

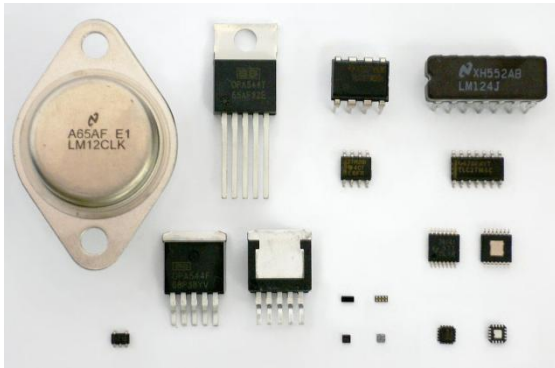
ANALOG CIRCUITS DESIGN

AE7: Power stages at low frequencies

Course overview

- 1. Introduction
- 2. The bipolar transistor
- 3. Push-pull stage
- 4. Classes of operation
- 5. Class D amplifier
- 6. Heatsink calculation

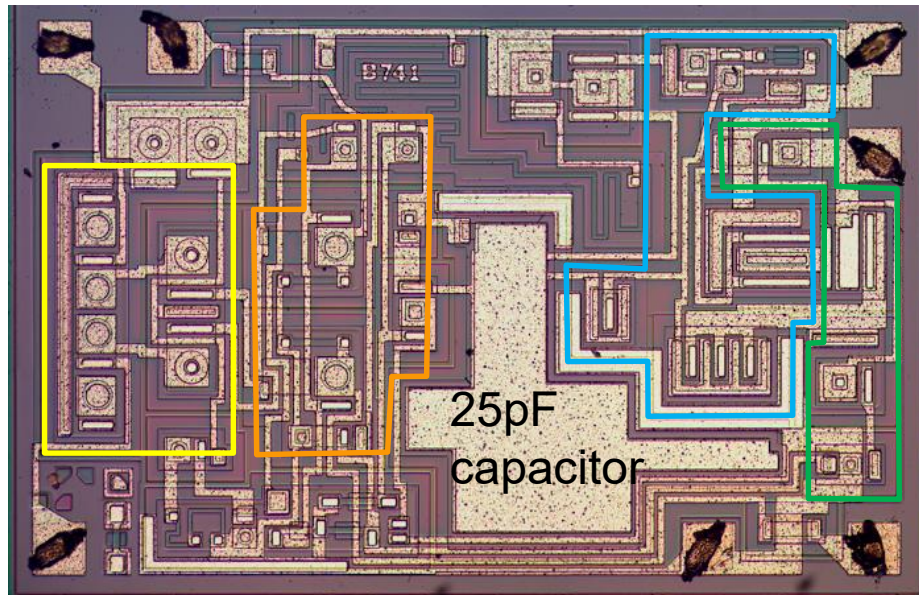
1. Introduction: inside the 741 operational amplifier



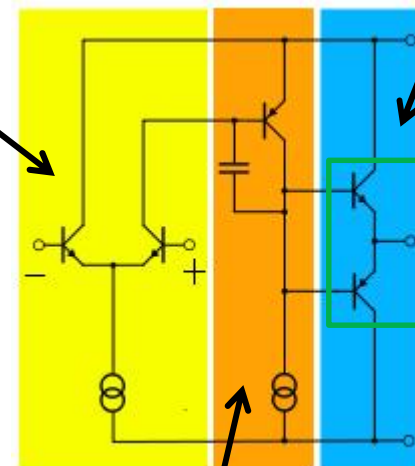
Difference amplifier stage
 $\mu\text{A} \dots \text{tens of } \mu\text{A}$

