

$$P(A=0) = 0.2$$

$$P(A=1) = 0.8$$

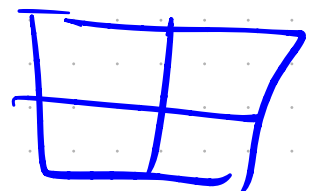
$$P(A=0, B=1) = \dots$$

$P(A, B)$

$$\begin{aligned} &P(A=0, B=0) \\ &+ P(A=1, B=0) \\ &= P(B=0) \end{aligned}$$

	A		
	0	1	
0	0.2	0.4	0.6
1	0.1	0.3	0.4
			P

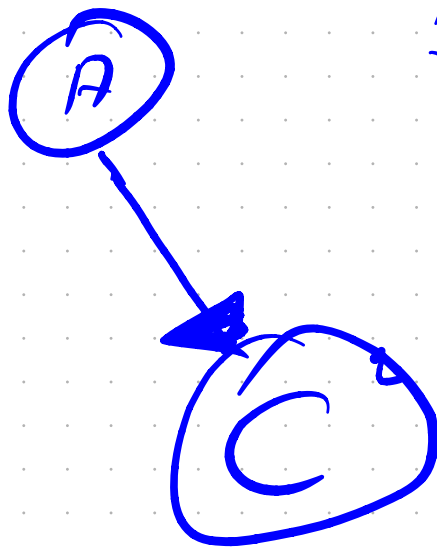
$$P(A) \quad P(B) = P(A, B)$$



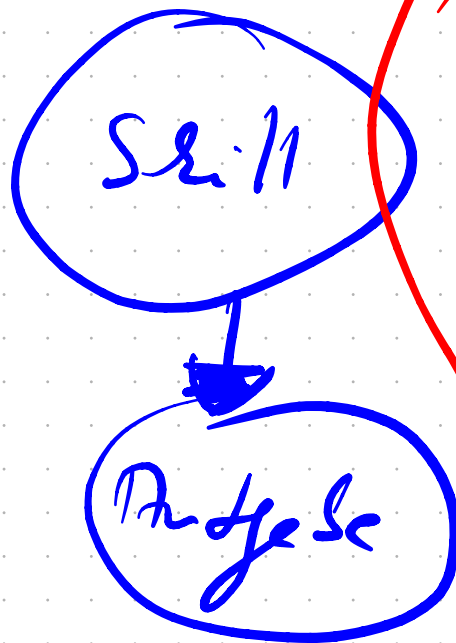
$$P(A|B) = \frac{P(A, B)}{P(B)}$$

$$P(A|B) = \frac{P(B|A) P(A)}{P(B)}$$

$$\underline{P(A, C) = P(C|A) P(A)}$$



$$\sum P(S, A) \\ \text{Skill} \\ = P(A)$$



$$P(\text{Skill}) = \begin{pmatrix} 0.8 \\ 0.2 \end{pmatrix}$$

Gesucht:

$$P(\text{Aufgabe})$$

$$P(\text{Skill}, \text{Aufgabe}) = \frac{P(\text{Aufgabe} | \text{Skill})}{P(\text{Skill})}$$

$$\frac{P(\text{Aufgabe} | \text{Skill})}{P(\text{Skill})}$$

$$P(\text{Skill}) \begin{pmatrix} 0.8 \\ 0.2 \end{pmatrix}$$

$$\begin{pmatrix} 0.9 & 0.2 \\ 0.1 & 0.8 \end{pmatrix} \begin{pmatrix} 0.8 \\ 0.2 \end{pmatrix} = P(A, S)$$

