H and the thermal degrees of freedom, i.e.

$$G = H - TS \quad (5)$$

or

$$dG = -SdT + \Omega dp \quad (6)$$

In the case of a reversible isothermal reaction at constant pressure ( $T$ ,  $p$  = constant),  $dG = 0$ , i.e.  $G$  remains invariant.

Also,  $H$ ,  $F$  and  $G$  can readily be used to obtain the heat capacity  $C$  ( $C_p$  or  $C_\Omega$ ), entropy, isothermal ( $\chi_T$ ) and adiabatic ( $\chi_S$ ) compressibilities, the volume and the volume expansivity ( $\alpha_p$ ):

$$C_p = \left( \frac{\partial H}{\partial T} \right)_p = T \left( \frac{\partial S}{\partial T} \right)_p = -T \left( \frac{\partial^2 G}{\partial T^2} \right)_p \quad (7)$$

$$C_\Omega = \left( \frac{\partial E}{\partial T} \right)_\Omega = T \left( \frac{\partial S}{\partial T} \right)_\Omega = -T \left( \frac{\partial^2 F}{\partial T^2} \right)_\Omega \quad (8)$$

$$S = \left( \frac{\partial G}{\partial T} \right)_p = \left( \frac{\partial F}{\partial T} \right)_\Omega \quad (9)$$

$$\Omega = \left( \frac{\partial G}{\partial p} \right)_T \quad (10)$$

$$\chi_T \equiv -\frac{1}{\Omega} \left( \frac{\partial \Omega}{\partial p} \right)_T \quad (11)$$

$$\chi_S \equiv -\frac{1}{\Omega} \left( \frac{\partial \Omega}{\partial p} \right)_S \quad (12)$$

$$\alpha_p \equiv \frac{1}{\Omega} \left( \frac{\partial \Omega}{\partial T} \right)_p \quad (13)$$

At indicator, we furthermore have some important effects from isotherms of liquid-vapor phases which at the critical point must fulfill

$$\left( \frac{\partial p}{\partial \Omega} \right)_{T_c} = \left( \frac{\partial^2 p}{\partial \Omega^2} \right)_{T_c} = 0 \quad (14)$$

At  $T = T_c$ , the following physical properties become infinite, i.e.

$$C_p = T \left( \frac{\partial S}{\partial T} \right)_p = \infty \quad (15)$$

$$\alpha_p = \frac{1}{\Omega} \left( \frac{\partial \Omega}{\partial T} \right)_p = \infty \quad (16)$$

$$\chi_T = - \left( \frac{\partial \Omega}{\partial p} \right)_T = \infty \quad (17)$$

For a binary mixture, such as an A–B alloy consisting of  $c_A$  moles of component A and  $c_B$  moles of component B, rather than guiding to the fundamental values of their function, we define the function of mixing. For example, the Gibbs energy of mixing,  $G_M$ , is represented as

$$G_M = G(alloy) - c_A G_A^0 - c_B G_B^0 \quad (18)$$

where  $G_A^0$  and  $G_B^0$  are the Gibbs free energy of the two pure components. Equivalent definitions also exist for HM, SM and other functions. The integral quantities can also be divided into the partial quantities, i.e.

$$G_M = c_A \bar{G}_{M,A} + c_B \bar{G}_{M,B} \quad (19)$$

with

$$\bar{G}_{M,i} = RT \ln a_i \quad (i = A, B)$$

where  $\bar{G}_{M,i}$  are the partial Gibbs energies and  $a_i$  are the thermodynamic activities of the component i.  $G_M$  defines the stability of the phases in a binary mixture. The curves describing  $G_M$  against c deviation can, in general, have a shape like either curve a or curve b as displayed in figure 1. For  $G_M$  as in curve a, the homogeneous solution is stable at all values of c at  $T_1$ ; if not other phases (i.e. intermediate phases) in the system display more negative  $G_M$  values.

Figure 1: A schematic diagram symbolizing the Gibbs energy of mixing at constant T plotted against concentration. Curve a, complete mixing ( $T_1 < T_c$ ). Curve b, incomplete mixing ( $T_2 < T_c$ ),  $\Delta c$  represents the miscibility gap at  $T_2$ .