Output (power) stage
 $\mu\text{A} \dots \text{tens of mA}$

IN- NULL+ VCC



OUT

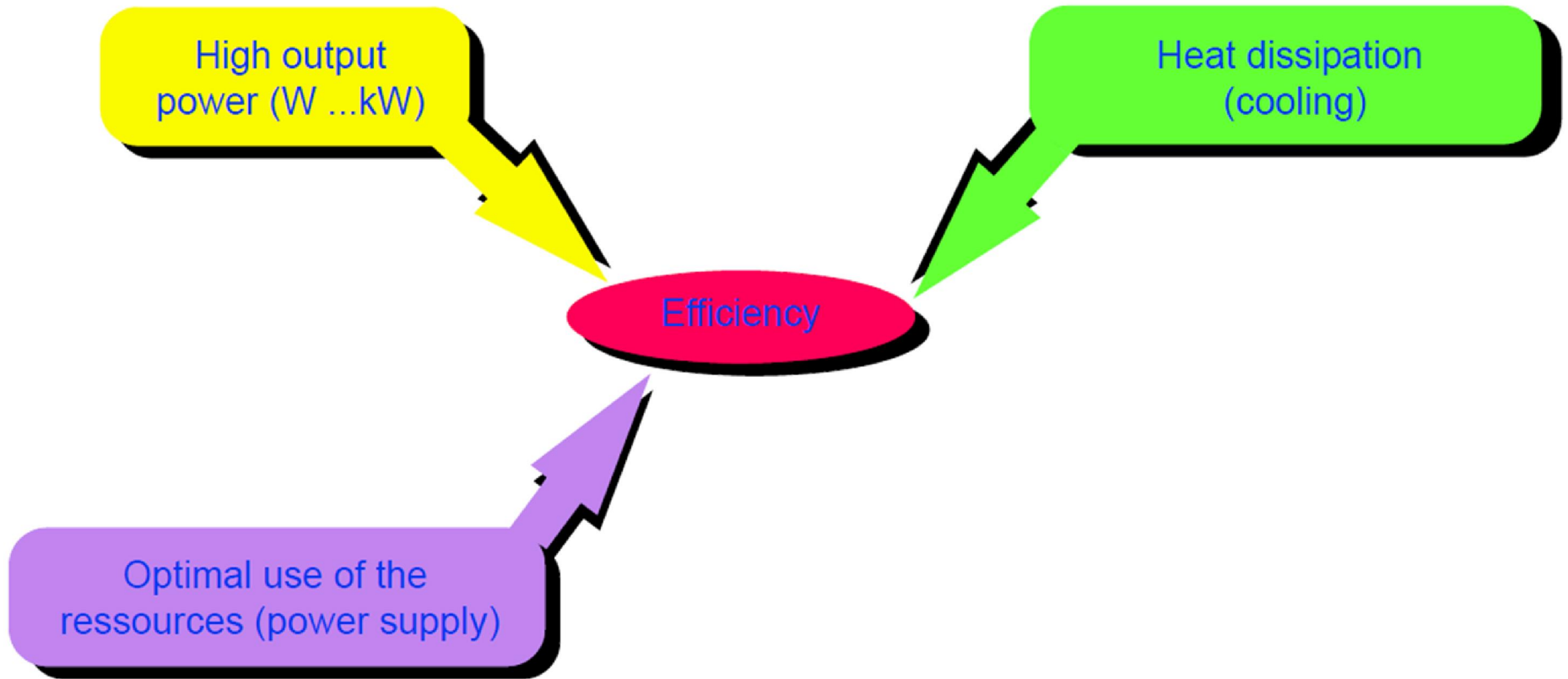


Short-circuit protection

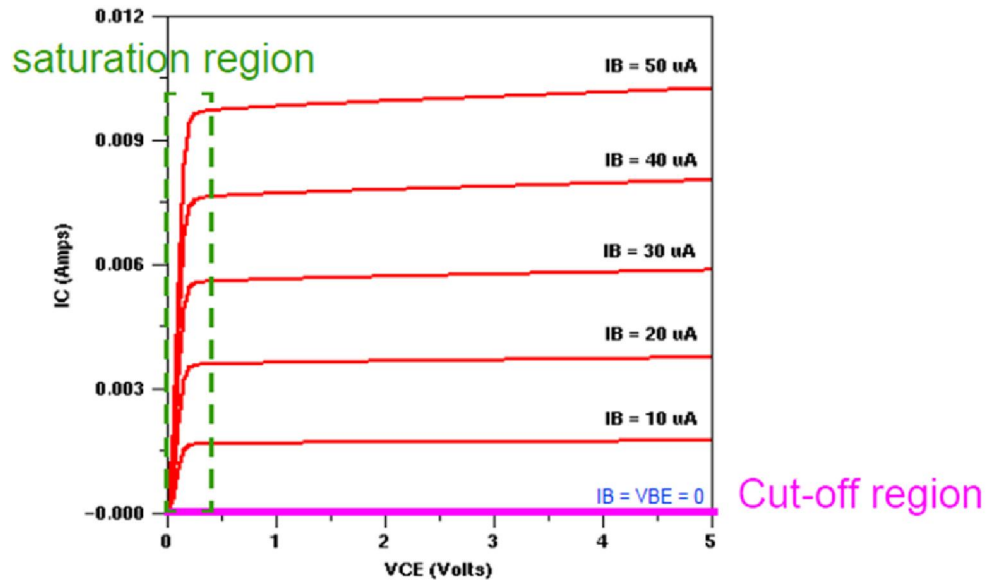
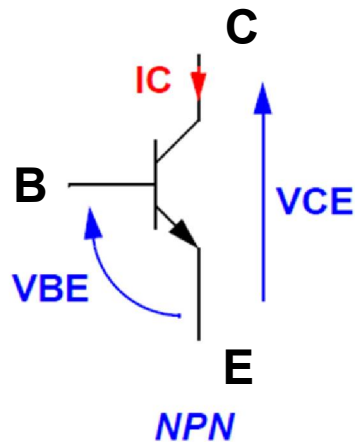
Gain stage(s)
 $\mu\text{A} \dots \text{tens of } \mu\text{A}$

IN+ VSS NULL-

1. Introduction: system overview



2. The bipolar transistor

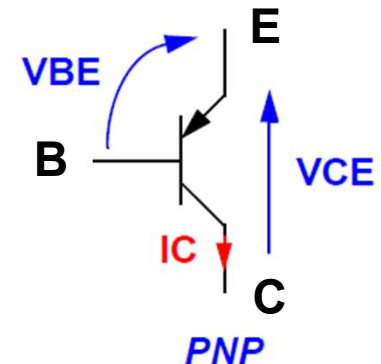


Current source (I_C) controlled by a voltage (V_{BE}) provided $V_{CE} > 300\sim 400\text{mV}$

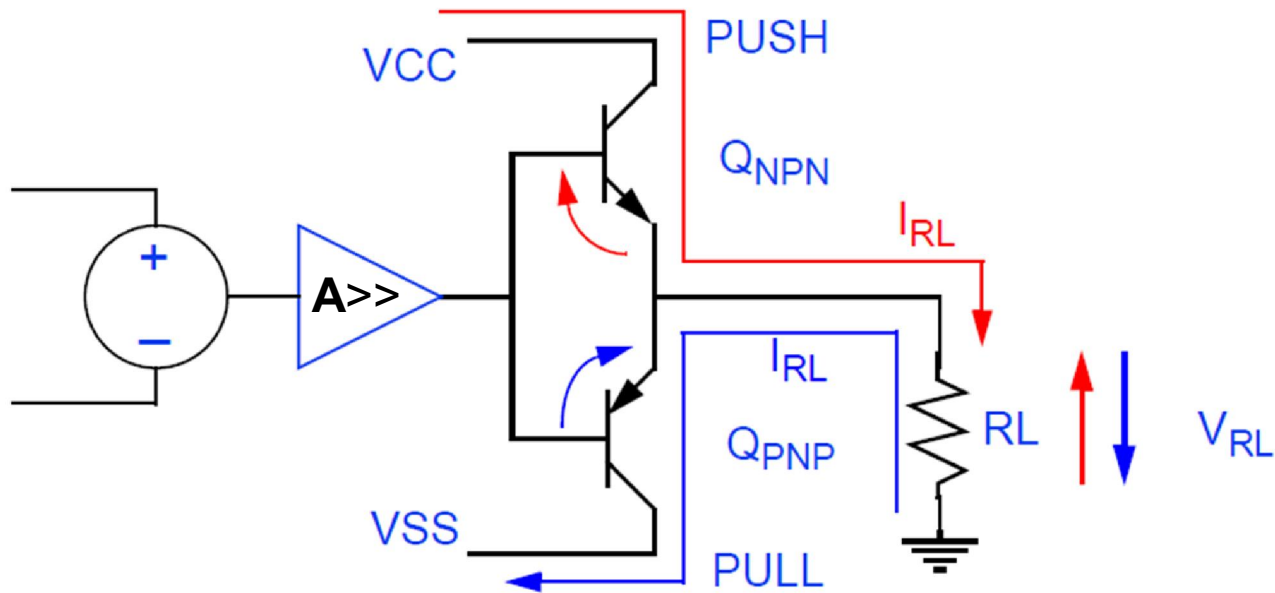
$$I_C = I_s \left(\exp\left(\frac{V_{BE}}{V_t}\right) - 1 \right)$$

$$V_{BE} \approx V_t \ln\left(\frac{I_C}{I_s}\right) \approx 0,6\text{V}$$

PNP & NPN: same behaviour, but voltages and currents are in the opposite direction

