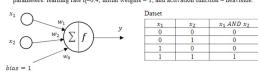


Assignment 4

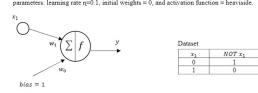
Wednesday, October 27, 2021 12:43 PM

1. [20 points] Train the perceptron network below to solve the following logical problems:

a. [10 points] Logical AND problem correctly classifying the dataset instances. Use the parameters: learning rate $\eta=0.1$, initial weights = 1, and activation function = heaviside.



b. [10 points] Logical NOT problem correctly classifying the dataset instances. Use the parameters: learning rate $\eta=0.1$, initial weights = 1, and activation function = heaviside.



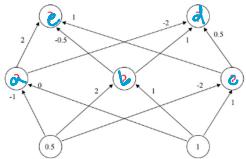
Dataset		x_1	x_2	$x_1 \text{ AND } x_2$	x_1	x_2	w_1	w_2	w_0	t	$z(\text{net})$	y	$(t-y)$	ηw_1	ηw_2	ηw_0
0	0	0	0	0	0	0	1	1	1	0	-1	0	0	0	-0.1	
0	1	0	1	0	1	1	1	1	0.6	0	1.6	1	-1	0	-0.6	-0.4
1	0	1	0	0	1	0	0.6	0.6	0.2	1	1.2	1	-1	-0.4	0	-0.4
1	1	1	1	1	1	1	0.6	0.6	0.2	1	1.2	1	0	0	0	0
0	0	1	0	0	0	0	0.6	0.6	-0.2	0	-0.2	0	0	0	0	0
0	1	1	0	0	0	1	0.6	0.6	0.2	0	0.4	1	-1	0	-0.4	-0.4
1	1	0	1	0	1	0	0.6	0.6	0.2	0	0.4	0	0	0	0	0
1	1	1	0	0	1	0	0.6	0.6	0.2	1	0.2	1	0	0	0	0
0	0	0	1	0	0	1	0.6	0.6	0.2	0	0.6	0	0	0	0	0
0	1	0	1	0	0	1	0.6	0.6	0.2	0	0.6	0	0	0	0	0
1	0	1	0	0	0	1	0.6	0.6	0.2	0	0.6	0	0	0	0	0
1	1	1	1	1	1	1	0.6	0.6	0.2	1	0.2	1	0	0	0	0

Dataset		x_1	x_2	$\text{NOT } x_1$	x_1	x_2	w_1	w_2	w_0	t	$z(\text{net})$	y	$(t-y)$
0	1	0	0	1	0	0	1	1	1	1	1	0	1
1	0	1	0	0	1	0	1	1	1	0	-1	0	-1

2. <https://github.com/NooCode/CS4210-Assignment4/blob/master/Perceptron/perceptron.py>

3. [20 points] The figure below is a network of linear neurons, that is the output of each neuron is identical to its input (linear activation function). The numbers at the connections indicate the weights of the links.

- a. [10 points] Find the value at the output nodes of the network for the given input (0.5,1).



- b. [5 points] Find the value at the output nodes of the network for the input (1,2). [5 points]
 Do you need to repeat the computations all over again? Why?

- c) a) $0.5 * 1 + 1 * 0 = -0.5$
 b) $0.5 * 2 + 1 * 1 = 2$
 c) $0.5 * -2 + 1 = 0$
 d) $-2 * -0.5 + 1(2) + 0.5(0) = 3$
 e) $2(-0.5) + -0.5(2) + 1(0) = -2$

- b) If the values were changed to (1,2) it would be equivalent to multiplying the original (.5,1) by 2.
 Therefore each of the outputs will follow the same ratio and be doubled. The computation between each of the neurons do not need to be repeated.

- a) -1
 b) 4
 c) 0
 d) 6
 e) -4

4. <https://github.com/NooCode/CS4210-Assignment4/blob/master/DeepLearning深深学习.py>

5. [15 points] Consider the dataset below.