For curve b, the homogeneous solution is varying in the composition range  $\Delta c$ , because  $G_M$  can be reduced if the mixture separates into two phases. The composition of these phases is provided by the points of contact P and Q of the common tangent line to the  $G_M(c)$  curve. The reduced  $G_M$  values of these two phases are given by this line. Within the composition range  $\Delta c$  only the portions of the two phases change if the total composition of the alloy modifications. At P( $c_1$ ) and Q( $c_2$ ) the partial Gibbs energies of the components of both diverged phases are equivalent,

$$\overline{G}_{M,i}(c_1) = \overline{G}_{M,i}(c_2) \quad (i = A, B)$$

Hence P and Q indicate the limit of thermodynamic equilibrium.  $G_M$  diverges as a function of temperature from a concave to a convex surface for  $\Delta c$  at the spinodal. The points of inflection in the curves define the spinodal line. The critical composition and the critical temperature are determined from the conditions at  $T = T_c$

$$\left( \frac{d^2 G_M}{dc^2} \right)_{c=c_c} = 0 \quad (20)$$

$$\left( \frac{d^3 G_M}{dc^3} \right)_{c=c_c} = 0 \quad (21)$$

At this step, it should be pointed out that the long-wavelength limit ( $q \rightarrow 0$ ) of the structure factor  $S_{cc}(q)$  which is well known as the concentration fluctuation,  $S_{cc}(0)$ , is also correlated to the thermodynamic function, i.e

$$S_{cc}(0) = RT \left( \frac{d^2 G_M}{dc^2} \right)_{T,P}^{-1} \quad (22)$$

As  $c \rightarrow c_c$  and  $T \rightarrow T_c$ , one sees that

$$S_{cc}(0) \rightarrow \infty \quad (23)$$

Thus, a phase separation in a binary mixture is signaled by a strong enhancement of the concentration fluctuations. The ideal solution behavior (HM = 0) of a binary mixture is presented by

$$G_M^{id} = RT(c_A \ln c_A + c_B \ln c_B). \quad (24)$$

The distinctions in the thermodynamic behavior of a real binary solution and an ideal solution are represented by the excess quantities, i.e.

$$G_M^{xs} = G_M - G_M^{id} \quad (25)$$

or using equation (5)

$$G_M^{xs} = H_M - TS_M^{xs} \quad (26)$$

with

$$S_M^{xs} = S_M + R(c_A \ln c_A + c_B \ln c_B) \quad (27)$$

## 2. Observable indicators

### 0.1 Segregating liquid alloys

From the point of view of interatomic interactions, a binary alloy is either (i) an ordered alloy, where unlike atoms are chosen as nearest neighbors over like atoms, or (ii) a segregated alloy, where like atoms are chosen to pairs as nearest neighbors over unlike atoms. Unfortunately, there is no direct way to distinguish the constituent atoms and hence the identification of a nearest-neighbor pair of atoms is challenging. In this case either the structural data or the experimental thermodynamic functions (such as activity, the heat of mixing, excess Gibbs energy of mixing, excess heat capacity, etc) or other thermophysical data (such as viscosity, diffusivity, density, surface tension, electrical resistivity, etc) are supposed to extract information associated with interatomic interactions. Some of the empirical criteria as well as microscopic parameters which are used to identify segregated alloys are summarized below.

- (a) Alloys displaying positive deviations from Raoult's law.
- (b) The heat of formation and the excess Gibbs energy of mixing are positive.
- (c) The concentration fluctuation in the long-wavelength limit ( $S_{cc}(0)$ ) is greater than the ideal value.

Table 1 provides a list of  $G_M^{xs}$ ,  $H_M$  and  $S_M^{xs}$  at the equiatomic composition of segregating liquid alloys which are arranged according to the type

Table 1: Thermodynamic properties of liquid binary alloys at equiatomic composition displaying segregation. The values are from Ref. [(i) Hultgren et al 1973, (iii) Yu 1994]

Alloys	Ref.	T (K)	$G_M^{xs}/RT$	$H_M/RT$	$S_M^{xs}/R$
Al-Bi	(i)	900	0.814	0.823	0.09
Al-In		1150	0.54	0.49	-0.05
Al-Pb		1700	0.527	0.847	0.32
Bi-Ga	(ii)	550	0.493	0.433	-0.06
Bi-Zn		880	0.36	0.60	0.24

of their phase equilibria. Of these Bi-Zn, Pb-Zn, Cu-Pb, Cd-Ga, Al-Bi, Al-In, Al-Pb, etc, exhibit liquid immiscibility.  $G_M^{xs}$  and  $H_M$  are comparatively large positive quantities. For these alloys only a few experimental heat capacity data are available. The data, in general, show a decrease in  $C_p$  with increasing temperature. The energetic and structural effects in the solution phase can be more directly seen by the excess heat capacity  $\Delta C_p$  values:

$$\Delta C_p = C_p(c) - c_A C_{p,A} - c_B C_{p,B} \quad (28)$$

$\Delta C_p$  are positive and indicate maximum values near to  $T_c$  and  $c_c$ .