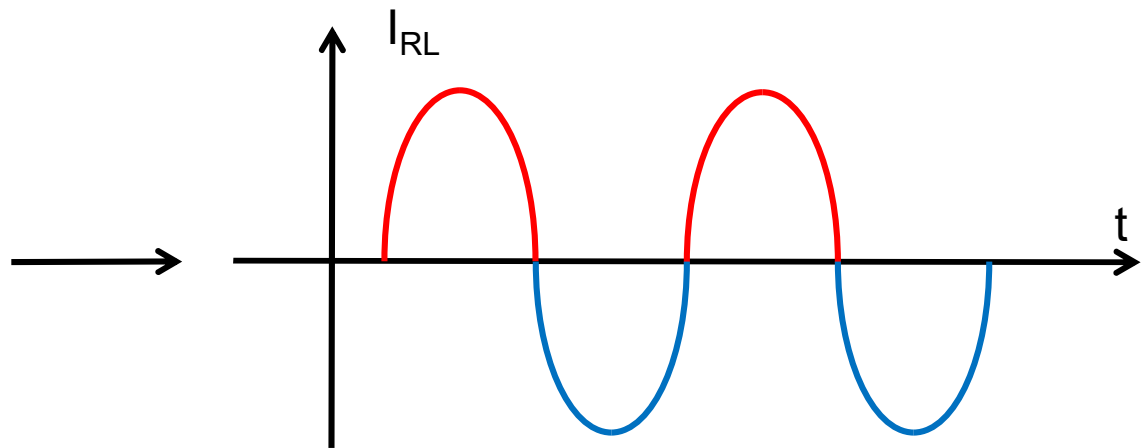


3. Push-pull output stage: operation



Q_{NPN} and Q_{PNP} are complementary transistors

Zero bias (quiescent) current



3. Push-pull output stage: efficiency

Assumption: symetric supply $V_{CC} = |V_{SS}|$

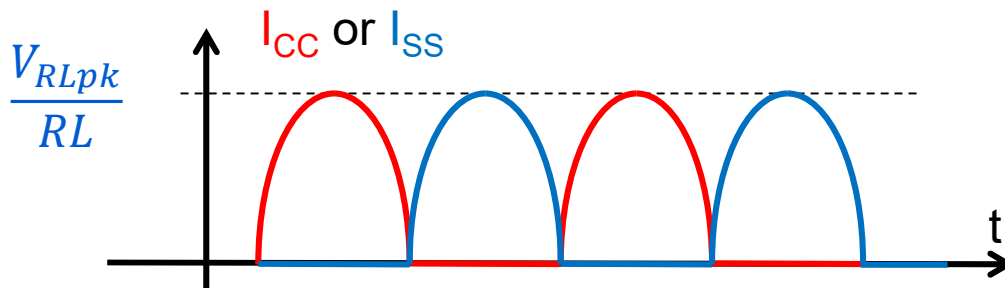
- Power delivered to the load:
- Efficiency

$$P_{RL} = \frac{(V_{RLpk})^2}{2 \cdot RL}$$

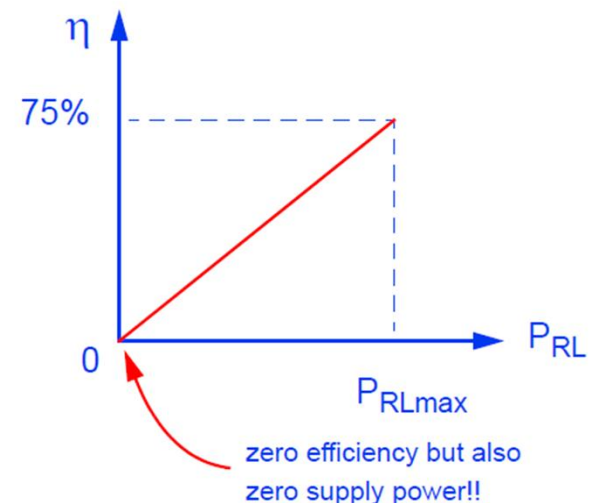
$$\eta = \frac{P_{RL}}{P_{supply}} = \frac{\pi \cdot V_{RLpk}}{4 \cdot V_{CC}}$$

- $P_{supply} = P_{VCC} + P_{VSS}$

$$P_{supply} = V_{CC} I_{CCavg} + V_{SS} I_{SSavg}$$

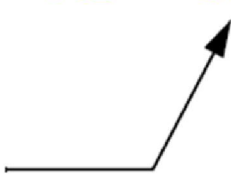
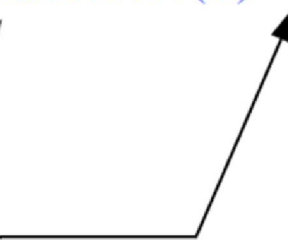


$$P_{supply} = 2 V_{CC} \frac{V_{RLpk}}{\pi RL}$$



3. Push-pull output stage: power losses

General methodology: $\Sigma P_{\text{supply}} = P_{\text{RL}} + P_{\text{transistor(s)}} + \varepsilon$

power stage only 
the rest of the circuit (may usually be neglected) 

Power dissipated when the input signal is a sine wave (for 2 transistors):

$$P_{\text{diss}} = \frac{2 \cdot V_{\text{CC}} \cdot V_{\text{RLpk}}}{\pi \cdot R_{\text{L}}} - \frac{V_{\text{RLpk}}^2}{2 \cdot R_{\text{L}}} \quad \text{reaches maximum at } V_{\text{RLpk}} = \frac{2 \cdot V_{\text{CC}}}{\pi}$$