$$P(A|S)$$

$$P(S)$$

$$P(A, S)$$

$$\begin{pmatrix} 0.72 \\ 0.24 \end{pmatrix} \\ P(A)$$

$$0 \quad \text{Skill} \quad 1$$

Aufgabe

0	0.9	0.2
1	0.1	0.8

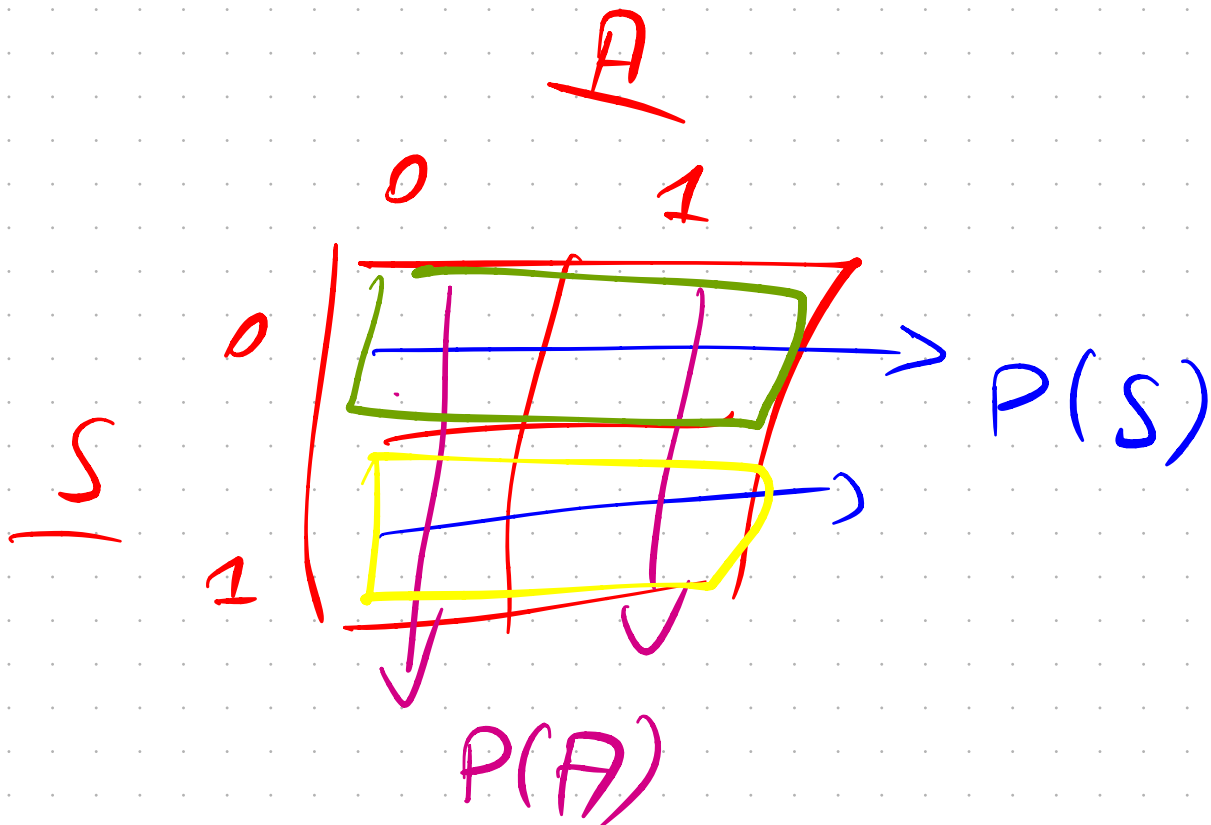
sep
joints

Marginalisieren: $P(A, S)$
