Emotional Algebra

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Contents

| 1 | Preface | 2 | |
|---|------------------------|---|--|
| 2 | Conditions | | |
| | 2.1 Time | 2 | |
| | 2.1.1 Now | 3 | |
| | 2.1.2 Past | 3 | |
| | 2.1.3 Future and doubt | 3 | |
| | 2.2 Emotional events | 3 | |
| | 2.3 Real Situations | 4 | |
| | 2.4 Atmosphere | 5 | |
| | 2.5 Leib | 5 | |
| | 2.6 Actions | 6 | |
| | 2.7 Motivations | 6 | |
| | 2.8 Outline | 6 | |
| 3 | Symbols and parameters | | |
| 4 | Inference Rules | | |

1 Preface

HE FORMALIZATION of logic allowed us, a long period of time after it's discovery by Aristotle, to build computers that can outsource some of our mental facilities. They allowed us to perform logical reasoning on a great number of propositions automatically.

We do very bad with things that cannot be put easily in front of us. A lot of problems humanity faces are the results of denying subjective experience and declaring only physical events as true. Physical events are more easily formalized than emotional ones and therefore offer a false feeling of more confidence in the results. Once something is formalized, we have easier access to it because we can manipulate it in our mind without having to life through all of the real consequences. Imagine an architect, building buildings which collapse every time until they don't anymore after 'fixing all the bugs'. This is unacceptable. But we do it in our emotional world all the time, because there is no easy way to externalizing them and looking at their possible emotional consequences rigorously.

In this paper, I'd like to try to formalize emotions a similiar way we have formalized math. This, if it works, may lead to greater understanding of humans.

I will not try to explain what the basic words (like emotion) mean. You have to understand what they mean naturally, as you have to understand 'sets' in set theory naturally. If you don't know what something like 'feels bad' mean think seriously about cutting off your arm. This would have consequences that you subjectively most likely consider 'bad' in the now (pain) and the future (inability to use arm).

2 Conditions

We need to define some conditions that affect human emotion first. I believe these are the most important facilities that do that.

2.1 Time

Every human emotion is resided in the now. Even if we think about past or worry about the future, we do it *now*. And the now, although it always is, never really is. Once contemplated, it is already gone and slipped into the past.

Therefore, we need to define a time operator. I will suggest these:

| E | E is any emotional event |
|--------------------------|--------------------------------------------------------------|
| nE | E depends mainly on the current situation |
| pE | E depends mainly on a past situation |
| fE | E depends mainly on future situations ('worry') |
| $(n \wedge f)E$ | <i>E</i> depends on the current situation now and the future |
| $(f \wedge p)E$ | E depends on the future and the past |
| $(n \wedge p)E$ | E depends on the now and the past |
| $(n \wedge f \wedge p)E$ | E depends on the now, the future and the past |
| | |

2.1.1 Now

As every moment is always depending on the 'now', we can treat it analogously to the multiplication operation and leave it out like we leave out the multiplication symbol if it should not be preciously stretched that the situation is depending on the now and mainly the now, so nE = E.

2.1.2 Past

For this section, I will define reality as that on which external observers and I can agree to be the fact.

Sometimes, people misremember and therefore construct a past for themselves that did not really happen. In formalization I suggest to label events with $\mathcal{E}(t, E)$ if this happens, where t is the level of accuracy of the remembrance, where 1 means very reliable memory and 0 means very unreliable memory. Therefore, a complete sentence would be:

$$n\Big(p\big(\mathscr{E}(t,E_1)\wedge E_2\big)\Big) \tag{1}$$

This would mean that the current situation is depending on a misremembered event E_1 and a real event E_2 .

2.1.3 Future and doubt

As the past is not here anymore and cannot be known with the same certainty than the present, the future cannot be known with any certainty. Therefore, future events are doubtful.

Doubt is the human condition of not-being-sure. Though I deny the possibility of absolute certainty we may define a formalization of doubt as $\mathcal{E}(t, E)$, where t is between 0 and 1, where 0 means 'I know nothing about the possibility of this event' and 1 means 'I feel certain that this event will happen'.

An example:

$$n\left(f\left(\mathcal{E}(0.1, E_1) \wedge E_2\right)\right) \tag{2}$$

This means:

"My current emotional situation depends on two things that depend on something tomorrow, of which one (E_1) will likely not occur and E_2 will certainly occur"

Leaving out the $\mathcal{E}(t, E)$ defaults to t = 1, meaning $E = \mathcal{E}(1, E)$.