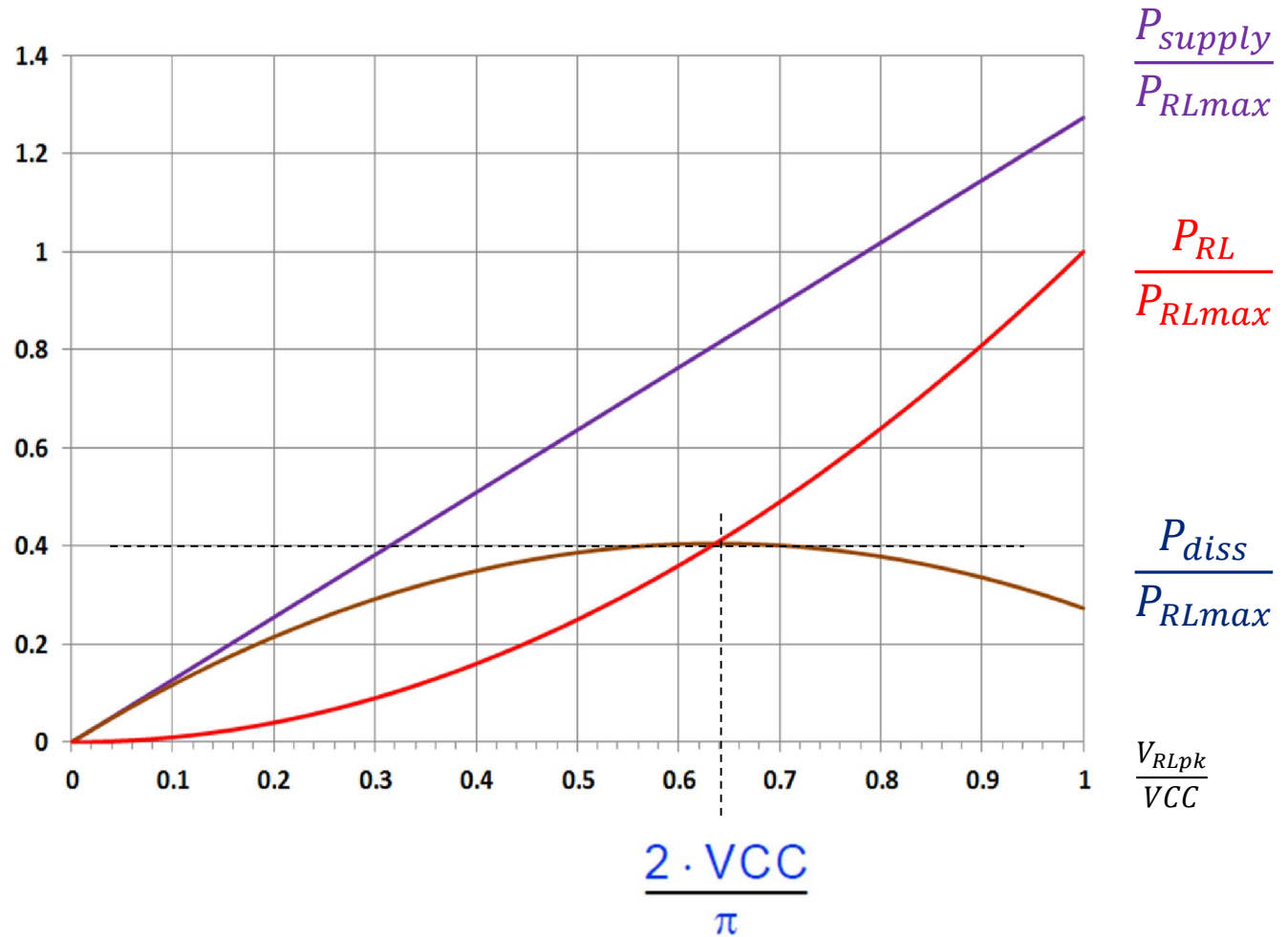
$$P_{\text{diss(max)}} = \frac{2 \cdot V_{\text{CC}}^2}{\pi^2 \cdot R_{\text{L}}}$$

