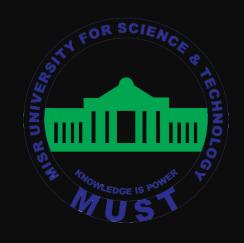
MISR UNIVERSITY FOR SCIENCE AND TECHNOLOGY COLLEGE OF ENGINEERING MECHATRONICS DEPARTMENT



MTE 506 DIGITAL CONTROL

LAB 3 - SPRING 2020

Goals of The Lab

Discretization of Analog Control Systems





Converting differential model into algebraic model



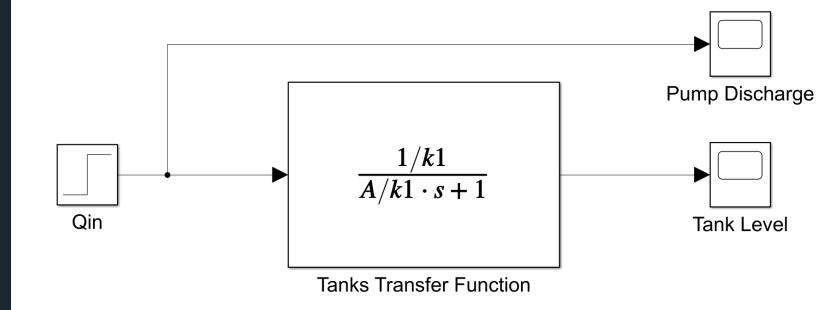
Computing steady state error and system types

Automatic Control

Closed Loop System

Open Loop System

Using Simulink



Closed Loop System

Simple example

Previously (Tank Simulation):

$$A\frac{dh}{dt} + k_1 h(t) = q_i(t)$$

Taking Laplace Transform

$$A(sH(s) - h_0) + k_1H(s) = Q_i(s)$$

$$AsH(s) - Ah_0 + k_1H(s) = Q_i(s)$$

$$\therefore H(s) = \frac{Q_i(s) + Ah_0}{As + k_1}$$

Can you convert diff. eqn. into Laplace Transform using MATLAB script?



 \therefore Asuming $h_0 = 0$ (empty tank)