2.2 Emotional events

Every emotional event can be ordered in roughly 3 categories. 'Good', 'bad' and 'neutral'. This is the way an honest person would describe the emotion when asked how it felt.

Examples.

Eating a really good meal in a good atmosphere results in an event that would be described as 'good'.

Running for your life would result in an event called 'bad'.

Having a catatonic schizophrenic episode (the ones where people just don't react to anything and stop feeling entirely) can be considered als neutral (since the person does not feel anything anymore).

I would like to define operators to describe these 3 categories. All of the arrow-operators are right-associative and only get one parameter, which is why you can leave out brackets without losing information about which event is meant.

These operators are not exclusive, because every event can have facets that are good, bad and neutral altogether.

 $\uparrow E$ Event E is seen as good $\downarrow E$ Event E is seen as bad Event *E* is seen as emotionally neutral $\uparrow^{0.1} E$ Event E is a bit good $(\uparrow = \uparrow^1)$ $\downarrow_{0.9} E$ Event *E* is a very bad $(\downarrow = \downarrow_1)$ $\rightarrow_0 E$ Event *E* is seen as emotionally neutral and I don't care about it¹ Event E is seen as emotionally neutral but I still care about it some way² $\rightarrow_1 E$ $\uparrow E$ One is torn-apart if the event is good, bad or neutral (doubtful), equal to $\uparrow E \land \downarrow E \land \rightarrow E$ Leaving out the arrow should be a way for shortening it from $\rightarrow E$, so that $E = \rightarrow E$.

$$n\Big(f\left(\mathscr{E}(0.1,\uparrow E_1)\land\downarrow E_2\right)\Big) \tag{3}$$

"My current emotional situation depends on two things that depend on something tomorrow, of which one (E_1) will likely not occur which I am very happy about and which is important to me and E_2 will certainly occur which I am negative about"

2.3 Real Situations

Every moment is a complex mixture of influences from the (real and perceived) past, present and future. But some of these components are more important than others. The number of roof tiles in the room where I was born is an event in the past, but has barely any meaning to my situation at all. The people my parents were on the other hand we're very important. Therefore, it is important to give a formalism to ascribe importance. I suggest:

$$\mathcal{I}(i,E)$$
 (4)

That means event E is i important, where i is between 0 (not important at all) to 1 (very important).

$$n\left(f\left(\mathscr{I}\left(1,\mathscr{E}\left(0.9,\uparrow E_{1}\right)\right)\wedge\left(\mathscr{I}\left(0.1,\downarrow E_{2}\right)\right)\right)\right)\tag{5}$$

"My current emotional situation depends on two things that depend on something tomorrow, of which one (E_1) will likely occur which is very important to me which I am very

 $^{^2\}mathrm{E.g.}$ a situation where some body tells me the number of rice corns eaten every year

²E.g. the fact that Donald Knuth was born on the 10th of January 1938, which I care about, but it has no emotional significance over any other date that could be his birthday.

happy about and E_2 will certainly occur which I would be a bit negative about of which I also would don't really care much about if it happens"

An example situation would be that I am very happy that the sun will rise tomorrow again (E_1) (most probably) and I hope that the moon does not crash into the earth before that (E_2) , which I find highly unlikely to happen.

2.4 Atmosphere

Every situation is filled with an atmosphere. An atmosphere is the general way a world around one is perceived in the moment of perception.

Atmospheres consist of a mix of expectations what will happen in a place (future) and what has happened (past) without them really neccessarily happening in the moment of perception. I will use the same Formalization as with Events, nA being an atmosphere which is what it is because of what is currently happening, pA an atmosphere that depends on the past and fA an atmosphere that depends on the future.

Think of dark alley at night being scary or a swimming pool party with friends in summer as happy, so, as with Events, they get arrows indicating good $\uparrow A$, bad $\downarrow A$ and neutral $\rightarrow A$.

A good atmosphere now $(n \uparrow A)$ in a place which is based on good events that happened there in the past $(p \uparrow E)$ can be written as:

$$n \uparrow A \Big(\uparrow A \supset (p \uparrow E) \Big) \tag{6}$$

2.5 Leib

The Leib (old german for 'body') is not the body. The Leib is where we feel ourselves. We don't feel the bodily actions of severing nerves and so on, but pure pain when severing off a hand. The pain may be the result of a bodily event, but is not equal in extension, as pain is something mental.