 $\Rightarrow P(A)$

$$P(A) = \sum_S P(A, S)$$

$$= \underbrace{P(A, S=0)} + \underbrace{P(A, S=1)}$$

$P(A, S)$



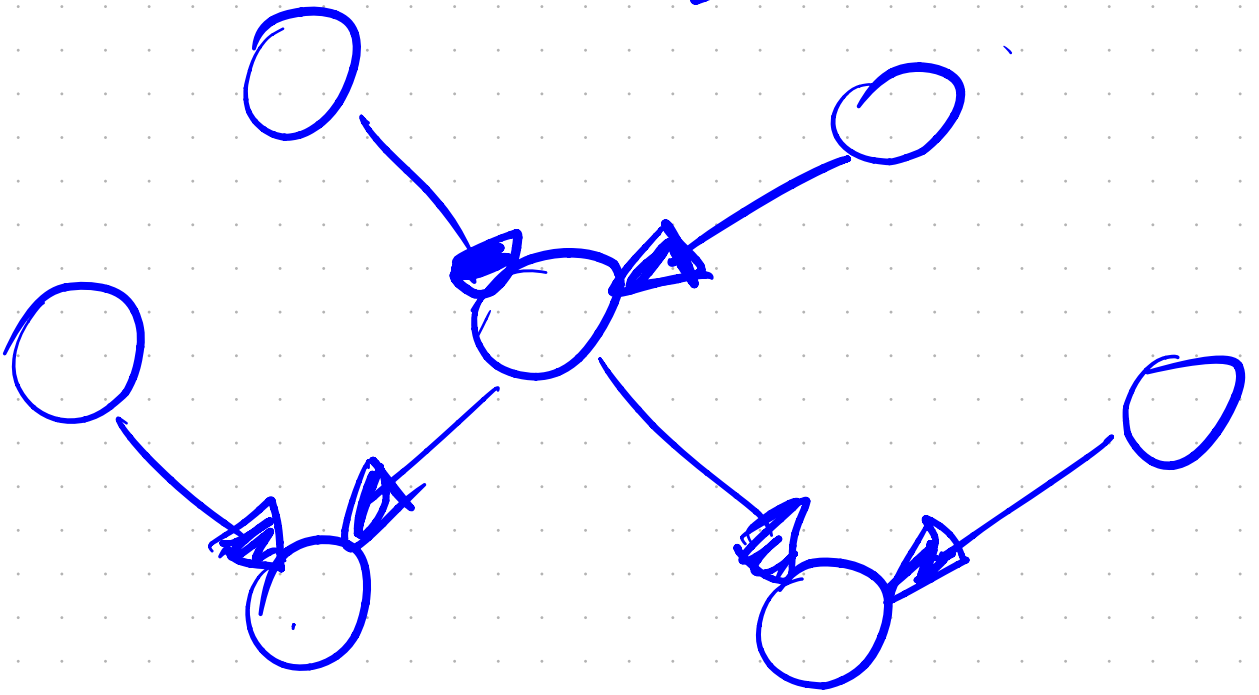
$$P(S_{N1} | S_{A,1})$$

		$S_{A,1}$	
		0	1
S_{N1}	0	w_2	w_3
	1	$1-w_2$	$1-w_3$
Σ		1	1