$$\therefore \frac{H(s)}{Q_i(s)} = \frac{1}{As + k_1} = \frac{K}{\tau s + 1}$$

$$\therefore \frac{H(s)}{Q_i(s)} = G(s) = \frac{K}{\tau s + 1}$$

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Laplace table

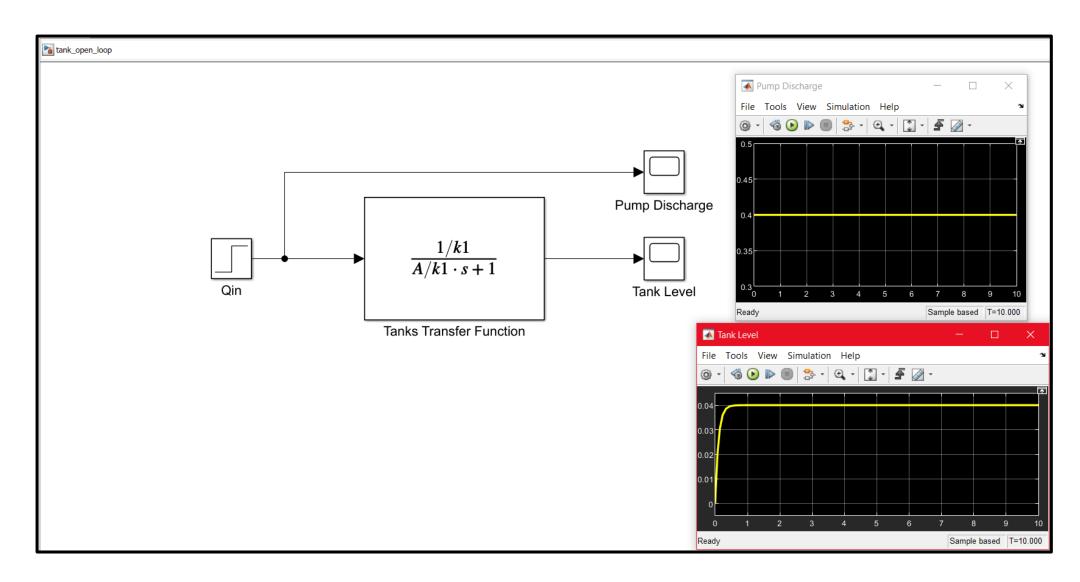
PDF

Table of Laplace Transforms					
	$f(t) = \mathcal{L}^{-1}\{F(s)\}$	$F(s) = \mathfrak{L}\{f(t)\}\$		$f(t) = \mathcal{L}^{-1}\left\{F(s)\right\}$	$F(s) = \mathfrak{L}\{f(t)\}$
1.	1	$\frac{1}{s}$	2.	\mathbf{e}^{at}	$\frac{1}{s-a}$
3.	t^n , $n=1,2,3,$	$\frac{n!}{s^{n+1}}$	4.	t^p , $p >$ -1	$\frac{\Gamma(p+1)}{s^{p+1}}$
5.	\sqrt{t}	$\frac{\sqrt{\pi}}{2s^{\frac{3}{2}}}$	6.	$t^{n-\frac{1}{2}}, n=1,2,3,\dots$	$\frac{1\cdot 3\cdot 5\cdots (2n-1)\sqrt{n}}{2^n s^{n+\frac{1}{2}}}$
7.	$\sin(at)$	$\frac{a}{s^2 + a^2}$	8.	$\cos(at)$	$\frac{s}{s^2 + a^2}$
9.	$t\sin(at)$	$\frac{2as}{\left(s^2+a^2\right)^2}$	10.	$t\cos(at)$	$\frac{s^2 - a^2}{\left(s^2 + a^2\right)^2}$
11.	$\sin(at) - at\cos(at)$	$\frac{2a^3}{\left(s^2+a^2\right)^2}$	12.	$\sin(at) + at\cos(at)$	$\frac{2as^2}{\left(s^2+a^2\right)^2}$
13.	$\cos(at) - at\sin(at)$	$\frac{s\left(s^2-a^2\right)}{\left(s^2+a^2\right)^2}.$	14.	$\cos(at) + at\sin(at)$	$\frac{s\left(s^2+3a^2\right)}{\left(s^2+a^2\right)^2}$

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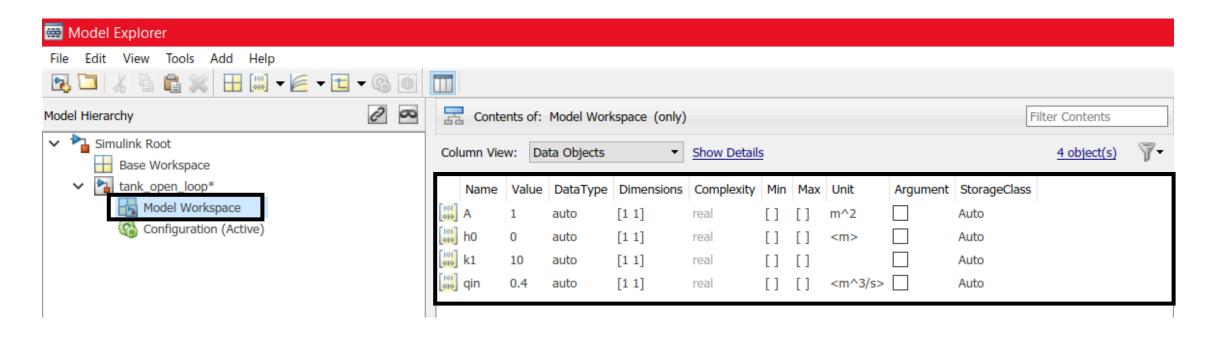
Open Loop Simulink Model