$\approx 40\%$ of maximum P_{RL}

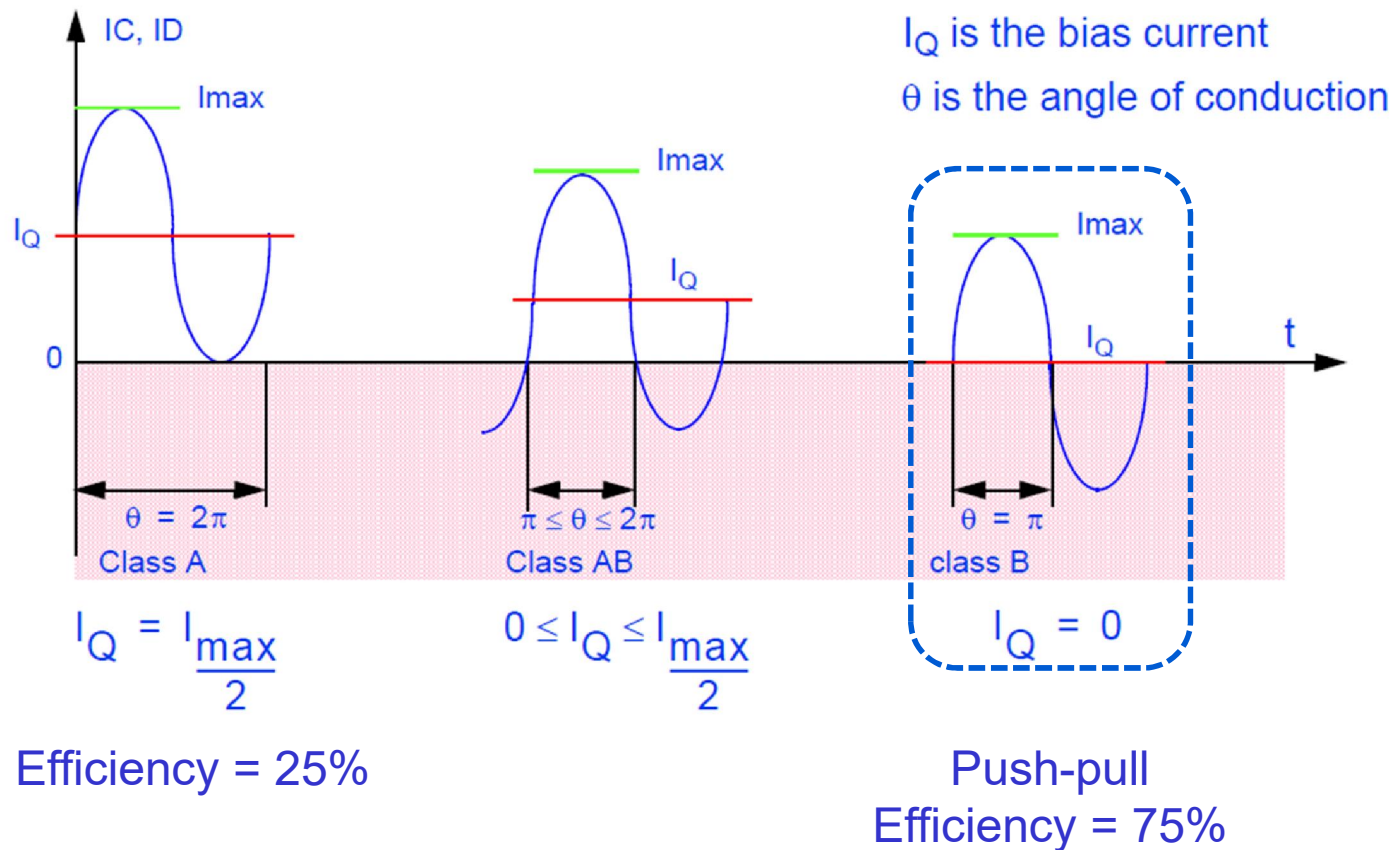
3. Push-pull output stage: power losses

$$P_{\text{diss(max)}} = \frac{2 \cdot V_{CC}^2}{\pi^2 \cdot R_L}$$

$\approx 40\%$ of maximum P_{RL}



4. Class of operation

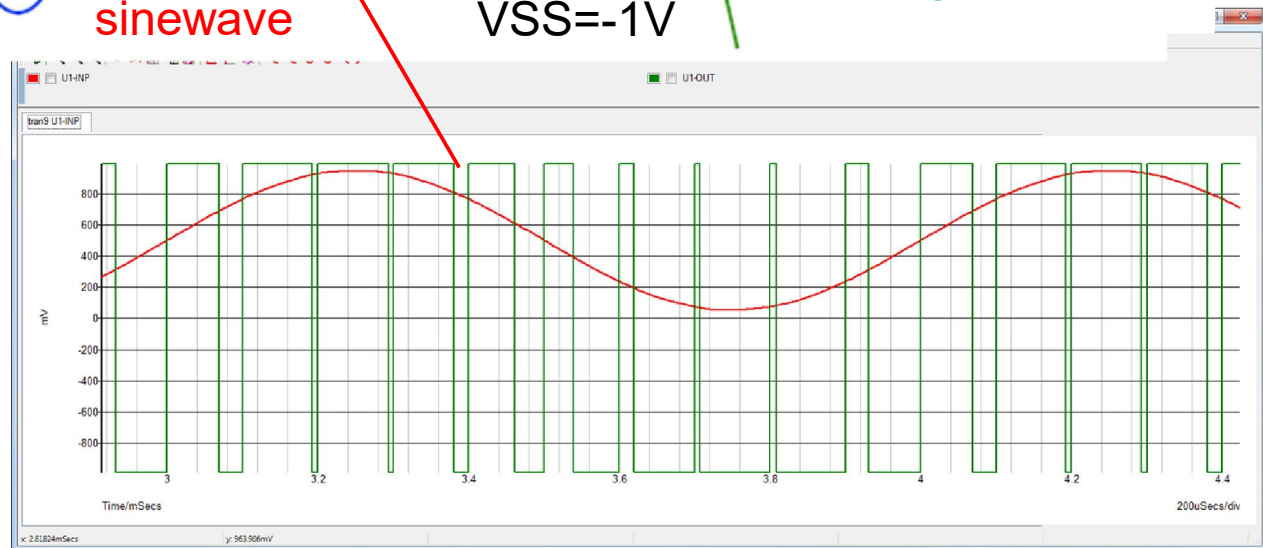
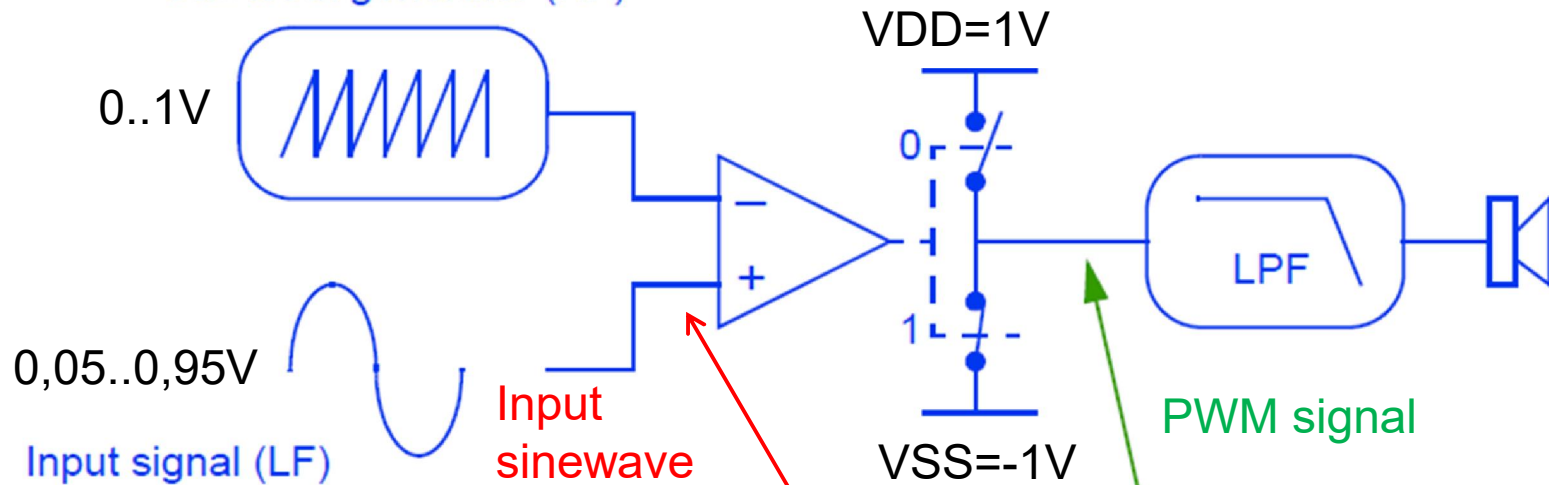