Since the pioneering work by Hume-Rothery and his coworkers (see, for example, Hume-Rothery and Raynor 1954), a substantial effort has been assembled to identify the factors impacting the alloying behavior of liquid metallic mixtures, such as the difference in atomic sizes, valence differences, electronegativity differences, etc. For the sake of a brief perusal, we enroll the basic physical, thermochemical and structural properties of pure liquid metals (near the melting points) in table 2 which are the components of the binary mixture of table 1. These properties are also useful for further discussions. At this step, it is not possible to single out any individual elemental properties which might be held reliable for demixing of liquid alloys. Yet, the practical analyses recommend that quantities such as atomic size, the heat of



vaporization, and electronegativity together hold the key to the knowledge of the segregation or order in a liquid alloy.

### Thermodynamic properties

Some of the thermodynamic properties of equiatomic segregating liquid alloys are tabulated in table 1. Here we intend to discuss briefly the salient features of the various experimental techniques and the specific results that exist as a function of concentration and temperature. The experimental methods used to obtain reliable thermodynamic data at constant pressure as a function of composition and temperature are briefly summarized. The entropy of formation  $S_M$  of an alloy can only be defined directly from  $C_p(c, T)$  data

$$S_M(c, T) = \int_0^T \frac{\Delta C_p(c, T)}{T} dT \quad (29)$$

To obtain  $S_M$  according to equations (28) and (29) the  $C_p$  values of the components and the alloy have to be known down to 0 K as well as the entropy of transformations that take place below  $T$ . There are several problems. At first, the differences between the  $C_p$  values of the mechanical mixture and the alloy are small and one has to know the  $C_p$  values to high accuracy to get reliable results for  $S_M$ . Equation (29) uses likewise to ordered crystalline substances in the solid-state only. Alloys are occasionally disordered at room temperature and remain so down to 0 K.  $S_M$  values of a liquid alloy cannot be acquired from equation (29) because the  $C_p$  values of the undercooled liquid state for the components and the alloys have to be verified specifically. Since for multicomponent systems, the reference state is the mechanical mixture of the pure components in the same state as the solution, the entropy of formation of solid and liquid alloys are, hence, typically confined from experimentally obtained  $G_M(c, T)$  and  $H_M(c, T)$  values according to equation (5).

### Calometric measurements

The enthalpy of formation  $H_M$ , their partial values  $\bar{H}_{M,i}$  and the heat capacity of liquid alloys can be directly specified by calorimetric methods. An isoperibolic type of calorimeter which operates at constant  $T$  is particularly

Some physical, chemical and structural properties of liquid metals (near melting temperature) are associated with the formation of segregating type metallic mixtures.  $m$ , atomic weight ( $1u = 1.66 \times 10^{-27} \text{ kg}$ );  $T_m$ , melting point;  $\Omega$ , volume;  $\Delta H_m$ , enthalpy of melting;  $\Delta H_v$ , enthalpy of evaporation;  $\Delta S_m$ , entropy of melting;  $\Delta S_v$ , entropy of vaporization;  $r_1$  nearest-neighbour distance;  $Z$ , first shell coordination;  $\Gamma$ , surface tension;  $x$ , Pauling electronegativity value. (i) After Iida and Guthrie (1988), (ii) after Waseda (1980); (iii) after Pauling (1960)