$$P(S_{N1} | S_{A,1}, S_{G,1})$$

		S_A		S_G	
		0		1	
		0	1	0	1
S_{N1}	0				
	1				

Markov Blanket
für Directed, GM



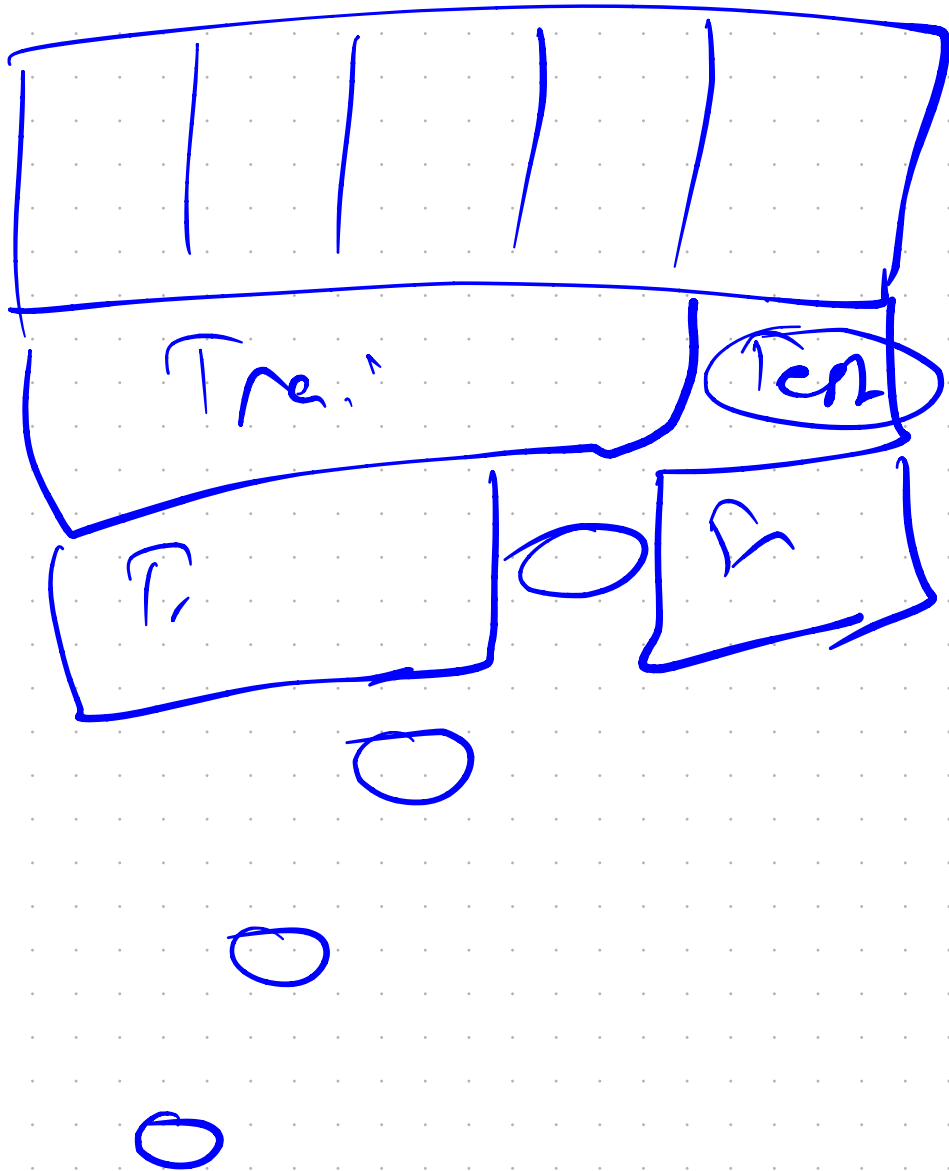
Maximum Likelihood
Parameter Finder

$$L(\theta) = \prod_D p(\cdot | \theta)$$