Class A, AB, B ➡ limited or bad efficiency due to simultaneous presence of voltage and current on the active device

Class D ➡ switching operation cancels losses in active devices

5. Class-D amplifiers: operation

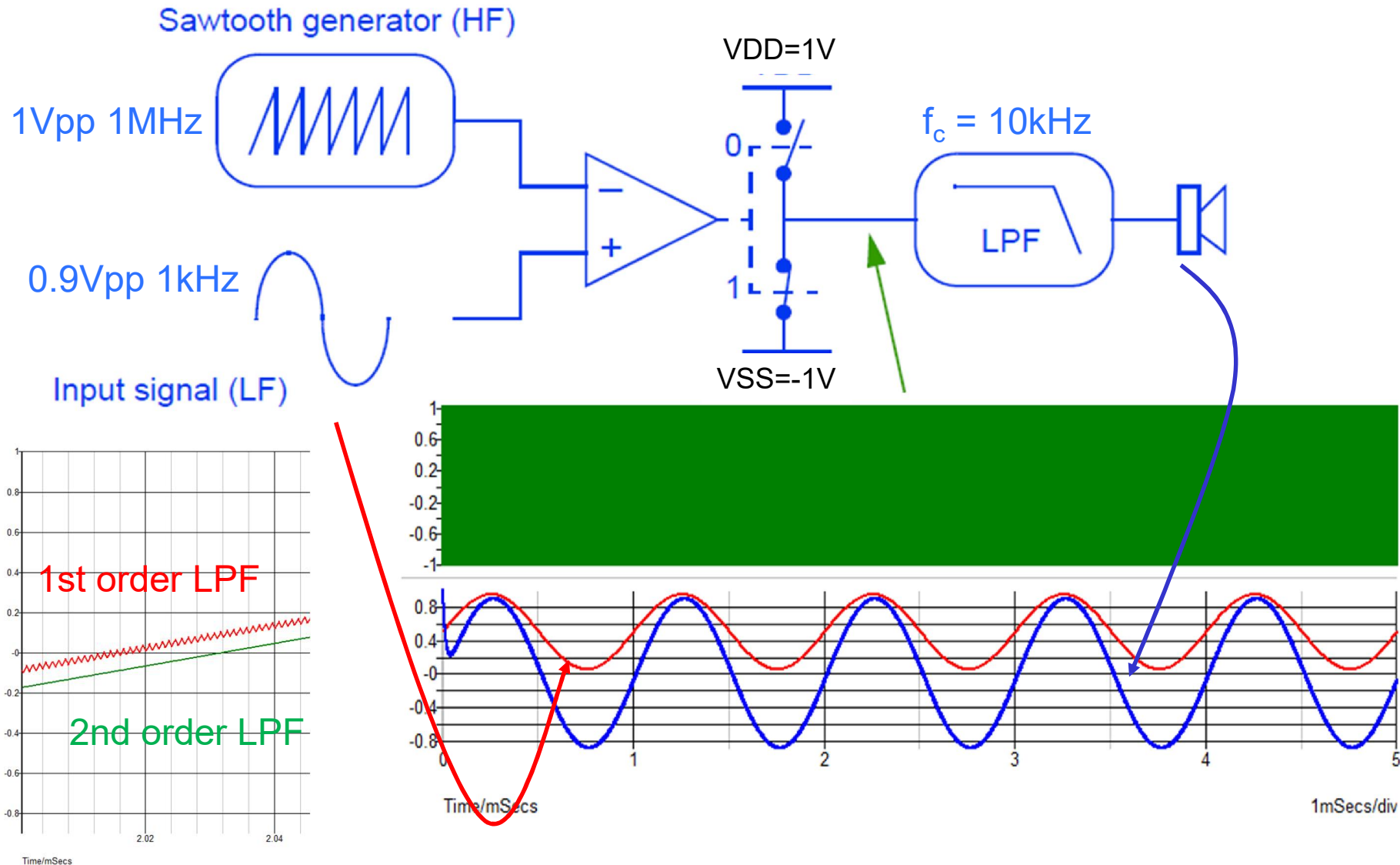
Sawtooth generator (HF)



