

Ford Fulkerson Algorithm for Max Flow.

⇒ Find the maximum flow through the given network using Ford Fulkerson algorithm.

✓ The Ford Fulkerson method is used for solving maximum flow problem.

2. Basic terms:

→ source

• sink

• capacity and bottle neck capacity.

• flow

• Augmenting path.

• Residual capacity.

✓ The source vertex has all outward edge, no inward edge.

✓ Sink will have all inward edge, no outward edge.

Notes: in given graph v_1 is the source vertex.

while v_7 have an sink edge.

3. capacity:- weight b/w from one vertex to another.

while Bottle neck capacity of the we find as the capacity of the path is the minimum capacity of the path any edge on the path.

ex: like in given graph 1 to 2 its weight is capacity same 2 to 5 weight is known as capacity.

→ Note we use Bottle neck capacity for the path. Like example we have chosen source s to t as a path.

so 1 to 2 and 2 to 5 and 5 to t vertex on that path 7, 5, 10 weight which will the minimum is known as bottle neck capacity.

and 7, 5, and 10 so 5 is minimum known as bottle neck capacity.

4, flow: $\frac{\text{flow}}{\text{capacity}} = \frac{4}{5}$

5, Augmenting Path when we are finding capacity from 1 to 2, 2 to 5 and 5 to t our Bottle neck capacity, so that whole path is called Augmenting Path.

1 to 2, 2 to 5 and 5 to t is known as augmenting Path.

6, Residual capacity Every edge of a residual graph has a value called residual capacity. which is equal to original capacity minus current flow.

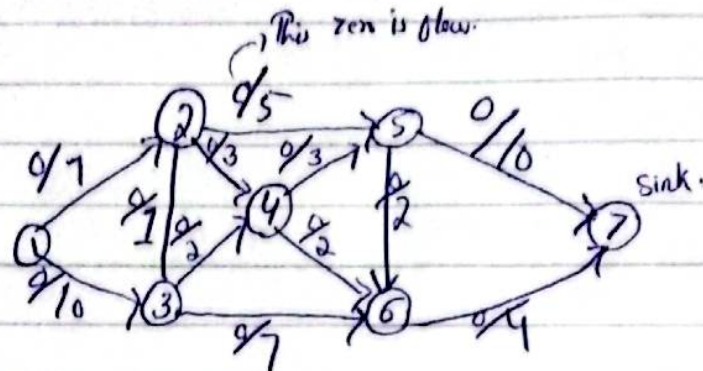
so, Residual capacity = Original capacity - current flow.

ex: $\frac{4}{5}$ flow/capacity

$5 - 4 = 1$ This will become residual capacity

Let's take an example and calculate it

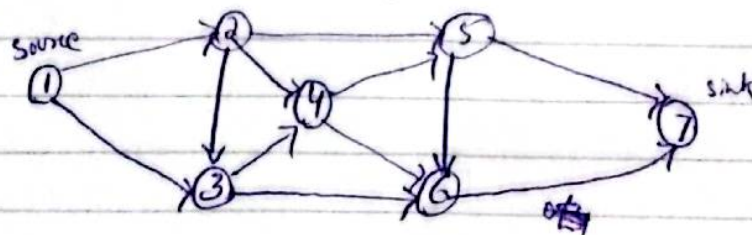
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Step 1: we have to calculate the flow and initially we have to make 0 (zero) to all.

Step 2: create another graph

Solution



after making initially to zero Now take or select any path randomly. source to sink.

For solving it we have to make an table.

so we have select as an Augmenting path as a 1-2-5-7 so for that path we have to find Bottle neck capacity

Like this:

Augmenting Path	Bottleneck capacity:
$1 \rightarrow 2 \rightarrow 5 \rightarrow 7$	

so for given path $1 \rightarrow 2 \rightarrow 5 \rightarrow 7$ Bottleneck capacity will remain 7 or 5 and 10 weight 5 is the minimum, Bottleneck capacity.