Metals	$m^{(i)}(u)$	$T_m^{(i)}$	$\Omega^{(i)}$	$\Delta H_m^{(i)}$	$\Delta H_v^{(i)}$	$\Delta S_m^{(i)}$	$\Delta S_v^{(i)}$	$r_1^{(ii)}$	$Z^{(ii)}$	$\Gamma^{(i)}$	$(x)^{(iii)}$
Al	26.98154	933.35	11.6	10.46	291	11.2	104	2.82	11.5	914	1.5
Bi	208.9804	544.1±0.05	20.80	10.88	179	20.0	97.4	3.38	8.8	378	1.9
Cd	112.41	594.05	14.00	6.40	100	10.8	96.2	3.11	10.3	570	1.7
Ga	69.72	302.93±0.005	11.40	5.59	270	18.4	100	2.82	10.4	718	1.6
In	114.82	429.55	16.3	3.26	232	7.58	98.9	3.23	11.6	556	1.7
Pb	207.2	600.55	19.42	4.81	178	8.02	88.0	3.33	10.9	458	1.8
Zn	65.38	692.62	9.94	7.28	114	10.5	96.6	2.68	10.5	782	1.6

appropriate for calculating  $H_M$  and  $\overline{H}_{M,i}$  of a liquid alloy as a function of composition at constant T directly. The  $H_M$  values acquired for liquid In–Cd alloys at 628 K are shown in figure 2 as an example.

Figure 2: Enthalpy of mixing of liquid Cd–In alloys

If the modification in concentration  $\Delta c_A$  is small for each successive step (i.e.  $< 1 \text{ at.}\%$ ),  $dH_M(c)/dc$  can be confined in a suitable approximation by

$$\frac{dH_M(c)}{dc_A} \left( c_A + \frac{\Delta c_A}{2} \right) = \frac{H_M(c_A + \Delta c_A) - H_M(c_A)}{\Delta c_A} \quad (30)$$

The partial values of a multi-component system are obtained by

$$\overline{H}_{M,i} = H_M + \sum_{j=2}^r (\delta_{ij} - c_j) \frac{\partial H_M(c)}{\partial c_j} \quad (31)$$

with  $\delta_{ij} = 0$  for  $i \neq j$  and  $\delta_{ij} = 1$  for  $i = j$ .  $r$  is the number of components. Figure 3 shows the experimentally determined slope  $dH_M/dc_{C_d}$  of liquid In–Cd alloys at 628 K. These results undoubtedly show that small deviations from a standard solution behaviour ( $H_M(c) = Ac_{ACB}$ ) exist.

The heat capacity of liquid alloys can be specified directly by adiabatic calorimetry. Adiabatic calorimetry applies to calculate the heat input  $\Delta Q$  to a sample and the associated temperature increase  $\Delta T$ . Heat losses have to be minimized by proper surroundings to approximate an adiabatic chamber for the sample. The specific heat over the temperature increase is given by

$$C_p = \frac{\Delta Q}{m\Delta T} \quad (32)$$

where  $m$  is the mass of the sample.

Figure 3: Calorimetrically determined slope of the enthalpy of mixing of liquid Cd–In alloy at 628 K (after Predel and Oehme 1977).

## Section - 1

### Optimization of thermodynamic data

Thermodynamic calculations of phase equilibria are widely used to check the consistency of data got from different experimental measurements (phase diagram data, results of calorimetry ). Model descriptions using statistical thermodynamics or polynomial expressions are used to represent the thermodynamic properties of all phases applied. The adjustable coefficients are determined by a weighted least-squares method (e.g. Lukas and Fries 1992). The essential feature of this procedure is to obtain a uniform set of model parameters in an analytical representation. This helps one to gather into temperature and concentration regions where the direct experimental determination is difficult. It also allows one to estimate safely the thermodynamic data of metastable phases. Finally, the thermodynamic description of multi-component systems can be gathered from those already calculated for their subsystems. The strategy of such a critical assessment will be demonstrated for the demixing Al–In, Al–Pb, Cd–Ga, and Bi–Zn systems.

#### (a) The Al–In System

The  $H_M$  values near the equiatomic composition received by Predel and Sandig (1969a) are about 50% more enormous than the values determined by Girard (1985) and Sommer et al (1993). The alloy samples, each of about 0.5 g, were included in a closed graphite crucible which was encapsulated under argon in a quartz glass ampule. The quartz glass ampules were mechanically vibrated at about 1200 K to ensure a homogeneous liquid alloy before the DTA experiment on cooling was formed to obtain the binodal. The critical temperature amounted to 1112 K.

