

Domáca úloha 1

1.5.4 Definujte množinu

$Q^-$  všetkých záporných rac. čísel

$$Q^- = \left\{ -\frac{p}{q} \mid p \in \mathbb{N}, q \in \mathbb{N}^+ \right\}$$

alebo vieme aj takto:

$$Q^- = \left\{ \frac{p}{q} \mid p \in \mathbb{Z}, q \in \mathbb{N}^+, \text{NSD}(p, q) = 1, \frac{p}{q} < 0 \right\}$$

↳ Najväčší spoločný deliteľ  
aby boli v základnom tvare

1.5.10 g)  $(0,1) \approx (0,27) \cup (4,7)$

$$\overset{a}{0}; \overset{b}{0,5} > \approx \overset{c}{0}; \overset{d}{2}$$

$$\varphi(x) = \frac{(x-0)(2-0)}{(0,5-0)} + 0 = \frac{2x}{\frac{1}{2}} = 4x$$

$$\begin{aligned} x &\in (0; 0,5) \\ \varphi(0) &= 4 \cdot 0 = 0 \checkmark \\ \varphi(0,5) &= 4 \cdot \frac{1}{2} = 2 \checkmark \end{aligned}$$

$$(0,5; 1) \approx (4,7)$$

$$\varphi(x) = \frac{(x-0,5) \cdot (7-4)}{(1-0,5)} + 4 = \frac{3x - \frac{3}{2}}{\frac{1}{2}} = 6x - 3 + 4 = 6x + 1$$

$x \in (0,5; 1)$

$$\varphi(0,5) = \frac{6}{2} + 1 = 4 \checkmark$$

$$\varphi(1) = 6 \cdot 1 + 1 = 7 \checkmark$$



$$|\{7k+2 \mid k \in \mathbb{N}\}| = |\mathbb{N}|$$

$$\{0, 9, 16, 23, 30\} \dots = \{7k+2 \mid k \in \mathbb{N}\}$$

$$\begin{array}{ccccccc} \{0, 9, 16, 23, 30\} & \dots & = & \{7k+2 \mid k \in \mathbb{N}\} \\ \downarrow \downarrow \downarrow \downarrow \downarrow & & & \\ \{0, 1, 2, 3, 4\} & \dots & = & \{\mathbb{N}\} \end{array}$$

$$f(x) = 7x + 2, \quad x \in \mathbb{N} \quad (\{7k+2 \mid k \in \mathbb{N}\}) = |\mathbb{N}|$$

$$f_2(x) = \begin{cases} \frac{x-2}{7} & ; x > 0, x \in \mathbb{N} \\ 0 & ; x = 0, x \in \mathbb{N} \end{cases} \quad (N = |\{7k+2 \mid k \in \mathbb{N}\}|)$$