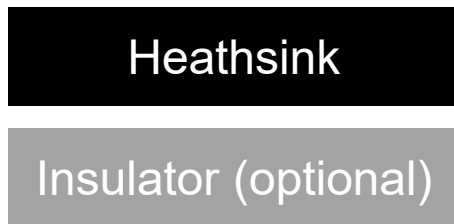
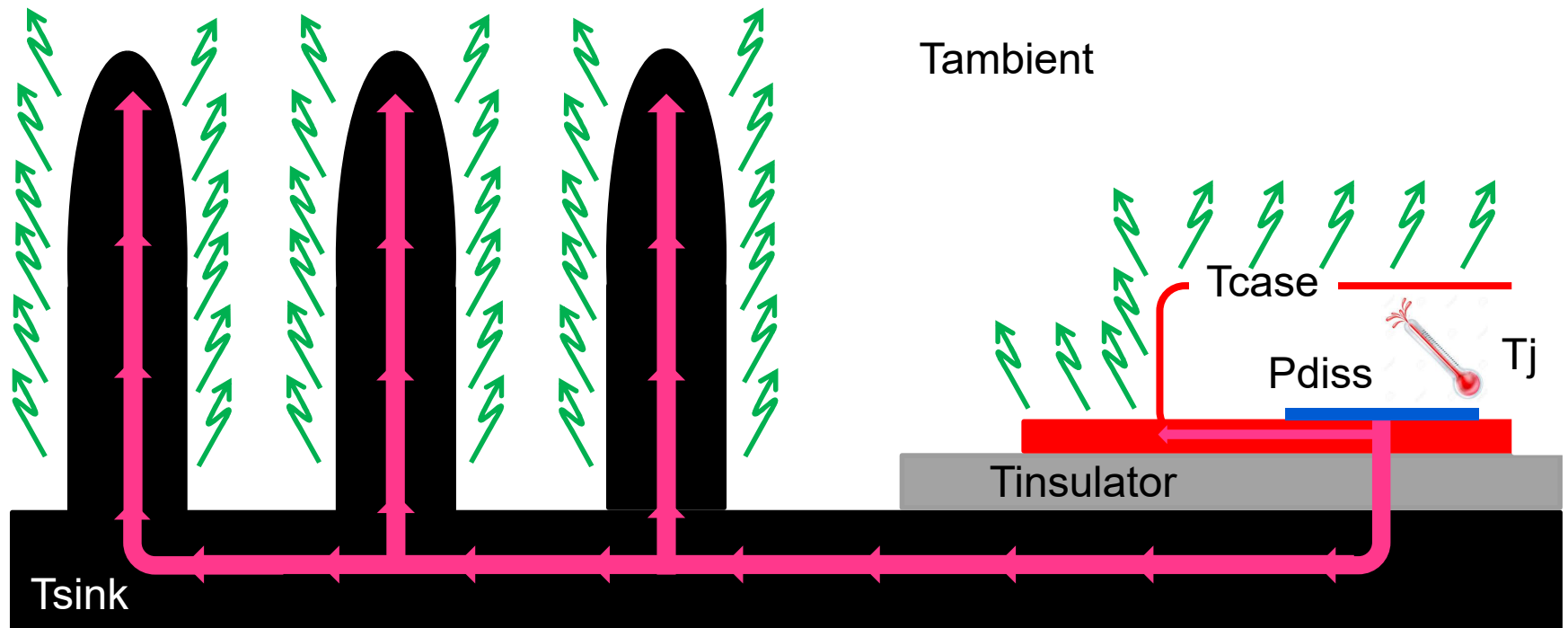
switch open: non-zero voltage, zero current
switch closed: non-zero current, zero voltage

no dissipated power, 100% efficiency

5. Class-D amplifiers: more realistic example



6. Heatsink calculation: thermal model



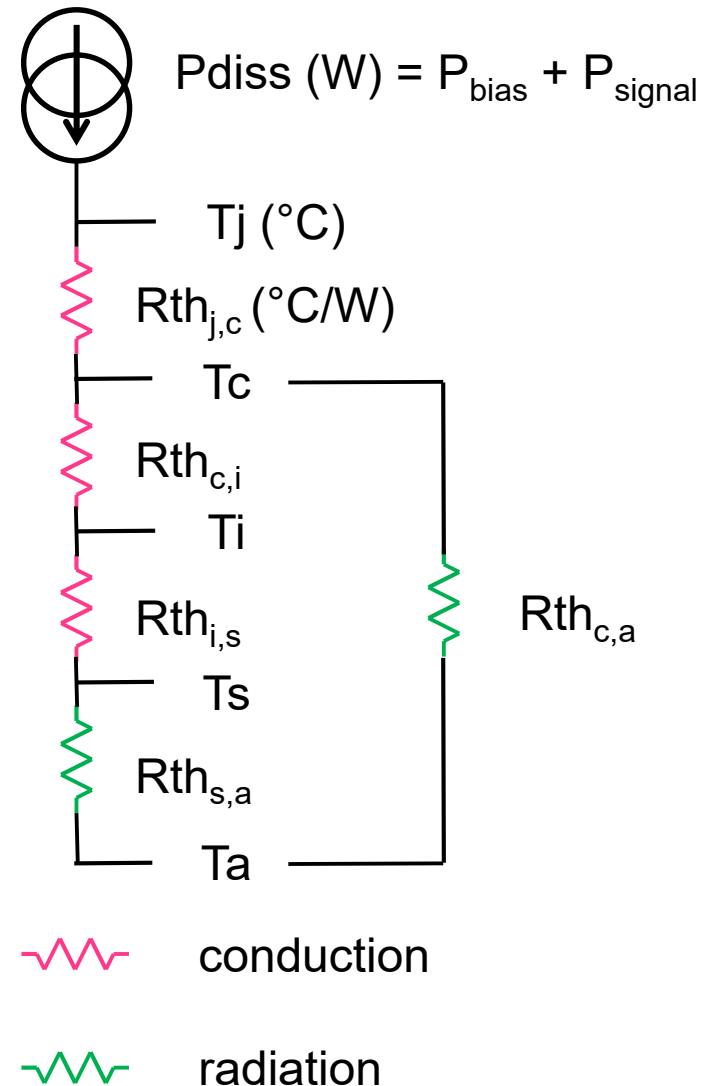
6. Heatsink calculation: thermal-electrical model

Power \longleftrightarrow Current
 Temperature \longleftrightarrow Voltage
 Thermal resistance \longleftrightarrow Resistance