Open Loop



Model Workspace

Store model parameters

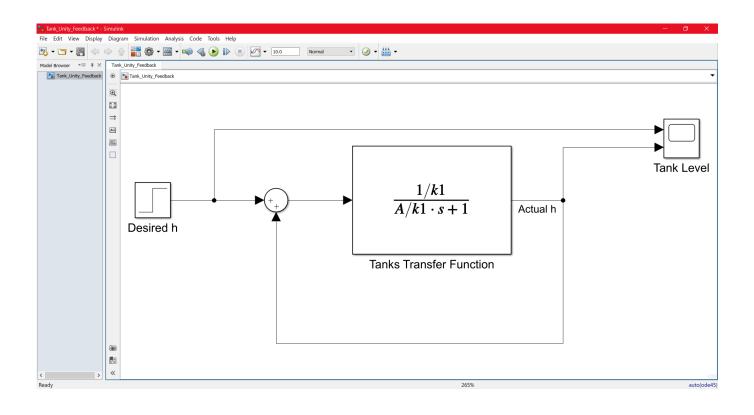


Automatic Control

Closed Loop System

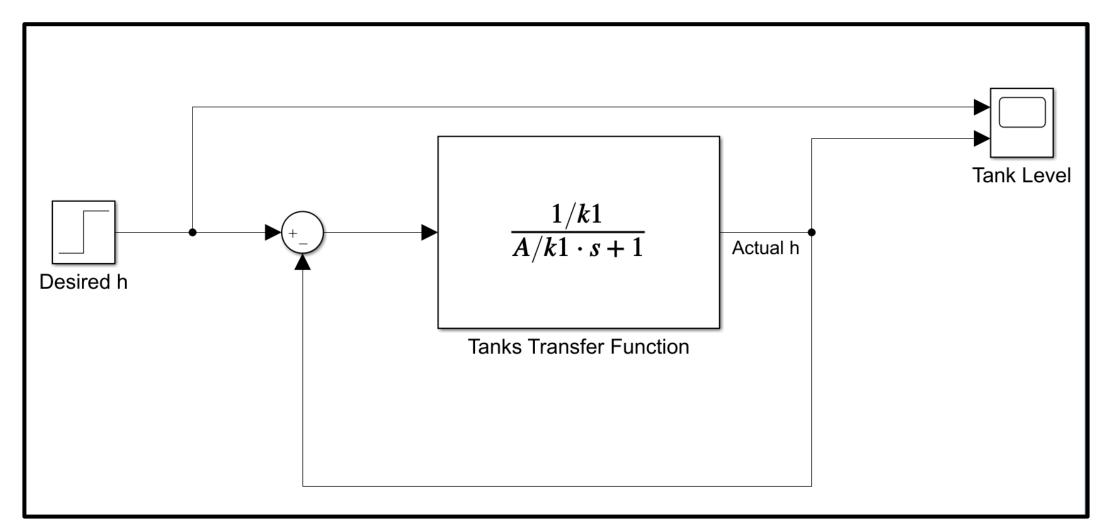
Closed Loop System

Using Simulink



Closed Loop System

Unity Feedback



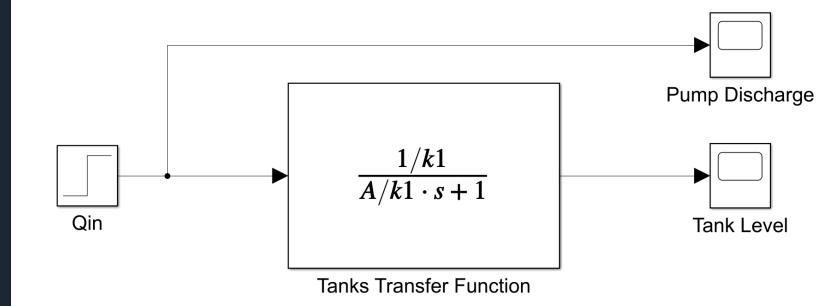
Lab 3 Closed Loop System Unity Feedback Error 🖺 😭 🔒 🦫 🔍 🤏 🖑 🗑 🐙 🔏 - 📗 🔡 🕟 **Calculate the steady state error** using pen and paper: K1 = 10, A=1, and Desired h = 4 m