In the background of this information, the optimization is performed. The major task is to characterize the thermodynamic properties as a power-series law whose coefficients (say, A, B, C, D, . . .) are determined by the least-squares method. The heat capacity can be expressed as

$$C_p = -C - 2DT - 2ET^{-2} - .... \quad (33)$$

The enthalpy and energy is given by

$$H = H(T_0) + \int_0^T C_p dT \quad (34)$$

or

$$H = A - CT - DT^2 + 2ET^{-1} - \dots$$

and

$$S = S(T_0) + \int_0^T \frac{C_p}{T} dT \quad (35)$$

or

$$S = -B - C(1 + \ln T) - 2DT + ET^{-2} - \dots$$

Using equation (5), the T dependence of the Gibbs energy may be written as

$$G = A + BT + CT \ln T + DT^2 + ET^{-1} + \dots \quad (36)$$

The composition dependency of the excess Gibbs energy of mixing is given by a polynomial such as the Redlich–Kister polynomial (Redlich and Kister 1948):

$$G_M^{xs}(c, T) = c_A c_B \sum_{l=0}^m K_l(T) (c_A - c_B)^l \quad (37)$$

with  $K_l(T) = A_l + B_l T + C_l T \ln T + D_l T^2 + \dots$ . The coefficients  $K_l$  have the same temperature dependence as  $G$  in equation (37). The partial quantities are given by

$$\overline{G}_A^{xs}(c, T) = c_B^2 \sum_{l=0}^m K_l(T) [(1 + 2l)c_A - c_B] (c_A - c_B)^{l-1} \quad (38)$$

$$\overline{G}_B^{xs}(c, T) = c_A^2 \sum_{l=0}^m K_l(T) [c_A - (1 + 2l)c_B] (c_A - c_B)^{l-1} \quad (39)$$

The pure solid elements Al and In in their stable form at 298.15 K and 1bar were chosen as the reference state of the system. The Gibbs energies of the elements as functions of the

Figure 4: calculated phase diagram (continuous curve) using the coefficient set given in table 3.

Table 2: Optimized coefficient set of  $G_M^{xs}$  (equation (37)) for liquid Al–In alloys

l	$A_l$ ( $Jmol^{-1}$ )	$B_l$ ( $Jmol^{-1}K^{-1}$ )
0	18641.14	1.74886
1	558.36	1.14350
2	10692.88	7.47862
3	1346.56	0

Figure 5: Calculated enthalpy of mixing (continuous curve) using the coefficient set given in table 3.

temperature were compiled by Dinsdale (1991) and no solid solubility was considered. The excess Gibbs energy of the liquid alloy is represented by equation (37). The optimized coefficients are given in table (3) and the phase diagram in figure (4).

#### (b) The Al–Pb system.

The experimental results on Al–Pb imply a vast liquid miscibility gap due to the strong segregation tendency of the components. The solubility of lead in solid aluminum is less than 0.025 at.% Pb at the monotectic temperature of around 932 K. The solubility of Al in Pb is basically negligible. A lot of phase diagram data are available at temperatures below 1200 K in narrow terminal sides below 3 at.% Pb and above 90 at.% Pb. These data are in acceptable agreement as the evaluation of McAlister (1984) has shown. McAlister has evaluated a critical temperature of 1839 K at 44.8 at.% Pb. This  $T_c$  value is considerably higher than the value specified by Predel and Sandig (1969b) operating DTA. Yu et al (1996) have redetermined the binodal using a new isopiestic method (Wang et al 1993). There are only a few thermodynamic data available, due to the experimental difficulties associated with the small solubility of liquid aluminum and lead, and the high vapor pressure of lead at high temperatures.

The phase equilibria are calculated by choosing the pure elements in their stable state at 298.15 K and 1 bar as the reference state of the system. Their Gibbs energies are given by Dinsdale (1991). The excess Gibbs energy of the

Table 3: Optimized coefficient set of  $G_M^{xs}$  (equation (37)) for liquid Al–Pb alloys

l	$A_l$ ( $Jmol^{-1}$ )	$B_l$ ( $Jmol^{-1}K^{-1}$ )
0	47993.6	-10.71995
1	14407.33	-6.65287
2	4742.36	-0.72034

liquid alloy is represented by equation (37). The calculation carried out by Yu et al (1996) takes into account the elemental thermodynamic data due to Dinsdale (1991), the phase diagram data at temperatures above 1500 K that are obtained with the isopiestic method, and the data of Predel and Sandig (1969b) on the Pb-rich side below 1600 K. The resulting optimized set of parameters are given in table (4). The entire phase diagram is given in figure (6). The calculated lead activity at 1533 K and their metastable extension into the miscibility gap

Figure 6: Calculated phase diagram (continuous curve) using the coefficient set given in table 4.