Let's use *L* for a 'Leibliches' Event.

There are many different ways that the Leib can interact with our emotions. We can feel free for example. Think about having achieved a lot in a day and then going to bed happily, free of obligations left on that day. Or we can feel trapped, when we are in a situation where we don't know how to get out. These Events L can therefore be either good (\uparrow), bad (\downarrow) or neutral (\rightarrow), which can also be supplemented with numbers like $\downarrow_1 L$ for '10 of 10'-pain or $\uparrow^1 L$ for a moment of great pleasure (e. g. a well-earned orgasm with a person one loves). Leaving out the number set's it to 1.

Generally, these can be sorted like Events, as they are a special subcategory of Events. We have the modifiers \uparrow , \downarrow and \rightarrow to ascribe how we feel towards something. Cutting off ones arm would probably be $\downarrow L$, eating something really delicious and healthy most probably leads to something like $\uparrow L$.

It's important to note that these must not be 'objective' criteria, but more subjective ones.

One may feel that cutting off ones arm (H) may be a good action (\uparrow) , even though it turns out not to be in the future which makes us unhappy in the future $(\downarrow fE)$. This would be

formalized as:

$$n\Big(f\downarrow \big(f\downarrow E\supset\uparrow H\big)\Big) \tag{7}$$

2.6 Actions

Sometimes we act like we do because of the past, sometimes because of the present and sometimes because of the future, and sometimes a complex mix of these. For example, you might have been screwed in a contract earlier (past), and now you set up a better contract for not getting screwed in the future.

Let's call Acts *H* for german 'Handlung' (Act).

Sometimes acts don't turn out the way you wanted them to go. For acts that turn out good, let's use $\uparrow H$, for bad ones $\downarrow H$, for neutral ones $\rightarrow H$ and for mixtures of these $\uparrow H$. As with events and atmospheres, let's assign values between 0 and 1, like: $\uparrow^{0.9} H$ for an act that turned out to be good or \downarrow_1 for an act that turned out to be very bad.

An act can follow situations and atmospheres. Think of running away (H) from the dark alley mentioned earlier. You do this because the atmosphere A is bad because you know several people were murdered there (E) in the past and you want to go away from there right now. This would be described as:

$$n\Big(\big(\downarrow A\supset p:\downarrow E\big)\supset H\Big) \tag{8}$$

2.7 Motivations

Let's call Motivations M. Not every act we do is fully motivated by conscious reasons.

If important, we can write this with $\mathcal{C}(c, M)$, where c is between 0 and 1, where 0 means 'fully unconscious' and 1 means 'fully conscious'.

When going into 'autopilot', e. g. in a dangerous situation, c will be very low. Imagine again running away from war. The Motivation M is to survive, but it is so basic that you don't need much conscious reflection on that.

Running away (H) successfully (\uparrow) from war ($\downarrow E$) to survive (M) would be formalized as:

$$n\left(\left(\downarrow\left(n\land p\land f\right)E\supset\mathscr{C}(0,M)\right)\supset\uparrow H\right) \tag{9}$$

Successfully and very consciously moving your body (H) to get to a party (E) in the future you are happy about (\uparrow) can be written as:

$$n\Big(\big(\uparrow fE\supset \mathscr{C}(1,M)\big)\supset \uparrow H\Big) \tag{10}$$

2.8 Outline

There are these types of things that control emotion:

| x | Type |
|------------------|-------------|
| E | Events |
| M | Motivations |
| H | Actions |
| \boldsymbol{A} | Atmospheres |
| L | Leib |

Each of these can be prepended with one or more of the operators \uparrow (good/successful), \downarrow (bad/unsuccessful) and \rightarrow (neutral).

Each of these modifiers can have options from 0 to one, where positive options are in superscript and negative actions are in subscript, like very good actions \uparrow^1 and very bad actions \downarrow_1 . When no number is written, it will default to 1, so that $\uparrow=\uparrow^1$.

Any of these can lay in the past, present or future or any combinations of these, but at least one. When nothing is written, x = px.

Every emotion is always bound in time and felt right now, therefore, every expression must start with

$$nx$$
 (11)

where x is any of E, M, H, A or L. Therefore, the 'n' can be left away, meaning x = nx. Also, any of these can be dependent on the past p, present (n) and/or future (f).