Outlook	Temperature	PlayTennis
Sunny	Hot	No
Overcast	Cool	Yes
Overcast	Hot	Yes
Rain	Cool	No
Overcast	Mild	Yes

We will apply steady state Genetic Algorithms ($r = 0.5$) to solve this classification problem, by using a similar approach of the Find-S algorithm. If the instance matches the rule pre-condition of the chromosome, you predict according to its post-condition; otherwise you predict the opposite class defined by the chromosome (there must be a prediction for each instance then). Follow the planning below to build your solution.

- Representation: single if-then rule by using bit strings (binary encoding).

- o Outlook < Sunny, Overcast, Rain >
- o Temperature < Hot, Mild, Cool >
- o Examples:
 - o Outlook = Overcast \rightarrow 010
 - o Outlook = Overcast \vee Rain \rightarrow 011
 - o Outlook = Sunny \vee Overcast \vee Rain \rightarrow 111
 - o Outlook = (Overcast \wedge Rain) \wedge (Temperature = Hot) \rightarrow 011100
 - o Outlook = Sunny \wedge Temperature = Hot then PlayTennis = yes \rightarrow 100100
- o Initial population (Chromosomes) : $C_1=1001001$, $C_2=0100100$, $C_3=1011000$, $C_4=1101000$.

Solution format:

$$\begin{aligned} \text{Fitness}(C_1) &= ? \quad C_1 = 1001001 = 15 = .2 \\ \text{Fitness}(C_2) &= ? \quad C_2 = 0100101 = 16 = .6 \\ \text{Fitness}(C_3) &= ? \quad C_3 = 0100000 = 1 = .9 \\ \text{Fitness}(C_4) &= ? \quad C_4 = 1101000 = 21 = .4 \end{aligned}$$

1st generation (C_1, C_2, C_3, C_4):

$$\begin{aligned} \text{Pr}(C_1) &= ? (4^{\text{th}}) \quad C_1 = .1 \\ \text{Pr}(C_2) &= ? (3^{\text{rd}}) \quad C_2 = .7 \\ \text{Pr}(C_3) &= ? (2^{\text{nd}}) \quad C_3 = .3 \\ \text{Pr}(C_4) &= ? (1^{\text{st}}) \quad C_4 = .4 \end{aligned}$$

$$C_1 = ??????? \rightarrow C_1 = ??????? \quad C_1 = 1011000$$

$$C_2 = ??????? \rightarrow C_2 = ??????? \quad C_2 = 1101000$$

$$\text{Fitness}(C_1) = ? C_1 = .6$$

$$\text{Fitness}(C_2) = ? C_2 = .6$$

$$\text{Fitness}(C_3) = ? C_3 = 1011001 = 16 = .6$$

$$\text{Fitness}(C_4) = ? C_4 = 1101001 = 21 = .4$$

2nd generation (C_1, C_2, C_3, C_4):

$$\begin{aligned} \text{Pr}(C_1) &= ? (4^{\text{th}}) \quad C_1 = .217 \\ \text{Pr}(C_2) &= ? (3^{\text{rd}}) \quad C_2 = .217 \\ \text{Pr}(C_3) &= ? (2^{\text{nd}}) \quad C_3 = .286 \end{aligned}$$