Joint Probability

Datensatz

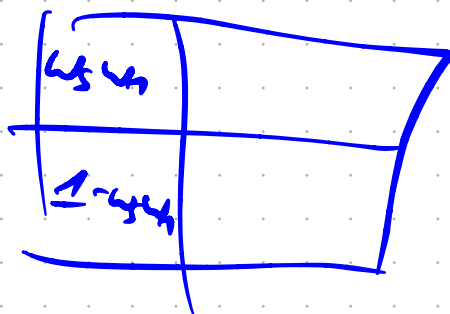
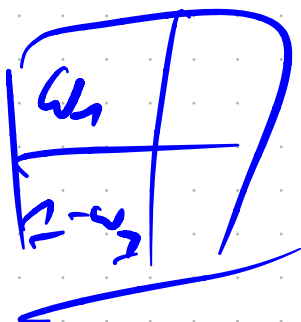
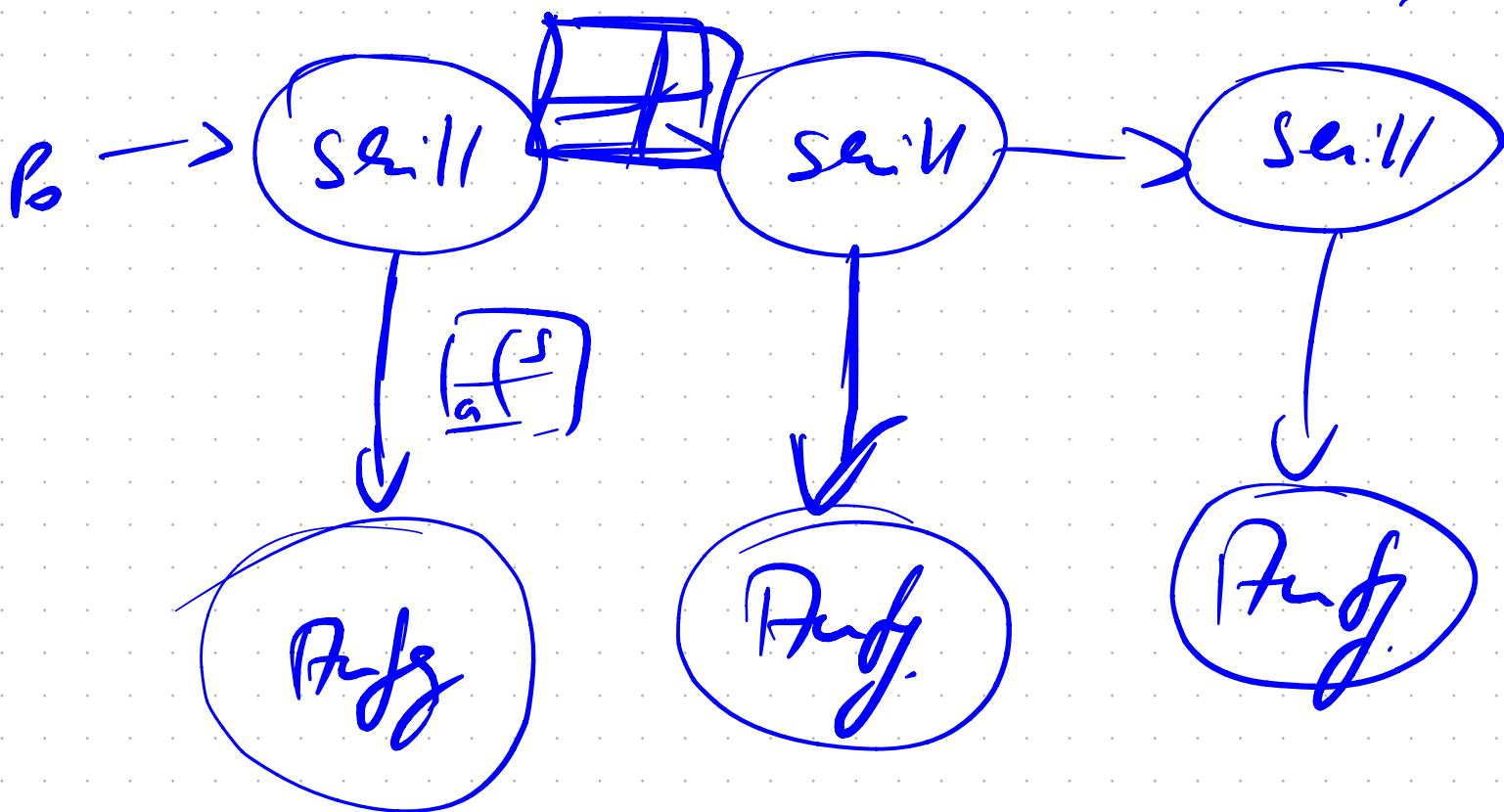
11



$t-1$

t

$t+1$



$$\frac{1}{1+e^{-\cdot}}$$

ρ

$$\frac{e^{\dots}}{1+e^{\dots}}$$