An Event *E* can consist of multiple sub-factors, like having gone to a party successfully $(p \uparrow H)$ and now experiencing a good atmosphere $(n \uparrow A)$ there would be formalized as:

$$n\left(\left(p\uparrow H\land n\uparrow A\right)\supset n\uparrow E\right) \tag{12}$$

Some good emotional events $\uparrow E$ that happens in the future because of something you do now would but don't really want to do (like cleaning up your room) ($\downarrow A$) would be formalized as:

$$n(n \downarrow A \supset f \uparrow E) \tag{13}$$

Some of these values have specification-functions.

Events E can me misremembered or remembered correctly. They can be modified with $\mathcal{E}(t, E)$, where t = 0 for very unreliable and t = 1 for very reliable subjective memories of the events. For future events, This can be used as a certainty-meter how certain (0 = not all certain) and 1 = very certain we are that they will occur. We can define that $M = \mathcal{E}(1, E)$.

Motivations M can be modified with the level of consciousness they require with $\mathcal{C}(t,M)$, where t=0 means zero consciousness required (e. g. the will to survive) and t=1 meaning high level of consciousness required, e. g. solving mathematical equations in order to obtain a goal. Leaving this out will mean $\mathcal{C}(1,M)=M$.

All of these situations x can be ascribed with an importance level, where t=0 no importance and t=1 is extreme importance. We define this as $\mathcal{I}(t,x)$. When left out, we define $x=\mathcal{I}(1,x)$.

3 Symbols and parameters

| Symbol | Туре |
|-------------------------------------------|--------------------------------------------------------------------------------------------------------------------------------------------------------------------------|
| I | Any item possible or combination of items |
| p, f, n | Past, future and present |
| \uparrow , \downarrow , \rightarrow | Positive, negative and neutral |
| (,) | Brackets, create groups of elements in order to overcome standard precedence rules |
| ٨ | Logical and, $I_1 \wedge I_2 \wedge I_3 = I_1 \wedge (I_2 \wedge I_3) = (I_1 \wedge I_2) \wedge I_3$ |
| $I_1 \supset I_2$ | I_2 depends on I_1 , $I_1 \supset I_2 \supset I_3 = I_1 \supset (I_2 \supset I_3)$ |
| $I_1 \vee I_2$ | Locigal or, $I_1 \vee I_2$ |
| $\neg I_1$ | Negates I_1 , so that $\neg \downarrow I_1 = \uparrow I_2$ and $\neg \mathscr{C}(1, I_1) = \mathscr{C}(0, I_1)$ and $(\neg E)$ meaning 'E does not occur' ³ |

4 Inference Rules

The modifier functions $\mathcal I$ (importance), $\mathcal E$ (certainty) and $\mathcal E$ (consciousness required) are defined like this:

$$\mathcal{I}(t_1, E_1) \wedge \mathcal{I}(t_2, E_2) = \mathcal{I}(\frac{t_1 + t_2}{2}, E_1 \wedge E_2)$$
 (14)

So having to tasks E_1 , E_2 that are 0.8 and 0.7 important respectively can be described as

$$\mathscr{I}(0.8, E_1) \wedge \mathscr{I}(0.7, E_2) = \mathscr{I}\left(\frac{0.8 + 0.7}{2}, E_1 \wedge E_2\right) = \mathscr{I}(0.75, E_1 \wedge E_2) \tag{15}$$

Having them or'ed multiplies the values:

$$\mathscr{I}(0.8, E_1) \vee \mathscr{I}(0.7, E_2) = \mathscr{I}(0.8 \cdot 0.7, E_1 \vee E_2) = \mathscr{I}(0.56, E_1 \vee E_2) \tag{16}$$

As a single event can have both negative and positive consequences simultaneously, we define

$$n \uparrow E = f \downarrow E \land p \uparrow E \tag{17}$$

Positive and negative *do not* add up to neutral, but rather to torn-apart (1):

$$\uparrow E = \downarrow E_1 \land \uparrow E_2 \tag{18}$$

Neutral events do not change the output of an equation, like:

$$\downarrow E = \downarrow E_1 \land \to E_2 \tag{19}$$

³Here grouping with brackets is important, since $\neg \uparrow E$ may mean either 'the god event E will not occur' or $\downarrow E$, but with $(\neg \uparrow)E$ it is clear that what is meant is 'the event E is bad' $(\downarrow E)$.