$$C_1 = .2 / 2 = .1$$

$$C_2 = .6 / 2 = .3$$

$$C_3 = .4 / 2 = .2$$

$$C_4 = .4 / 2 = .2$$

Crossover

mask = 1110000

1011000 \rightarrow 1110000

1101000 \rightarrow 1101000

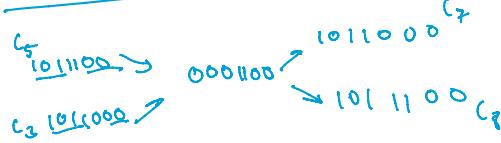
- Outlook = Overcast \vee Rain \rightarrow 011
 - Outlook = Sunny \vee Overcast \vee Rain \rightarrow 111
 - Outlook = (Overcast \vee Rain) \wedge (Temperature = Hot) \rightarrow 011100
 - Outlook = Sunny \wedge Temperature = Hot then PlayTennis = yes \rightarrow 1001001
- Initial population (Chromosomes) : $C_1=1001001$, $C_2=0100101$, $C_3=1011000$, $C_4=1101100$. Population size should remain the same (4 individuals) over time.
- Fitness function: accuracy
- Penalty criterion: no penalty.
- Selection method: The best two chromosomes are carried over to the next generation. The other two are selected for crossover by using the roulette wheel (simulation).
- Crossover strategy: single-point crossover with mask 110000 in the 1st generation, two-point crossover with mask 0001100 in the 2nd generation. Use the following chromosomes to perform crossover (simulating the process of spinning the roulette wheel) according to the relative fitness (sectors of a roulette wheel), generating two offspring for each crossover:
 - (1st and 3rd) in the 1st generation
 - (1st and 2nd) in the 2nd generation
- Mutation: on the 6th bit of the chromosome(s) 1011000 generated during the 2nd generation.
- Termination criteria: accuracy = 1.0. Return the corresponding chromosome(s) – your model.

$$\begin{aligned}
 & \text{2nd generation } (C_1, C_2, C_3, C_4) \\
 & \Pr(C_1) = ? (4^{\text{th}}) \xrightarrow{C_4} C_4 = .717 \\
 & \Pr(C_2) = ? (3^{\text{rd}}) \xrightarrow{C_3} C_3 = .219 \\
 & \Pr(C_3) = ? (2^{\text{nd}}) \xrightarrow{C_2} C_2 = .046 \\
 & \Pr(C_4) = ? (1^{\text{st}}) \xrightarrow{C_1} C_1 = .026 \\
 & C_1 = ?????? \rightarrow C_1 = ?????? \quad C_2 = (011010) \\
 & C_2 = ?????? \rightarrow C_2 = ?????? \quad C_3 = 1011100 \\
 & \text{Applying mutation on } 1011000 \quad C_4 = 1011100 \\
 & \text{Fitness}(C_1) = ? \quad C_1 = .8 \\
 & \text{Fitness}(C_2) = ? \quad C_2 = .1 \\
 & \text{Fitness}(C_3) = ? \quad C_3 = .9 \\
 & \text{Fitness}(C_4) = ? \quad C_4 = 1 \\
 & \text{Final answer: } C_1 = 1011000 \quad C_2 = 1011100 \\
 & C_3 = 1011000 \quad C_4 = 1011100
 \end{aligned}$$

1101000 $\xrightarrow{\dots\dots\dots} \rightarrow 1101000$

$$\begin{aligned}
 & P_1() \\
 & C_3 = C_5 = .2 / .8 = .25 \\
 & C_2 = C_6 = .6 / .8 = .75
 \end{aligned}$$

Double Crossover



6. [15 points] Consider the combinatorial optimization problem known as the "0-1 Knapsack problem", where we need to fill a knapsack with objects of different weights and values. The goal is to fill the Knapsack with the highest possible value, not exceeding its maximum capacity (weight supported) and carrying only one type of each object inside. Below is the list of available objects, with their respective weights and values.

Maximum weight capacity (C) = 15 kg.

Object	Tablet	Laptop	Projector
Weight (w_i)	5 kg	8 kg	10 kg
Value (v_i)	\$ 570.00	\$ 710.00	\$ 640.00

Apply generational Genetic Algorithms ($r = 1$) to solve this optimization problem strictly following the planning below.

- Representation: binary, identifying whether the object should be included or not, with the 1st, 2nd, and 3rd positions of the chromosomes referring to the Tablet, Laptop, and Projector respectively.
- Initial population (Chromosomes) : $(C_1=000, C_2=001, C_3=010, C_4=100)$. Population size should remain the same (4 individuals) over time.
- Fitness function: $\sum_{i=1}^n w_i x_i$, with n being the number of objects in the knapsack and x_i being the number of instances of object i to include in the knapsack (1, if the object is included and 0, otherwise).
- Constraint: $\sum_{i=1}^n w_i x_i \leq C$.
- Penalty criterion: If the maximum capacity of the knapsack (C) is exceeded, discard the obtained chromosome (offspring) and replicate the best among the two of its parents.
- Selection method: roulette wheel (simulation)
- Crossover strategy: single-point crossover with mask 110 in the 1st generation, single-point crossover with mask 100 in the 2nd generation. Use the following chromosomes to perform crossover (simulating the process of spinning the roulette wheel) according to the relative fitness (sectors of a roulette wheel), generating two offspring for each crossover:
 - (2nd and 3rd) and (2nd and 1st) in the 1st generation
 - (1st and 2nd) and (1st and 3rd) in the 2nd generation
- Mutation: on the 3rd bit of the chromosome(s) 101 generated during the 2nd generation.
- Termination criteria: stop at the end of the 2nd generation. Return the best chromosome found.