Automatic Control

Closed Loop System

Open Loop System

Steady State Error

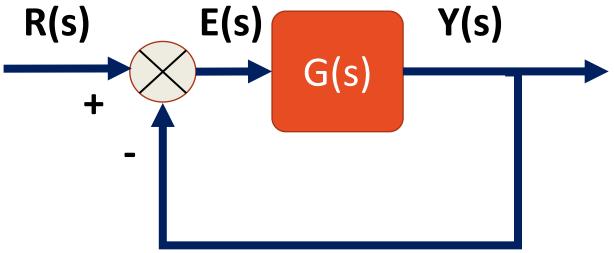


Closed Loop System

Steady State Error

Final Value Theorem

$$e(\infty) = \lim_{s \to 0} sE(s) = \frac{sR(s)}{1 + G(s)}$$



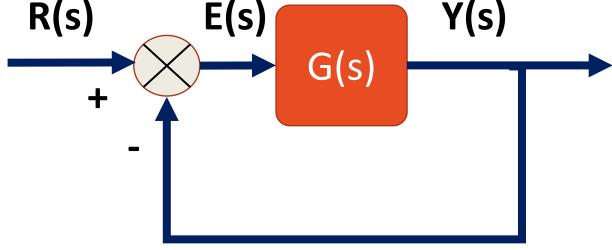
$$e(\infty) = \lim_{s \to 0} \frac{s\frac{4}{s}}{1 + \frac{K}{\tau s + 1}} = \frac{4}{1 + \frac{(\frac{1}{10})}{1}} = 3.6 \to (4 - 0.4)$$

Closed Loop System

Steady State Error

Tank is Type 0 (why?)

$$e(\infty) = \frac{step \ value \ (h_{desired})}{1 + \lim_{s \to 0} G(s)}$$



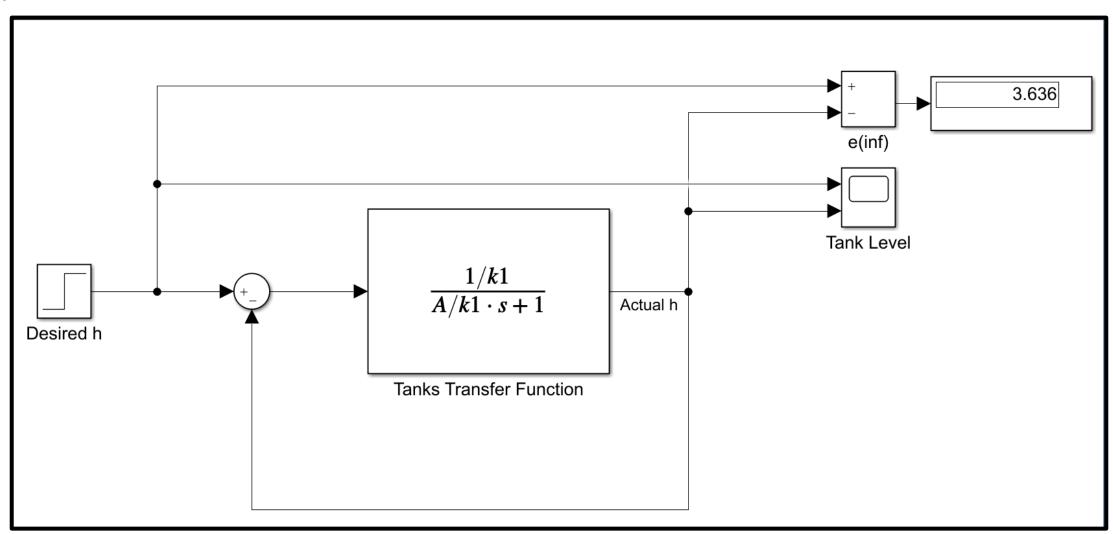
$$e(\infty) = \frac{step\ value}{1 + K_p} \to K_p = \lim_{s \to 0} G(s)$$

$$e(\infty) = \frac{1}{1 + 0.1} = 3.6$$

 $K_p = 0.1$ (Static Error Constant)

