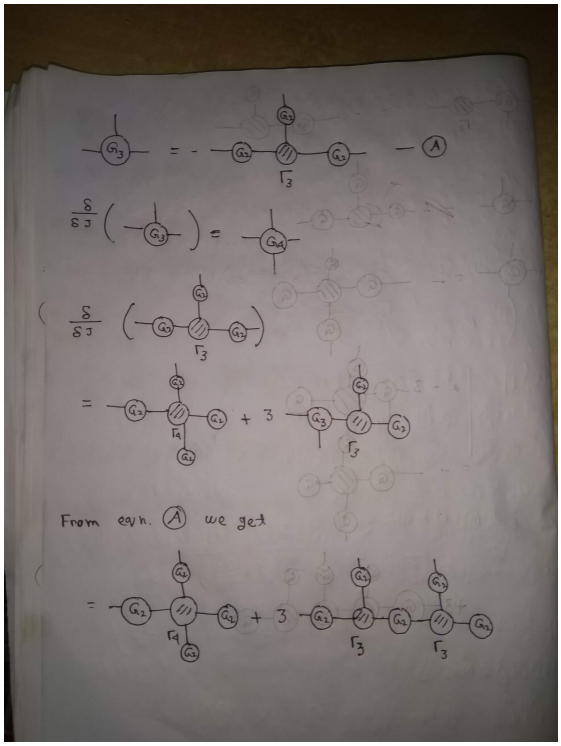
For 3-point connected Green funtion we get

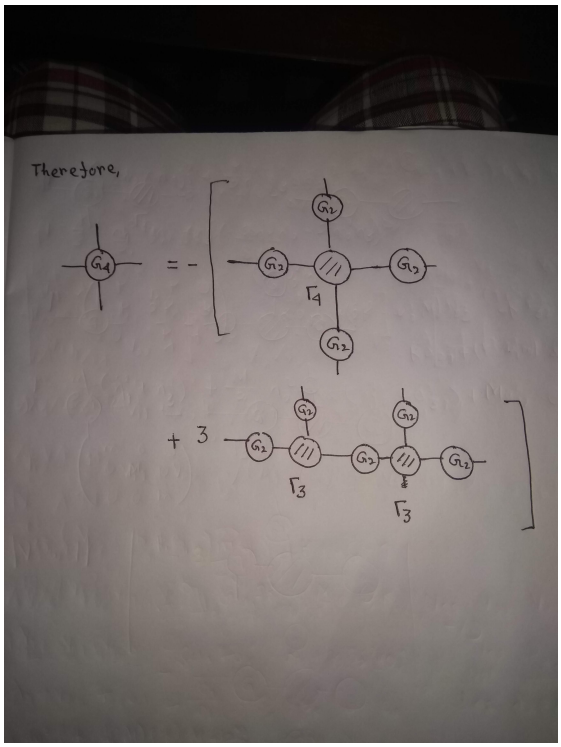
$$\Gamma_3(G_2)^3 = -G_3 \tag{1}$$

Differentiating with respect to ϕ^c

$$\begin{aligned}
&\frac{\delta}{\delta\phi^c}\Gamma_3(G_2)^3 + \Gamma_3\frac{\delta(G_2)^3}{\delta J}\frac{\delta J}{\delta\phi^c} = \frac{\delta G_3}{\delta J}\frac{\delta J}{\delta\phi^c} \\
\implies &\Gamma_4(G_2)^3 + 3\Gamma_3(G_2)^2 G_3(G_2)^{-1} = -G_4(G_2)^{-1} \\
\implies &\Gamma_4(G_2)^4 + 3\Gamma_3(G_2)^2 G_3 = -G_4 \\
\implies &\Gamma_4(G_2)^4 - 3\Gamma_3(G_2)^2 G_2\Gamma_3(G_2)^2 = -G_4 \qquad \text{[from eqn (1)]}
\end{aligned}$$

Digramatically will be




Therefore,
G_4
$= -$
G_2
G_2
G_2
G_2
Γ_4
$+ 3$
G_2
G_2
G_2
G_2
G_2
Γ_3
Γ_3