

Lecture Notes for Sep 16, 2025

Overshooting (loose bound)

Basis

$$T(n) = 2T\left(\frac{n}{2}\right) + 2$$

$$T(n) = O(n^2)$$

$$T(n) \leq cn^2$$

Inductive Hypothesis

It holds for $k < n$, specifically $k = \frac{n}{2}$.

$$T\left(\frac{n}{2}\right) \leq c\left(\frac{n}{2}\right)^2$$

Substitution

$$T(n) = 2T\left(\frac{n}{2}\right)$$

$$T(n) \leq 2c\left(\frac{n}{2}\right)^2 + n$$

Undershooting

Run extended form of guess