Summary of the optimization function: $\max \sum_{i=1}^n v_i x_i$

subject to $\sum_{i=1}^n w_i x_i \leq C$ and $x_i \in \{0,1\}$

Solution format:

$$\begin{aligned}
 & \text{Fitness}(C_1) = ? \quad C_1 = 000 = 0 \\
 & \text{Fitness}(C_2) = ? \quad C_2 = 001 = 640 \\
 & \text{Fitness}(C_3) = ? \quad C_3 = 010 = 710 \\
 & \text{Fitness}(C_4) = ? \quad C_4 = 100 = 570 \\
 & \text{1st generation } (C_1, C_2, C_3, C_4) \\
 & \quad C_1, C_2, C_3, C_4 \\
 & \Pr(C_1) = ? (4^{\text{th}}) \quad C_1 = 0 \\
 & \Pr(C_2) = ? (3^{\text{rd}}) \quad C_2 = .292 \\
 & \Pr(C_3) = ? (2^{\text{nd}}) \quad C_3 = .375 \\
 & \Pr(C_4) = ? (1^{\text{st}}) \quad C_4 = .370 \\
 & C_1 = ?????? \rightarrow C_1 = ?????? \quad C_5 = 000 \quad C_7 = 010 \\
 & C_2 = ?????? \rightarrow C_2 = ?????? \quad C_6 = 101 \quad C_8 = 000 \\
 & \text{Fitness}(C_5) = ? \quad C_5 = 000 \rightarrow 0 \\
 & \text{Fitness}(C_6) = ? \quad C_6 = 101 \rightarrow 120 \\
 & \text{Fitness}(C_7) = ? \quad C_7 = 010 \rightarrow 710 \\
 & \text{Fitness}(C_8) = ? \quad C_8 = 000 \rightarrow 0 \\
 & \text{2nd generation } (C_5, C_6, C_7, C_8) \\
 & \quad C_5, C_6, C_7, C_8 \\
 & \Pr(C_5) = ? (4^{\text{th}}) \quad C_5 = 0 \\
 & \Pr(C_6) = ? (3^{\text{rd}}) \quad C_6 = 0 \\
 & \Pr(C_7) = ? (2^{\text{nd}}) \quad C_7 = .375 \\
 & \Pr(C_8) = ? (1^{\text{st}}) \quad C_8 = .625 \\
 & C_5 = ?????? \rightarrow C_5 = ?????? \quad C_9 = 100 \quad C_{11} = 150 \\
 & C_6 = ?????? \rightarrow C_6 = ?????? \quad C_{10} = 100 \quad C_{12} = 001 \\
 & \text{Applying mutation on } 100000101 \\
 & \text{Fitness}(C_9) = ? \quad C_9 = 150 \\
 & \text{Fitness}(C_{10}) = ? \quad C_{10} = 150 \\
 & \text{Fitness}(C_{11}) = ? \quad C_{11} = 120 \\
 & \text{Fitness}(C_{12}) = ? \quad C_{12} = 640 \\
 & \text{Final answer: } C_{11} \rightarrow 110
 \end{aligned}$$

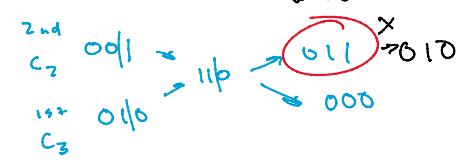
P_G

$$C_1 = 0 \\ C_2 = \frac{640}{1920} = .333$$

$$C_3 = \frac{710}{1920} = .375$$

$$C_4 = \frac{570}{1920} = .292$$

Crossover 1st Gen



Crossover 2nd Gen