$$T_j - T_a = P_{diss} \sum R_{th}$$

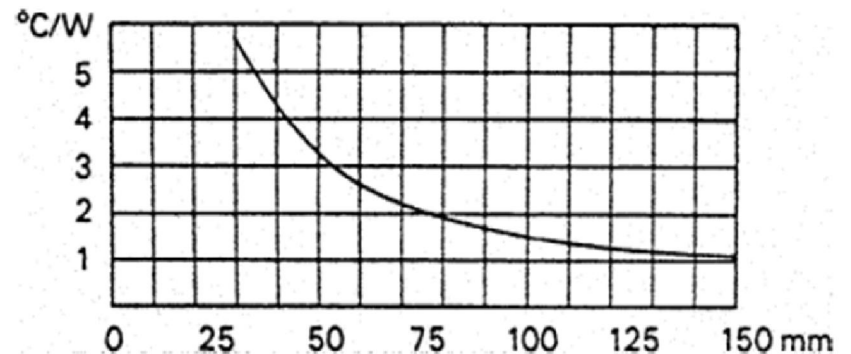
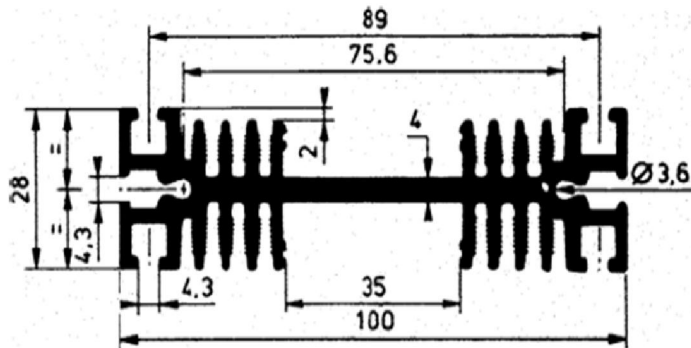
$$R_{th_{s,a}} = \frac{T_j - T_a}{P_{diss}} - R_{th_{j,c}} - R_{th_{c,i}} - R_{th_{i,s}}$$

($R_{th_{c,a}}$ neglected)

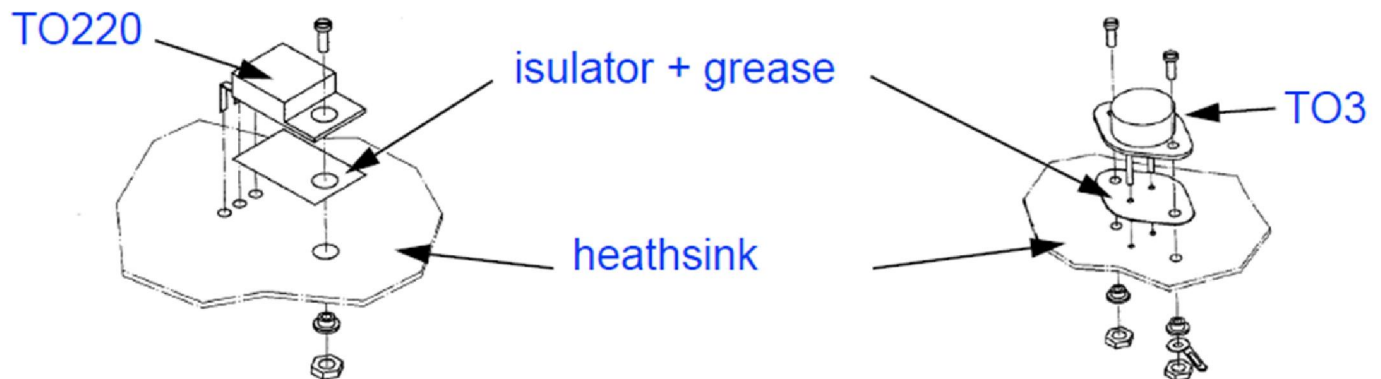


6. Heatsink calculation: mechanical considerations

- Thermal resistance depends on profile type and dimension:



- Mounting a transistor on the heatsink:



6. Heathsink calculation: voltage regulator example

Figure 4. Application circuits

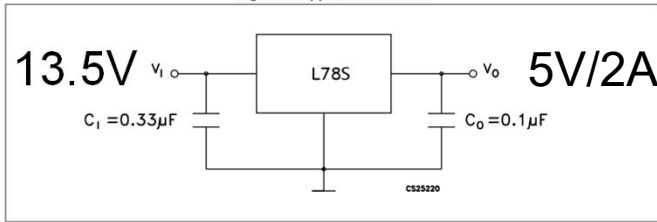


Table 3. Thermal data

Symbol	Parameter	TO-220	Unit
R_{thJC}	Thermal resistance junction-case	5	°C/W
R_{thJA}	Thermal resistance junction-ambient	50	°C/W

Table 2. Absolute maximum ratings

Symbol	Parameter		Value	Unit
V_I	DC input voltage	for $V_O = 5$ to 18V	35	V
		for $V_O = 24$ V	40	
I_O	Output current		Internally limited	
P_D	Power dissipation		Internally limited	
T_{STG}	Storage temperature range		-65 to 150	°C
T_{OP}	Operating junction temperature range		0 to 150	°C

Ambient temperature: $T_a = 30^\circ\text{C}$

$$P_{diss \max} = (13.5 - 5) \times 2 = 17\text{W}$$

Without heathsink:

$$T_j = P_{diss} \times R_{thj,a} + T_a = 880^\circ\text{C} !!!!$$

Heathsink calculation:
(no insulator)

$$T_j - T_a = P_{diss} (R_{thj,c} + R_{thc,s} + R_{ths,a})$$

Hint: limit T_j to 120°C , $R_{thc,s} = 0.2^\circ\text{C/W}$ (thermoconductive grease)

$$\sum R_{th} = 5.3^\circ\text{C/W} \rightarrow \text{no practical solution since that yields } R_{ths,a} = 0.1^\circ\text{C/W}$$



6. Heatsink calculation: voltage regulator example



41.6 x 25 x 63.5mm
3°C/W

$$\sum R_{th} = 8.2^{\circ}\text{C/W} \rightarrow P_{diss\ max} = 11\text{W}$$

- reduce current down to $\approx 1.3\text{A}$ max
- reduce input voltage down to 10.5V
- use another regulator (TO3 case)

6. Heatsink calculation: audio amplifier example

TDA7294 100W class-AB audio amplifier

$$P_{out} = 100W \rightarrow P_{diss\ max} = 40W$$

THERMAL DATA

Symbol	Description	Value	Unit
$R_{th\ j-case}$	Thermal Resistance Junction-case	Max 1.5	°C/W

Heatsink calculation:
(no insulator)

$$T_j - T_a = P_{diss} (R_{th\ j,c} + R_{th\ c,s} + R_{th\ s,a})$$

Hint: limit T_j to 120°C,
 $R_{th\ c,s} = 0.2^\circ\text{C/W}$ (thermoconductive grease)

$$\sum R_{th} = 2.25^\circ\text{C/W} \rightarrow R_{th\ s,a} = 0.55^\circ\text{C/W}$$

Forced air: $\approx 70\text{mm}$
Passive: $\approx 250\text{mm}$