Closed Loop System

Steady State Error

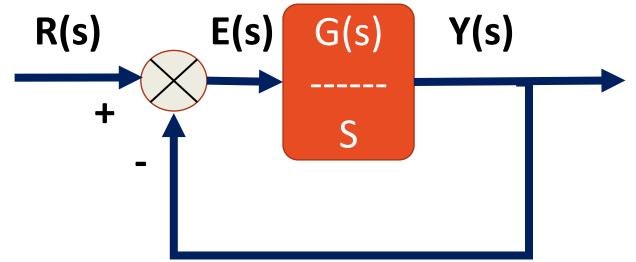


Closed Loop System

Steady State Error

Adding Integrator to the tank

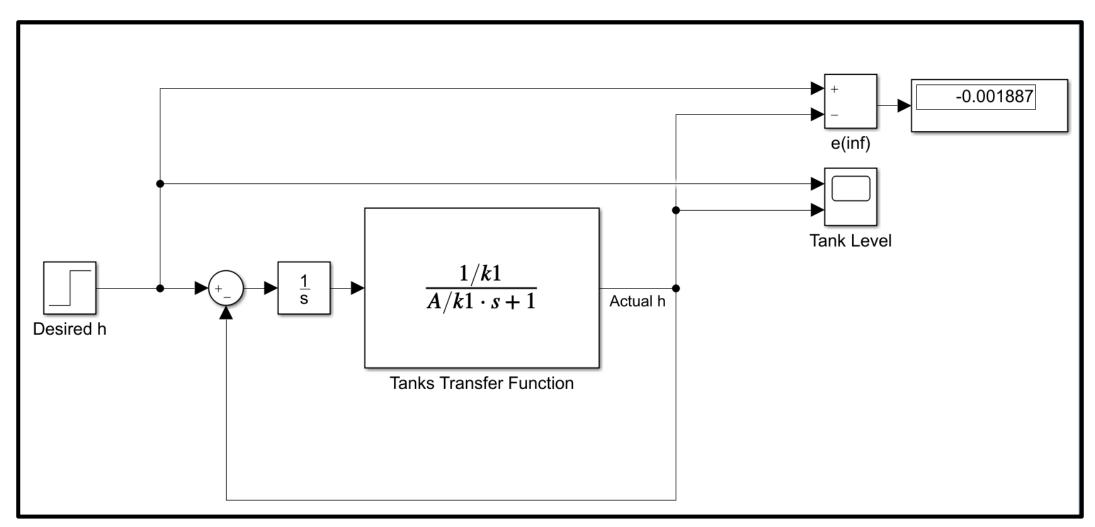
$$e(\infty) = \lim_{s \to 0} sE(s) = \frac{sR(s)}{1 + \frac{G(s)}{s}}$$



$$e(\infty) = \lim_{s \to 0} \frac{s\frac{4}{s}}{1 + \frac{1}{s}\frac{K}{(\tau s + 1)}} = \frac{4}{1 + \frac{(\frac{1}{10})}{0}} = \frac{4}{\infty} = 0 \quad (Type \ 1)$$

Closed Loop System

Steady State Error

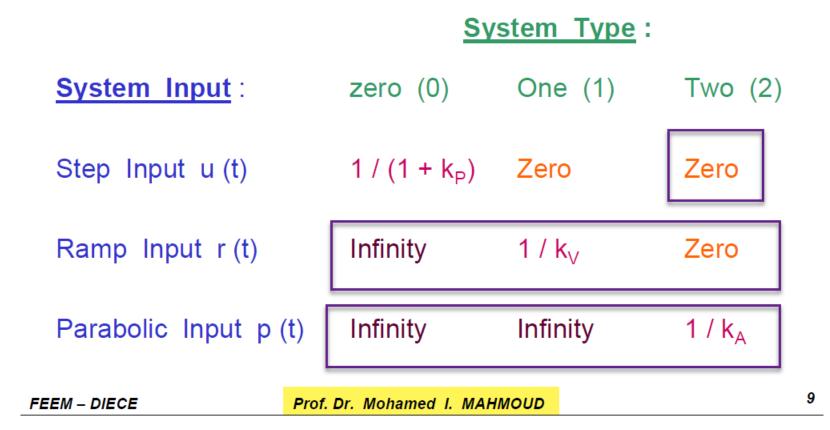


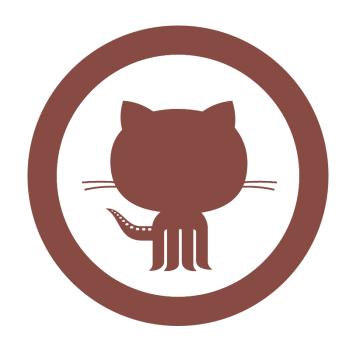
Closed Loop System

Steady State Error

Closed Loop Systems

Steady State Error Analysis





Don't forget to pull the lab update from.

http://github.com/wbadry/mte506

END OF Lab 3