Partition functions for two points is

$$\langle \phi_i \phi_j \rangle = \frac{1}{Z[J]} \frac{\partial^2 Z[J]}{\partial J_i \partial J_j}$$
 (1)

expanding to first order of lambda

$$Z[J] = \left[1 + \frac{\lambda}{4!} \left(\frac{\partial}{\partial J_i}\right)^4\right] \mathcal{N}_0 e^{\frac{1}{2}J_m \Delta_{mn} J_n}$$
 (2)

Then

$$\frac{\partial^2 Z[J]}{\partial J_i \partial J_j} = \frac{\partial^2}{\partial J_i \partial J_j} \left[e^{\frac{1}{2} J_m \Delta_{mn} J_n} + \frac{\lambda}{4!} \left(\frac{\partial}{\partial J_i} \right)^4 e^{\frac{1}{2} J_m \Delta_{mn} J_n} \right] \mathcal{N}_0 \bigg|_{J=0}$$
(3)