

\Rightarrow Isomorphism of graphs means mapping b/w two graphs
 $G_1 = (V_1, E_1)$

$G_2 = (V_2, E_2) \rightarrow$ simple graphs

$f: V_1 \rightarrow V_2$

it must be one-one and onto

$\therefore f$ - one-one, onto.

$\{a, b\} \rightarrow \text{edge} \Rightarrow \{f(a), f(b)\} - \text{edge}$

[Relation of adjacency is preserved]

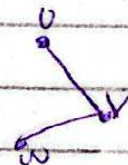
$\Rightarrow G_1$ and G_2 are isomorphic.

mean if we have 2 vertices in any graph
 ex



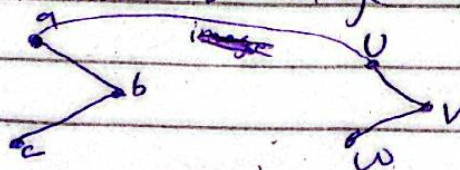
here a and b the edge occurs.

so if we have another graph like



so assume that a image have

u and b image have v so like.



so if we have image b/w a and U , so we must have the edge b/w U and V and that should be for every edge.

Simple
if a and b b/w have edge
then must have U and V .

then we said the Relation is preserve
of adjacency.

\Rightarrow important points to show the graph is
Not isomorphisms.

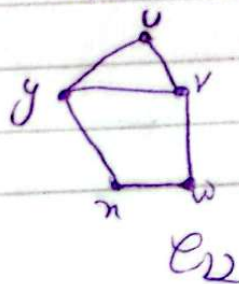
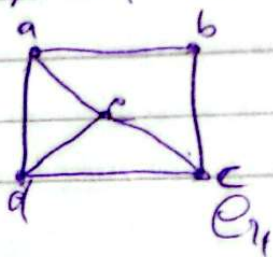
1. If G_1 and G_2 do not have
Same number of vertices. then
 $\Rightarrow G_1$ and G_2 are not isomorphism.

2. If G_1 and G_2 do not have same
number of edges.

$\Rightarrow G_1$ and G_2 are not isomorphism.

3. If G_1 and G_2 do not have same
number of vertices of degree.
 $\Rightarrow G_1$ and G_2 are not isomorphic.

ex-



1. In G_1 have same vertex as G_2 ✓
2. edges are same in $G_1 = 6$ and $G_2 = 6$
3. check degree two vertex, present in G_1 which is 6.

In G_1 6 is the only (1) vertex whose degree is 2.

in G_2 if we check the vertices whose degree is 2, then there are 3 vertices whose degree is 2.

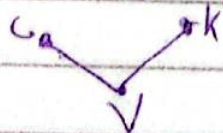
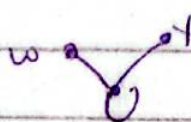
so G_1 have 1 vertex with degree 2 and G_2 have 3 vertices with degree 2

Hence it is not isomorphism ~~that's why it~~

4th point:- if $f(u) = v$ and degree of $u = v$

of vertices to u are not equal to the degree of vertices adjacent to $v \Rightarrow G_1$ and G_2 are not isomorphic.

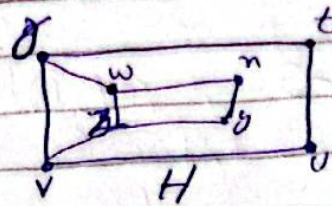
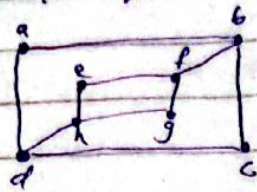
means:- u and v vertex degree must be equal



Like u is 2 degree and v is 2 degree

but other vertex like w and t each of u vertex, ~~if~~ if have different degrees, then still it will not considered it is isomorphism.

example 1



ex: take the vertex f and see what is the degree of f has 3 vertex.
and f has image like w or z or x or y because they have 3 degree.

→ assume that f has image $f(f) = w$.
→ now check adjacent vertex of f .
which is e, g and b
and degree of $e = 2$
deg of g is 2.
deg of $b = 3$

and image of f is w .
and adjacent vertex of w is
 z, n and s

$d(z)$ degree 3

$d(s) = 3$

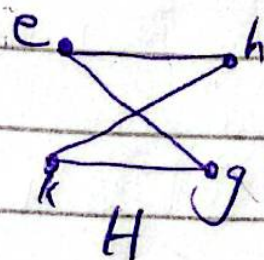
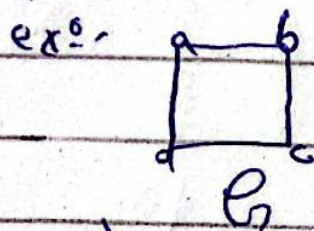
$d(n) = 2$

not f 's degree adjacent 2, 2, and 3
and w adjacent is 3, 3, 2

means f is w but not the same way
so it is not isomorphic. but
other f is g so it is not isomorphic.
hence not isomorphic.

$$\begin{array}{lcl}
 A \rightarrow da / \overset{\epsilon}{BC} & d, g, h, \epsilon, b, a & \\
 B \rightarrow g / \epsilon & d, g, h, \epsilon & \\
 C \rightarrow h / \epsilon & g, \epsilon & \\
 & h, \epsilon & \neq
 \end{array}$$

\Rightarrow Given that show that G and H are isomorphic.



\Rightarrow

$a \rightarrow e$
 $b \rightarrow k$
 $c \rightarrow h$
 $d \rightarrow g$

$f(a) = e, f(b) = k, f(c) = h, f(d) = g$
 f - one-one onto map b/w
 vertex sets.

Relation of adjacency is preserved
 Hence

Graph G and H are isomorphic.